



# Laboratoire de l'Accélérateur Linéaire (LAL) Orsay, mardi 18 janvier 2011

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## LABORATORY ASTROPHYSICS with HIGH-ENERGY-DENSITY FACILITIES

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**Emeric FALIZE and Bérénice LOUPIAS**

- **Claire MICHAUT and LUTH group (CNRS, Observatoire de Paris),**
- **Michel KOENIG and LULI group (CNRS, Ecole polytechnique),**
- **Xavier RIBEYRE (CEA-CESTA/CELIA, Université of Bordeaux),**

- **Nigel WOOLSEY and RAL group (University of York, UK),**

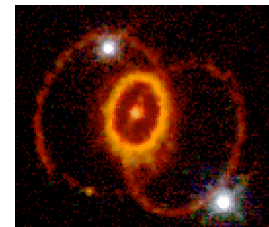
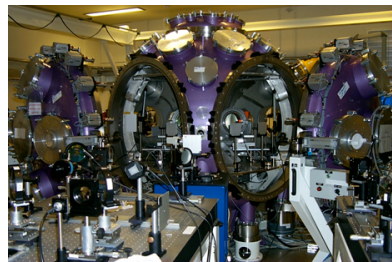
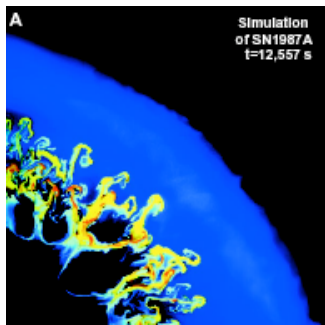
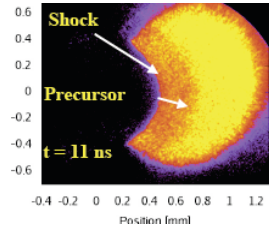
- **Paul DRAKE and his group (University of Michigan at Ann-Arbor, USA),**

- **Aki TAKABE and Ryosuke KODAMA groups (Institute of Laser Engineering, Osaka, Japan)**



# PHILOSOPHY of LABORATORY ASTROPHYSICS

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## USING HIGH ENERGY/POWER TOOLS

**Lasers (USA, Japan, UK, France ...)**

**Z-pinches (Sandia, Imp. Coll.- UK ...)**

**Spheromacks (Caltech', LLNL ...)**

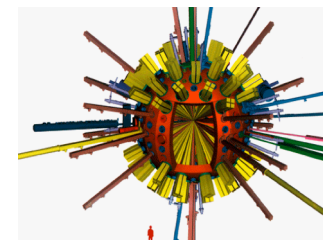
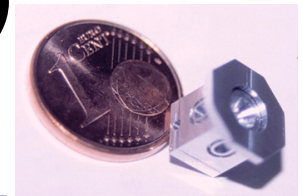
## TO REPRODUCE OR TO SIMULATE

### in the LABORATORY

## ASTROPHYSICAL PHENOMENA

and/or

## PIECES OF ASTRONOMICAL OBJECTS





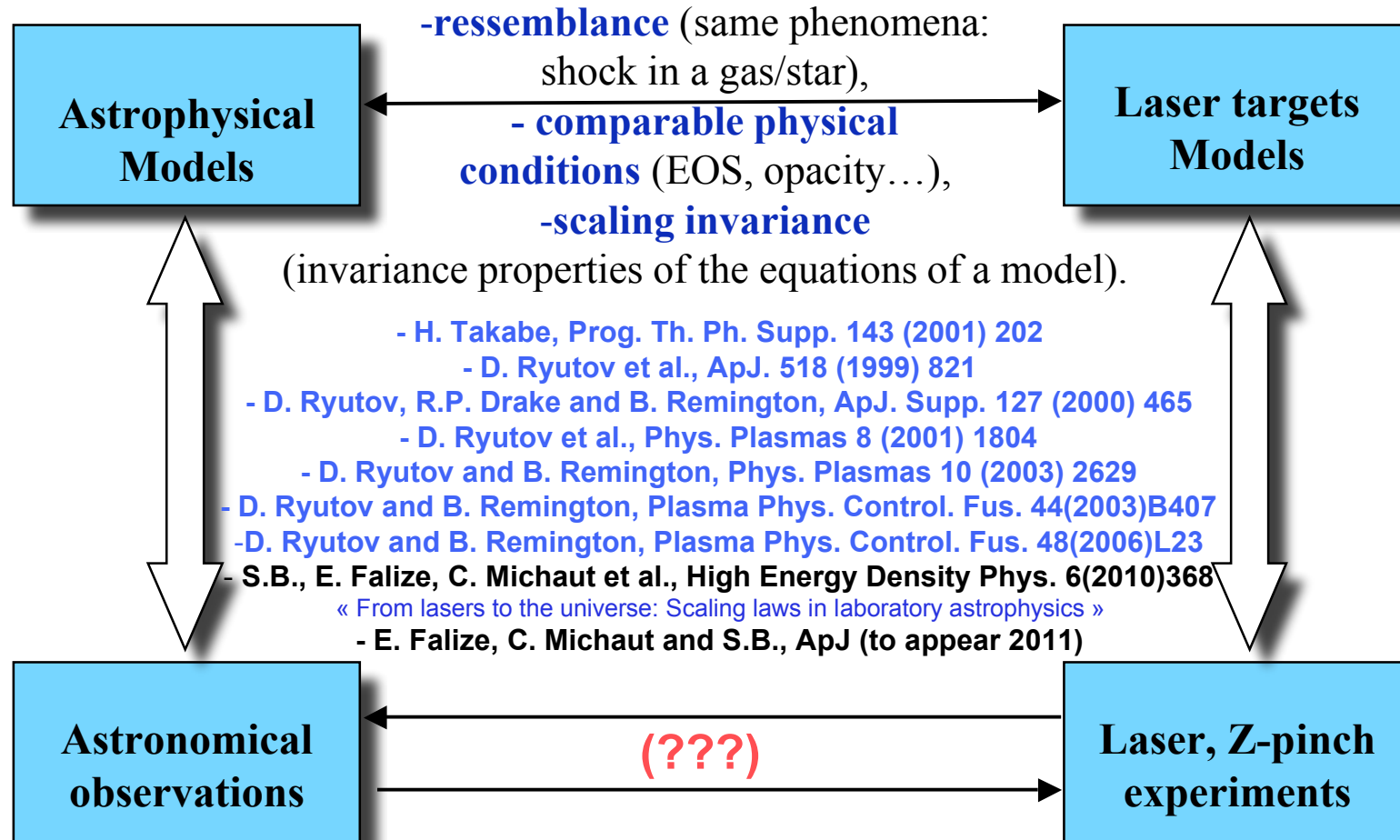
# OUTLINE

- 1) - LABORATORY ASTROPHYSICS
- 2) - LASER FACILITIES
- 3) - ASTROPHYSICAL RADIATIVE SHOCKS (RS)  
and LASER EXPERIMENTS
- 4) - ASTROPHYSICAL JETS and LASER  
EXPERIMENTS
- 5) - CONCLUSION



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# LASER EXPERIMENTS versus ASTRONONOMICAL OBSERVATIONS

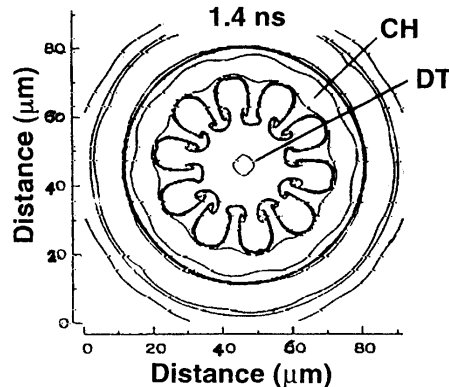


## CONNECTION BETWEEN LASER EXPERIMENTS AND ASTRONONOMICAL OBSERVATIONS

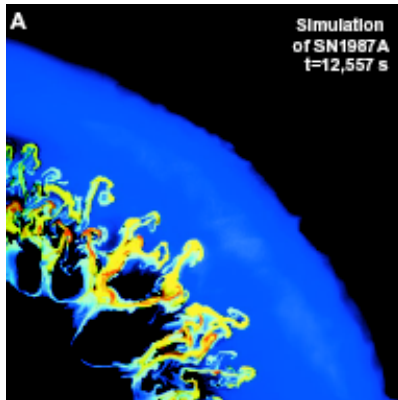
# AN EXAMPLE: LASER TARGET versus SUPERNOVA

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## RAYLEIGH-TAYLOR INSTABILITY



Imploding laser target



Exploding star : supernova  
Among the most violent phenomena  
In the universe !!!

### Typical quantities for laser target (S1) and supernovae (S2)

Physical quantities	Laser target (S1)	Supernova (S2)
Characteristic length	$l_1 \approx 100 \mu\text{m} \approx 10^{-2} \text{ cm}$	$l_2 \approx 10^{12} \text{ cm}$
Characteristic time	$\tau_1 \approx 10^{-9} \text{ s}$	$\tau_2 \approx 1000 \text{ s}$
Characteristic velocity	$V_1 \approx 10^7 \text{ cm/s}$	$V_2 \approx c/10 \approx 10^9 \text{ cm/s}$
Characteristic acceleration	$g_1 \approx 10^{16} \text{ cm/s}^2$	$g_2 \approx 10^6 \text{ cm/s}^2$

The acceleration of the supernovae is very weak !!!

### Characteristics of the Rayleigh-Taylor Instability (RTI)

Physical quantities	S1 (target)	S2 (supernova)
Instability rate $\alpha_{\text{IRT}}$	$\alpha_{\text{IRT},1} \approx 10^9 \text{ s}^{-1}$	$\alpha_{\text{IRT},2} \approx 10^{-3} \text{ s}^{-1}$
Dimensionless numb. $N_{\text{IRT}}$	$N_{\text{IRT},1} \approx 1$	$N_{\text{IRT},2} \approx 1$

We should compare  $\alpha_{\text{IRT},i}$  to the proper time  $\tau_i$  of the system  $S_i$

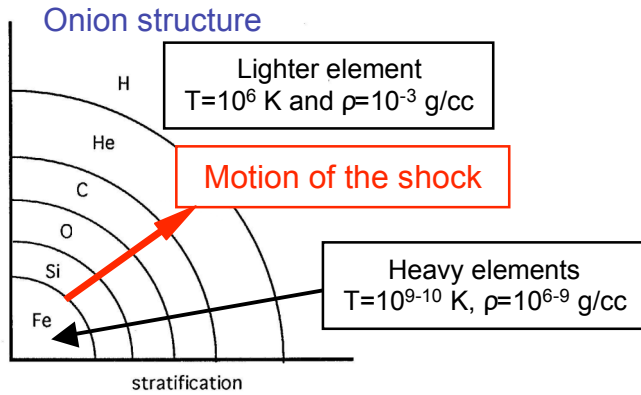
THE DIMENSIONLESS NUMBER  $N_{\text{IRT}}$  IS GIVEN BY  
THE PRODUCT  $N_{\text{IRT}} = \alpha_{\text{IRT}} \cdot \tau$  FOR EACH SYSTEM

$$N_{\text{IRT}}(\text{target}) = N_{\text{IRT}}(\text{supernova}) = 1 \quad \text{!!!}$$

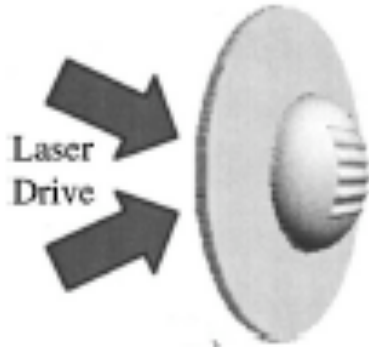
# SUPERNOVA SN87A (type II): SIMULATION versus EXPERIMENT

## Scaling laws : Rayleigh - Taylor instabilities in SNe

EXPERIMENTS from DRAKE's GROUP :



Robey et al., Phys. Plasmas 8 (2001) 2448



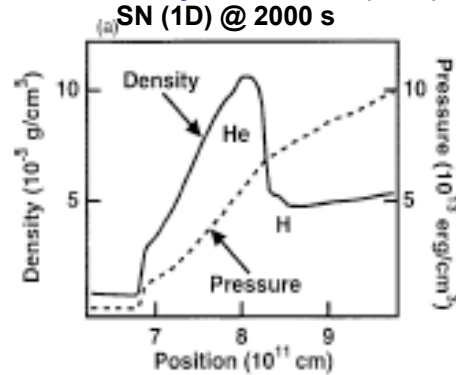
Length:  $100 \mu\text{m} \leftrightarrow 10^{11} \text{cm}$

and

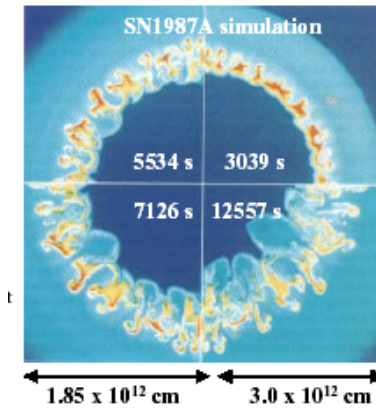
Time:  $20 \text{ns} \leftrightarrow 2000 \text{s}$

Therefore: Velocity:  $100 \text{km/s} \leftrightarrow 10\,000 \text{km/s}$

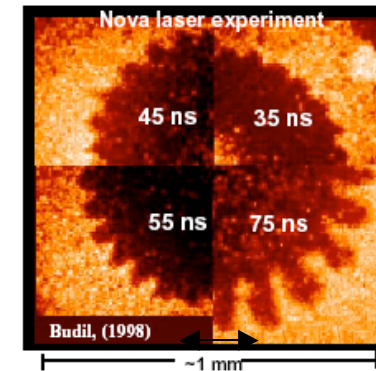
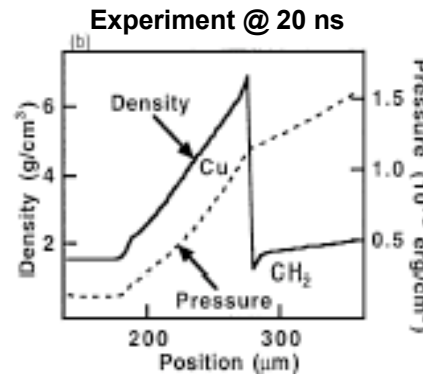
Ryutov et al., Phys. Plasmas 8 (2001) 1804



Muller et al., Astron. Astrophys. 251 (1991) 505



Ryutov et al., ApJ 518 (1999) 821



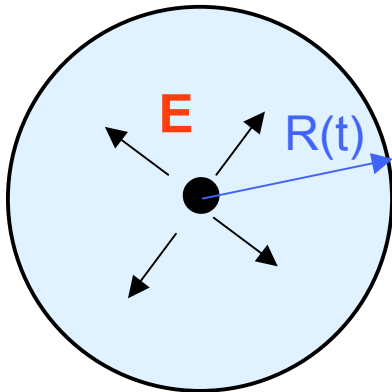
10 000 km/s is relevant for SN remnants  
100 km/s is relevant for laser targets

J. Kane et al., Phys. Plasmas 6 (1999) 2065

# STRONG EXPLOSION, DIMENSIONLESS NUMBER and SELF-SIMILAR SOLUTION

Strong point explosion with energy  $E$  in an ambient medium of uniform density  $\rho_0$

Fireball



density  $\rho_0$

Time position of the shock,  $R(t)$  ???

Use of Dimensional analysis

- Unit of mass:  $M$       $[E] = M.L^2.T^{-2}$
- Unit of length:  $L$       $[\rho_0] = M.L^{-3}$
- Unit of time:  $T$       $[R] = L$

- Ratio  $E/\rho_0 \sim L^5.T^{-2}$       $\longrightarrow$   $M$  disappears
- Product  $(E/\rho_0).t^2 \sim L^5$       $\longrightarrow$   $M$  and  $T$  disappear

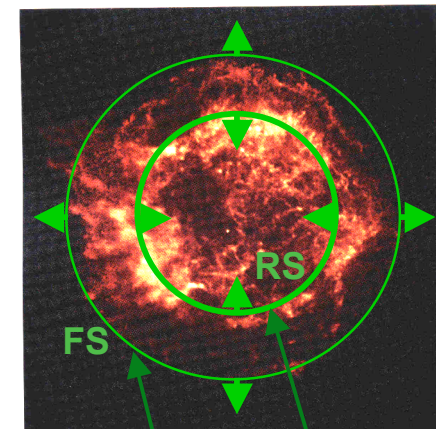
**Time  $t$  is inserted !!! Nice !!!**

CONCLUSION :  $(E/\rho_0).t^2 / [R(t)]^5 \sim \xi$  : Dimensionless Number

and  $R(t) \sim (E/\rho_0)^{1/5} .t^{2/5}$  Sedov - Taylor law

$R(t) \sim t^\alpha$  : SELF-SIMILAR EVOLUTION

Cassiopee A (1680)  
Type Ia SN



Reverse shock

Forward shock



# SEDOV - TAYLOR SOLUTION

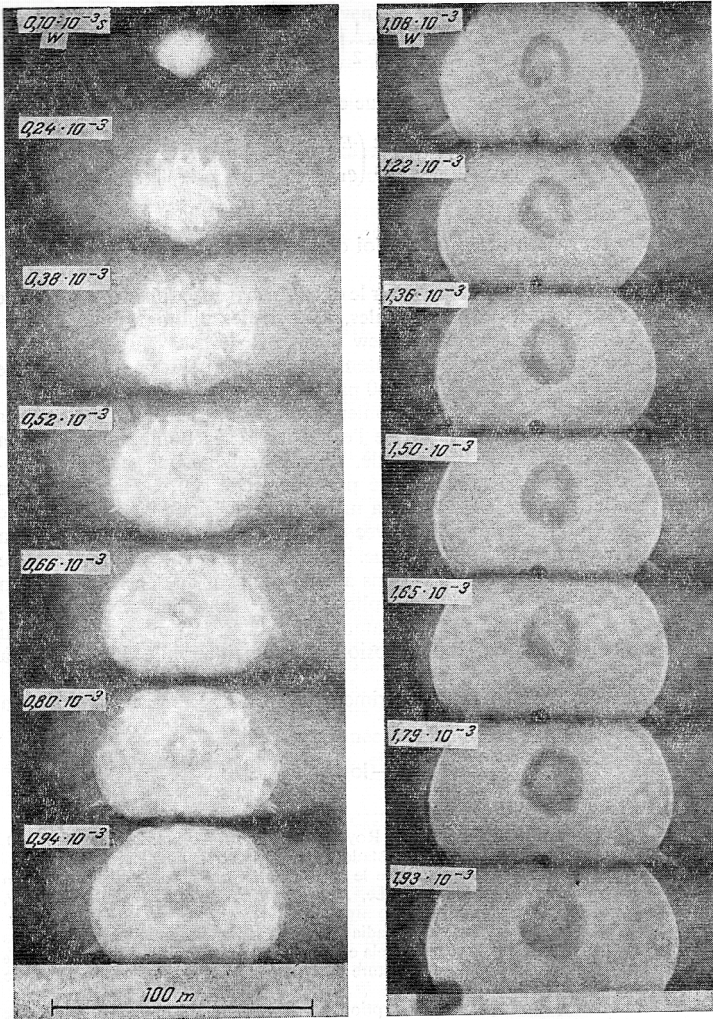


Fig. 67. Photographies d'une boule de feu prise dans l'intervalle de  $t=0,1 \cdot 10^{-3}$  à  $t=1,93 \cdot 10^{-3}$  s lors de l'explosion de la bombe atomique à New Mexico

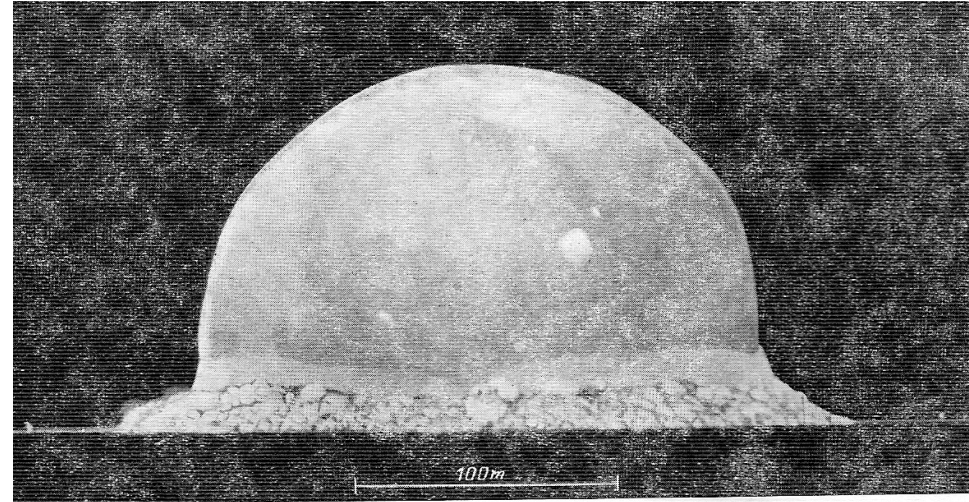
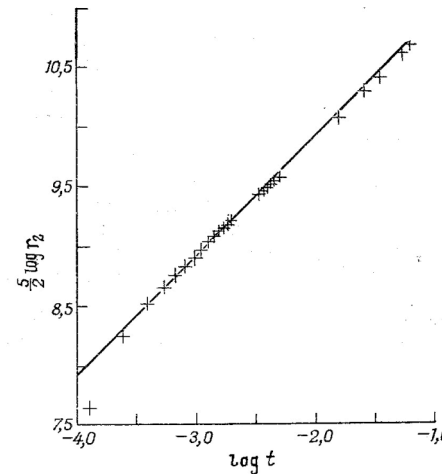


Fig. 68. Boule de feu à l'instant  $t=15 \cdot 10^{-3}$  s

## Measurements Vs. Theory



$$R(t) \sim t^{2/5}$$

## Self-Similar Solution (SSS)

- Fireball:  
 $R \sim 100 \text{ m} \sim 10^4 \text{ cm}$
- Supernova remnant:  
 $R \sim 1 \text{ pc} \sim 3 \cdot 10^{18} \text{ cm}$

**SAME BEHAVIOUR**

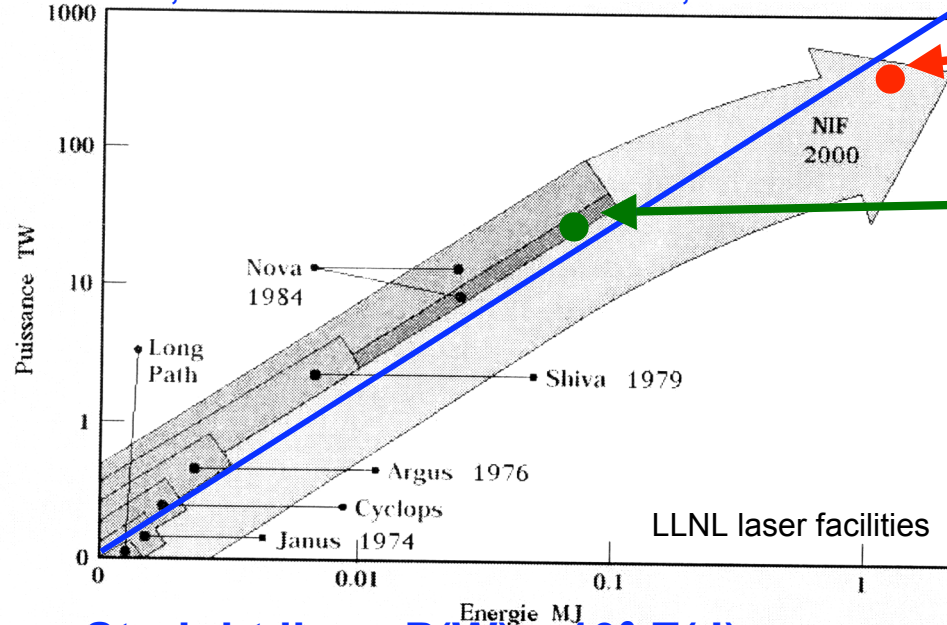


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# EVOLUTION OF THE LASER FACILITIES

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J.L. Bobin, *Les Déconvenues de Prométhée*, Atlantisciences (2001)



**Laser MégaJoule**  
**LMJ (1.8 MJ, ns)**  
**240 beams**

**Laser Integration Line**  
**LIL (60 kJ, ns)**

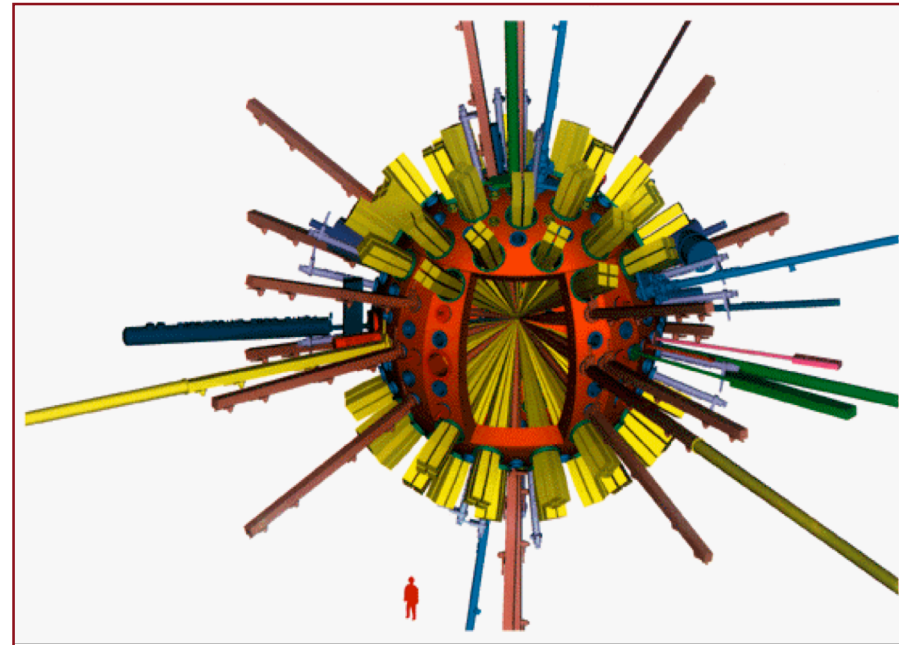
- **China** : ShenGuang II (10 kJ, 1 ns)  
 ShenGuang III (100 kJ, 60 beams)
- **Japan** : Gekko XII (10 kJ, 1 ns), LFEX (PW)
- **European array**:  
**UK**: Helen (TW), Vulcan (PW); **G**: Phelix (TW)  
**Prague**: PALS (TW), I: TW/PW, F: Luli2000,  
 etc ...

**Straight line :  $P(W) \propto 10^6 \cdot E(J)$**

- **Early 70 's** : intense development of laser facilities,
- **1984** : second big step with **NOVA** (10 beams, 45 kJ),
- **End 90 's** : third step **OMEGA** (Rochester-USA, 60 beams, 60kJ)
- **Begin. 2000** : new progress **NIF** (National ignition facility, LLNL-USA, 192 beams, 1.8 MJ), working now,
- **Since 2004**: **LIL** (Laser integration line, CEA/CESTA, 4 beams, 30 kJ)
- **In 2014**: **LMJ** (Laser MégaJoule, CEA/CESTA, 240 beams, 1.8 MJ)

- The **Laser MégaJoule (LMJ)** is a venture undertaken by the French **Atomic Energy Commission (CEA)** for the study of **Inertial Confinement Fusion (ICF)**,
- The **LMJ** will be operating on **2014** (first target shots) and **ignition** is planned for **2016**,
- The construction takes place in **Bordeaux** at **CEA-CESTA** (Centre d'Etudes Scientifiques et Techniques d'Aquitaine).

Target Chamber

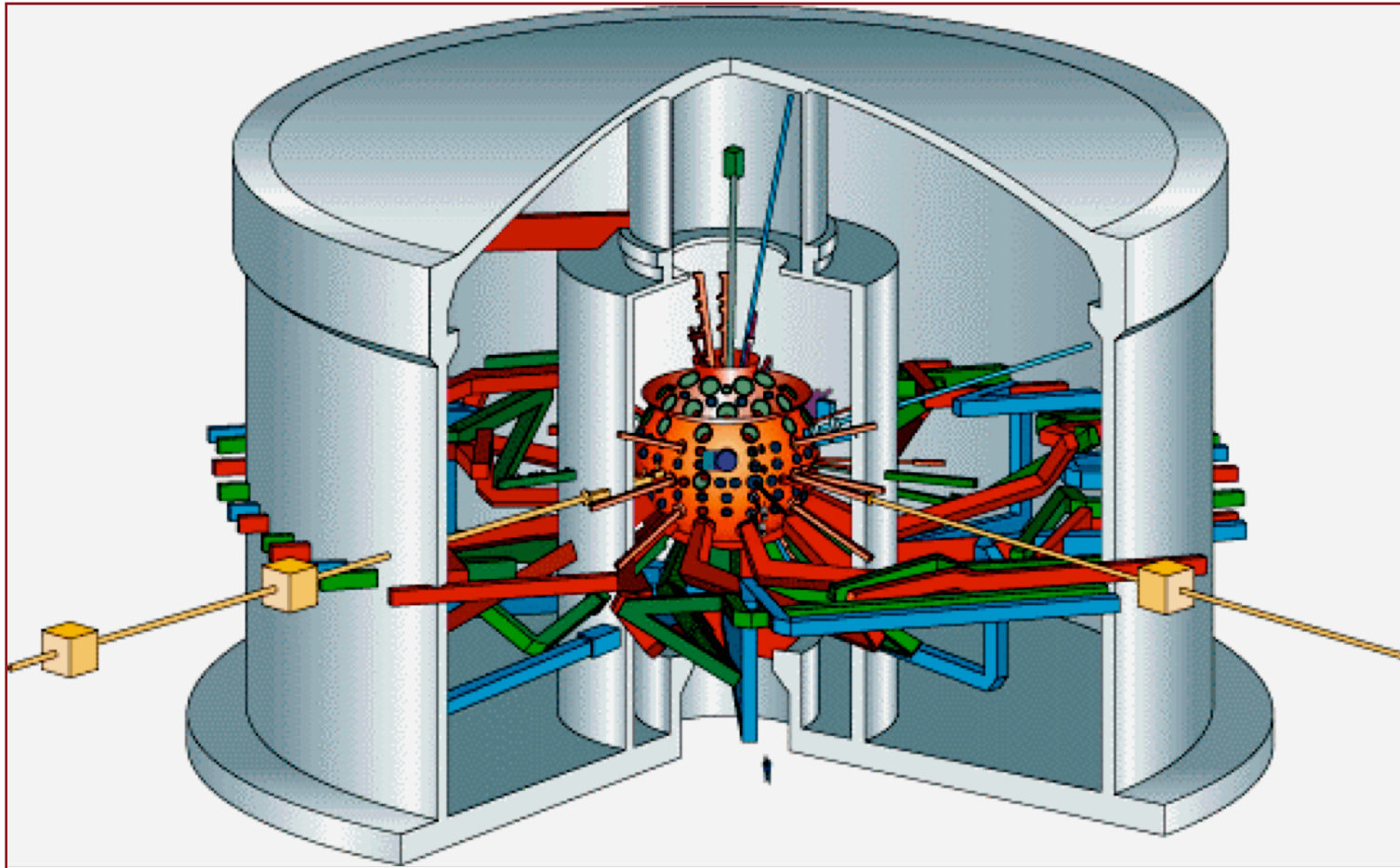


**10 meter** diameter target chamber  
(chamber inserted in the target bay in Dec.06)

**Makes the energy contained in ten 0% fat yogourts !!!**

**But over 1 s duration, that is  $10^{10}$  yogourts = 2 yogourts per human being/s**

# VIEW OF THE TARGET HALL

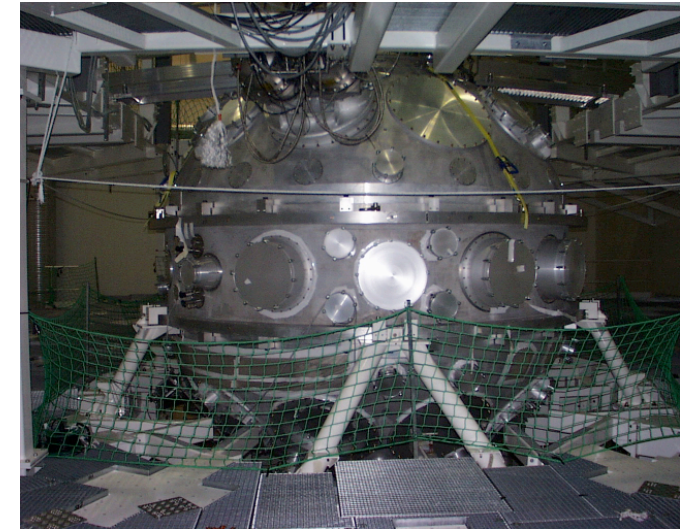


40 meters high with a 60 meter diameter

Dwarf physicist

# LMJ and LIL BUILDINGS

**LIL:** target chamber from Nova



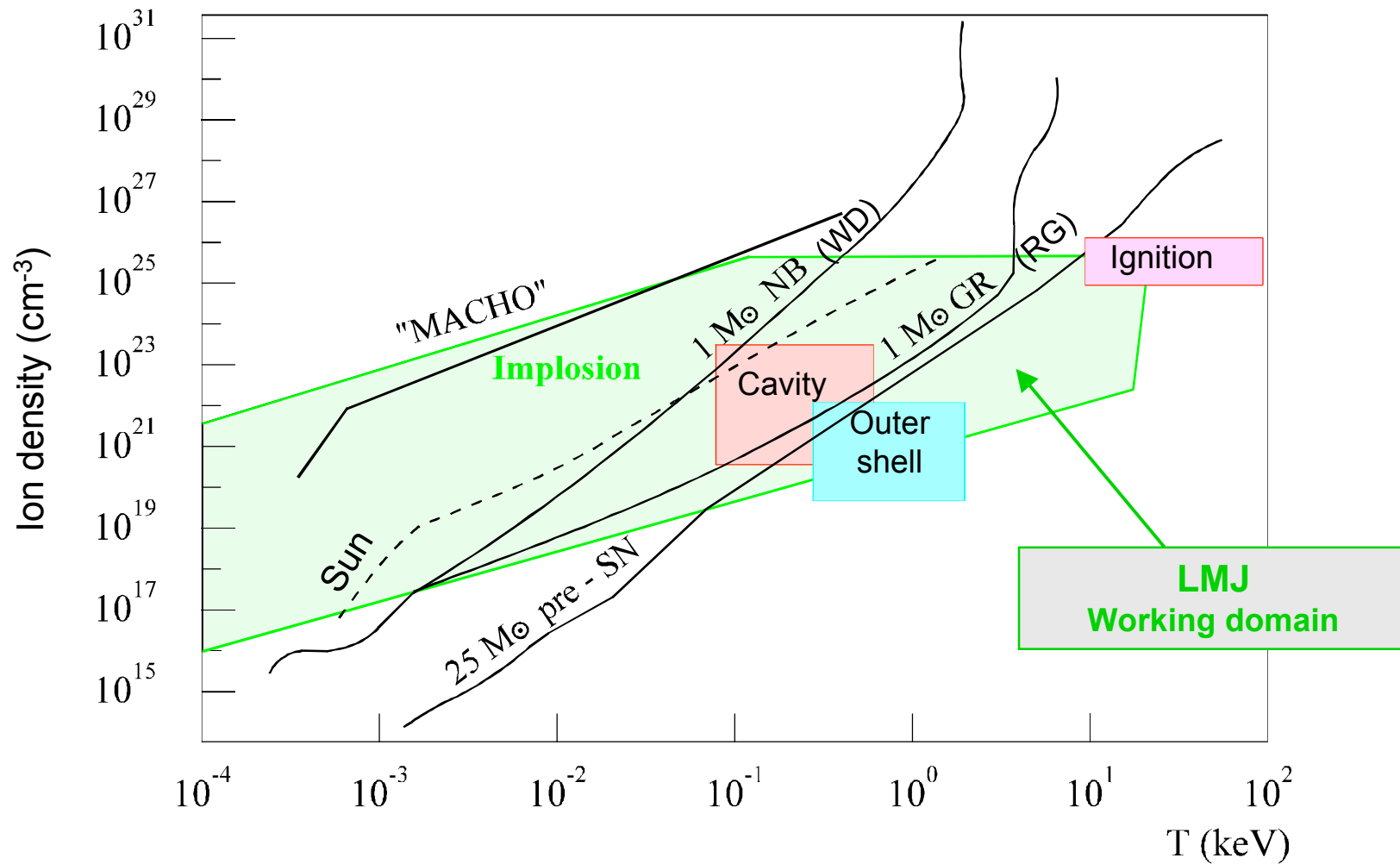
**4.5 meter diameter**

**LIL Building**

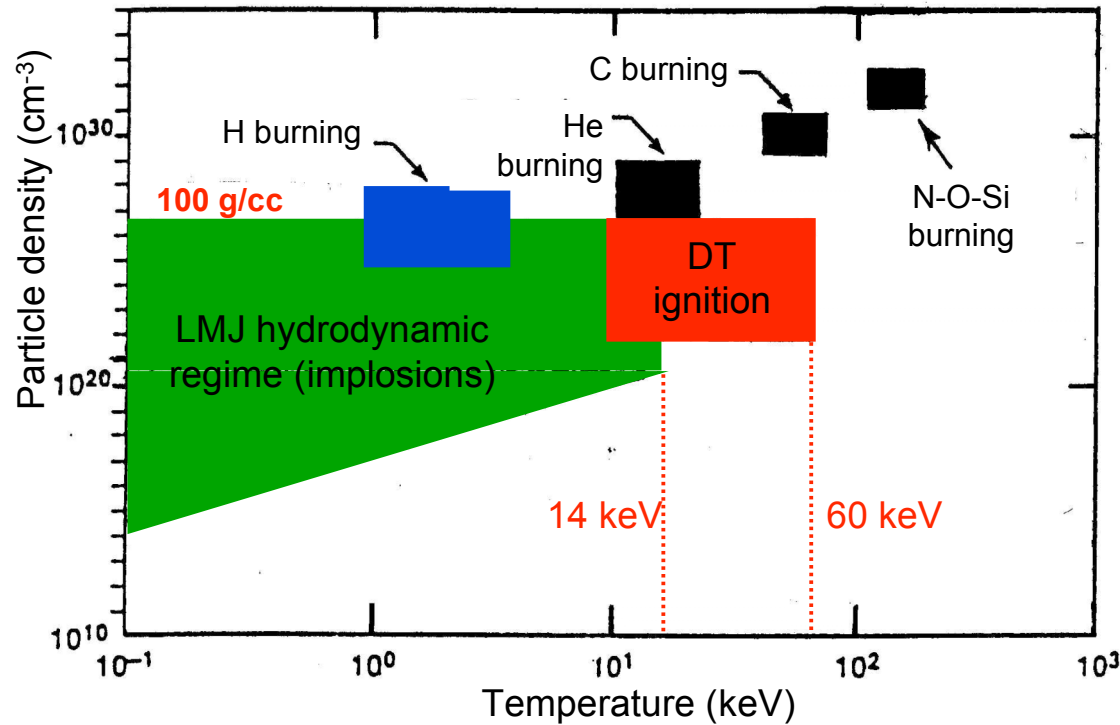
**LMJ Building**  
**300x150 m<sup>2</sup>**

Nice case for the **Eiffel Tower** which could lay down in this building !!!

# ASTRONOMICAL OBJECTS and LASER PLASMAS



■ + ■ = LMJ working domain (or NIF)

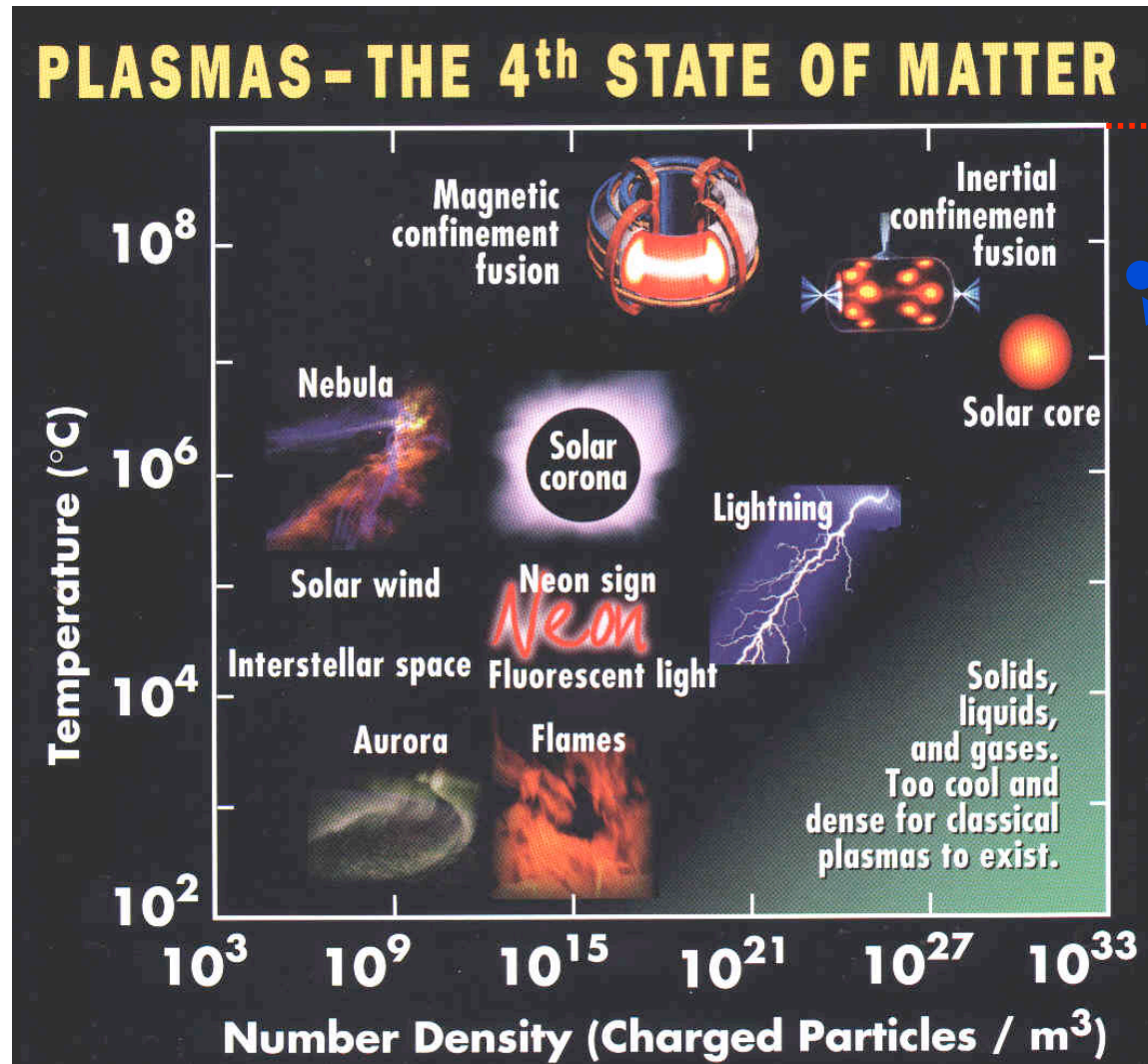


- PURE HYDRODYNAMIC REGIME :  
Condition similar to **Solar type star** with **H-burning**

- IGNITION REGIME :  
Later stage of stellar evolution  
**He-burning**  
Temperature similar (**60 keV**)  
to **C-burning** evolved stars  
(density is too low)

Sun :  $\rho \approx 150 \text{ g/cc}$  ;  $T \approx 15 \text{ MK} \approx 1.5 \text{ keV}$





**Neutron star**  
 $T_c \approx 10^{8-9} \text{ K}$ ,  $\rho_c \approx 10^{12} \rho_\odot$

**White dwarf**  
 $T_c \approx 10^{7-8} \text{ K}$ ,  $\rho_c \approx 10^{4-5} \rho_\odot$

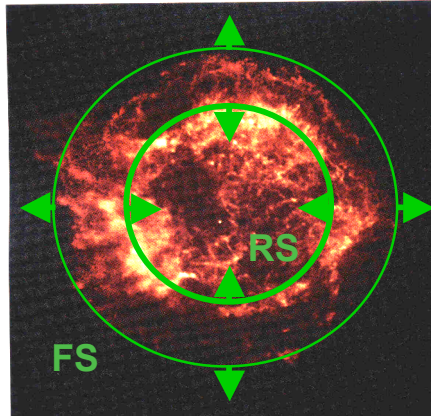


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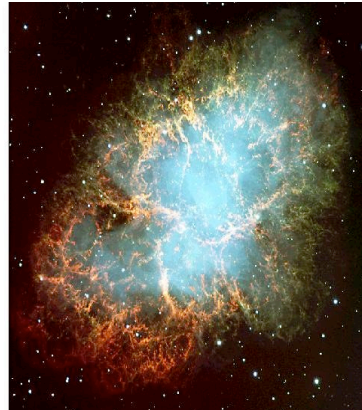
# RADIATIVE SHOCKS in SUPERNOVAE and in SUPERNOVA REMNANTS

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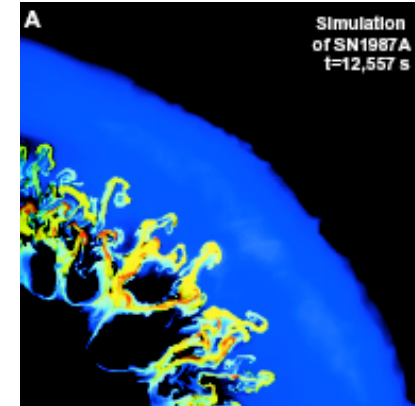
Cassiopeia A (1685)



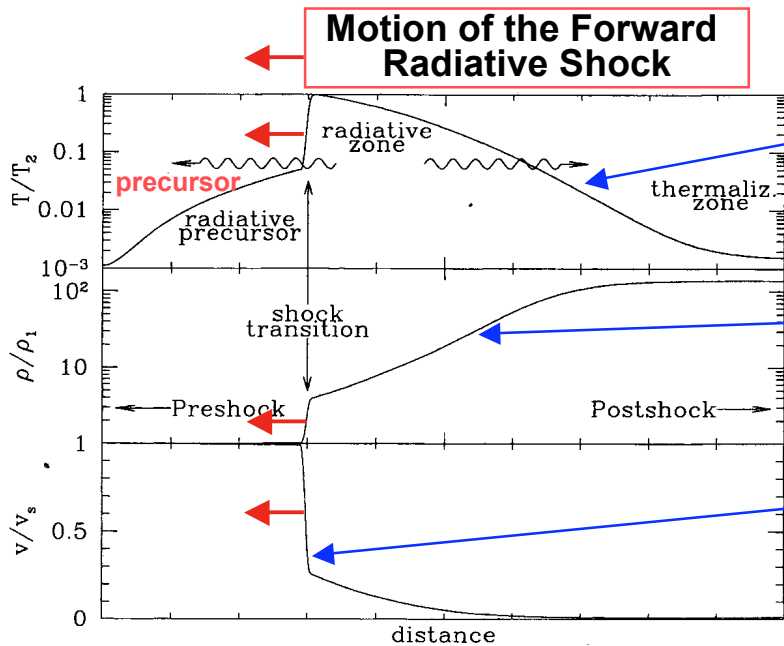
Crab Nebula (1054)



SN1987a (Feb. 23, 1987)



Muller et al. *Astron. Astrophys.* (1991)



**Motion of the Forward Radiative Shock**

T decreases due to the cooling (radiative flux ahead the sock)

therefore

$\rho$  increases (first the compression is 4 and becomes much larger)

The velocity is normalized to the shock velocity

Also in supernovae:

$$\rho_{\text{downstr.}} / \rho_{\text{upstr.}} = 7 \quad (\gamma = 4/3)$$

H. Bethe, *Astrophys. J.* (1997)

**Radiative precursor:** the energy goes through the discontinuity and heats the medium ahead of the shock

B.T. Draine & C.F. McKee, *Annual Rev. Astron. Astrophys.* 31 (1993) 373

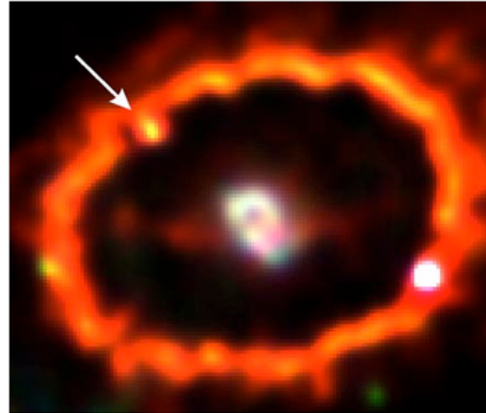
**Radiative Shocks** are very common in astrophysical processes & objects



Jets in Protostars



Bow shock in Orion



Supernova SN87A

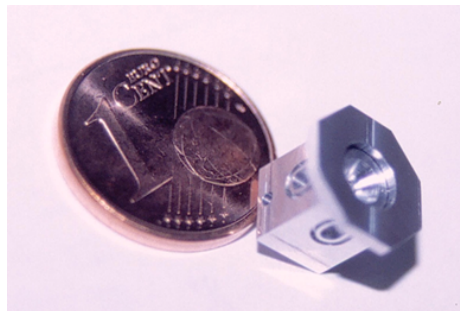
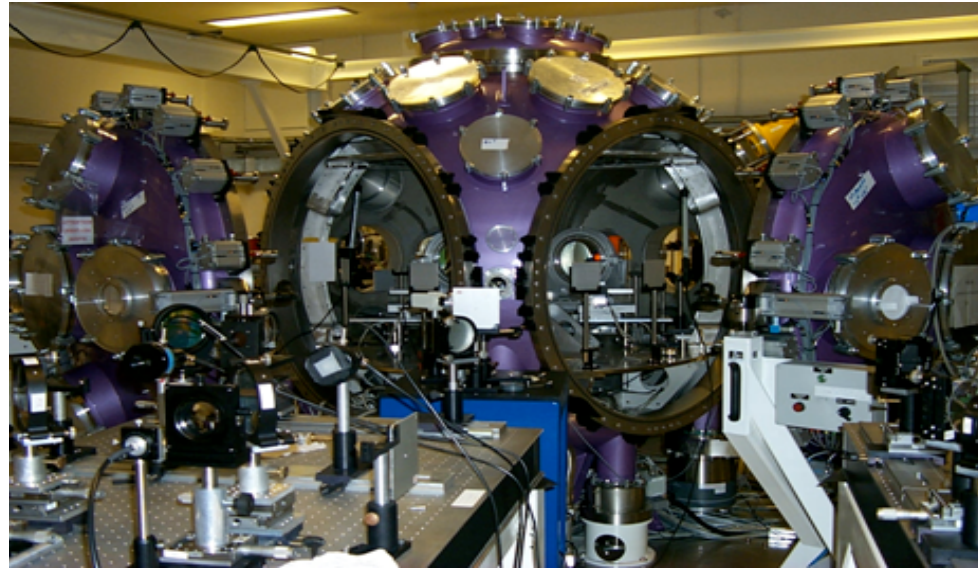
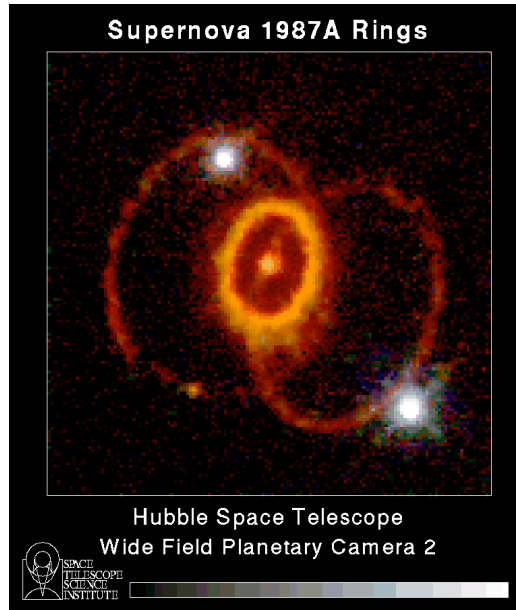


Crab nebula

To understand **RS's**, analytical modeling and numerical simulations bring key answers  
**BUT**, we need **also** to perform laboratory experiments : vary initial conditions ...

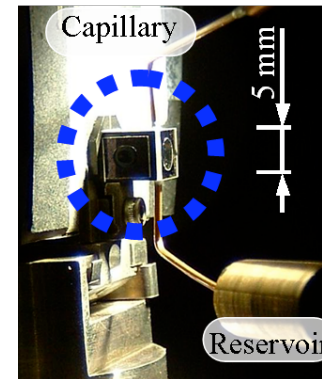
# LULI LASER FACILITY: LULI2000

LULI2000,  $\leq 1$  kJ, 1 ns **Michel KOENIG group**



**LULI2000 targets**  
**(Paris observatory and LULI)**

**Claire MICHAUT group**  
**Patrice BARROSO**

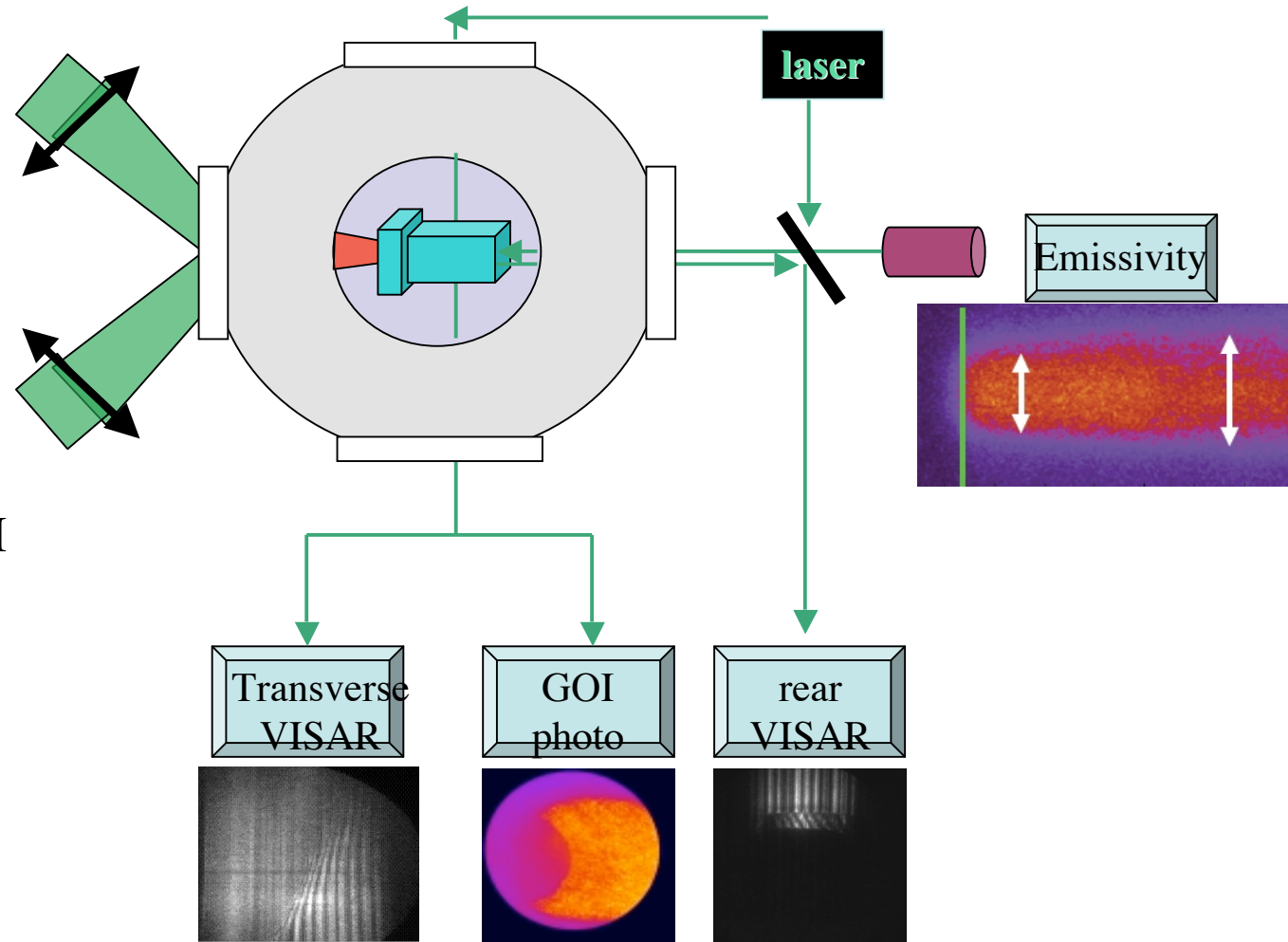


## 2 laser beams

$E = 1 \text{ kJ}$   
 $\lambda = 0,53 \text{ }\mu\text{m}$   
 $\Delta t = 1,4 \text{ ns}$

$I = 10^{14} \text{ W/cm}^2$

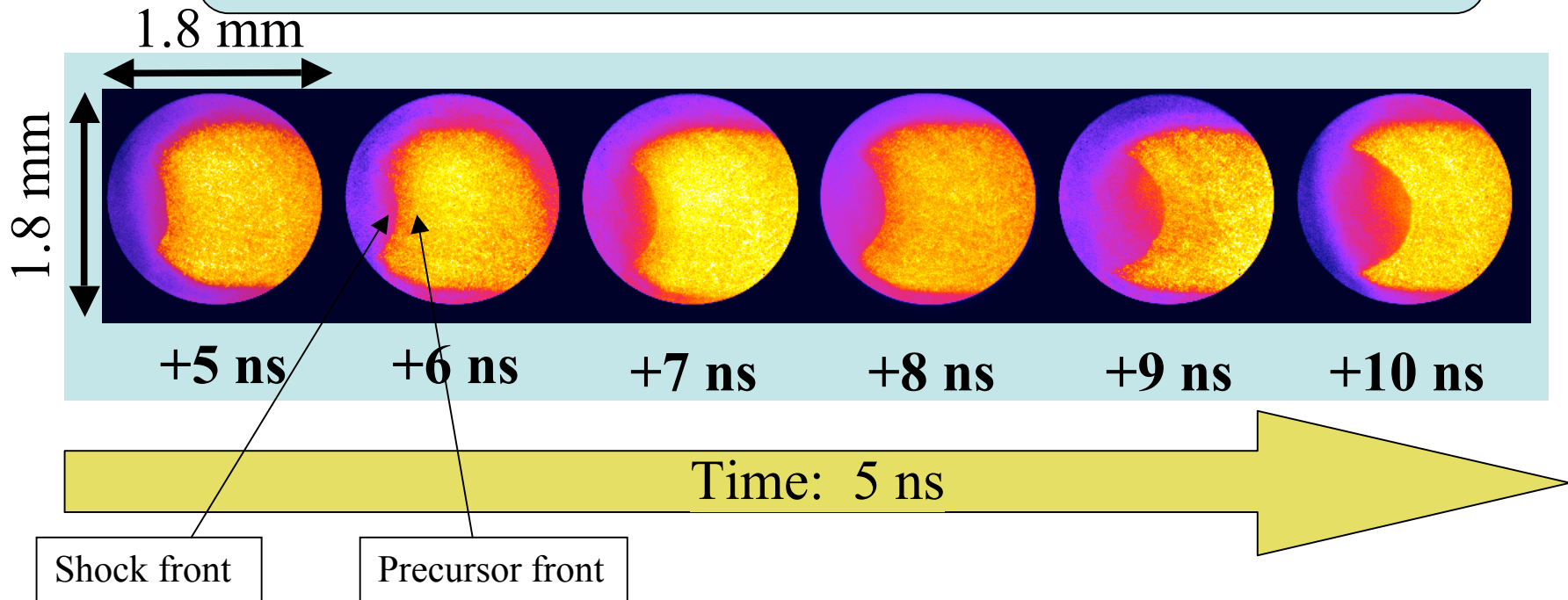
$\varnothing = 500 \text{ }\mu\text{m FWHM}$



# 2D-IMAGING OF THE SHOCK FRONT

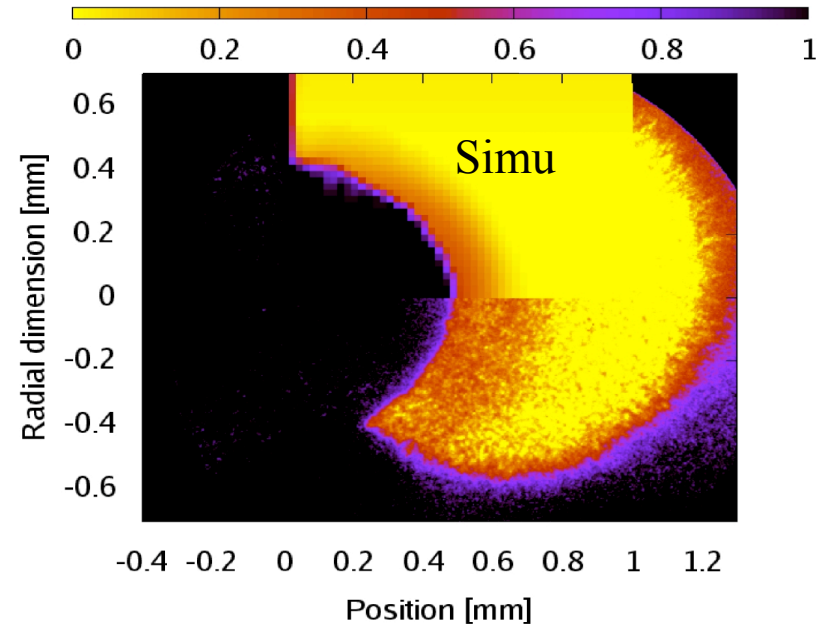
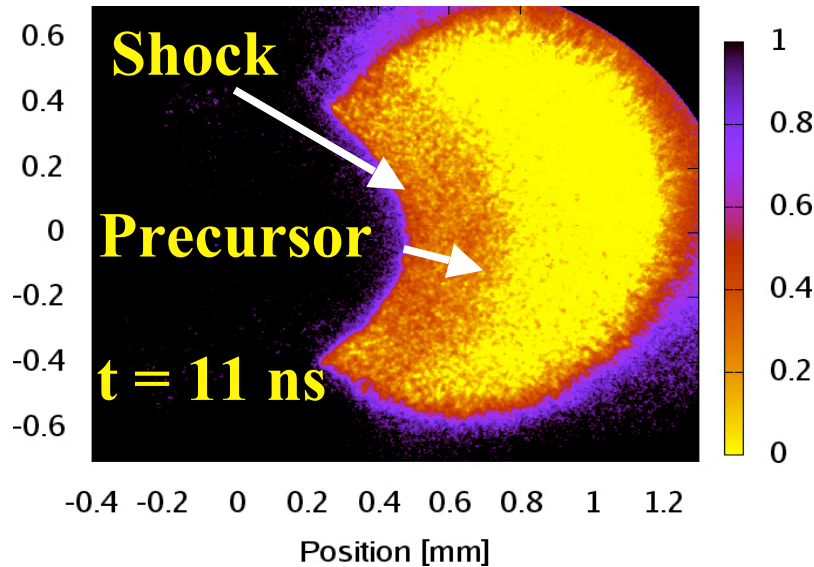
GOI (Gated Optical Imager) Exposure time: 100ps

Series of Snapshots for initial pressure  $P_{Xe}=0.1$  bar



Paul DRAKE experiments (OMEGA): Xe is denser (atmospheric pressure) - Keiter et al. PRL (2002)  
 - no precursor, BUT  
 - collapsed dense layer behind the shock front:  
 radiative losses  $\propto (\text{density})^{\text{power}}$  are important and compression rate  $\sim 50-100$

C. MICHAUT et al., *Astrophys. Space Science* 307(2007)159



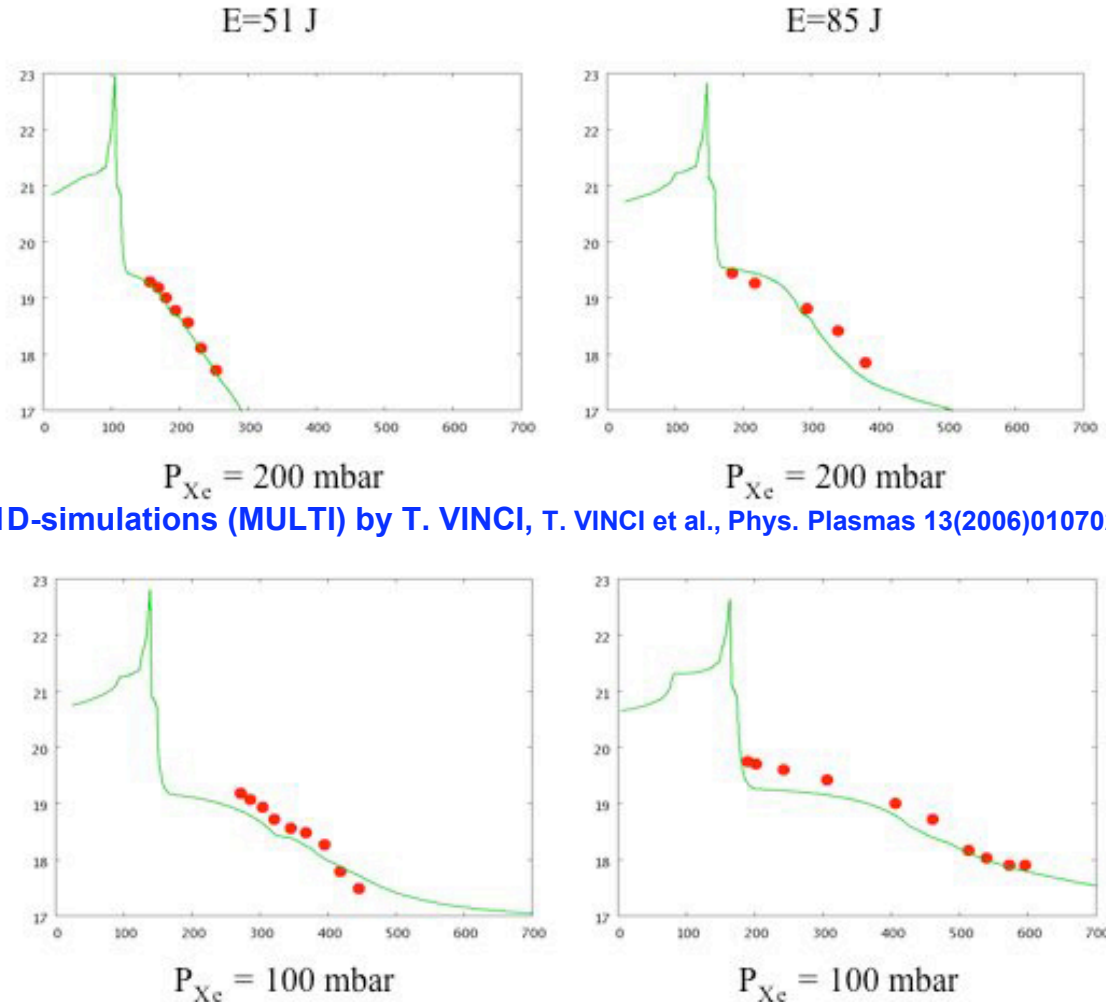
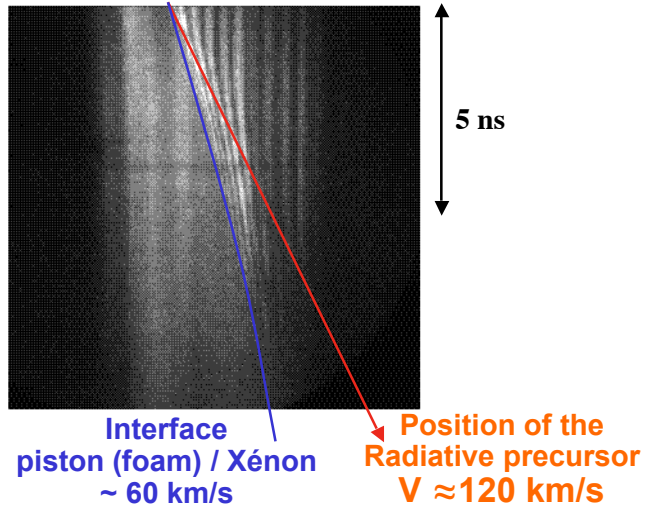
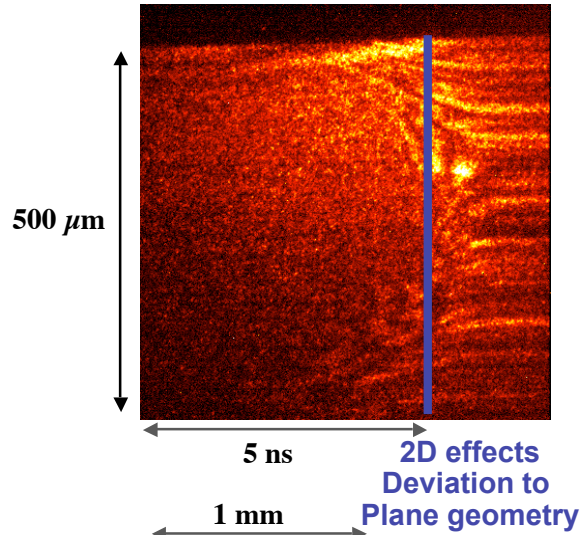
Tommaso Vinci (LULI) + Stefano Atzeni (ROMA)

- Diagnostic reproduction
- Temperature : 15 eV
- Good curvature
- Precursor length too short



# 6 BEAM-FACILITY ( $\leq 100$ J) AT LULI

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1D-simulations (MULTI) by T. VINCI, T. VINCI et al., Phys. Plasmas 13(2006)010702

Bouquet et al., PRL (2004), Koenig et al., APJP-AIP, CP926 (2007) 110, Michaut et al., Astrophys. Space Science 322(2009)77



# OMEGA EXPERIMENTS (ROCHESTER-USA)

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Amy Reighard-Cooper (LLNL), R.Paul Drake (U. of Michigan @ Ann Arbor)

Laurent Boireau, Paul students ...

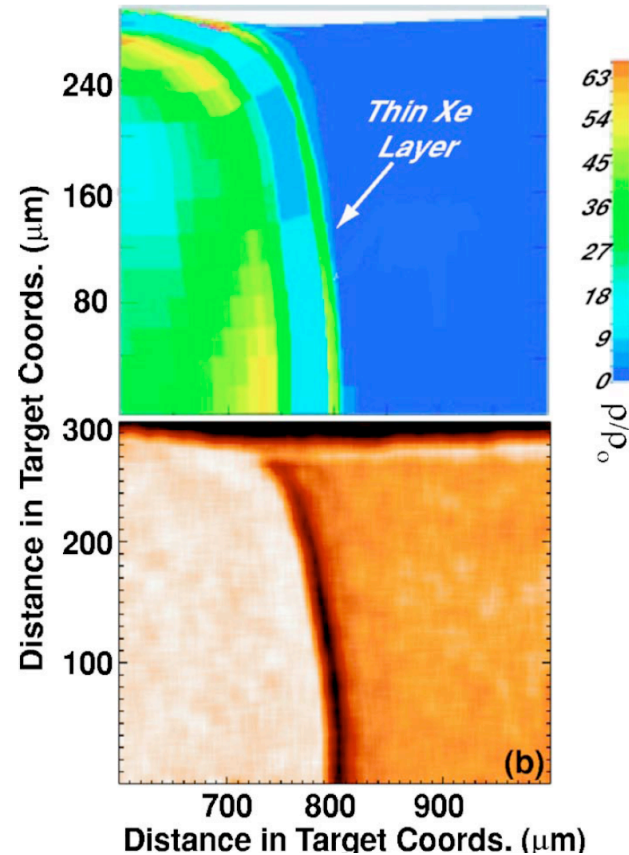
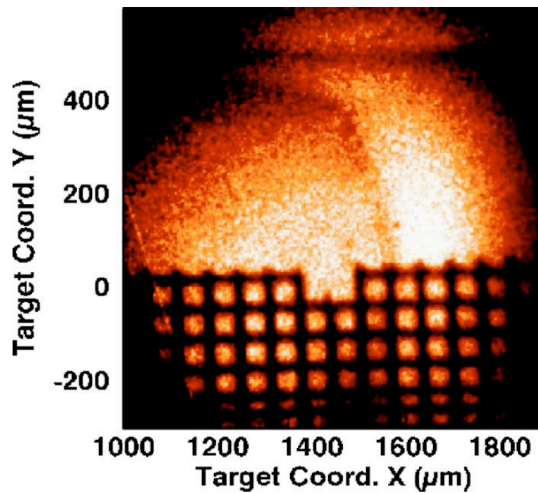
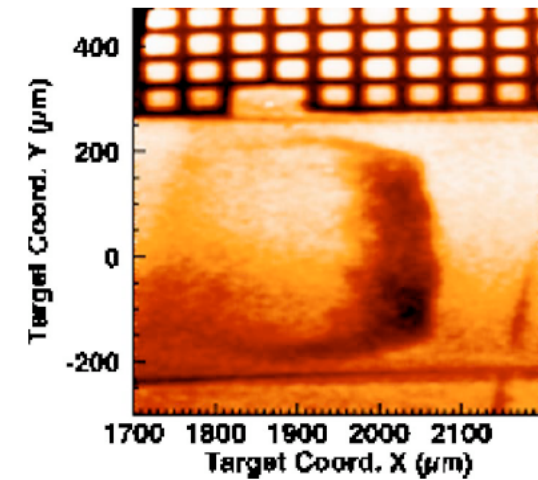
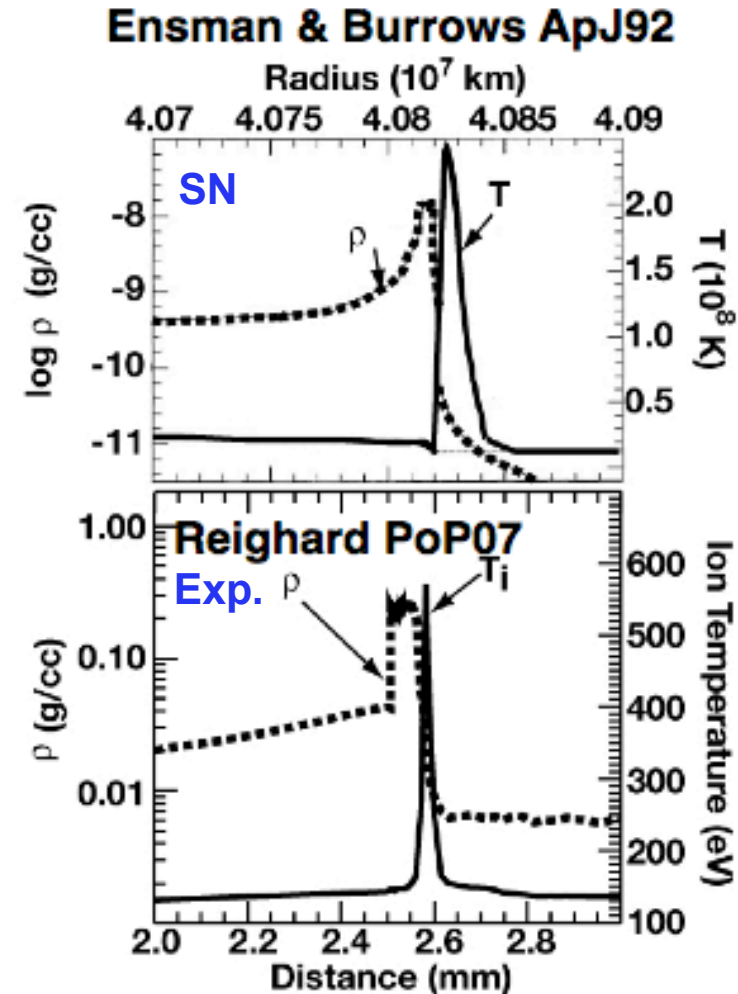


FIG. 5. (Color online) (a) Density profile at 7 ns, from a 2D simulation of the experiment, using the FCI code. The shock is moving to the right. The color bar calibrates the density as a ratio to the initial gas density. (b) Simulated radiograph, using density data from (a). Poisson noise and a point-spread function from data are included.

Reighard et al., Physics Plasmas 13 (2006) 032901



- **Radiative shocks have strong radiative energy transport that determines the shock structure**
- **Our experiments**
  - have behavior and dimensionless parameters relevant to shocks emerging from supernovae
  - We should see any important unanticipated physics
  - Good code test in any event
- **There are ongoing active observations of supernova breakout shocks**



$$I = 10^{15} \text{ W/cm}^2 = 10 \times \text{LULI2000}$$

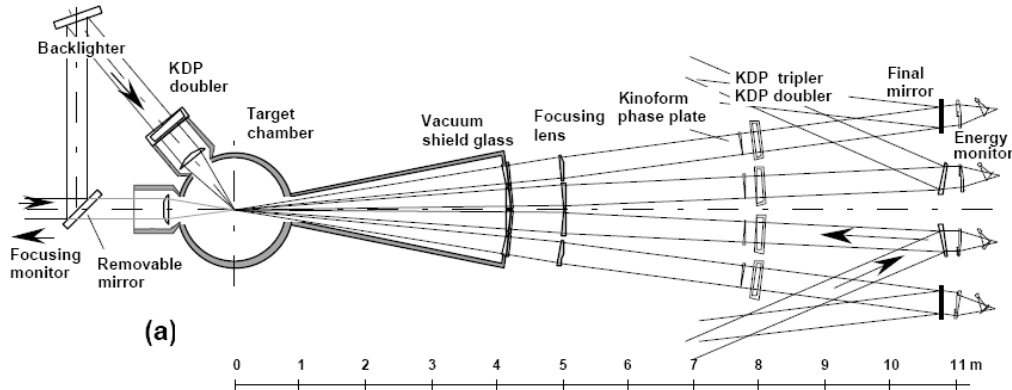
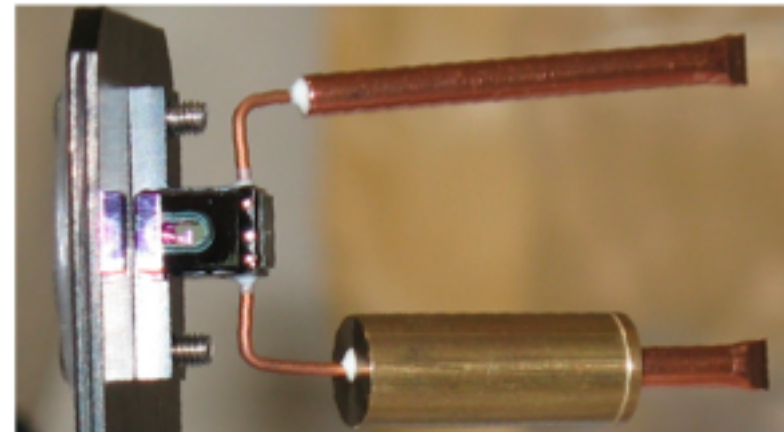


FIG. 1 HIPER focusing system. (a): schematic optical arrangement, (b): arrayed KDP cells, and (c): final mirror bundle.

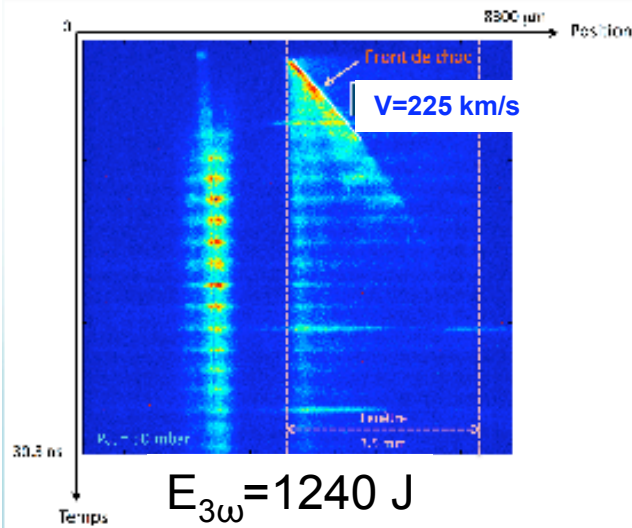
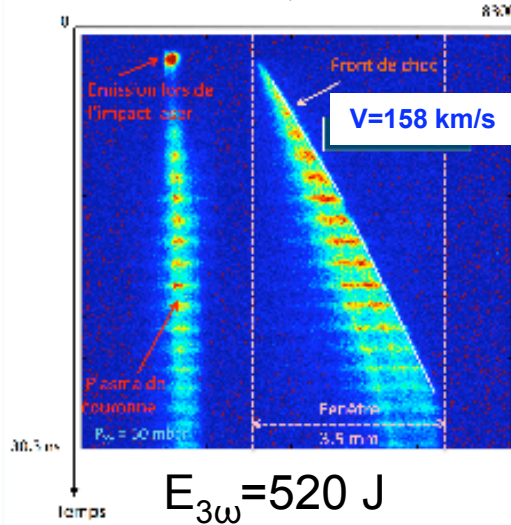
**HIPER:**  
 High Intensity Plasma  
 Intense Research  
 12 faisceaux du même côté



Michaut group, LUTH  
 Koenig group, LULI  
 Sakawa group and Kodama group  
 (OSAKA)

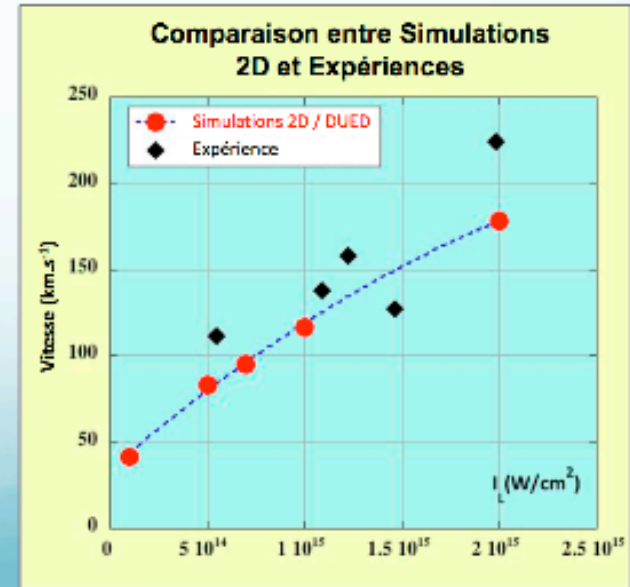
# RADIATIVE SHOCKS ON GEKKO XII

From C. Michaut, Radiative shock experiments on GEKKO XII, Workshop France/Japon, Les Houches, 9 au 14 janvier 2011



## Transverse streaked self-emission optical pyrometry

- ✓ Mean velocities around **150 km/s** with  $E_{3\omega} \approx 520 \text{ J}$  and **225 km/s** with  $E_{3\omega} \approx 1240 \text{ J}$  at **same pressure** ( $P_{Xe} = 50 \text{ mbar}$ )
- ✓ In adequation with 2D simulations
- ✗ non observed precursor with SOP → too small gas pressure (density and temperature)?

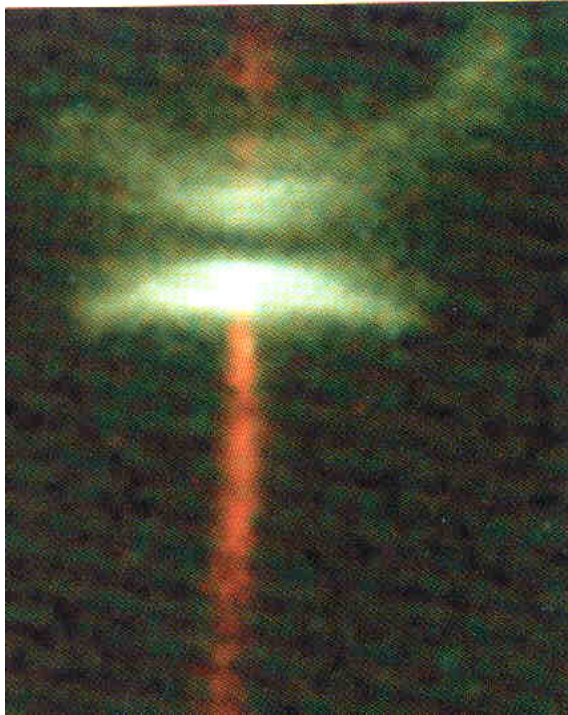




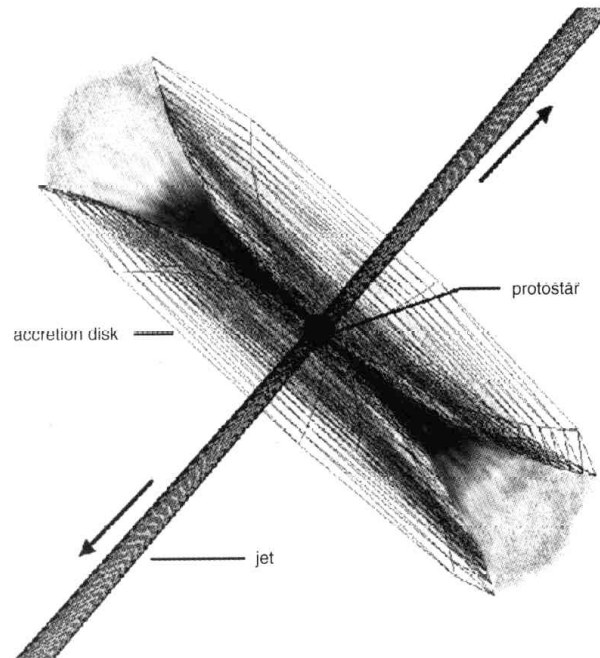
- 1) - LABORATORY ASTROPHYSICS**
- 2) - LASER FACILITIES**
- 3) - ASTROPHYSICAL RADIATIVE SHOCKS (RS)  
and LASER EXPERIMENTS**
- 4) - ASTROPHYSICAL JETS and LASER  
EXPERIMENTS**
- 5) - CONCLUSION**

# ACCRETION DISK AND JETS

Protostellar **disks** always produce protostellar **jets** via **B** : D. Lynden-Bell, astro-ph/0203480 (2002)



Protostar HH30 and its **surrounding dusty disk + jets**. The **direction of the jets is perpendicular to the disk**.



The **magnetic field B** « transforms » the strong kinetic momentum energy into high axial velocity jets (ideal Frozen MHD).

## Jet Properties :

- hypersonic (Mach=20)  
 $v = 50$  to  $250$  km/s,
- length/diameter = 20,
- $T = 1$  to a few eV,
- $\eta = \rho_{\text{jet}} / \rho_{\text{ambient}}$  between 0.1 and 10.

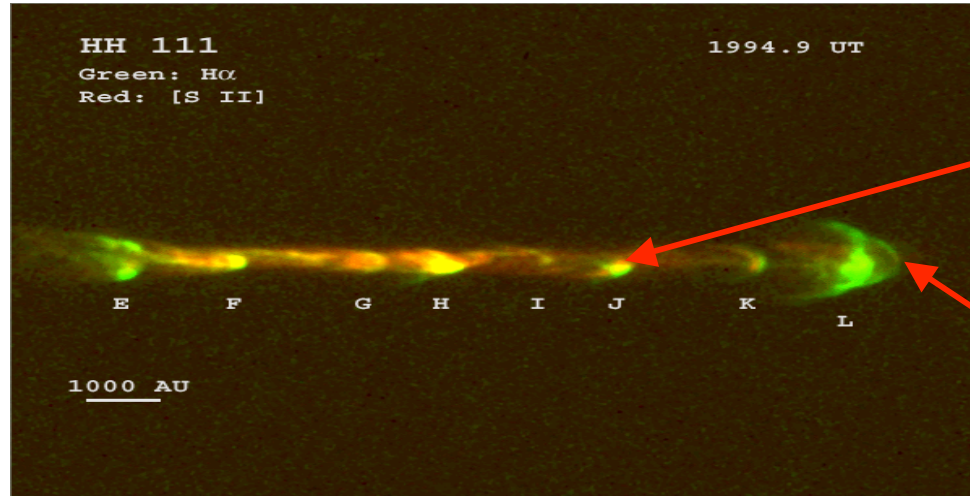
## Use of lasers and

### Z-pinches:

**Twisted magnetic field lines**

Lebedev et al., Ciardi et al., etc...

# HERBIG-HARO OBJECTS

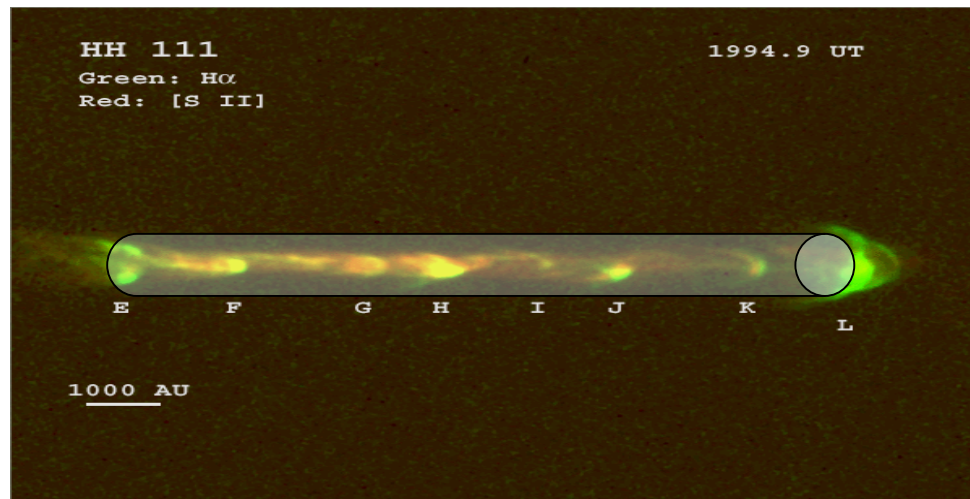


## Knots:

- Kelvin-Helmholtz instability (interface : shear with the ambient medium)
- Pulsating source

## Bow shock:

- Structure
- Stability

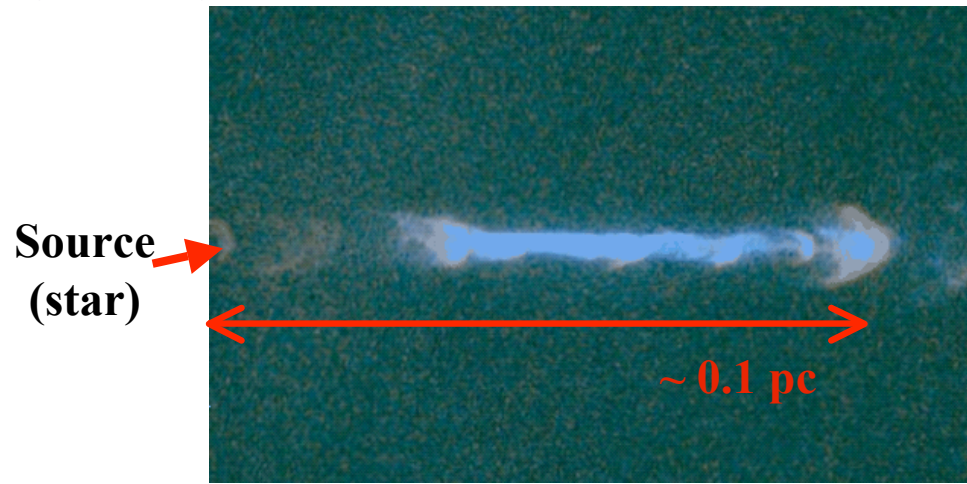


## COLLIMATION

- Radiative cooling ?
- Magnetic field ?
- Both ?



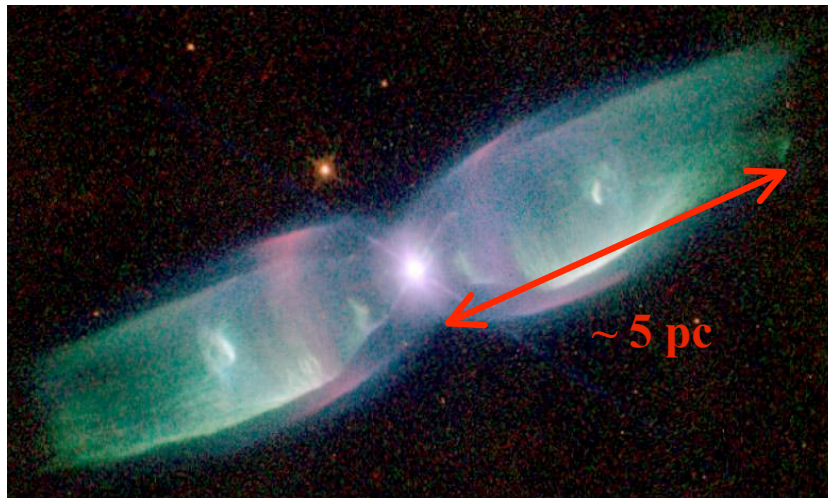
# WHERE ELSE DO WE FIND JETS ?



Source  
(star)

~ 0.1 pc

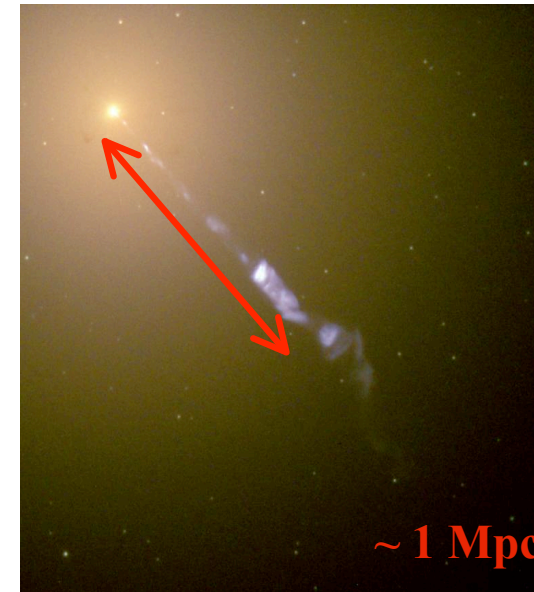
Young stars



Planetary nebulae

1 a.u =  $1.5 \cdot 10^{12}$  cm , 1 pc =  $3 \cdot 10^{18}$  cm

From a black hole



~ 1 Mpc

X-binaries (SS433)

QUASARS

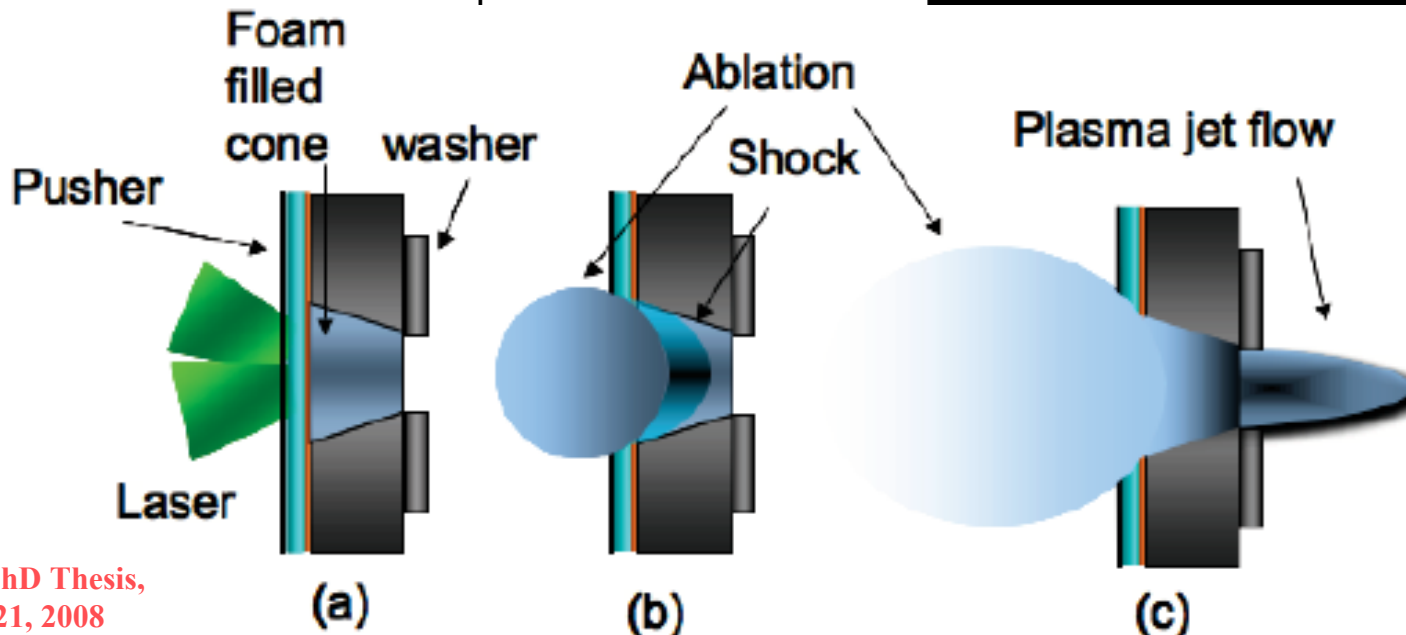
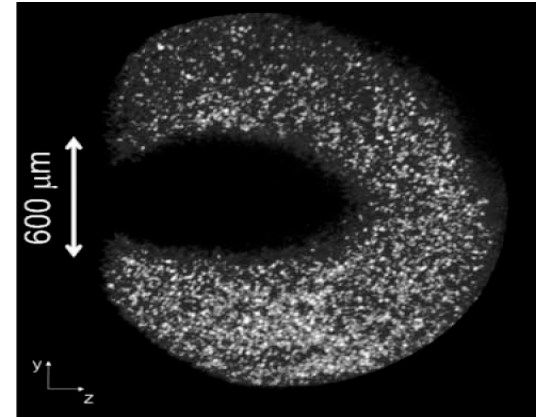
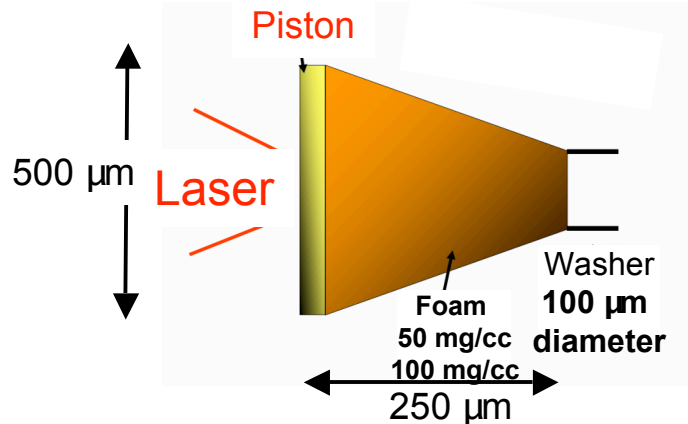
(Radio-emission of galaxy core)

QSO

(galaxy core, no emission)

# CH-FOAM FILLED CONES

## Shadowgraphy 10 ns after the shock break-out (LULI)



B. LOUPIAS, PhD Thesis,  
Paris, October 21, 2008

B. Loupias et al., Phys. Rev. Lett. 99 (2007) 265001

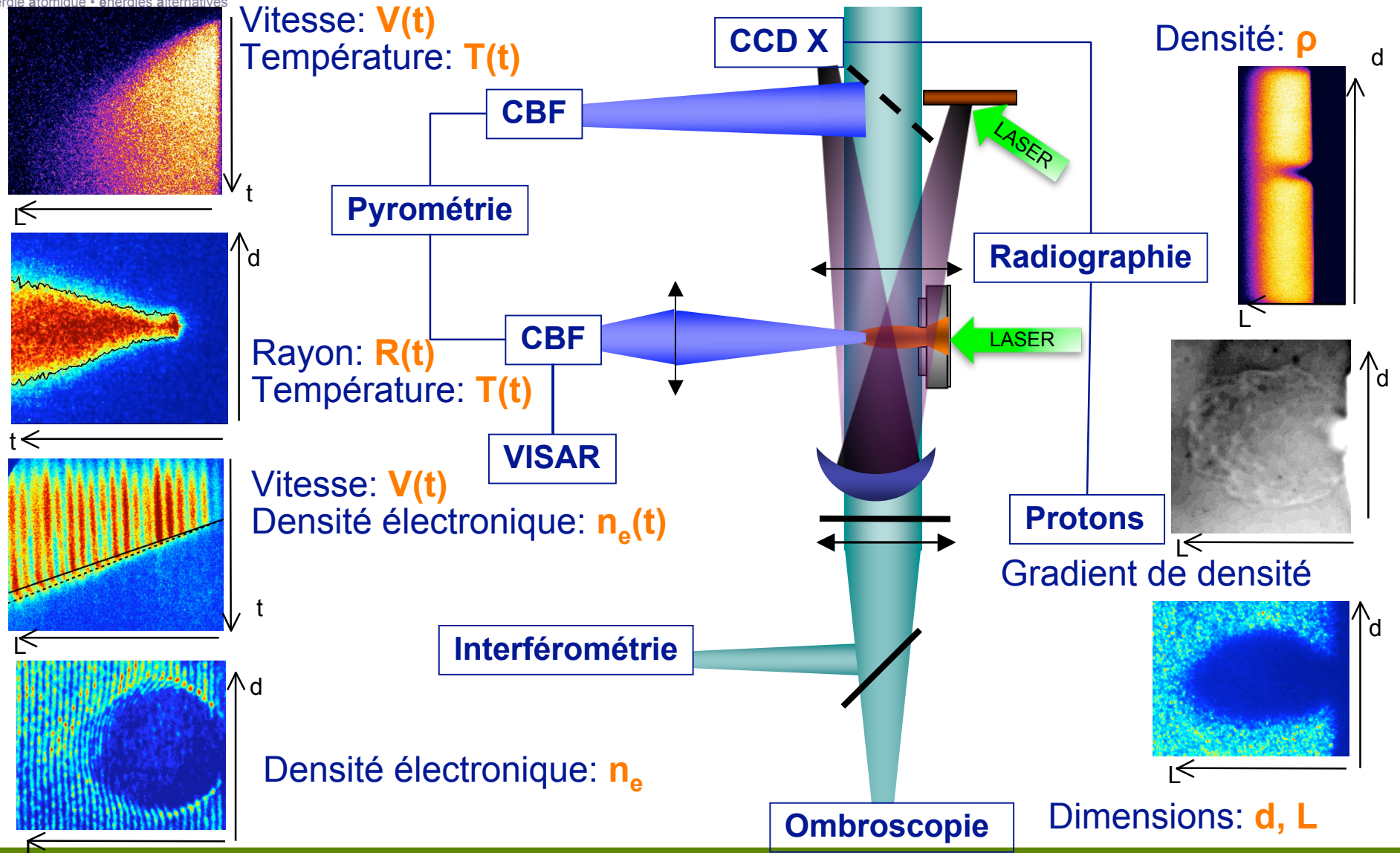
C.D. Gregory et al., PPCF 50(2008)124039

B. Loupias et al., Plasma Phys. Controlled Fus. 51 (2009) 124027

C.D. Gregory et al., PoP 17(2010)052708

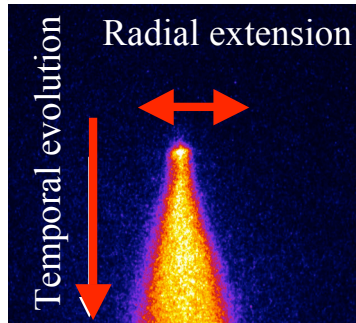
# SEVERAL DIAGNOSTICS

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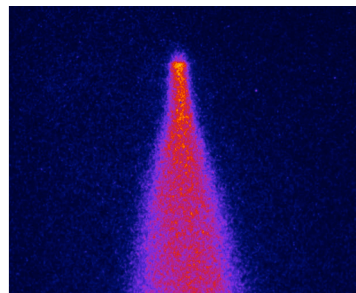


# COMPARISON BETWEEN THEORY and JET EXPERIMENTS

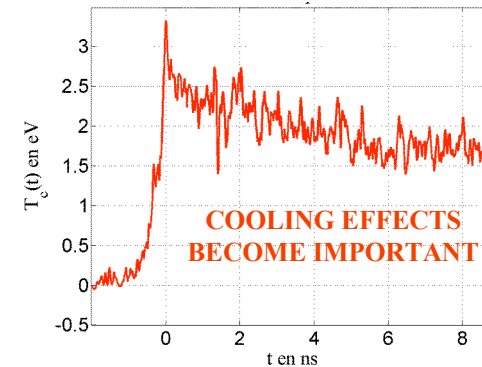
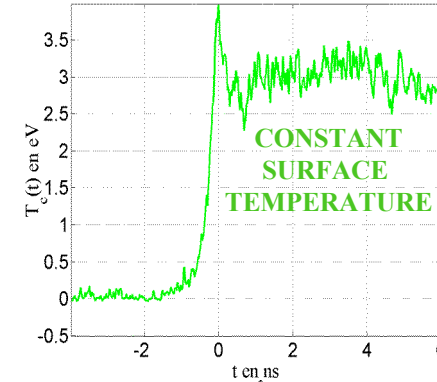
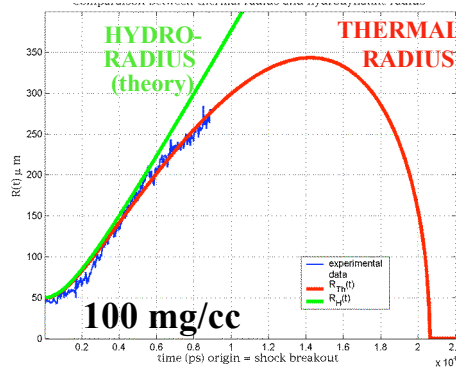
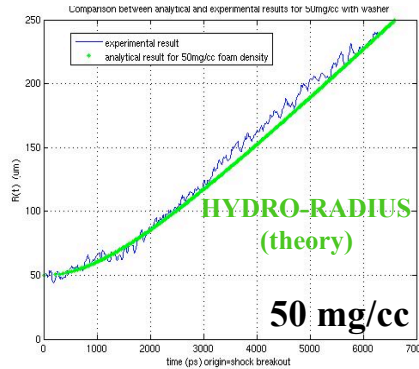
energie atomique • energies alternatives



Into vacuum



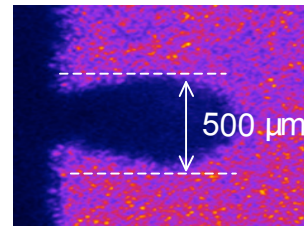
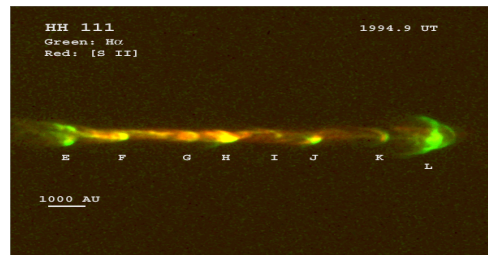
Into vacuum



	Re	Pe = $F_{conv}/F_{cond}$	$\chi = t_{cool}/t_{dyn}$	Mach	$\zeta = \lambda_{mfp}/L_{hydro}$
YSO jet	$10^7$	$10^6$	0.1 - 10	10 - 30	$10^{-7}$
Exp. 5 ns	$10^6$	$10^3$	100	2	$10^{-7}$
Exp. 25 ns	$10^5$	$10^2$	10	20	$10^{-7}$

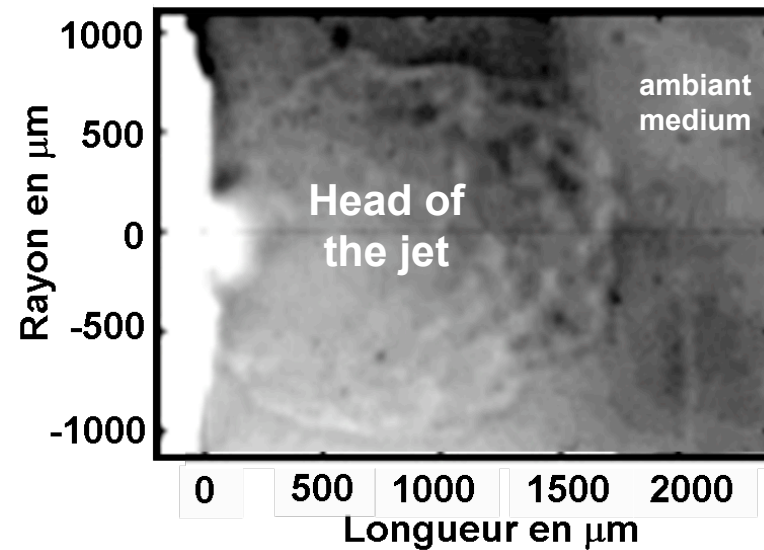
E. FALIZE, PhD Thesis,  
Paris, October 23, 2008

E. Falize et al., Journal Physics: Conf. Series 112 (2008) 042015; Astrophys. Space Science (2009)



Into vacuum

Into argon gas (ambient medium),  $t = 30 \text{ ns}$



Rayleigh – Taylor instability (RTI):

$$\omega = \sqrt{At \cdot g \cdot k}$$

$$At = \frac{\rho_2 - \rho_1}{\rho_2 + \rho_1} : \text{Atwood, } \rho_2: \text{heavy, } \rho_1: \text{light, } g: \text{deceleration, } k: \text{wave number}$$

$$\rho_2 = 1 \text{ mg/cc, } \rho_1 = 0.04 \text{ mg/cc, } \eta = \rho_{\text{jet}} / \rho_{\text{ambient}} = 25 (= 0.1 - 10), At = 1$$

$$g = 60 \text{ (km/s)} / 30 \text{ (ns)} = 2 \text{ } \mu\text{m} / (\text{ns})^2, \lambda = 100 \text{ } \mu\text{m}$$

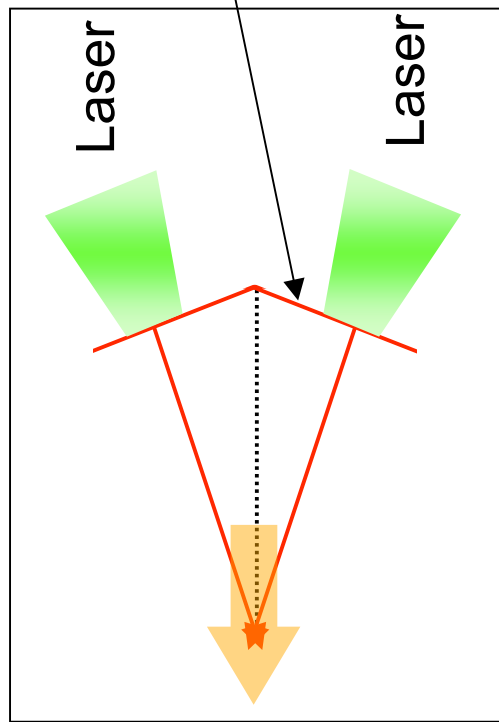
$$\tau_{RTI} = 1 / \omega \approx 3 \text{ ns}$$

RTI may play a role in the structure of the BOW SHOCK

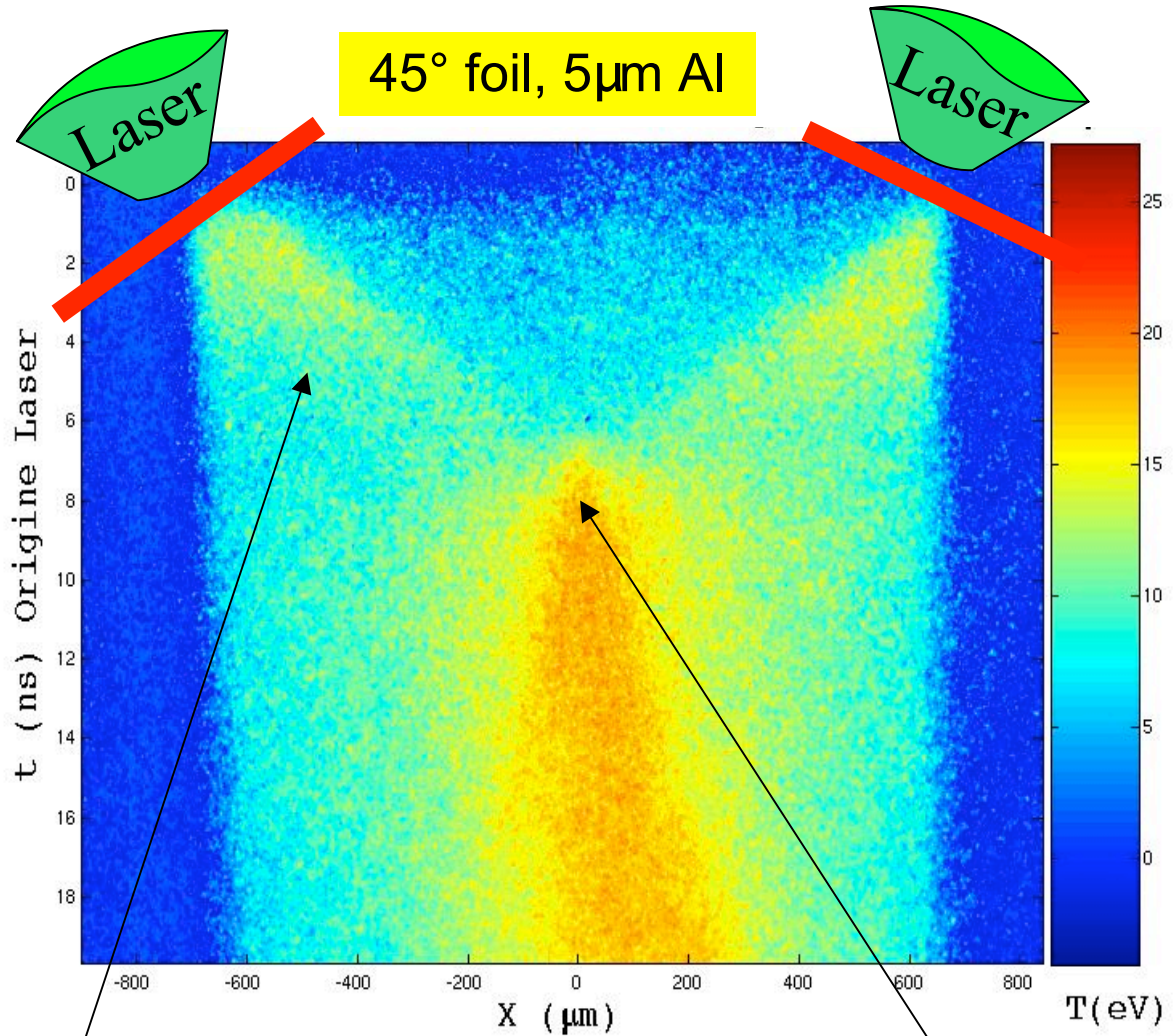
HIGHER RESOLUTION REQUIRED IN OBSERVATIONS + Compressible effects ...

# ANOTHER TYPE of TARGET

## V-FOIL TARGET



COLLIDING PLASMAS

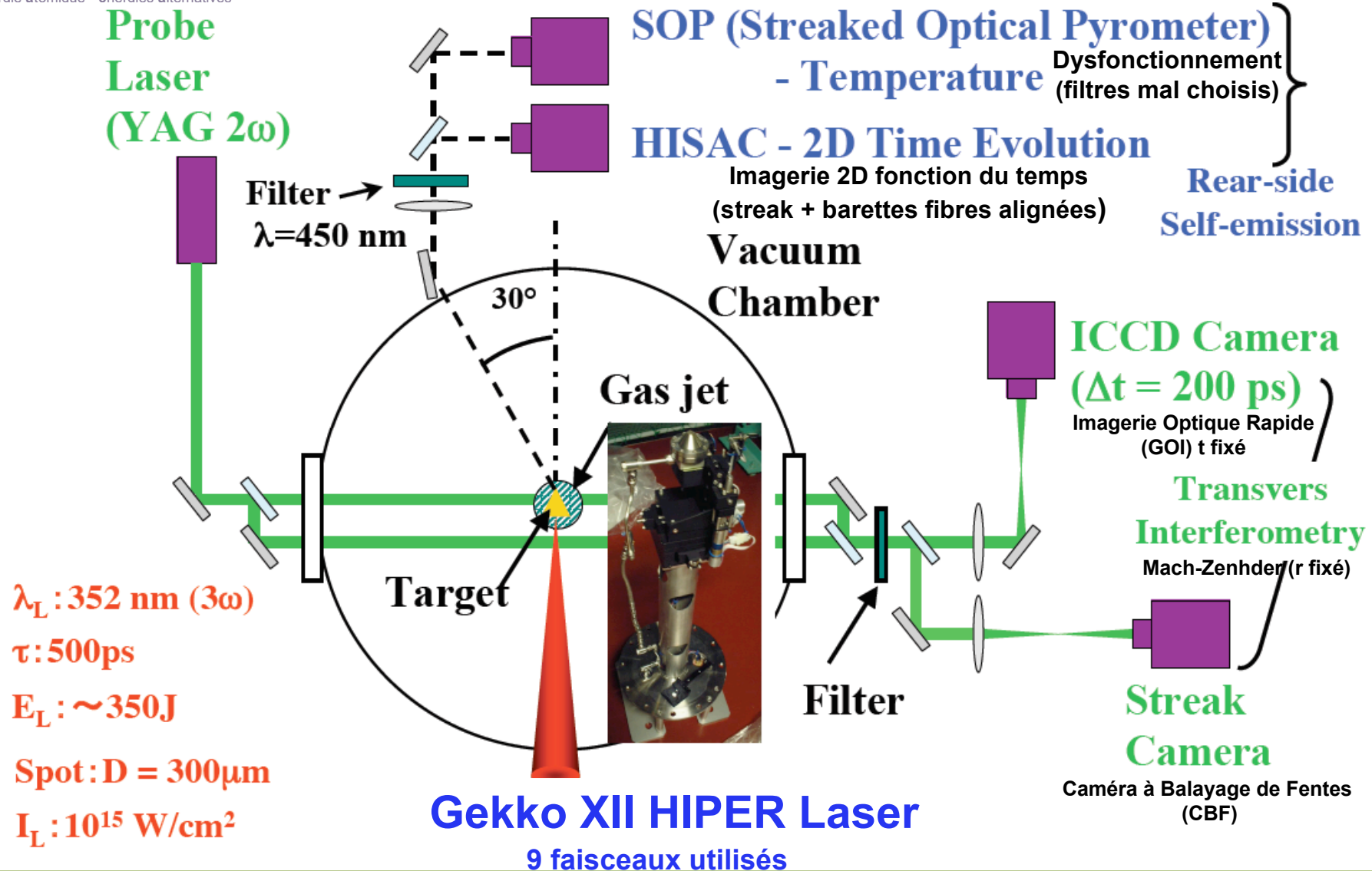


Rear side plasma expansion

Collision

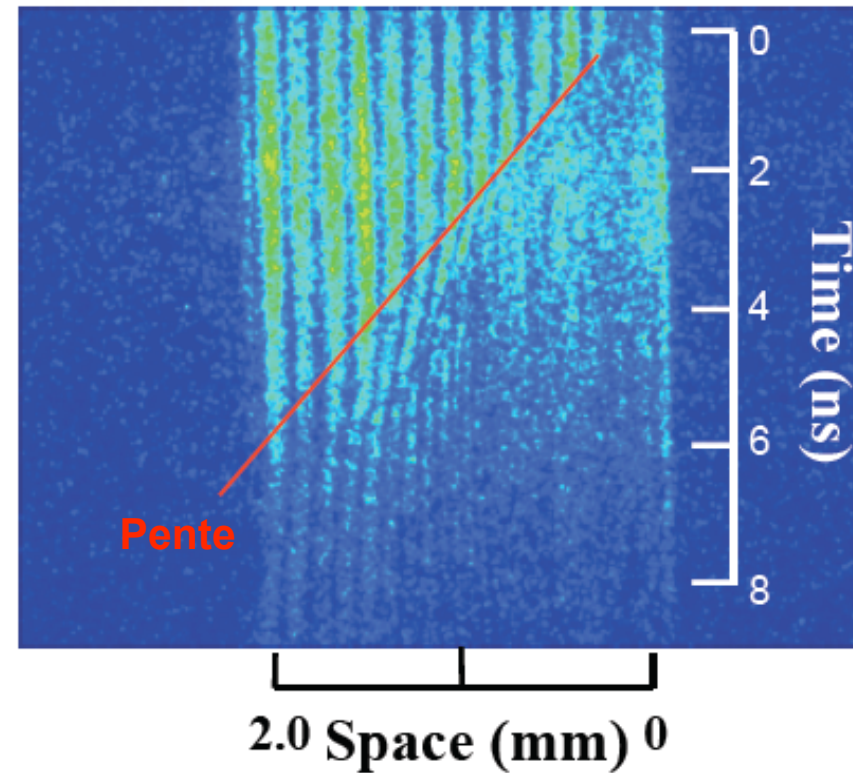
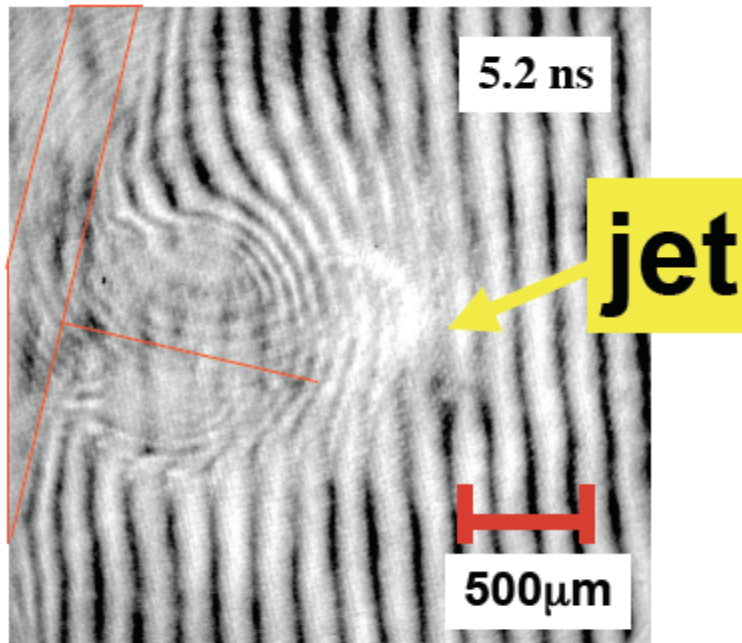
# GEKKO EXPERIMENTAL SET-UP

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# TRANSVERSE INTERFEROMETRY

Vitesse de propagation + densité électronique  $n_e(r \text{ fixé}, z, t)$



Jet velocity = 2/6 mm/ns : environ **330 km/s**

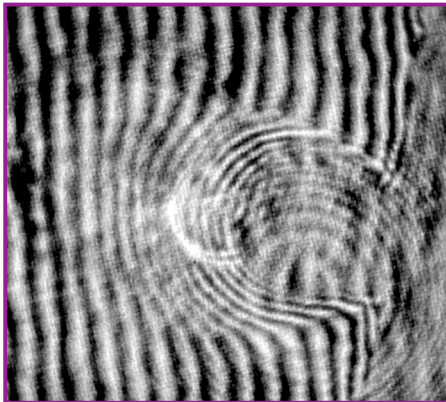


# WITH NO AMBIENT GAS

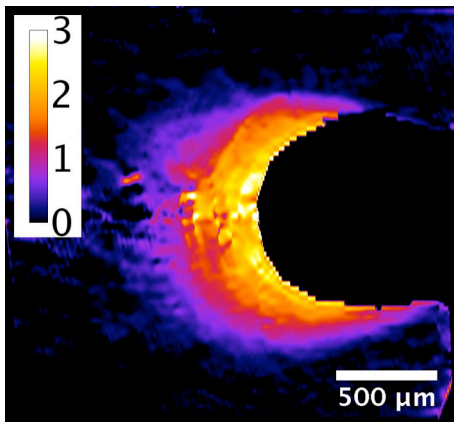
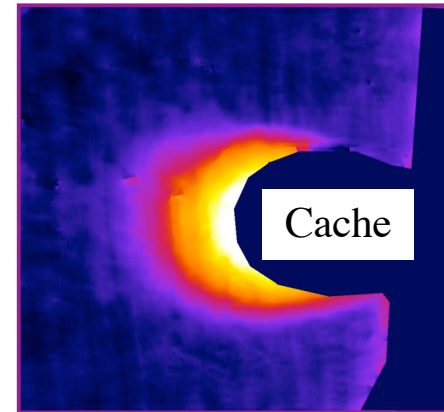
To generate higher temperature, the beams were focused directly into the foam to propagate **radiative shock** through the foam.

## Interferometry result without ambient gas

7ns



Phase map result



$$\delta\phi = \int \frac{\omega n_e}{2n_c c} dl \quad \longrightarrow \quad n_e(r, z, t \text{ fixé})$$

$\delta\phi$  = phase shift       $\omega$  = frequency

$n_c$  = critical density       $c$  = speed of light

$l$  = length of plasma traversed by probe beam

Jet velocity : **285km/s**

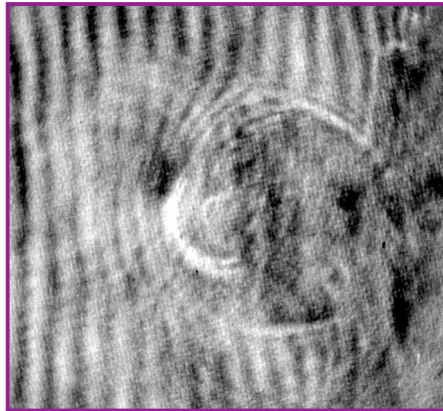
The scale is  $n_e \times 10^{19}$  per cc

# WITH AMBIENT GAS

## Interferometry result with ambient gas

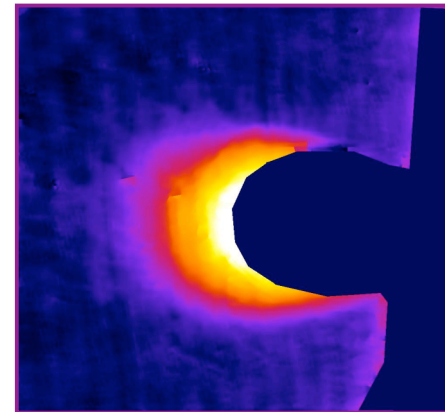
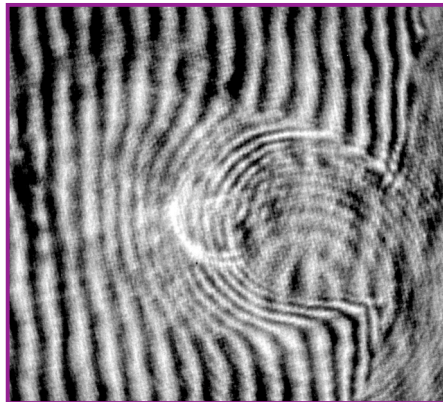
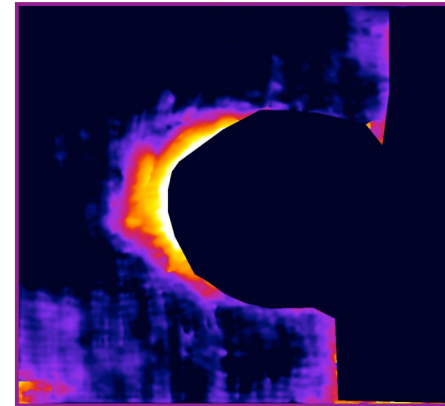
Helium gas: Pressure 1 atm, atom density =  $3 \cdot 10^{19} \text{ cm}^{-3}$

7ns



Phase map  
result

Jet velocity :  
**250km/s**



**The ambient medium seems to confine and slow down the plasma propagation ahead of jet.**



## **ET AUSSI LES LOIS D'ECHELLE ...**



# INVARIANCE and SCALING LAWS

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Model equation: Non-linear heat equation

$$\frac{\partial T}{\partial t} = D \cdot \frac{\partial^2 T^n}{\partial x^2}$$

**T**: temperature (D: diffusion coefficient = cst.)

Solution: **T = S(x,t)** where **S** is a known function

INVARIANCE under the transformation:  $A_x$ ,  $A_t$  and  $A_T$  : **Scaling parameters**

D. Ryutov et al., ApJ 518 (1999) 821

Independent variables:  $x$  and  $t$

$$x = A_x \cdot \bar{x}, \quad t = A_t \cdot \bar{t}$$

Dependent variable:  $T(x,t)$

$$T = A_T \cdot \bar{T}$$

$$\frac{A_T}{A_t} \cdot \frac{\partial \bar{T}}{\partial \bar{t}} = \frac{(A_T)^n}{(A_x)^2} \cdot D \cdot \frac{\partial^2 \bar{T}^n}{\partial \bar{x}^2}$$

$$\frac{\partial \bar{T}}{\partial \bar{t}} = \frac{A_t (A_T)^{n-1}}{(A_x)^2} \cdot D \cdot \frac{\partial^2 \bar{T}^n}{\partial \bar{x}^2}$$

$$\boxed{\frac{\partial \bar{T}}{\partial \bar{t}} = D \cdot \frac{\partial^2 \bar{T}^n}{\partial \bar{x}^2}} \quad \boxed{\frac{A_t \cdot (A_T)^{n-1}}{(A_x)^2} = 1}$$

$A_x$  and  $A_t$  are arbitrary !

$$A_T = [(A_x)^2 / (A_t)]^{1/(n-1)}$$

The equation is **invariant** under the transformation

Solution:  $\bar{T} = \bar{S}(\bar{x}, \bar{t})$  but  $\bar{S} = S$

The solution is **invariant**

The solution is **the same** at **both scales**

# INVARIANCE OF RADIATION HYDRODYNAMICS ?

## Optically thin radiation hydrodynamics

$$\bullet \frac{\partial \rho}{\partial t} + \vec{\nabla}_N \cdot [\rho \vec{v}] = 0$$

N=0: plane, N=1: cylindrical, N=2: spherical geometry

$$\bullet \left[ \frac{\partial}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \right] \cdot \vec{v} = -\frac{1}{\rho} \vec{\nabla} P \quad \text{and} \quad \left[ \frac{\partial}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \right] \cdot P - \gamma \frac{P}{\rho} \cdot \left[ \frac{\partial}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \right] \cdot \rho = -(\gamma - 1) \cdot \Lambda(\rho, P)$$

$\Lambda(\rho, P)$  = cooling function

$$\Lambda(\rho, P) \rightarrow \Lambda(\rho, T)$$

$$P = C_{EOS}(Z) \cdot \rho^\mu \cdot T^\nu$$

$C_{EOS}$  = constant

exponents  $\mu$  and  $\nu$  and  $\gamma = (\nu - \mu) / (\nu - 1)$ , I.G.:  $\mu = \nu = 1$

$$\Lambda(\rho, P) = \Lambda_0 \cdot \rho^\epsilon \cdot P^\zeta$$

$\Lambda_0$  = constant

power law form

exponents  $\epsilon$  and  $\zeta$

## • Invariance ? Scaling parameters: $A_q$ (q: any physical quantity)

$$t_{\text{astro}} = A_t \cdot t_{\text{lab}}$$

$$v_{\text{astro}} = A_v \cdot v_{\text{lab}}$$

$$T_{\text{astro}} = A_T \cdot T_{\text{lab}}$$

$$C_{EOS, \text{astro}} = A_{C_{EOS}} \cdot C_{EOS, \text{lab}}$$

$$x_{\text{astro}} = A_x \cdot x_{\text{lab}}$$

$$p_{\text{astro}} = A_p \cdot p_{\text{lab}}$$

$$\Lambda_{\text{astro}} = A_\Lambda \cdot \Lambda_{\text{lab}}$$

$$\Lambda_{b, \text{astro}} = A_{\Lambda_b} \cdot \Lambda_{b, \text{lab}}$$

$$\rho_{\text{astro}} = A_\rho \cdot \rho_{\text{lab}}$$

**Yes !**

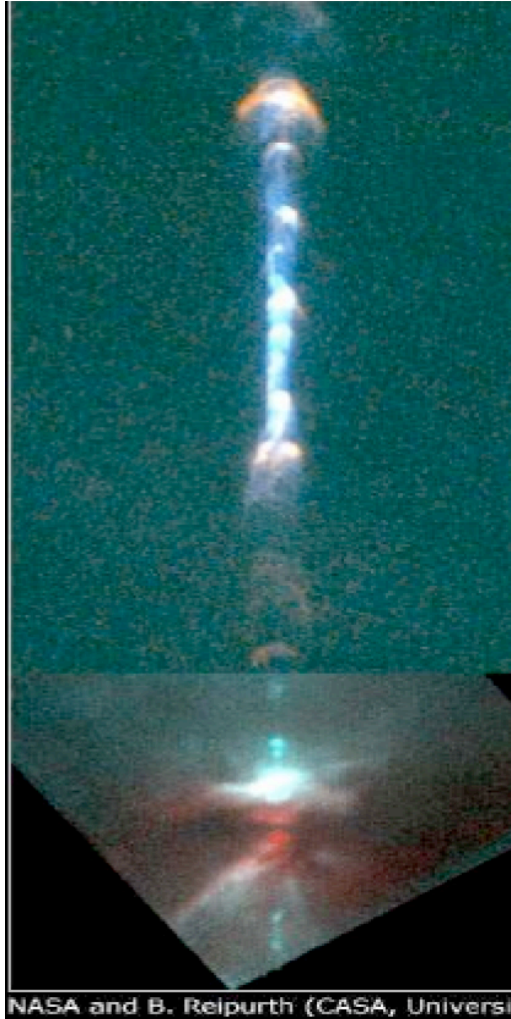
# ASTROPHYSICS and LABORATORY EXPERIMENTS

$$A_\rho \equiv \rho_{\text{astro}}/\rho_{\text{lab}}, \quad A_P \equiv P_{\text{astro}}/P_{\text{lab}}, \quad A_\rho \approx 3 \quad A_P \approx 2 \cdot 10^{-19}$$

TWO CONDITIONS TO FIND  $A_\rho$  and  $A_P$ :

Velocities about 100 km/s in both cases and YSO time scale = 1000 years

(length: 0.1 pc) and laser jet time scale = 10 ns



NASA and B. Reipurth (CASA, University of Arizona)

**HH 111**

Physical quantities	Cold protostellar jet (HH111)	Experimental values	Scaling factor
Length (cm)	$3 \cdot 10^{17}$	0.1 (1 mm)	$3 \cdot 10^{18}$
Time (s)	$3 \cdot 10^{10}$ (1000 y)	$10^{-8}$ (10 ns)	$3 \cdot 10^{18}$
Velocity (km/s)	100	100	1
Density (g/cm <sup>3</sup> )	$10^{-22}$	$10^{-3}$ (1 mg/cc)	$10^{-19}$ ( $\approx A_\rho$ )
Density (part/cm <sup>3</sup> )	100	$5 \cdot 10^{20}$	$2 \cdot 10^{-19}$
Temperature (K)	10 000	10 000	1



- 1) - LABORATORY ASTROPHYSICS**
- 2) - LASER FACILITIES**
- 3) - ASTROPHYSICAL RADIATIVE SHOCKS (RS)  
and LASER EXPERIMENTS**
- 4) - ASTROPHYSICAL JETS and LASER  
EXPERIMENTS**
- 5) - CONCLUSION**

# CONCLUSION

- 1) – For the first time, rigorous derivation of scaling laws have been made and the connection between experiments and astrophysical objects is 1 to 1
- 2) – Coherence, consistence and redundance of the models
- 3) – Laboratory astrophysics is a relevant approach in spite of some difficulties: [Rad. Shocks, for instance.](#)

BUT:

- I have neglected  $E_{rad}$  and  $P_{rad}$  in the rescaling
- Although we know radiation produces significant  $E_{rad}$  and  $P_{rad}$  in SNe,
- And this is not yet achieved in laboratory experiments.

- 4) – EoS ( $H_2$ ,  $H_2+He$ ), opacities of heavy elements (N, C, O, Fe)

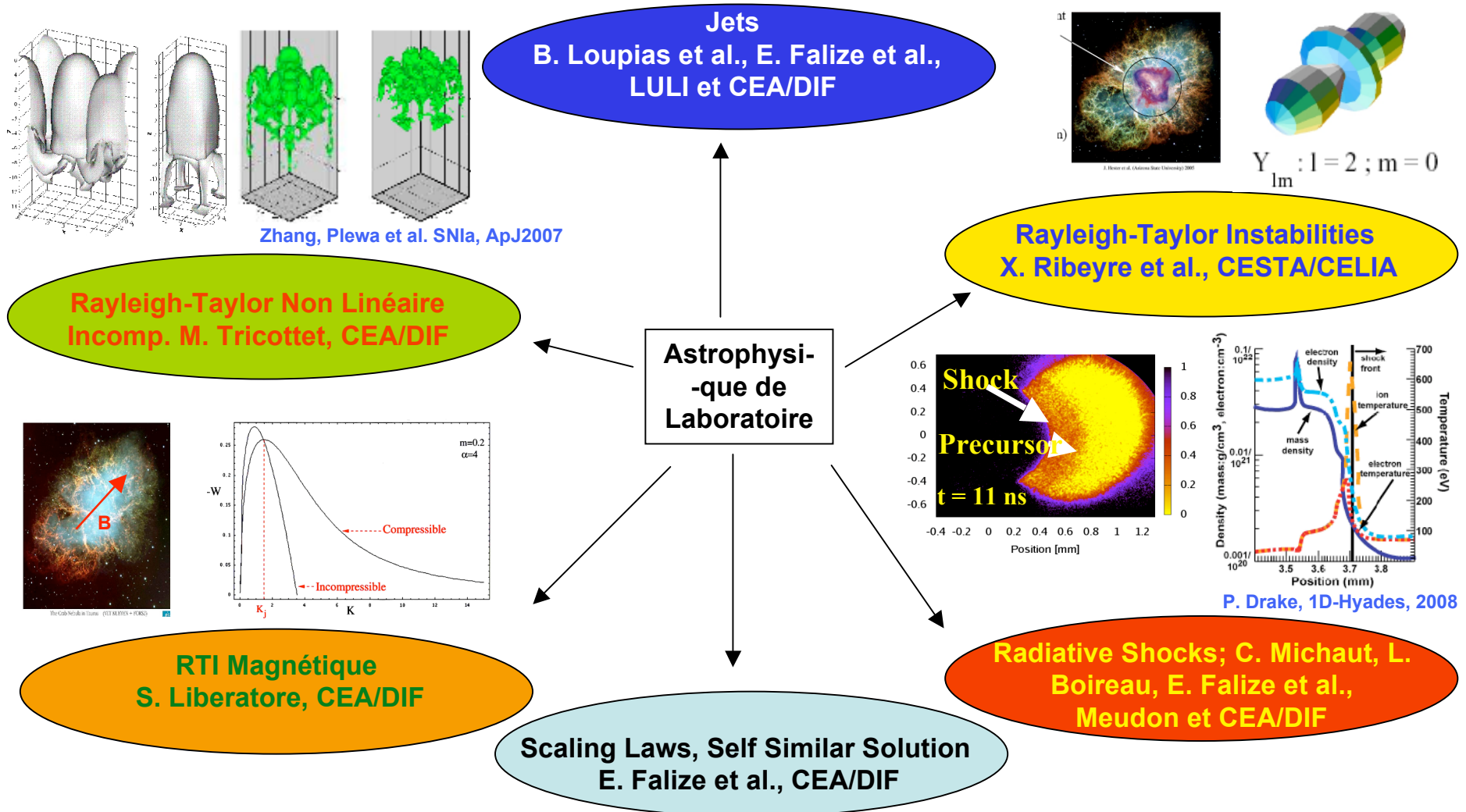
[P. LOUBEYRE \(CEA\)](#), [GUYOT \(Jussieu\)](#), [MAZEVET \(LUTH\)](#), [KOENIG \(LULI\)](#), [TURCK-CHIEZE \(CEA\)](#), [CHIEZE \(CEA\)](#) ...



# CONCLUSION (following)

energie atomique • énergies alternatives

**Lois d'Echelle :** Assise et justification de l'approche « Astrophysique de Laboratoire »





energie atomique • energies alternatives

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**Thank you !**