

# Flavour Physics: in the Standard Model and beyond

**Ecole de Gif 2012**

Physics at LHC

17 September - 21 September 2012, LAL Orsay, France

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Laboratory for High Energy Physics (LPHE)

Swiss Federal Institute of Technology Lausanne (EPFL)

Lausanne, Switzerland



# Plan of Lectures

- Direct-search versus Indirect-search
- Early History
- Standard Model Flavour Framework
- More of Weak Decay
- Current Status of  $V_{\text{CKM}}$
- Any Sign of New Physics
- Closer Look
- Epilogue

What is on the moon?



What is on the moon?



Of course going there...

What is on the moon?



Of course going there...



But you can study a lot from here before

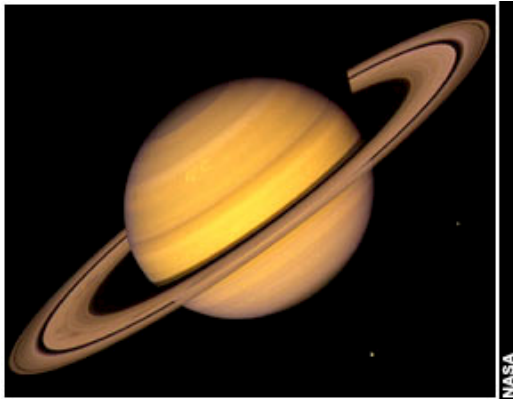
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And may be finding something new?

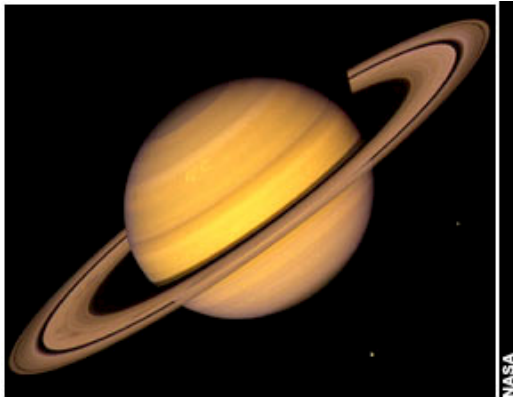
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And may be finding something new?



Instruments can be improved and

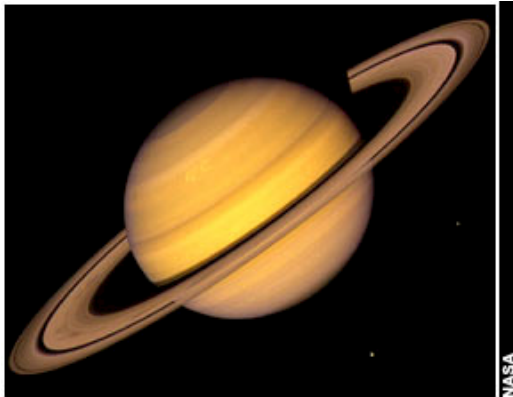
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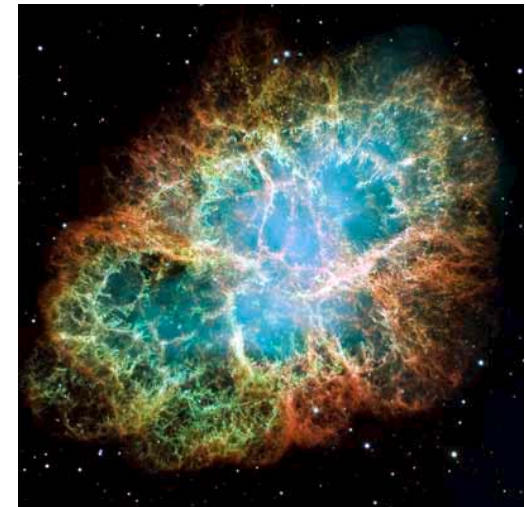
But you can study a lot from here before



And may be finding something new?



Instruments can be improved and



We see far beyond the direct reach...



# Plan of Lectures

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- **Early History**
- Standard Model Flavour Framework
- More of Weak Decay
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# Early History

Start with Isospin (Heisenberg)...

→ p and n are the doublets under SU(2)  
similarly  $\pi^+$ ,  $\pi^0$  and  $\pi^-$  are the triplets under O(3)



p and n (or  $\pi^+$ ,  $\pi^0$  and  $\pi^-$ ) are identical when switching off electromagnetic interactions, i.e. nuclear forces

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“Strangeness” played a role in establishing  
the concept of flavour quantum numbers  
(Gell-Mann 56, Nishijima 55)



Response to the discovery of long living particles (1947)  
selection rule based on a quantum number which is  
conserved in strong and electromagnetic interactions  
but not conserved in weak interactions

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(Gell-Mann 56, Nishijima 55)

“quark” in early 1960’s  
(Gell-Mann, Ne’eman, Han-Nambu, Nishijima, Sakata, Zweig, etc.)  
SU(3) flavour symmetry: (u, d, s)



Responding to the particle zoo, in particular the hyperons

# Early History

Start

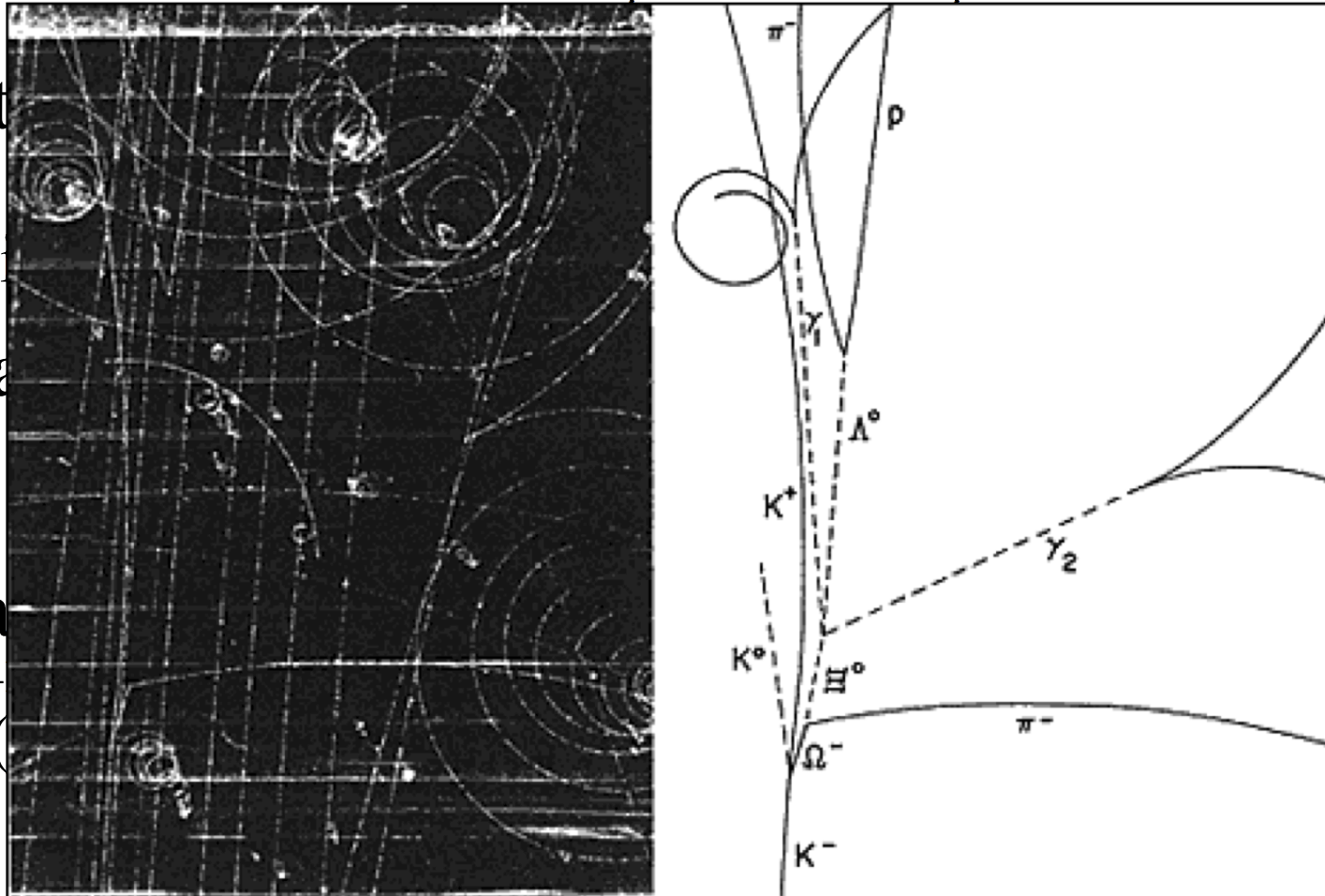
sim

“Stra

“qua

(Gell-

SU(



→  $\Omega^-$  (sss) prediction,  
discovered in 1964, Barmes et al.

# Early History

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My private reflection

Colour was needed for the constituent quark model:

$\Delta^{++}(Q=+2, \text{Spin } 3/2 \text{ baryon}) = (\mathbf{u} \uparrow, \mathbf{u} \uparrow, \mathbf{u} \uparrow)$ .

We know now: the spin of baryon is given little by the valence quark...?

# Early History

## Particle ( $K^0$ )-antiparticle ( $\bar{K}^0$ ) mixing:

PHYSICAL REVIEW

VOLUME 97, NUMBER 5

MARCH 1, 1955

### Behavior of Neutral Particles under Charge Conjugation

M. GELL-MANN,\* *Department of Physics, Columbia University, New York, New York*

AND

A. PAIS, *Institute for Advanced Study, Princeton, New Jersey*

(Received November 1, 1954)

Some properties are discussed of the  $\theta^0$ , a heavy boson that is known to decay by the process  $\theta^0 \rightarrow \pi^+ + \pi^-$ . According to certain schemes proposed for the interpretation of hyperons and  $K$  particles, the  $\theta^0$  possesses an antiparticle  $\bar{\theta}^0$  distinct from itself. Some theoretical implications of this situation are discussed with special reference to charge conjugation invariance. The application of such invariance in familiar instances is surveyed in Sec. I. It is then shown in Sec. II that, within the framework of the tentative schemes under consideration, the  $\theta^0$  must be considered as a "particle mixture" exhibiting two distinct lifetimes, that each lifetime is associated with a different set of decay modes, and that no more than half of all  $\theta^0$ 's undergo the familiar decay into two pions. Some experimental consequences of this picture are mentioned.

$$K^0 \leftrightarrow \pi^+\pi^- \leftrightarrow \bar{K}^0 \longrightarrow \begin{aligned} K_1 &= \frac{K^0 + \bar{K}^0}{\sqrt{2}} \\ K_2 &= \frac{K^0 - \bar{K}^0}{\sqrt{2}} \end{aligned}$$

under C symmetry,  $K_1$  and  $K_2$   
two very different lifetimes

Why?

(later  $\mathcal{C}$  discovered  $\rightarrow$  change to CP conservation)

# Early History

## Observation of Long-Lived Neutral $V$ Particles\*

Phys Rev Lett. 1956

K. LANDE, E. T. BOOTH, J. IMPEDUGLIA, AND L. M. LEDERMAN,  
*Columbia University, New York, New York*

AND

W. CHINOWSKY, *Brookhaven National Laboratory,  
Upton, New York*

(Received July 30, 1956)

cloud chamber exposure at BNL

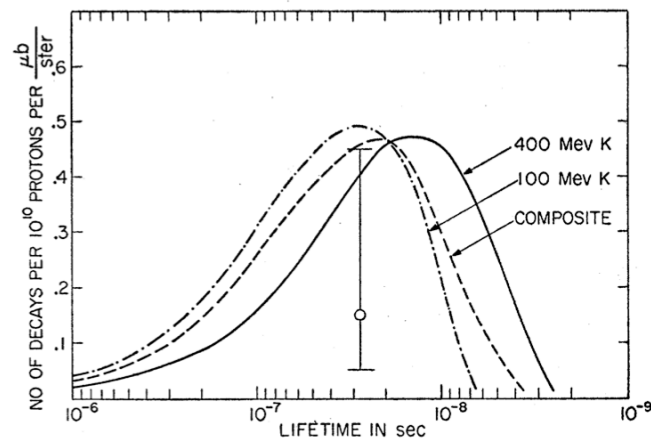


FIG. 2. Detection sensitivity for  $K$  mesons as function of lifetime. The composite curve is obtained with the spectra of reference 5. The point indicates the observed yield with a production cross section of  $\sim 20 \mu\text{b/sterad}$ .

lifetime for  $\pi^+\pi^-$  decay already known to be  $\sim 10^{-10}$  sec

lifetime measurement for 3-body decays ( $\pi\mu\nu, \pi e\nu, \pi^+\pi^-\pi^0$ )  $> 10^{-9}$  sec

Establish two particle states: short-living,  $K_S$ , decays into  $2\pi$  and long-living,  $K_L$ , decays into  $3\pi, \pi l\nu$ :  $K^0-\bar{K}^0$  mixing



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K. LANDE, E. T. BOOTH, J. IMPEDUGLIA, AND L. M. LEDERMAN,  
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AND

This seemed to have triggered the idea of  $\nu$ - $\bar{\nu}$  mixing (not the  $\nu$  flavour mixing) by Pontecorvo in 1957

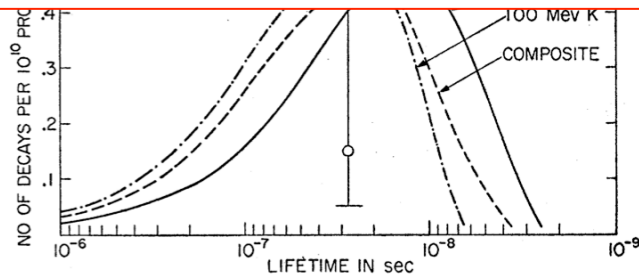


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# Early History

Cabibbo theory (Phys. Rev. Let. 1963)

UNITARY SYMMETRY AND LEPTONIC DECAYS

Nicola Cabibbo

CERN, Geneva, Switzerland

(Received 29 April 1963)

Why  $\Delta S=1$  decay process is suppressed?

e.g.  $\Gamma(K \rightarrow \mu\nu) \ll \Gamma(\pi \rightarrow \mu\nu)$  after correcting the phase space



Weak interaction charged current ( $\Delta Q=1$ )

$$J_\mu = \cos\theta \times j_\mu(\Delta S=0) + \sin\theta \times j_\mu(\Delta S=1)$$

$\theta$ : Cabibbo angle

(unitary through  $\cos^2\theta + \sin^2\theta = 1$ )

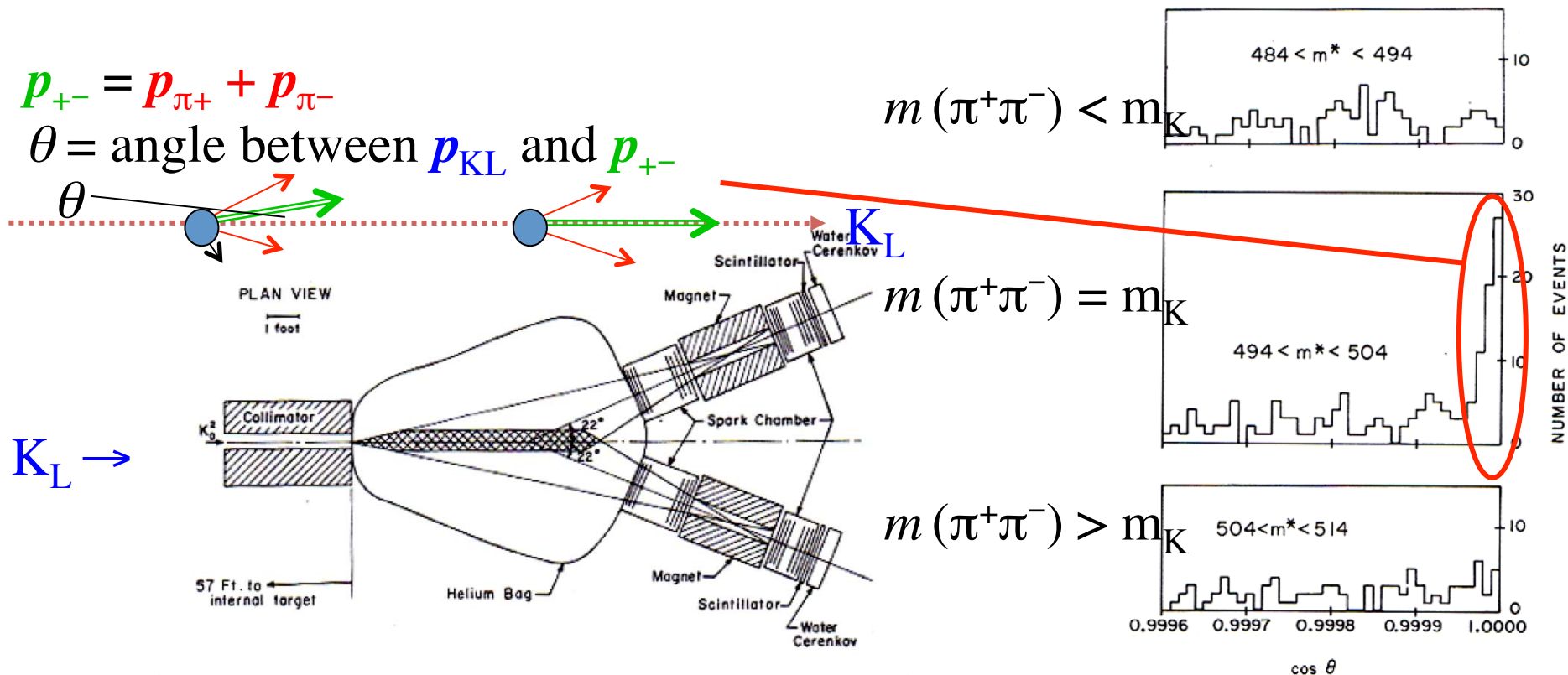
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CP violating  $K_L^0 \rightarrow \pi^+\pi^-$  decays: 1964, J.H. Christenson et al.



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UNITARY SYMMETRY AND LEPTONIC DECAYS

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CP violating  $K^0_L \rightarrow \pi^+\pi^-$  decays: 1964, J.H. Christenson et al.

This was beyond the comprehension of that time and no relation between the flavour considered:

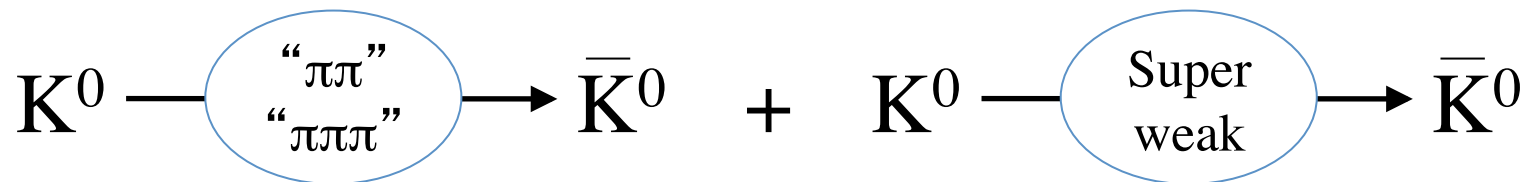
e.g. Superweak model (Phys. Rev. Let. 1964)

VIOLATION OF CP INVARIANCE AND THE POSSIBILITY OF VERY WEAK INTERACTIONS\*

L. Wolfenstein

Carnegie Institute of Technology, Pittsburgh, Pennsylvania

(Received 31 August 1964)



# Early History

Glashow–Iliopoulos–Maiani mechanism (Phys Rev D 1970)

Why  $\Delta m_K$  is so small and  $K_L \rightarrow \mu^+ \mu^-$  very suppressed?

## Weak Interactions with Lepton-Hadron Symmetry\*

S. L. GLASHOW, J. ILIOPOULOS, AND L. MAIANI†

*Lyman Laboratory of Physics, Harvard University, Cambridge, Massachusetts 02139*

(Received 5 March 1970)

We propose a model of weak interactions in which the currents are constructed out of four basic quark fields and interact with a charged massive vector boson. We show, to all orders in perturbation theory, that the leading divergences do not violate any strong-interaction symmetry and the next to the leading divergences respect all observed weak-interaction selection rules. The model features a remarkable symmetry between leptons and quarks. The extension of our model to a complete Yang-Mills theory is discussed.

# Early History

Glashow–Iliopoulos–Maiani mechanism (Phys Rev D 1970)

Why  $\Delta m_K$  is so small and  $K_L \rightarrow \mu^+ \mu^-$  very suppressed?

Having 4<sup>th</sup> quark already considered in  $\sim 1964$  (even with the name “charm”)

(Gell-Mann, Tarjanne and Teplitz, Hara, Björken and Glashow, )

$\nu_\mu$  discovered in 1962, Lederman, Schwartz and Steinberger,

$$\begin{pmatrix} u \\ d' \end{pmatrix} \begin{pmatrix} c \\ s' \end{pmatrix} \begin{pmatrix} \nu_e \\ e \end{pmatrix} \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}$$

$$d' = d \cos \theta + s \sin \theta$$

$$s' = -d \sin \theta + s \cos \theta$$

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$\bar{s}$	$\bar{u} \bar{c}$	$W^+$	$\nu_\mu$	$\mu^+$
$d$		$W^-$		$\mu^-$

$\bar{s}$	$\bar{u} \bar{c}$	$W^+$	$\bar{u} \bar{c}$	$\bar{d}$
$d$		$W^-$		$s$

$\bar{s}$	$W^+$	$\bar{u} \bar{c}$	$W^-$	$\bar{d}$
$d$		$u c$		$s$

$$Br(K^0 \rightarrow \mu^+ \mu^-) = F(m_c, \dots)$$

$$\Delta m_K = G(m_c, \dots)$$

$$\text{if } m_c = m_u, \propto \sin\theta \cos\theta - \sin\theta \cos\theta = 0$$

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Glashow–Iliopoulos–Maiani mechanism (Phys Rev D 1970)

Why  $\Delta m_K$  is so small and  $K_L \rightarrow \mu^+ \mu^-$  very suppressed?

Estimation of  $m_c \sim 1.5 \text{ GeV}$  (Gaillard and Lee, Phys Rev D 1974)

$K_L \rightarrow \mu^+ \mu^-$  suppressed

$K_L \rightarrow \gamma\gamma$  not suppressed

$\Delta m_K = m_L - m_S$  experimentally measured

$$d' = d \cos\theta + s \sin\theta$$

$$s' = -d \sin\theta + s \cos\theta$$

$\bar{s}$	$\bar{u} \bar{c}$	$W^+$	$\nu_\mu$	$\mu^+$
$d$		$W^-$		$\mu^-$

$$Br(K^0 \rightarrow \mu^+ \mu^-) = F(m_c, \dots)$$

$\bar{s}$	$\bar{u} \bar{c}$	$W^+$	$\bar{u} \bar{c}$	$\bar{d}$
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$\bar{s}$	$W^+$	$\bar{u} \bar{c}$	$W^-$	$\bar{d}$
$d$		$u c$		$s$

$$\Delta m_K = G(m_c, \dots)$$



# Early History

## Experimental Observation of a Heavy Particle $J/\psi$

J. J. Aubert, U. Becker, P. J. Biggs, J. Burger, M. Chen, G. Everhart, P. Goldhagen, J. Leong, T. McCorriston, T. G. Rhoades, M. Rohde, Samuel C. C. Ting, and Sau Lan Wu  
*Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139*

and

Y. Y. Lee

*Brookhaven National Laboratory, Upton, New York 11973*

(Received 12 November 1974)

We report the observation of a heavy particle  $J$ , with mass  $m = 3.1$  GeV and width approximately zero. The observation was made from the reaction  $p + \text{Be} \rightarrow e^+ + e^- + x$  by measuring the  $e^+e^-$  mass spectrum with a precise pair spectrometer at the Brookhaven National Laboratory's 30-GeV alternating-gradient synchrotron.

Mechanism (Phys Rev D 1970)

$\mu^+$  very suppressed?

and Lee, Phys Rev D 1974)

## Charm discovery with hadron and $e^+e^-$ machines

Aubert et al. and Augustin et al., 1974

### Discovery of a Narrow Resonance in $e^+e^-$ Annihilation\*

J.-E. Augustin,† A. M. Boyarski, M. Breidenbach, F. Bulos, J. T. Dakin, G. J. Feldman, G. E. Fischer, D. Fryberger, G. Hanson, B. Jean-Marie,† R. R. Larsen, V. Lüth, H. L. Lynch, D. Lyon, C. C. Morehouse, J. M. Paterson, M. L. Perl, B. Richter, P. Rapidis, R. F. Schwitters, W. M. Tanenbaum, and F. Vannucci‡

*Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305*

and

G. S. Abrams, D. Briggs, W. Chinowsky, C. E. Friedberg, G. Goldhaber, R. J. Hollebeek, J. A. Kadyk, B. Lulu, F. Pierre,§ G. H. Trilling, J. S. Whitaker, J. Wiss, and J. E. Zipse

*Lawrence Berkeley Laboratory and Department of Physics, University of California, Berkeley, California 94720*

(Received 13 November 1974)

We have observed a very sharp peak in the cross section for  $e^+e^- \rightarrow \text{hadrons}$ ,  $e^+e^-$ , and possibly  $\mu^+\mu^-$  at a center-of-mass energy of  $3.105 \pm 0.003$  GeV. The upper limit to the full width at half-maximum is 1.3 MeV.

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Aubert et al. and Augustin et al., 1974

Prog. Theor. Phys. Vol. 46 (1971), No. 5

## A Possible Decay in Flight of a New Type Particle

Kiyoshi NIU, Eiko MIKUMO  
and Yasuko MAEDA\*

*Institute for Nuclear Study  
University of Tokyo*

\*Yokohama National University

August 9, 1971

Emulsion exposed in a JAL Jet cargo plane  
One event of  $X \rightarrow \pi^0 + \text{one charged hadron}$

hypo.	$\pi^0 \pi^{\text{charged}}$	$\pi^0 p$
$\tau(\text{s})$	$2.2 \times 10^{-14}$	$3.6 \times 10^{-14}$
$m(\text{GeV})$	1.78	2.95

Observation of  $D \rightarrow K \pi^0$  decay in 1971?

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Third quark family (Kobayashi and Maskawa, Prog. Theor. Phys. 1973)

naturally introduces

CP violation

in weak interactions

**CP-Violation in the Renormalizable Theory  
of Weak Interaction**

Makoto KOBAYASHI and Toshihide MASKAWA

*Department of Physics, Kyoto University, Kyoto*

(Received September 1, 1972)

In a framework of the renormalizable theory of weak interaction, problems of CP-violation are studied. It is concluded that no realistic models of CP-violation exist in the quartet scheme without introducing any other new fields. Some possible models of CP-violation are also discussed.

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Flavour framework of the Standard Model established

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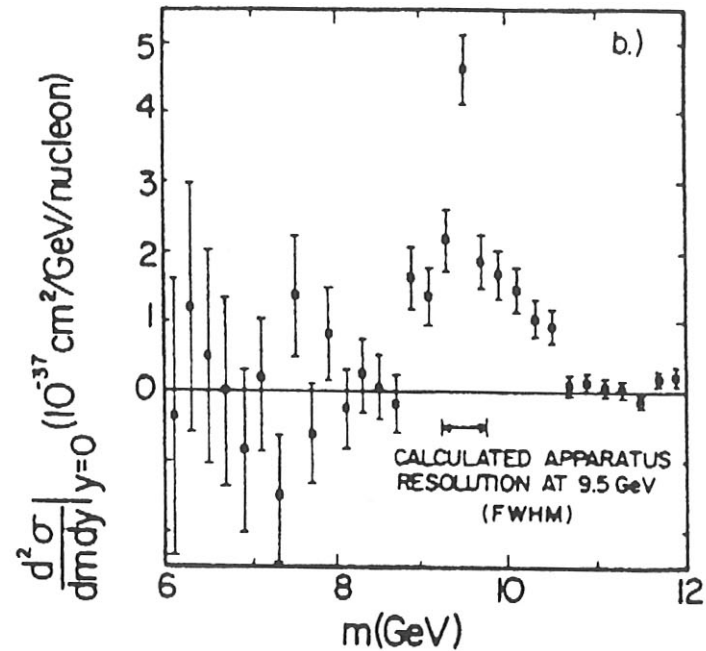
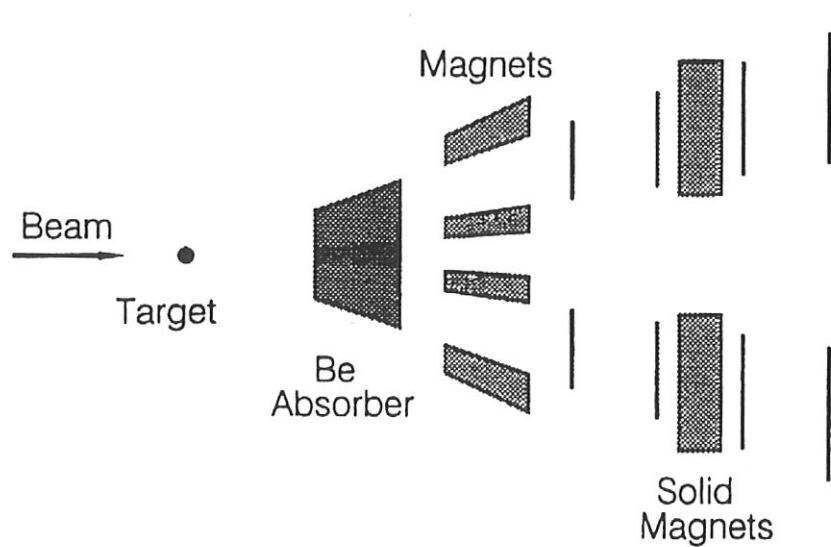
Third quark family (Kobayashi and Maskawa, Prog. Theor. Phys. 1973)

Flavour framework of the Standard Model established

And b quark discovered in 1977

# Early History

E288 experiment @ FNAL, S. Herb et al. in 1977



( $b\bar{b}$ ) bound states;  $\Upsilon(1S)$ ,  $\Upsilon(2S)$ ,  $\Upsilon(3S)$

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# Standard Model Flavour Framework

flavour eigenstates

-non-diagonal mass matrix

-strong and EM interactions

-flavour conservation

⇒

mass eigenstates

-diagonal mass matrix

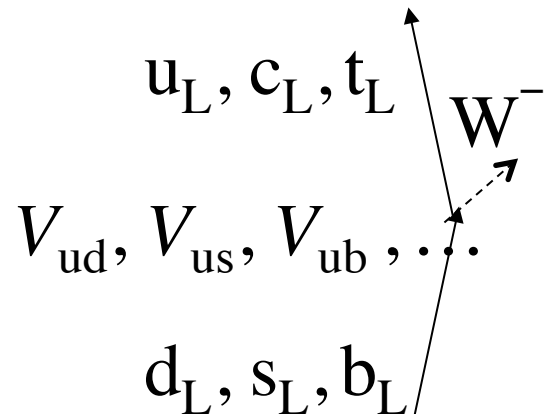
-weak interactions

-flavour changing

# Standard Model Flavour Framework

flavour eigenstates

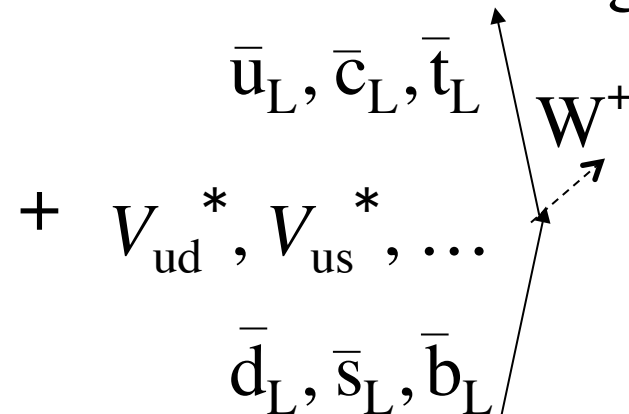
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$\Rightarrow$

masseigenstates

- diagonal mass matrix
- weak interactions
- flavour changing

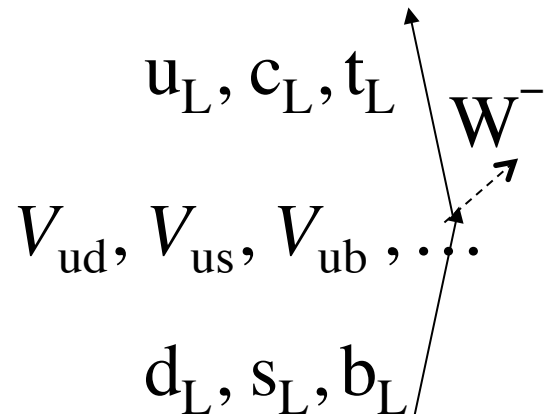


$$L \propto V_{ij} \bar{U}_i \gamma^\mu (1-\gamma_5) D_j W_\mu^\dagger + V_{ij}^* \bar{D}_i \gamma^\mu (1-\gamma_5) U_j W_\mu$$

# Standard Model Flavour Framework

flavour eigenstates

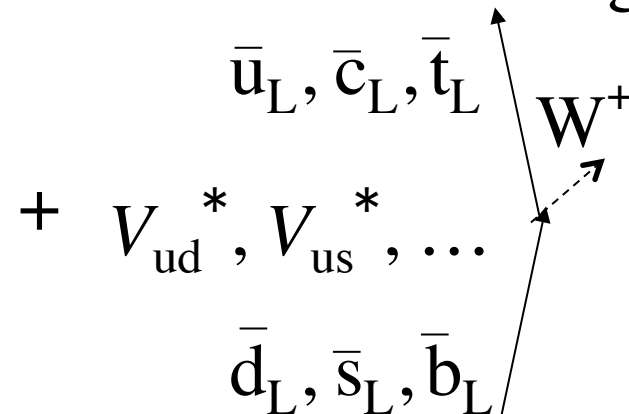
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$\Rightarrow$

masseigenstates

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- weak interactions
- flavour changing



$$L \propto V_{ij} \bar{U}_i \gamma^\mu (1-\gamma_5) D_j W_\mu^\dagger + V_{ij}^* \bar{D}_i \gamma^\mu (1-\gamma_5) U_j W_\mu$$

$\Updownarrow$  CP conjugation

$$L_{\text{CP}} \propto V_{ij} \bar{D}_i \gamma^\mu (1-\gamma_5) U_j W_\mu + V_{ij}^* \bar{U}_i \gamma^\mu (1-\gamma_5) D_j W_\mu^\dagger$$

# Standard Model Flavour Framework

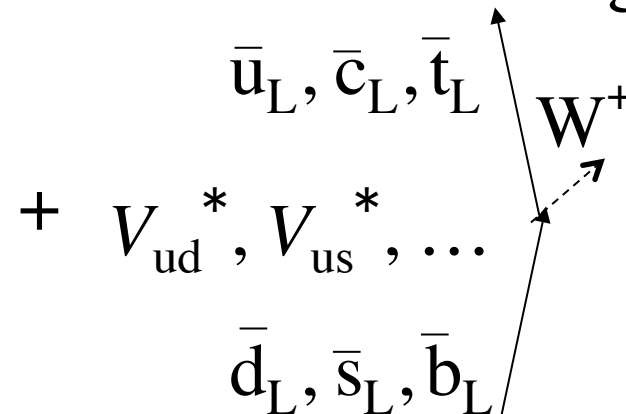
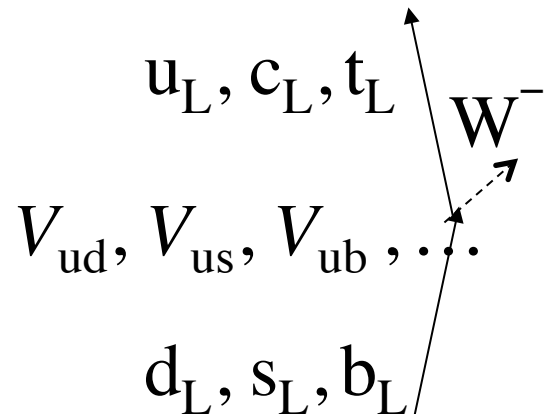
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masseigenstates

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- weak interactions
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↕ CP conjugation

$$L_{CP} \propto V_{ij} \bar{D}_i \gamma^\mu (1-\gamma_5) U_j W_\mu + V_{ij}^* \bar{U}_i \gamma^\mu (1-\gamma_5) D_j W_\mu^\dagger$$

If  $V_{ij}^* = V_{ij} \rightarrow L = L_{CP}$ : i.e. CP conservation

# Standard Model Flavour Framework

flavour eigenstates

-non-diagonal mass matrix

-strong and EM interactions

-flavour conservation

⇒

masseigenstates

-diagonal mass matrix

-weak interactions

-flavour changing

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$V_{\text{CKM}}$ : generally called  
CKM (mass mixing) matrix

$$V_{\text{CKM}}^\dagger \times V_{\text{CKM}} = 1$$

# Standard Model Flavour Framework

flavour eigenstates

- non-diagonal mass matrix
- strong and EM interactions
- flavour conservation

⇒

mass eigenstates

- diagonal mass matrix
- weak interactions
- flavour changing

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \sim \lambda & ? \\ \sim -\lambda & 1 - \frac{\lambda^2}{2} & ? \\ ? & ? & ? \end{pmatrix}$$

$$\lambda = \sin \theta_{\text{Cabibbo}} \approx 0.22$$

$V_{\text{CKM}}$ : generally called  
CKM (mass mixing) matrix  
 $V_{\text{CKM}}^\dagger \times V_{\text{CKM}} = 1$

Can you show this explicitly  
by using the arbitrary quark  
phases and unitarity?

Pre KM,  $V_{\text{CKM}}$  was  $2 \times 2$

With  $2 \times 2$  unitary matrix, one angle (1-2 rotation)

# Standard Model Flavour Framework

flavour eigenstates

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Pre KM,  $V_{\text{CKM}}$  was  $2 \times 2$

With  $2 \times 2$  unitary matrix, one angle (1-2 rotation)

With  $3 \times 3$  matrix, three angles (1-2, 2-3, 1-3 rotations) and one phase

⇒ with three families, some of  $V_{ij}$ 's are intrinsically complex

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$\Rightarrow$

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$$\hat{\rho} = \rho \left(1 - \frac{\lambda^2}{2}\right), \quad \hat{\eta} = \eta \left(1 - \frac{\eta^2}{2}\right)$$

$\lambda, A, \rho, \eta$ : Wolfenstein's parameterization

Approximation with expansions in  $\lambda$

NB  $A \neq 0, \rho \neq 0, \eta \neq 0$  for CP violation



# Standard Model Flavour Framework

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$\hat{\rho} = \rho \left(1 - \frac{\lambda^2}{2}\right), \hat{\eta} = \rho \left(1 - \frac{\eta^2}{2}\right)$

**JADE** Physics Letters B 1983

$\tau < 1.4 \times 10^{-12}$  s (95% CL)

Theoretical predictions e.g. V. Barger et al.

$0.8 \times 10^{-14} < \tau < 1.4 \times 10^{-13}$  sec, J. Phys. G 5, L147 (1979)

i.e. general prejudice was  $|V_{cb}| \approx |V_{us}|$

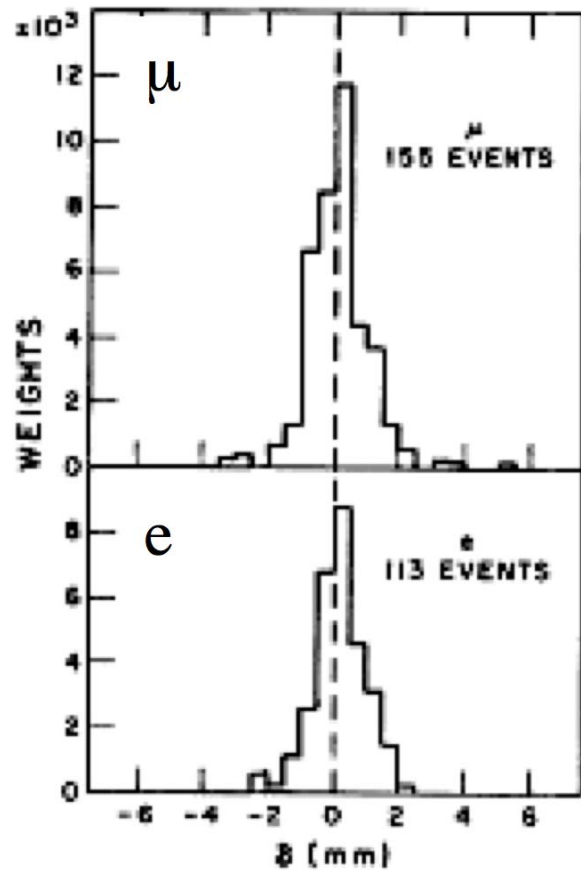
# Standard Model Flavour Framework

MAC

Phys. Rev. Lett. 51, (1983) 1022

**Lifetime of Particles Containing  $b$  Quarks**

$[1.8 \pm 0.6(\text{stat.}) \pm 0.4(\text{syst.})] \times 10^{-12}$  sec.

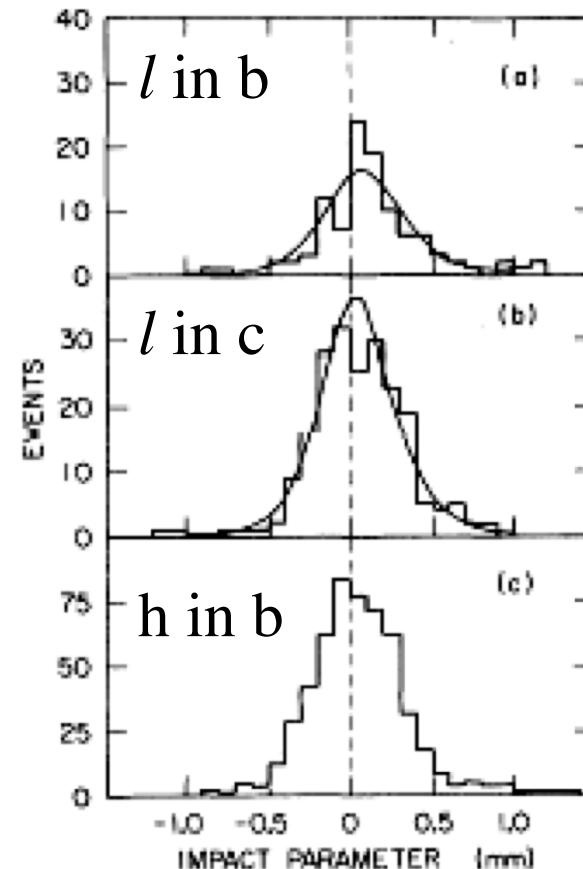


Mark II

Phys. Rev. Lett. 51, (1983) 1316

**Measurement of the Lifetime of Bottom Hadrons**

$\tau_b = (12.0^{+4.5}_{-3.6} \pm 3.0) \times 10^{-13}$  sec



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$\hat{\rho} = \rho \left(1 - \frac{\lambda^2}{2}\right), \hat{\eta} = \eta \left(1 - \frac{\lambda^2}{2}\right)$

discovery of large b lifetime, i.e. small  $|V_{cb}|$

MAC: Phys. Rev. Lett. 51, (1983) 1022

Mark II: Phys. Rev. Lett. 51, (1983) 1316

$$\tau_B \sim 10^{-12} \text{ sec}, |V_{cb}| \sim 0.05, \\ \text{i.e.} \ll \sin \theta_{\text{Cabibbo}} \sim 0.2$$

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Observation of  $b \rightarrow u/\nu$  decays:  $|V_{ub}| \neq 0$

(cf. like  $\theta_{13}$  in  $\nu$  now)

# Standard Model Flavour

flavour eigenstates

-non-diagonal mass matrix

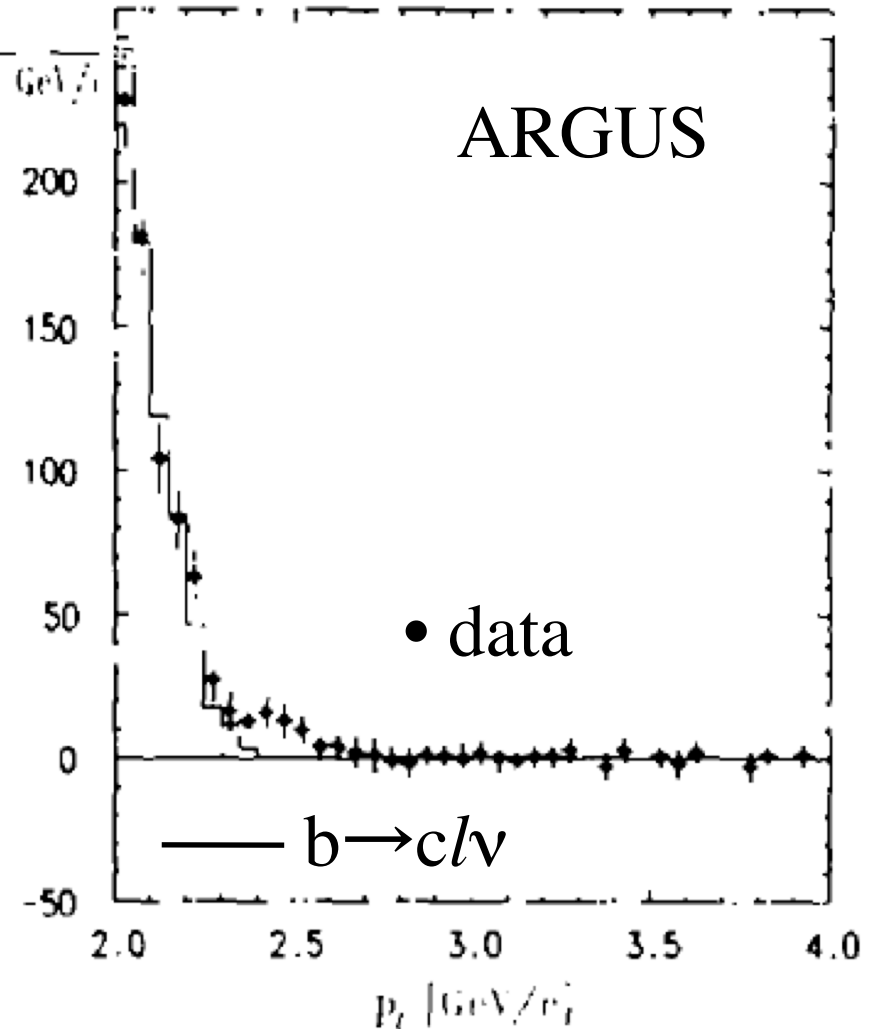
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$$\lambda = \sin \theta_{\text{Cabibbo}} \approx 0.22$$

$$A \approx 0.8$$



Observation of  $b \rightarrow u/\nu$  decays:  $|V_{ub}| \neq 0$

$|p_T| = 2.4 - 2.6 \text{ GeV}/c$  in the B rest frame

$= 76 \pm 18 \pm 8$  in  $2.4-2.6 \text{ GeV}/c$  CLEO 1990

$= 49 - (18.2 \pm 3.3)_{\text{background}}$  ARGUS 1990

$|V_{ub}|$  is very small  $\approx 0.005$

# Standard Model Flavour Framework

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Observation of  $B^0 - \bar{B}^0$  oscillations:  $|V_{td}| \neq 0$



# Standard Model Flavour Framework

Phys. Lett. B 192 (1987) 245

ARGUS, 1987

$$\begin{aligned} \Upsilon(4S) &\rightarrow B_d^0 \bar{B}_d^0 \\ &\rightarrow B_d^0 B_d^0 \text{ or } \bar{B}_d^0 \bar{B}_d^0 \\ &\rightarrow \ell^+ \ell^+ \text{ or } \ell^- \ell^- \\ &24.8 \pm 7.6 \pm 3.8 \end{aligned}$$

$$\Delta m(B_d) \sim 100 \times \Delta m(K^0)$$

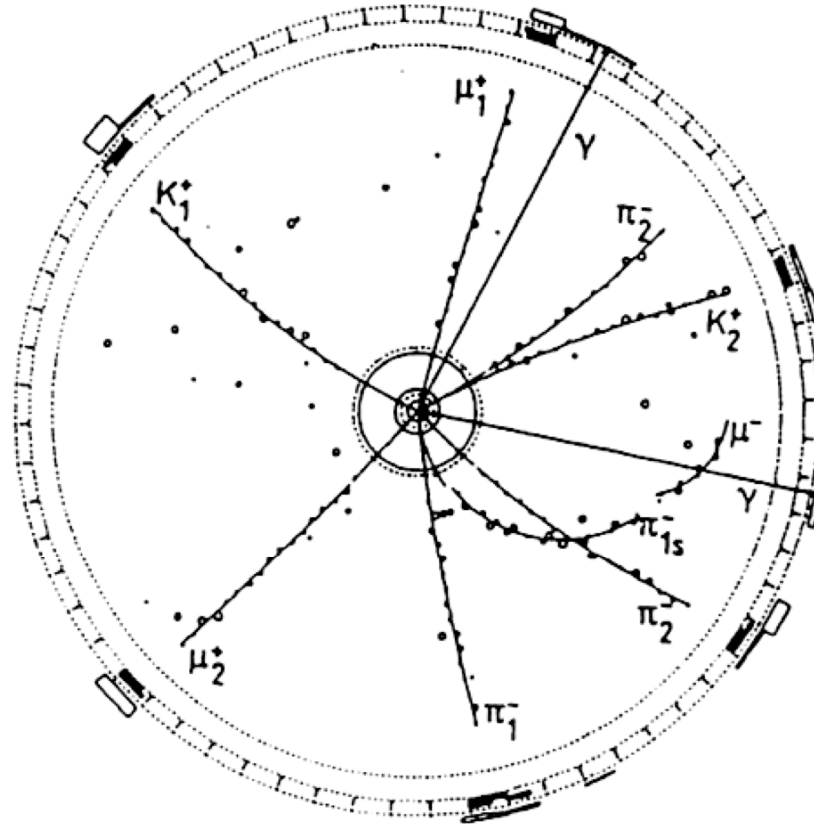
Volume 192, number 1,2

PHYSICS LETTERS B

## OBSERVATION OF $B^0$ - $\bar{B}^0$ MIXING

ARGUS Collaboration

Using the ARGUS detector at the DORIS II storage ring we have searched in three different ways for  $B^0$ - $\bar{B}^0$  mixing in  $\Upsilon(4S)$  decays. One explicitly mixed event, a decay  $\Upsilon(4S) \rightarrow B^0 \bar{B}^0$ , has been completely reconstructed. Furthermore, we observe a 4.0 standard deviation signal of 24.8 events with like-sign lepton pairs and a 3.0 standard deviation signal of 4.1 events containing one reconstructed  $B^0$  ( $\bar{B}^0$ ) and an additional fast  $\ell^+$  ( $\ell^-$ ). This leads to the conclusion that  $B^0$ - $\bar{B}^0$  mixing is substantial. For the mixing parameter we obtain  $r = 0.21 \pm 0.08$ .



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$\bar{b}$	$\bar{u} \quad \bar{c} \quad \bar{t}$	$W^+$	$\bar{t} \quad \bar{c} \quad \bar{u}$	$\bar{d}$
$d$		$W^-$		$b$
$\bar{b}$		$W^+$	$\bar{u} \quad \bar{c} \quad \bar{t}$	$\bar{d}$
$d$			$u \quad c \quad t$	$b$

$$\Delta m_B = G(|V_{td} V_{tb}|, m_t, \dots)$$

Volume 192, number 1,2

PHYSICS LETTERS B

25 June 1987

$$m_t > 50 \text{ GeV}/c^2$$

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Volume 192, number 1,2

PHYSICS LETTERS B

25 June 1987

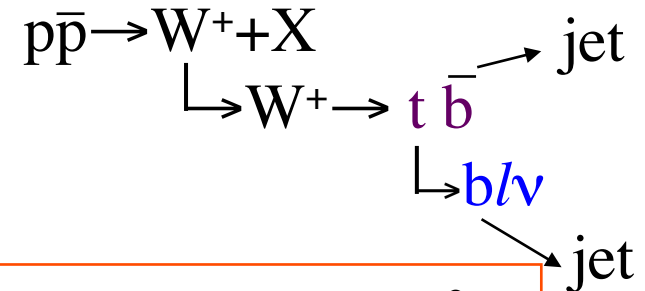
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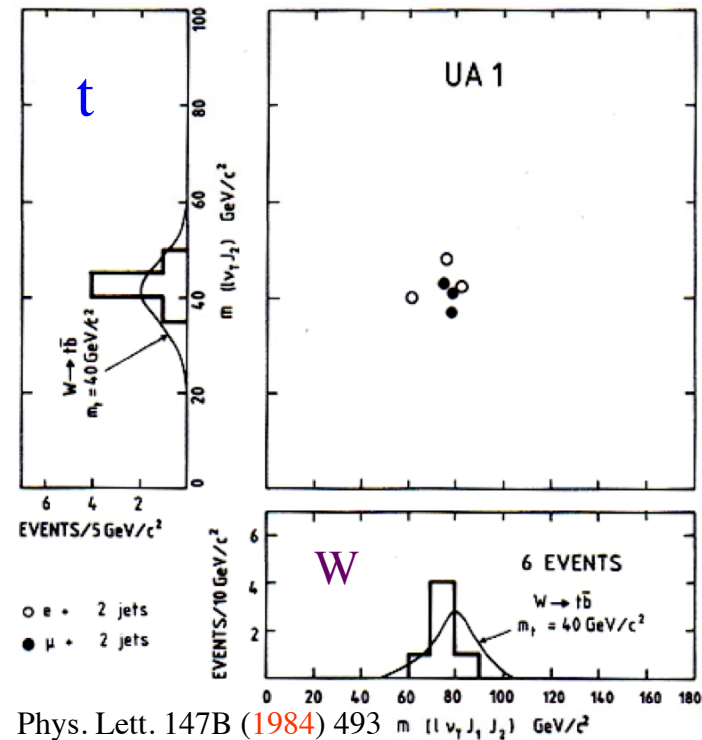
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UA1, 1984



$$m_t = 30 \sim 50 \text{ GeV}/c^2$$



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Volume 192, number 1,2

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LEP

electroweak fit

$$150 \sim 210 \text{ GeV}/c^2$$

1995

CDF

$$175 \pm 8 \pm 10 \text{ GeV}/c^2$$

D0

$$199_{-21}^{+19} \pm 22 \text{ GeV}/c^2$$

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My private reflection:

With  $\Delta m_d$  and  $\varepsilon_K$  (CPV in  $K-\bar{K}$  oscillation), CPV in  $B_d \rightarrow J/\psi K_S$  could be predicted without  $m_t$  mass, which was still unknown at that time.

Uncertainty was due to hadronic parameters:  $B_d f_d^2 / B_K$ .

This provided a benchmark  $L$  for B-factories under consideration.

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$$\hat{\rho} = \rho \left(1 - \frac{\lambda^2}{2}\right), \quad \hat{\eta} = \eta \left(1 - \frac{\lambda^2}{2}\right)$$

**It shows clearly  $\eta \neq 0$ , i.e. CPV!**

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$b \rightarrow s\gamma$  decays and  $B_s^0 - \bar{B}_s^0$  oscillations for  $|V_{ts}|$



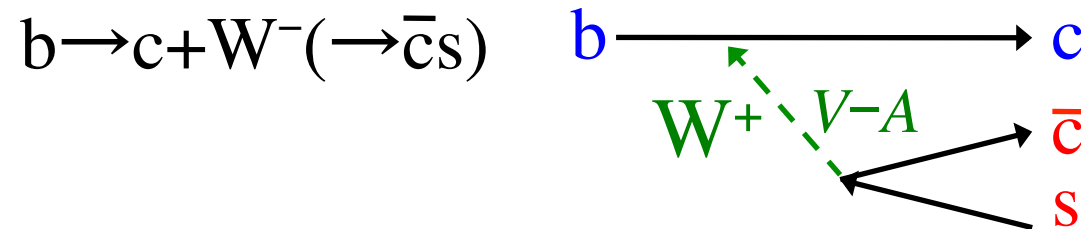
# Plan of Lectures

- Direct-search versus Indirect-search
- Early History
- Standard Model Flavour Framework
- **More of Weak Decay**
- Current Status of  $V_{\text{CKM}}$
- Any Sign of New Physics
- Closer Look
- Epilogue

# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

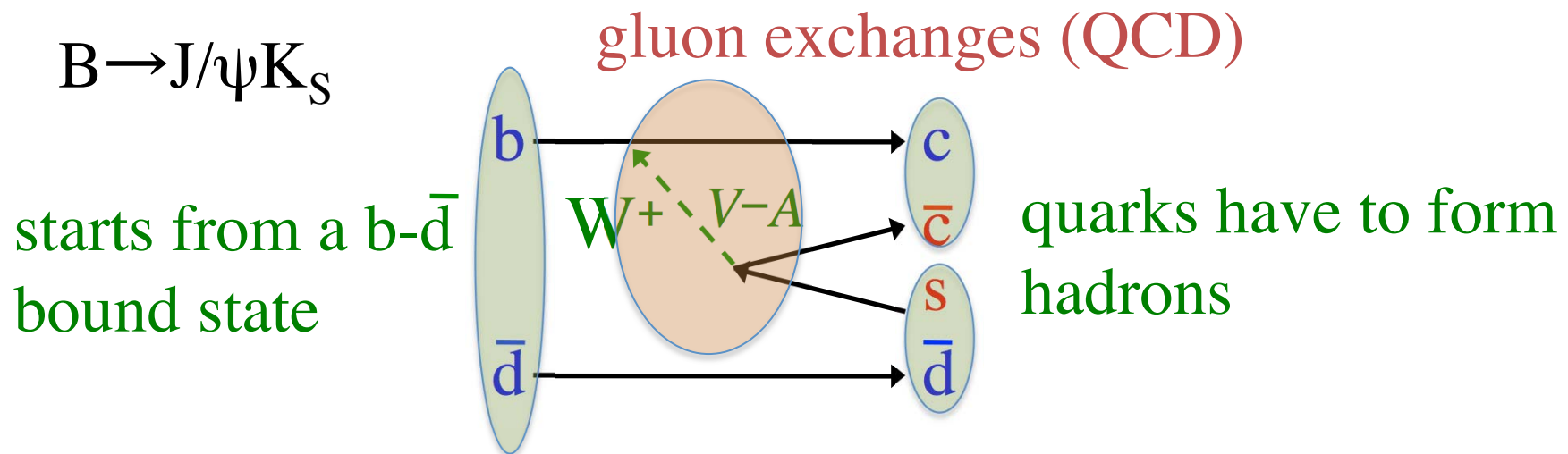
quark decay



# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

quark decay to hadron decay



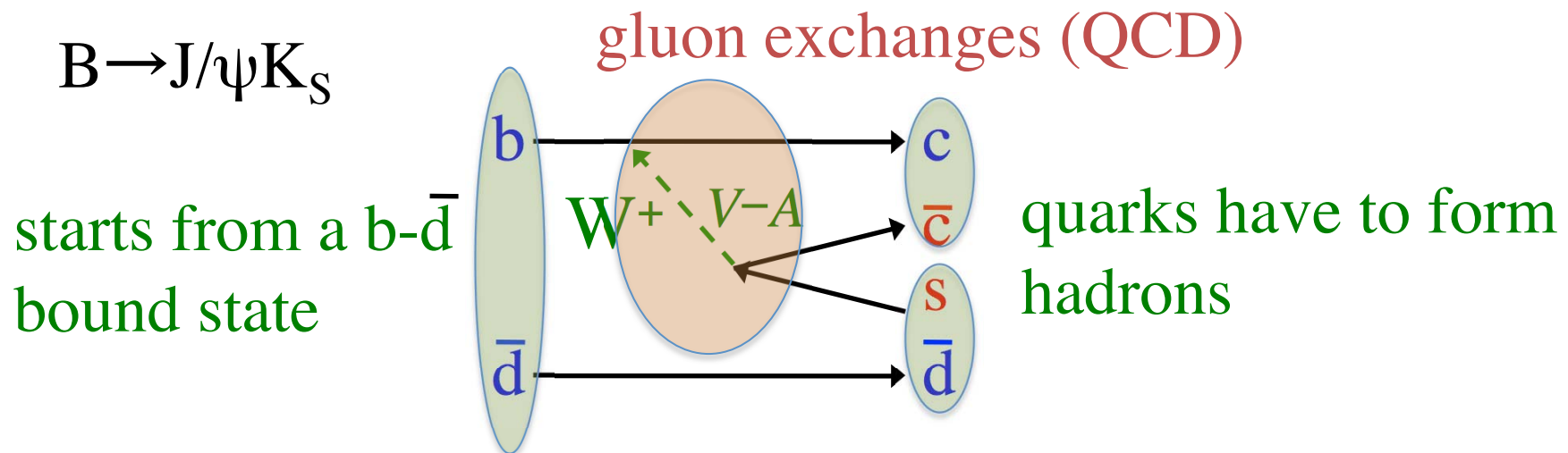
# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

Theoretical tool to describe the decay amplitude for  $M \rightarrow F$

$$A(M \rightarrow F) = \langle F | H_{\text{effective}}^{\text{weak decay}} | M \rangle = \frac{G_F}{\sqrt{2}} \sum_i \xi_{\text{CKM}}^i C_i(\mu) \langle F | Q_i(\mu) | M \rangle$$

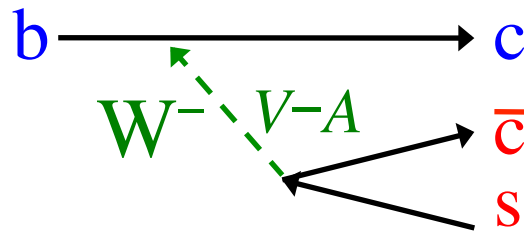
$Q_i$ : quark operators



# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

lowest order weak interactions ( $\Delta F = 1$ )



No QCD

# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

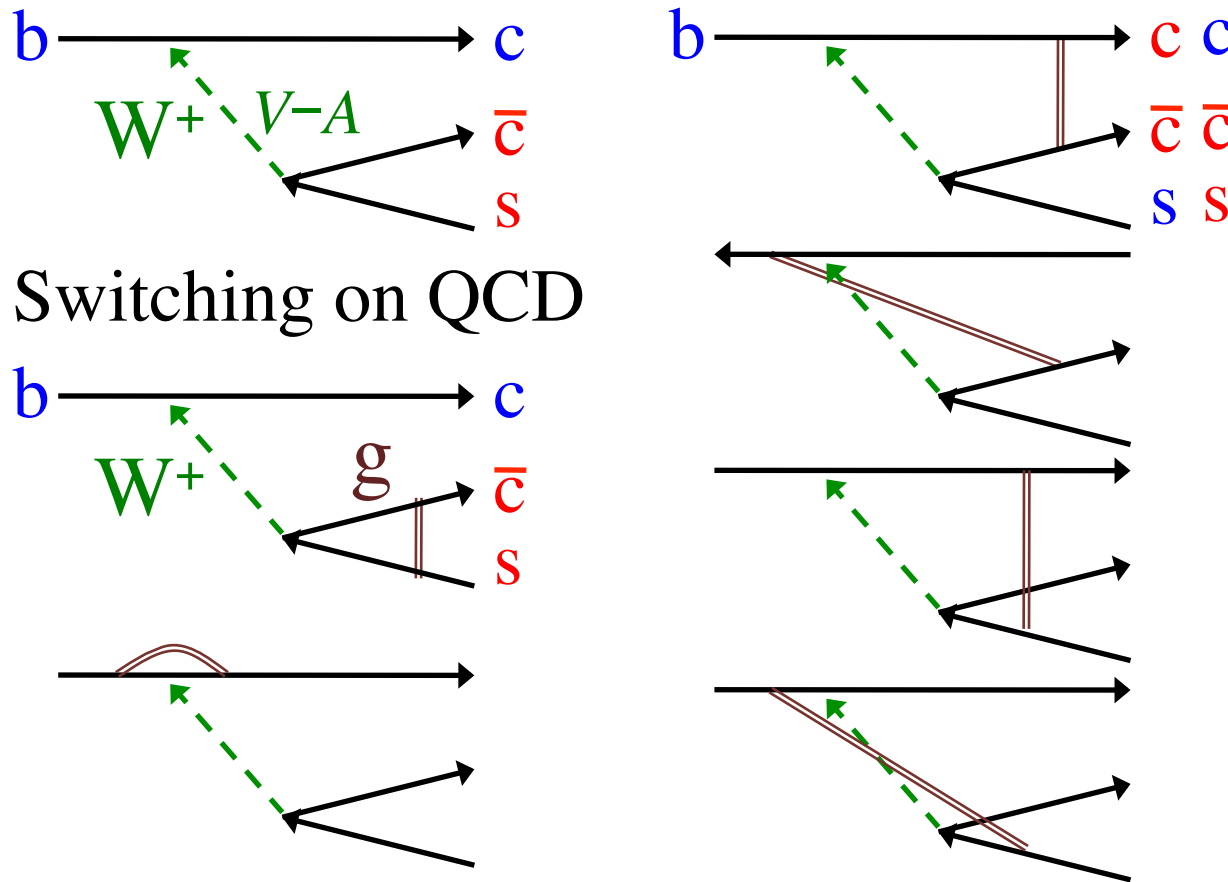
lowest order weak interactions ( $\Delta F = 1$ )

$$(\bar{c}_i b_i)_{V-A} (\bar{s}_j c_j)_{V-A}$$

# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

lowest order weak interactions ( $\Delta F = 1$ )



# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

lowest order weak interactions ( $\Delta F = 1$ )

$$(\bar{c}_i b_i)_{V-A} (\bar{s}_j c_j)_{V-A}$$

No-QCD tree diagram

+ one gluon =

tree diagrams with two  
different colour structures

$$(\bar{c}_i b_i)_{V-A} (\bar{s}_j c_j)_{V-A}$$

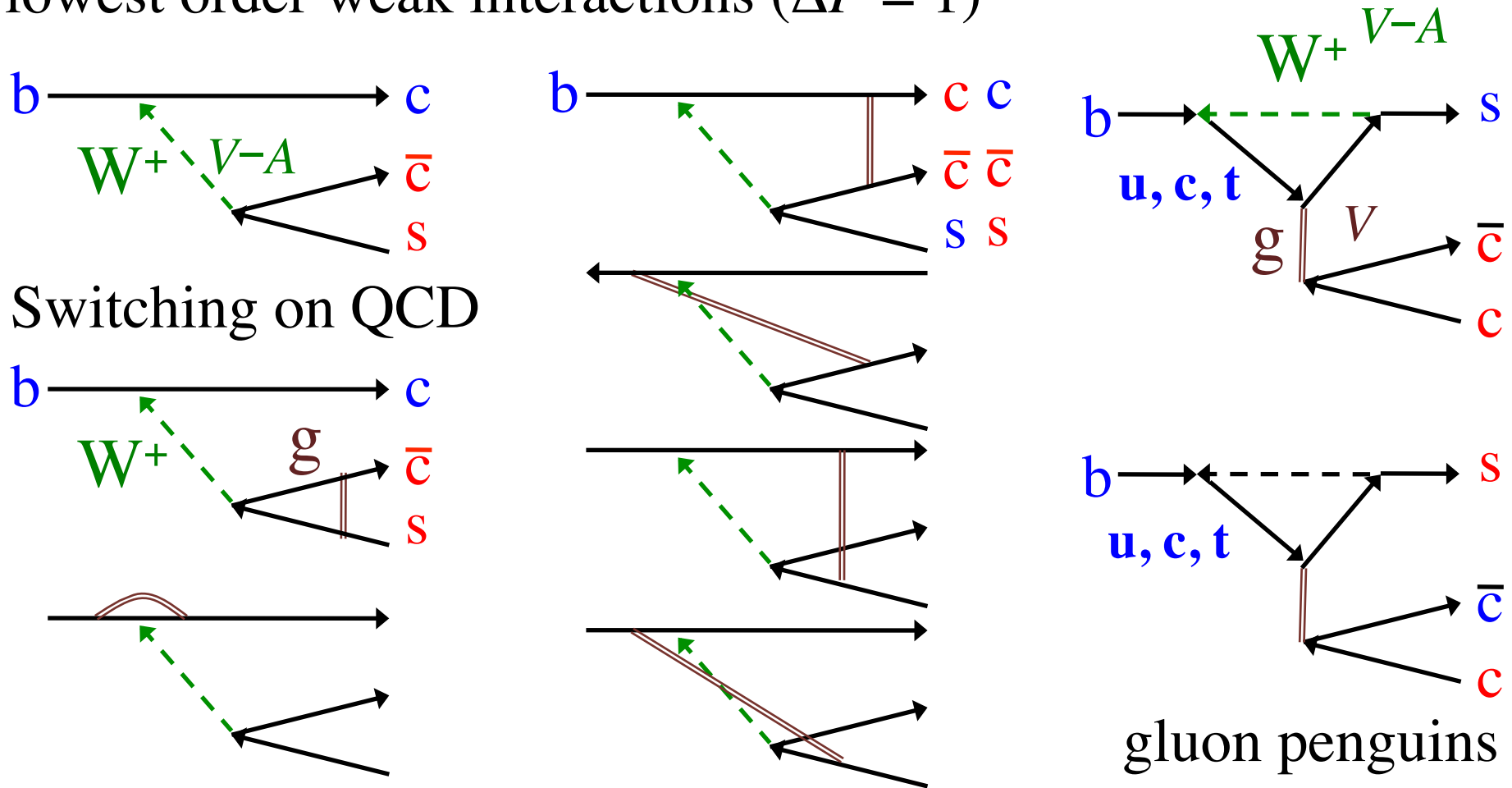
$$(\bar{c}_j b_i)_{V-A} (\bar{s}_i c_j)_{V-A}$$



# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

lowest order weak interactions ( $\Delta F = 1$ )



# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

lowest order weak interactions ( $\Delta F = 1$ )

$$(\bar{c}_i b_i)_{V-A} (\bar{s}_j c_j)_{V-A}$$

No QCD tree diagram

+ one gluon =

tree diagrams with two

different colour structures

$$(\bar{c}_i b_i)_{V-A} (\bar{s}_j c_j)_{V-A}$$

$$(\bar{c}_j b_i)_{V-A} (\bar{s}_i c_j)_{V-A}$$

$$(\bar{s}_i b_i)_{V-A} (\bar{c}_j c_j)_V$$

+ gluon penguins with two  
different colour structure

(gluon =  $V$ )

$$(\bar{s}_j b_i)_{V-A} (\bar{c}_i c_j)_V$$

# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

lowest order weak interactions ( $\Delta F = 1$ )

$(\bar{c}_i b_i)_{V-A} (\bar{s}_j c_j)_{V-A}$	$(\bar{c}_i b_i)_{V-A} (\bar{s}_j c_j)_{V-A}$
No QCD tree diagram	
+ one gluon	$(\bar{c}_j b_i)_{V-A} (\bar{s}_i c_j)_{V-A}$
tree diagrams with two different colour structures	$(\bar{s}_i b_i)_{V-A} (\bar{c}_j c_j)_{V-A}$
+ gluon penguins with two different colour structure	$(\bar{s}_i b_i)_{V-A} (\bar{c}_j c_j)_{V+A}$
(gluon = V)	
→ split to (V-A) + (V+A)	$(\bar{s}_j b_i)_{V-A} (\bar{c}_i c_j)_{V-A}$
(needed for the $Q^2$ evolution)	$(\bar{s}_j b_i)_{V-A} (\bar{c}_i c_j)_{V+A}$

# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

lowest order weak interactions ( $\Delta F = 1$ )

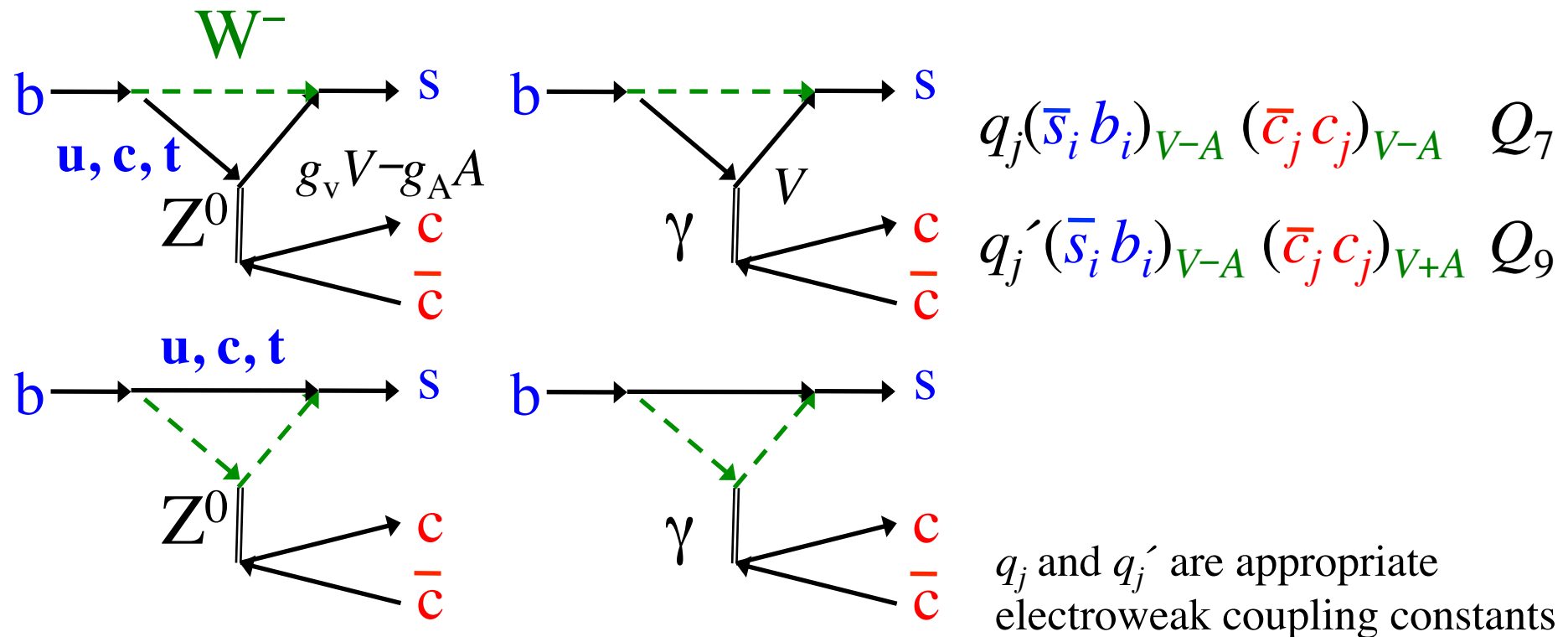
		operators
$(\bar{c}_i b_i)_{V-A} (\bar{s}_j c_j)_{V-A}$	$(\bar{c}_i b_i)_{V-A} (\bar{s}_j c_j)_{V-A}$	$Q_2$
No QCD tree diagram		
+ one gluon	$(\bar{c}_j b_i)_{V-A} (\bar{s}_i c_j)_{V-A}$	$Q_1$
tree diagrams with two different colour structures	$(\bar{s}_i b_i)_{V-A} (\bar{c}_j c_j)_{V-A}$	$Q_3$
+ gluon penguins with two different colour structure	$(\bar{s}_i b_i)_{V-A} (\bar{c}_j c_j)_{V+A}$	$Q_5$
(gluon = V)		
→ split to (V-A) + (V+A)	$(\bar{s}_j b_i)_{V-A} (\bar{c}_i c_j)_{V-A}$	$Q_4$
(needed for the $Q^2$ evolution)	$(\bar{s}_j b_i)_{V-A} (\bar{c}_i c_j)_{V+A}$	$Q_6$

# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

the second order electroweak interactions ( $\Delta F = 1$ )

electroweak penguins

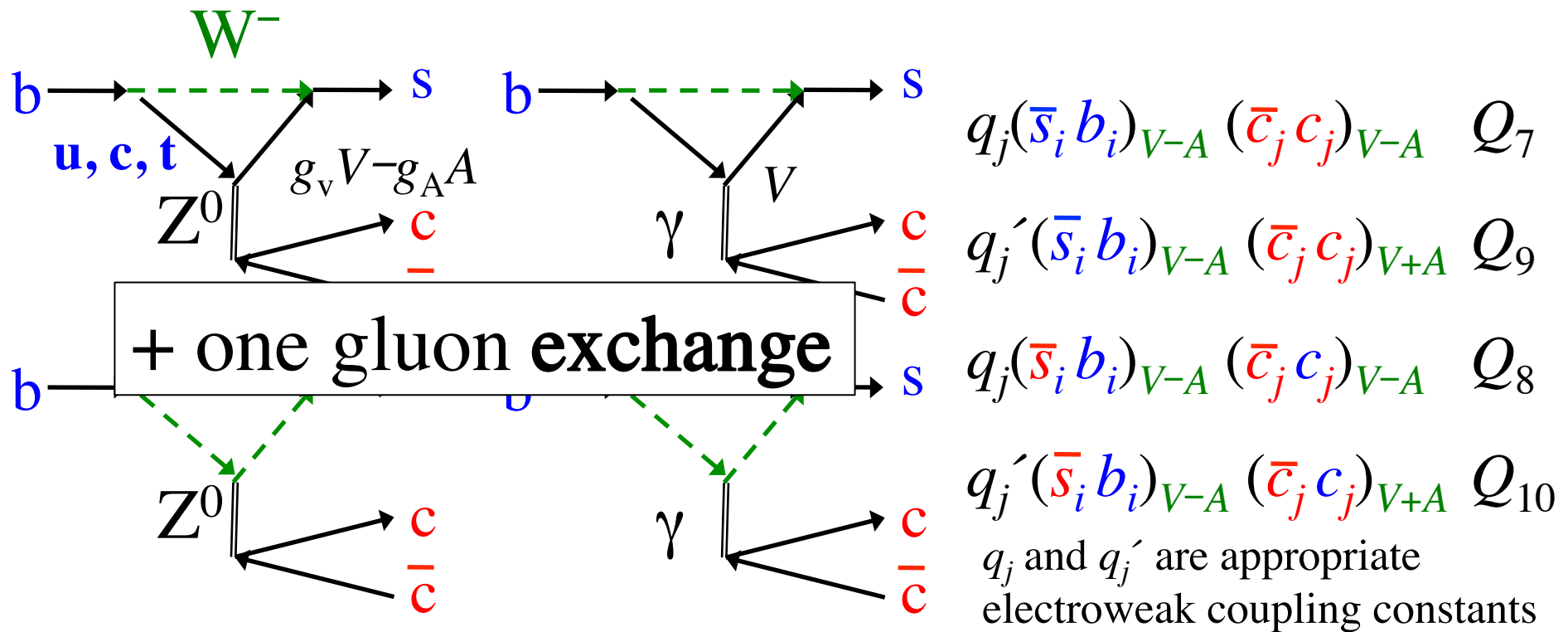


# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

the second order electroweak interactions ( $\Delta F = 1$ )

electroweak penguins + QCD

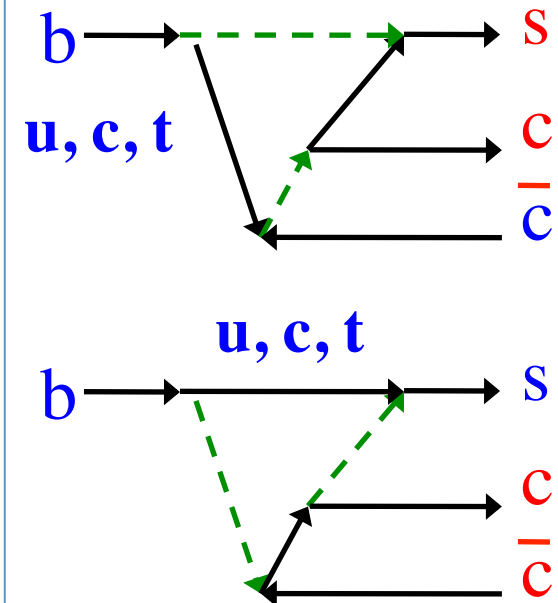
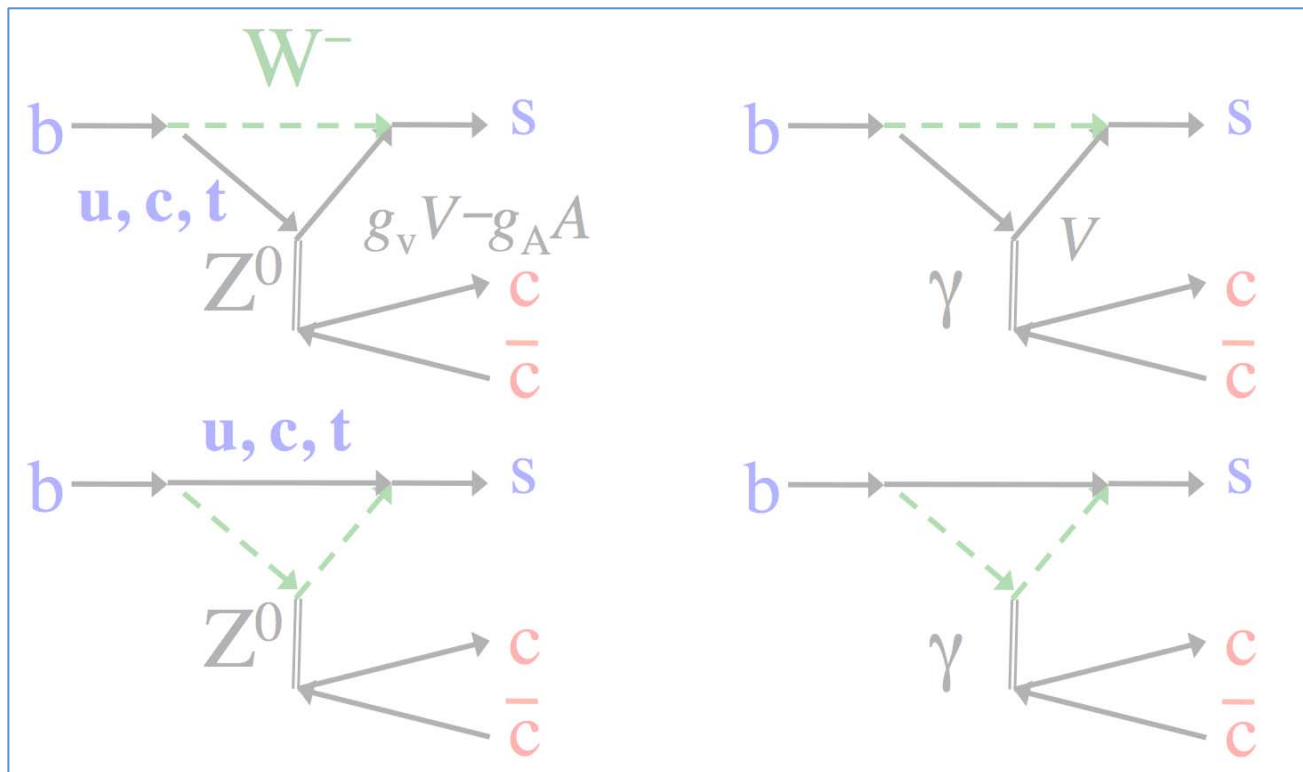


# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

also the second order electroweak interactions,  $\Delta F = 2$

Box diagrams



# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

Theoretical tool to describe the decay amplitude for  $M \rightarrow F$

$$A(M \rightarrow F) = \langle F | H_{\text{effective}}^{\text{weak decay}} | M \rangle = \frac{G_F}{\sqrt{2}} \sum_i \xi_{\text{CKM}}^i C_i(\mu) \langle F | Q_i(\mu) | M \rangle$$

$G_F$ : Fermi constant,

$Q_i(\mu)$ : Local four-fermion operators evaluated at energy scale  $\mu$   
calculable in perturbation

$C_i(\mu)$ : Coupling constants for  $Q_i(\mu)$  at energy scale  $\mu$   
i.e. Wilson coefficient, calculable in perturbation

$\langle F | Q_i(\mu) | M \rangle$ : Hadronic matrix element  
long distance effect

$\xi_i^{\text{CKM}}$ : Combination of the CKM elements

**the ultimate interest for Flavour Physics**  
**extraction of the CKM matrix, search for new physics**



# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

Theoretical tool to describe the decay amplitude for  $M \rightarrow F$

$$A(M \rightarrow F) = \langle F | H_{\text{effective}}^{\text{weak decay}} | M \rangle = \frac{G_F}{\sqrt{2}} \sum_i \xi_{\text{CKM}}^i C_i(\mu) \langle F | Q_i(\mu) | M \rangle$$

- Comparing the full and effective theory at  $\mu = m_W$   
 $\rightarrow C_i(\mu = m_W)$

- Scale  $C_i$  down to  $\mu \approx 1$  GeV (K),  $m_c$  (D),  $m_b$  (B)

$$C_i(\mu) = U_{ij}(\mu, \mu = m_W) C_j(\mu = m_W)$$

$U_{ij}$  not diagonal  $\Rightarrow$  mixing of the operators in the evolution

- Evaluate  $\langle F | Q_i(\mu) | M \rangle$  (hadronic matrix element)  
with non perturbative methods at  $\mu$   
lattice, HQET, QCD sum rule, etc.

**major source of uncertainties**

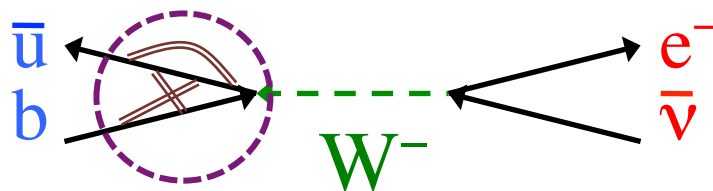
# More on Weak Decays

decay ( $\Delta F = 1$ ) and oscillation amplitudes ( $\Delta F = 2$ )

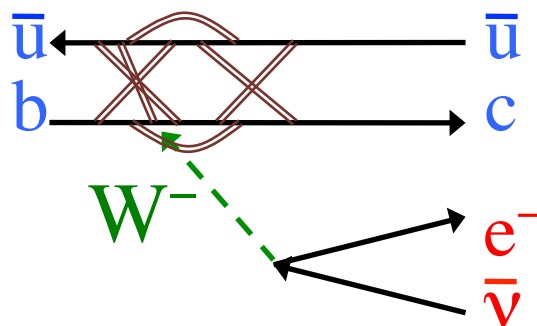
Theoretical tool to describe the decay amplitude for  $M \rightarrow F$

$$A(M \rightarrow F) = \langle F | H_{\text{effective}}^{\text{weak decay}} | M \rangle = \frac{G_F}{\sqrt{2}} \sum_i \xi_{\text{CKM}}^i C_i(\mu) \langle F | Q_i(\mu) | M \rangle$$

- Evaluate  $\langle F | Q_i(\mu) | M \rangle$  (hadronic matrix element)



One decay constant  $f_B$



Form factors  $f(q^2)$ :  
functions of momentum transfer  
 $B \rightarrow$  hadrons  
depend on the hadrons

Many theoretical models: **ultimately the lattice QCD**

# Plan of Lectures

- Direct-search versus Indirect-search
- Early History
- Standard Model Flavour Framework
- More of Weak Decay
- Current Status of  $V_{CKM}$
- Any Sign of New Physics
- Closer Look
- Epilogue

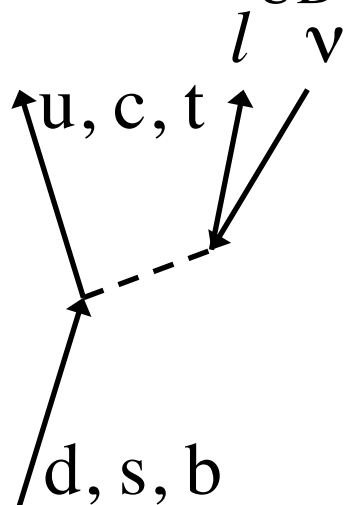
# Current Status of $V_{CKM}$

Can be extract from decay widths generated by the tree, penguin, and box processes

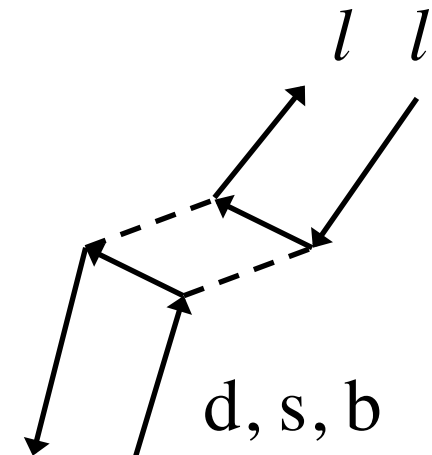
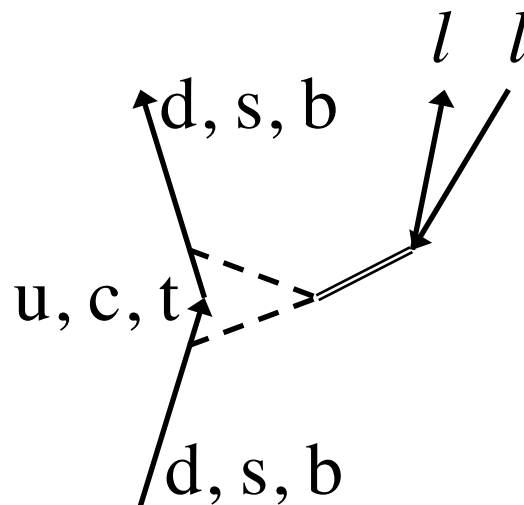
examples of semileptonic and leptonic decays

$$V_{UD} \begin{cases} U = u, c, t \\ D = d, s, b \end{cases}$$

$$\Gamma \propto |V_{UD}|$$



$$\propto |\sum_U V_{UD} V_{UD}^* f(m_U)|$$



# Current Status of $V_{\text{CKM}}$

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

First  $2 \times 2$  sub-matrix: four  $|V_{ij}|$  are measured by nucleus, pion, kaon and charm hadron decays

It is “almost” unitary with one single parameter

$$\lambda (\equiv \sin \theta_{\text{Cabibbo}}) = |V_{us}| = 0.2246 \pm 0.0012 \text{ (PDG 2012)}$$

$$V_{\text{CKM}} \approx \begin{pmatrix} 1 & \lambda & V_{ub} \\ -\lambda & 1 & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

# Current Status of $V_{\text{CKM}}$

$$V_{\text{CKM}} \approx \begin{pmatrix} 1 & \lambda & V_{ub} \\ -\lambda & 1 & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$|V_{cb}|$  and  $|V_{ub}|$  measured by semileptonic  $B_u$  and  $B_d$  decays

$$|V_{cb}| = \begin{cases} (41.9 \pm 0.7) \times 10^{-3} & \text{inclusive decays} \\ (39.6 \pm 0.9) \times 10^{-3} & \text{exclusive decays} \end{cases} \quad \begin{array}{l} 2.0\sigma \text{ discrepancy} \\ \text{(PDG 2012)} \\ \text{-errors limited theoretically-} \end{array}$$

$$|V_{ub}| = \begin{cases} (4.41 \pm 0.22) \times 10^{-3} & \text{inclusive decays} \\ (3.23 \pm 0.31) \times 10^{-3} & \text{exclusive decays} \end{cases} \quad \begin{array}{l} 3.1\sigma \text{ discrepancy} \\ \text{(PDG 2012)} \\ \text{-errors very limited theoretically-} \end{array}$$

exclusives systematically smaller than inclusives...?

# Current Status of $V_{\text{CKM}}$

$$V_{\text{CKM}} \approx \begin{pmatrix} 1 & \lambda & V_{ub} \\ -\lambda & 1 & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$|V_{cb}|$  and  $|V_{ub}|$  measured by semileptonic  $B_u$  and  $B_d$  decays  
 $\arg V_{cb} = 0$  by a phase convention

# Current Status of $V_{\text{CKM}}$

$$V_{\text{CKM}} \approx \begin{pmatrix} 1 & \lambda & V_{ub} \\ -\lambda & 1 & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$|V_{cb}|$  and  $|V_{ub}|$  measured by semileptonic  $B_u$  and  $B_d$  decays

$\arg V_{cb} = 0$  by a phase convention

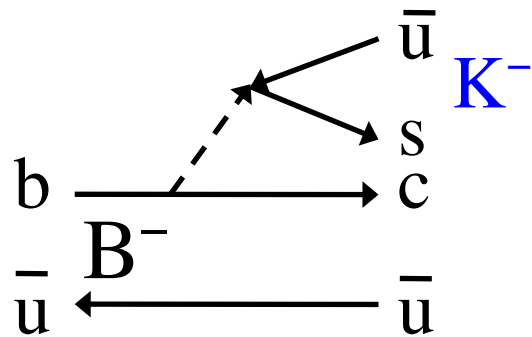
$\arg V_{ub}$  by CP violation in  $B \rightarrow DK$



# Current Status of $V_{CKM}$

arg  $V_{ub}$  so called angle “ $\gamma$ ”

two decay diagrams producing identical final states

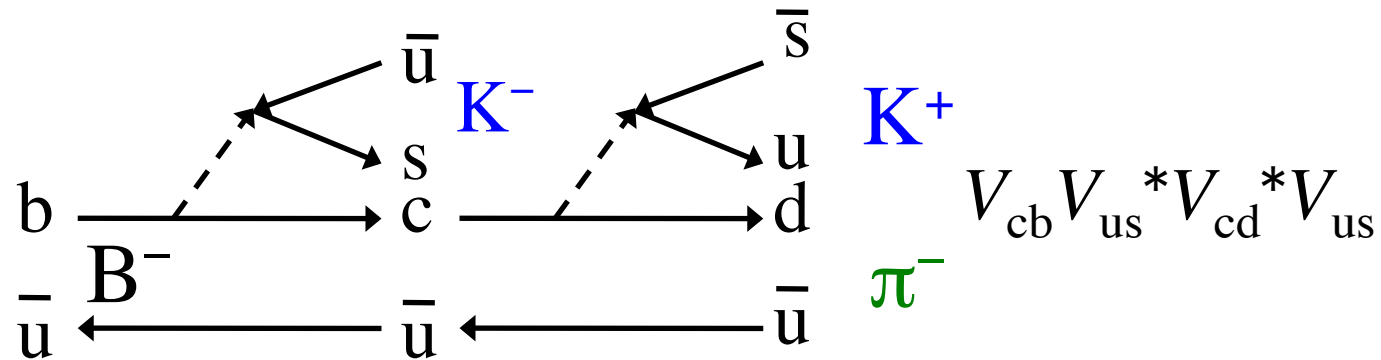


$$V_{cb} V_{us}^*$$

# Current Status of $V_{CKM}$

arg  $V_{ub}$  so called angle “ $\gamma$ ”

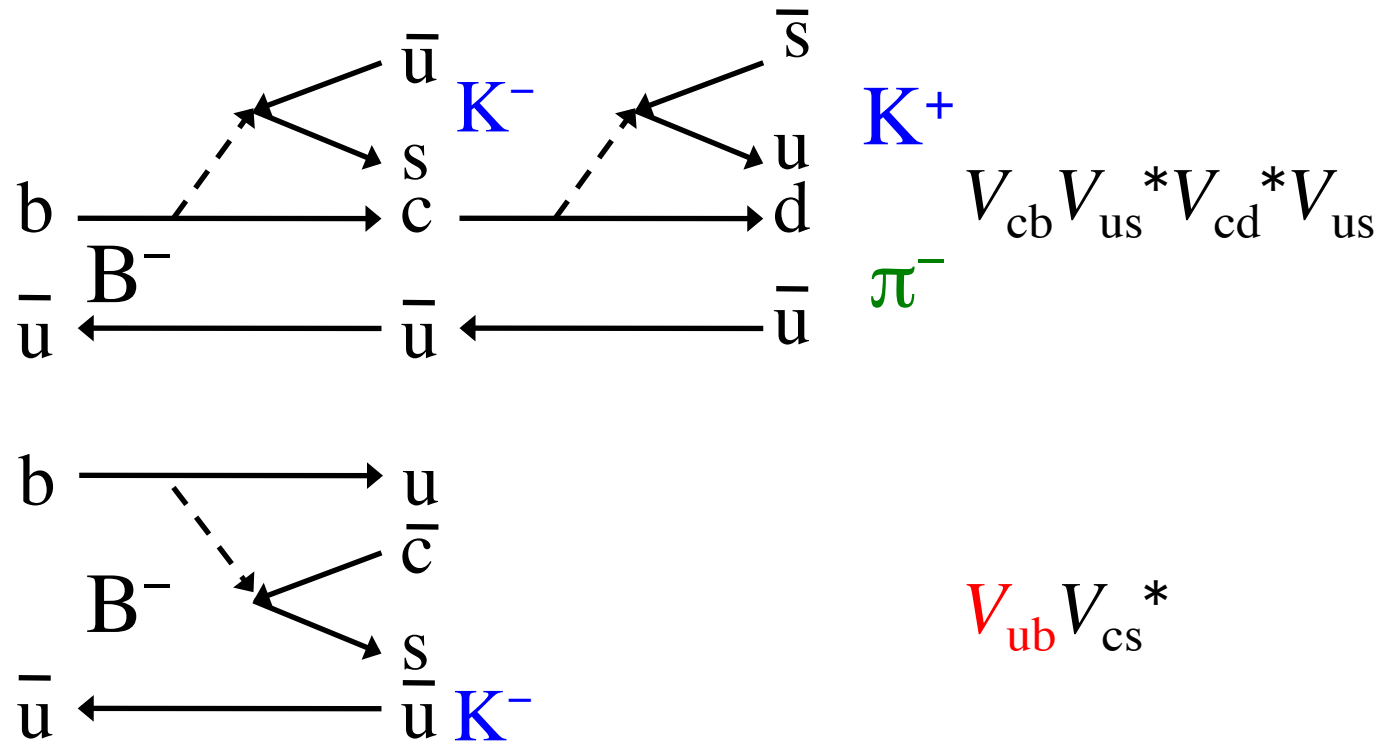
two decay diagrams producing identical final states



# Current Status of $V_{CKM}$

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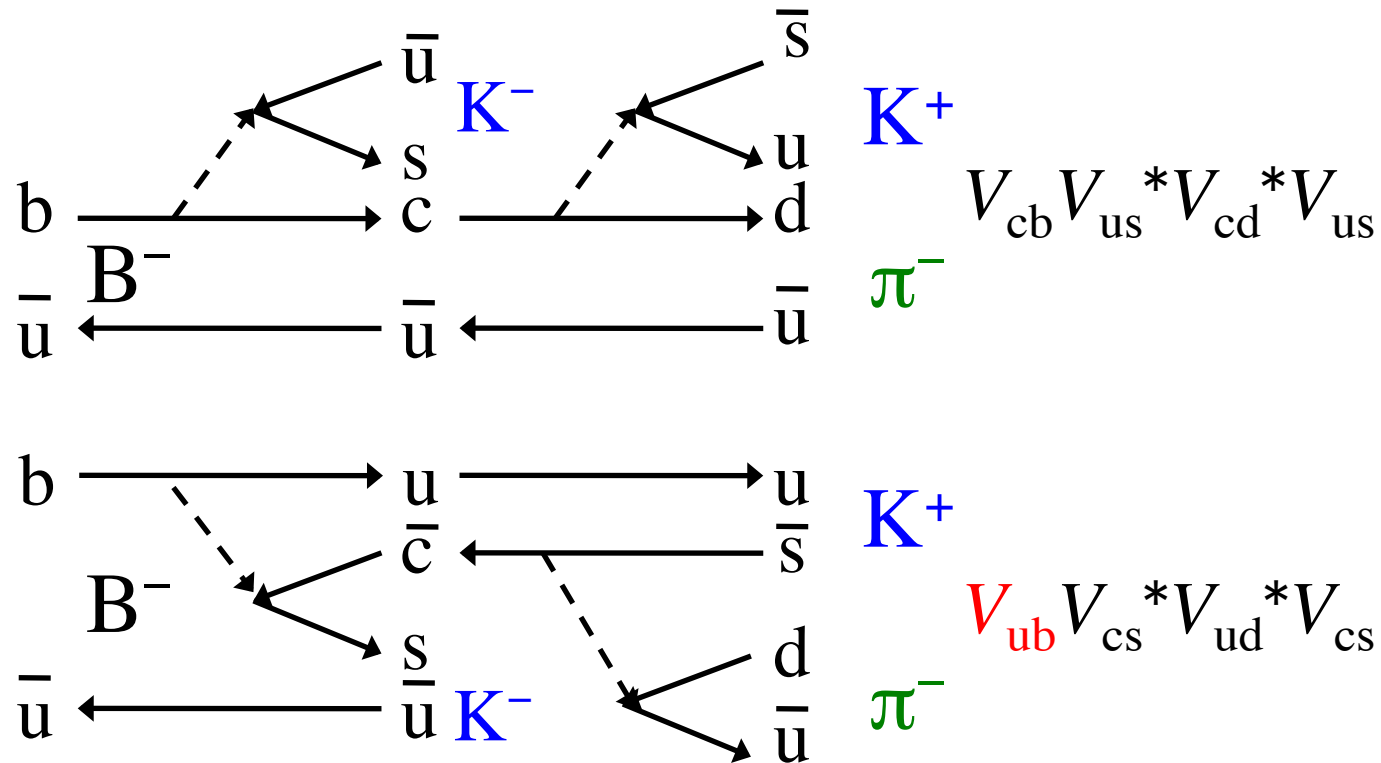
two decay diagrams producing identical final states



# Current Status of $V_{CKM}$

arg  $V_{ub}$  so called angle “ $\gamma$ ”

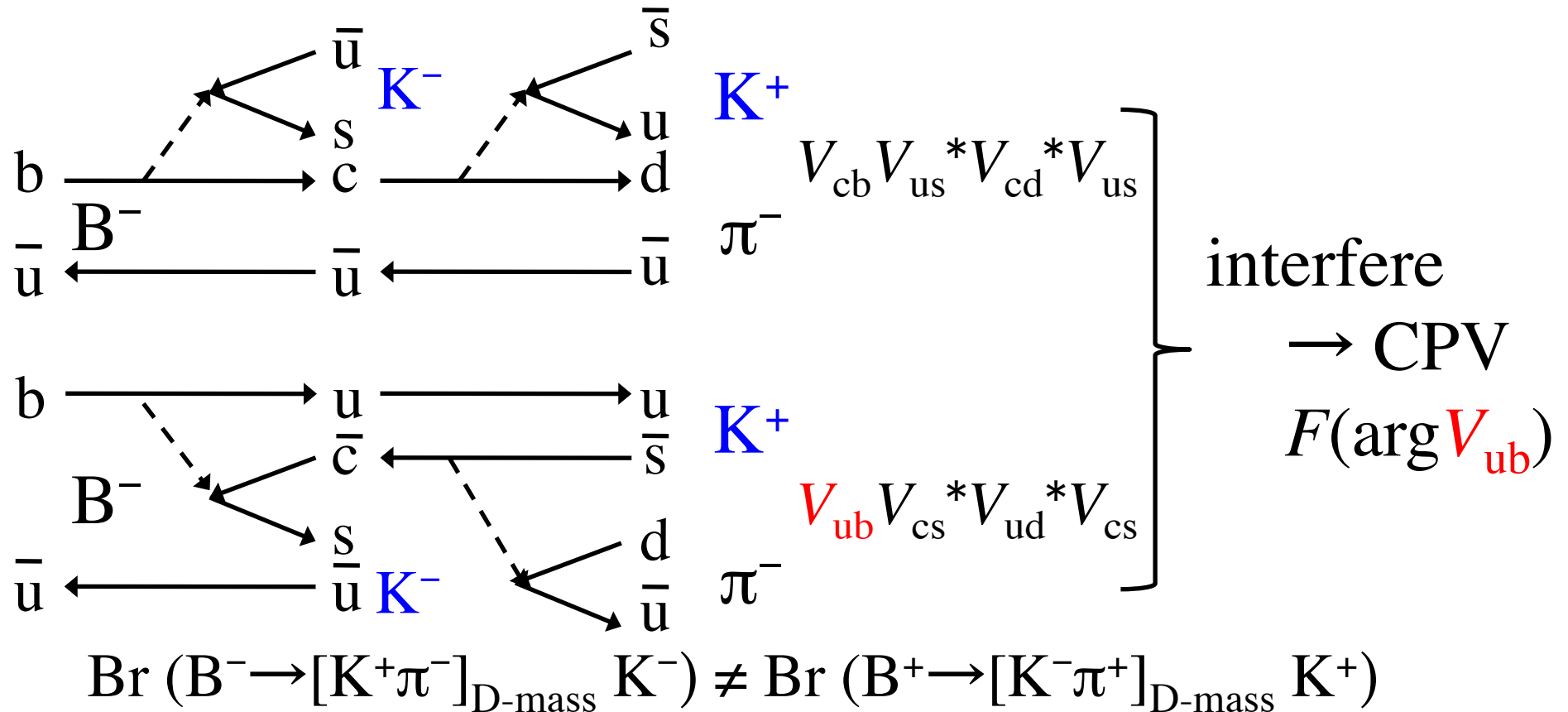
two decay diagrams producing identical final states



# Current Status of $V_{CKM}$

$\arg V_{ub}$  so called angle “ $\gamma$ ”

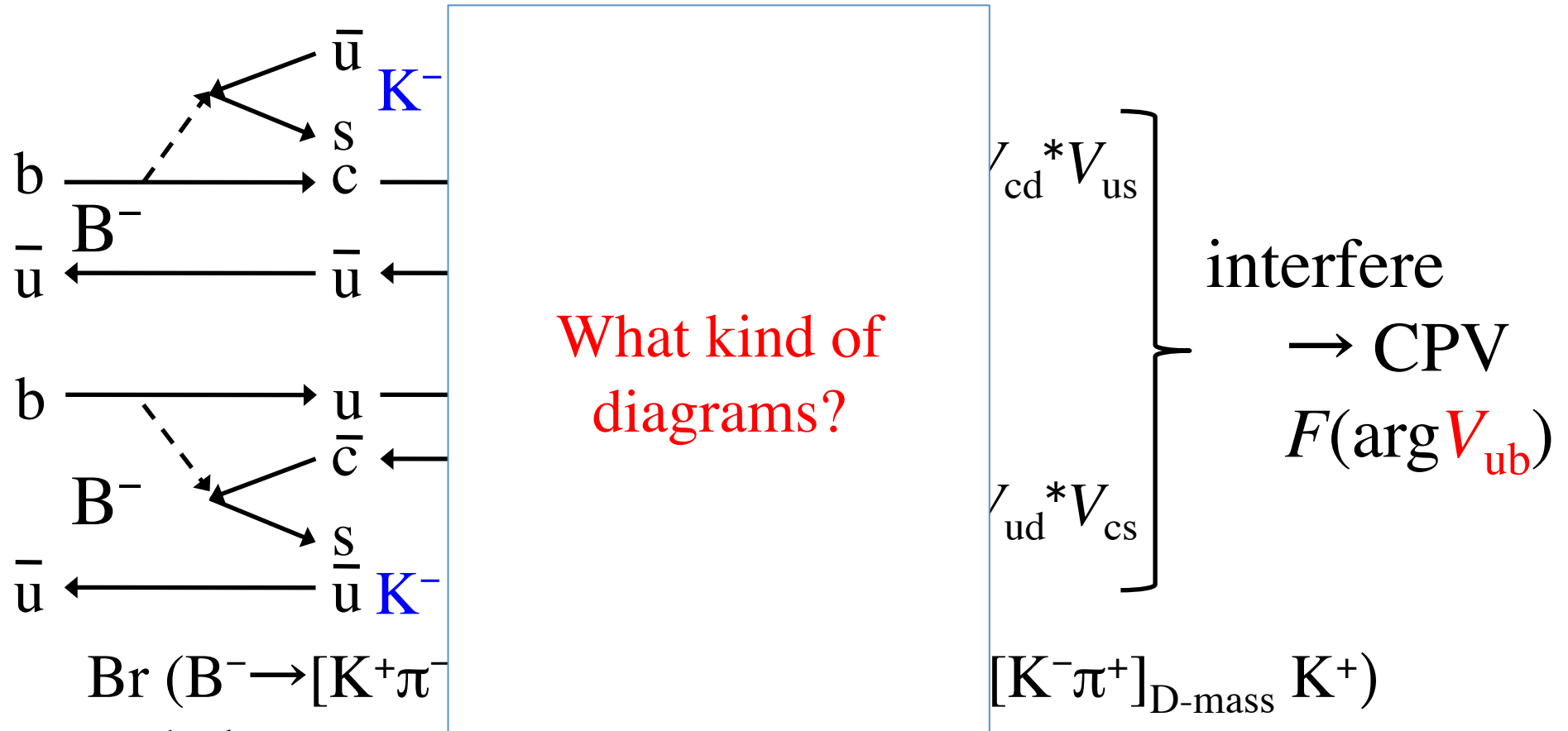
two decay diagrams producing identical final states



# Current Status of $V_{CKM}$

$\arg V_{ub}$  so called angle “ $\gamma$ ”

two decay diagrams producing identical final states



$\text{Br} (B^- \rightarrow [K^+ \pi^-]_{D\text{-mass}} K^+)$

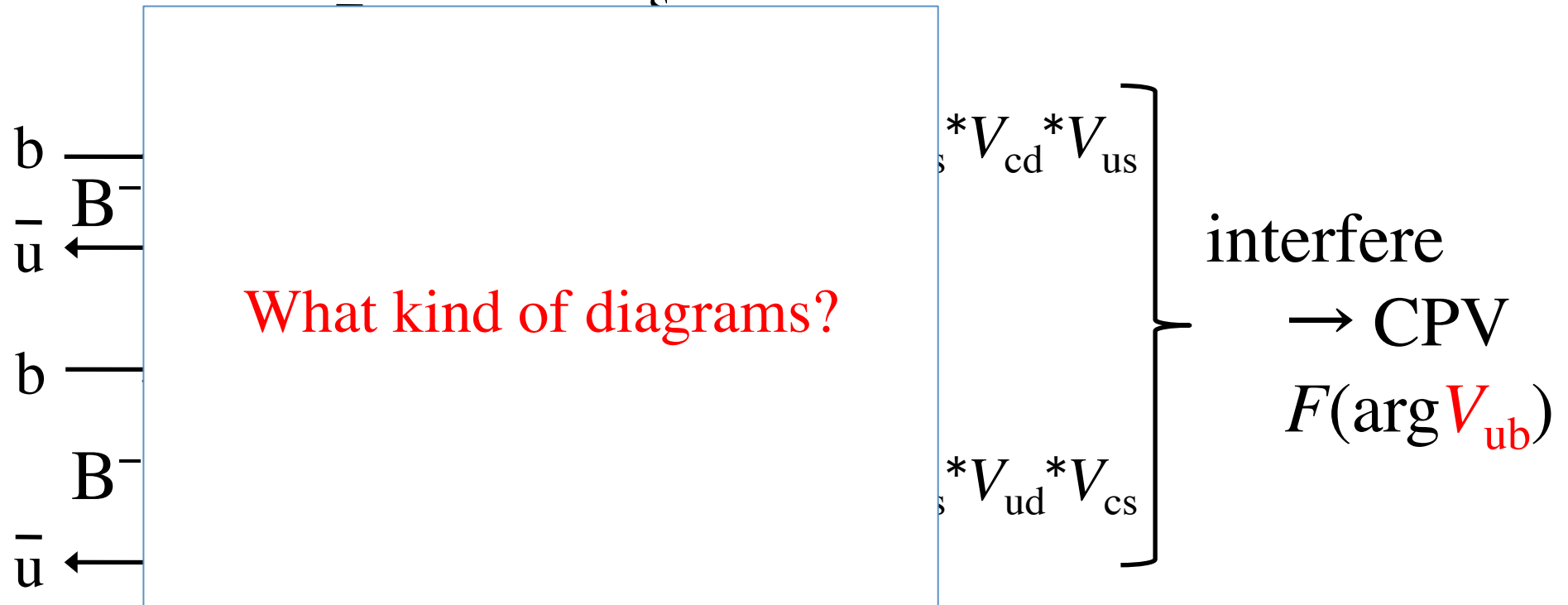
and also

$\text{Br} (B^- \rightarrow [K^- \pi^+]_{D\text{-mass}} K^-) \neq \text{Br} (B^+ \rightarrow [K^+ \pi^-]_{D\text{-mass}} K^+)$

# Current Status of $V_{CKM}$

arg  $V_{ub}$  so called angle “ $\gamma$ ”

two decay diagrams producing identical final states



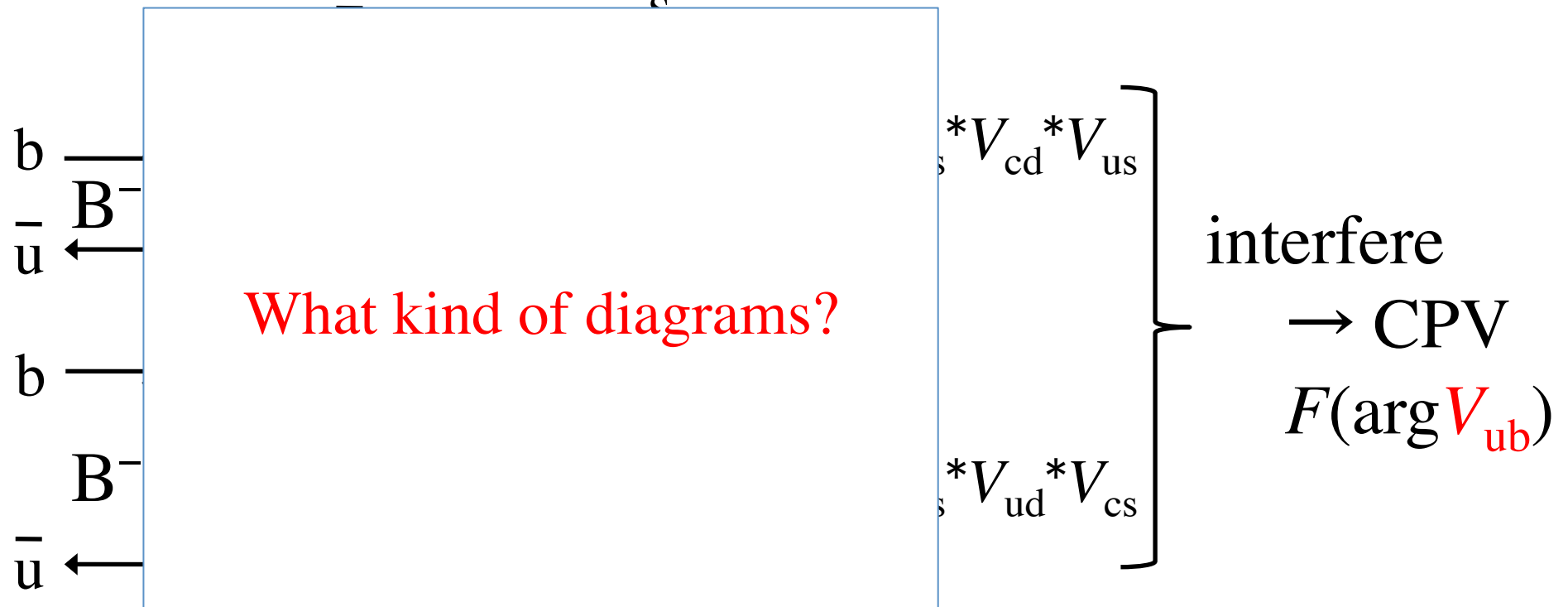
$$\text{Br} (B^- \rightarrow [K^+K^-]_{D\text{-mass}} K^-) \neq \text{Br} (B^+ \rightarrow [K^+K^-]_{D\text{-mass}} K^+)$$

$$\text{Br} (B^- \rightarrow [\pi^+\pi^-]_{D\text{-mass}} K^-) \neq \text{Br} (B^+ \rightarrow [\pi^+\pi^-]_{D\text{-mass}} K^+)$$

# Current Status of $V_{CKM}$

arg  $V_{ub}$  so called angle “ $\gamma$ ”

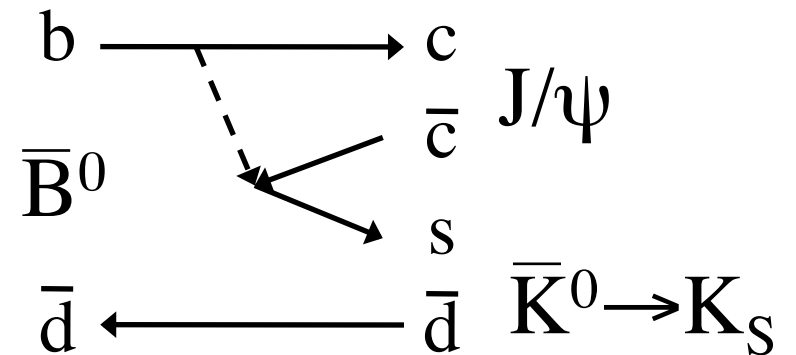
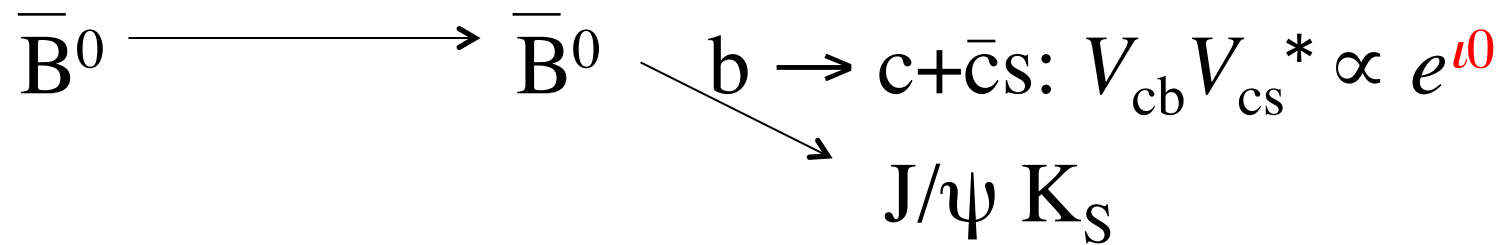
two decay diagrams producing identical final states



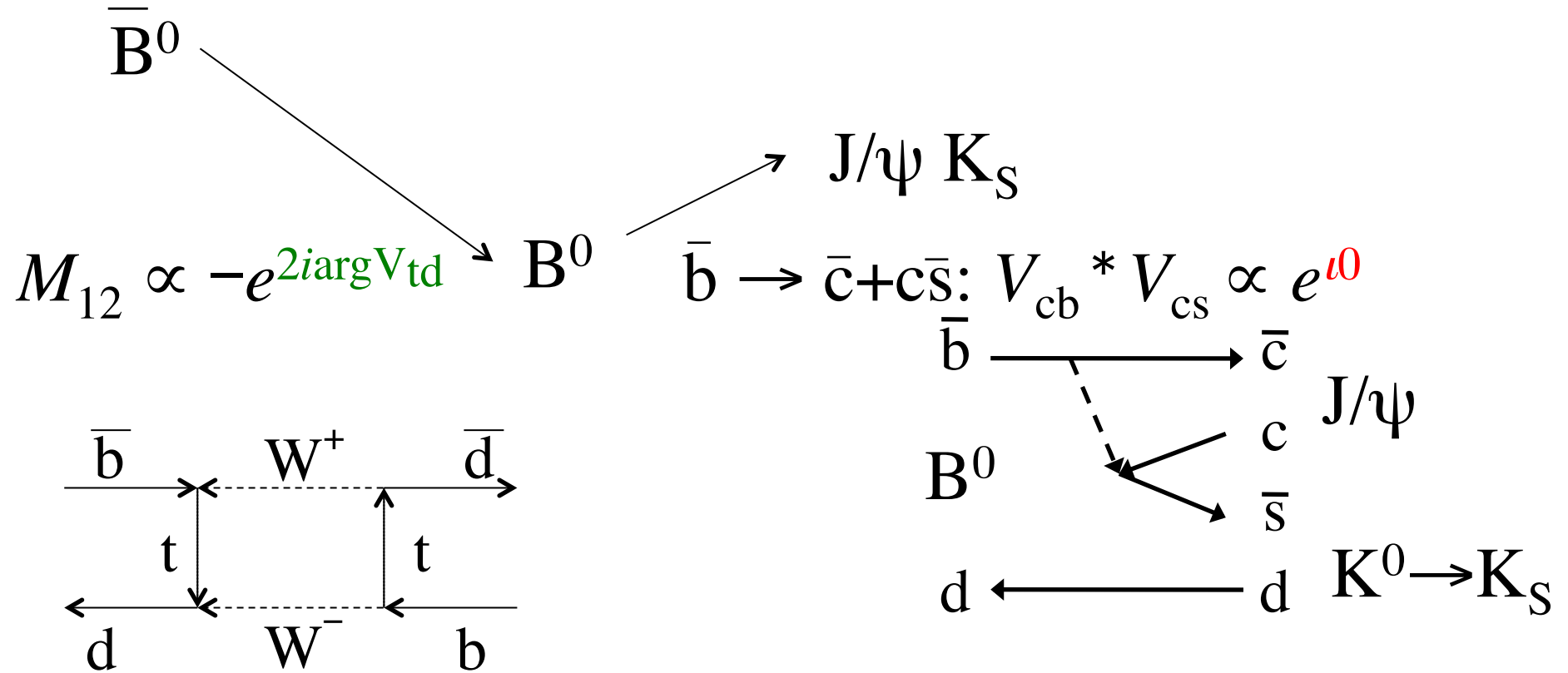
$$\text{Br} (B^- \rightarrow [K_S \pi^+ \pi^-]_{D\text{-mass}} K^-) \neq \text{Br} (B^+ \rightarrow [K_S \pi^+ \pi^-]_{D\text{-mass}} K^+)$$



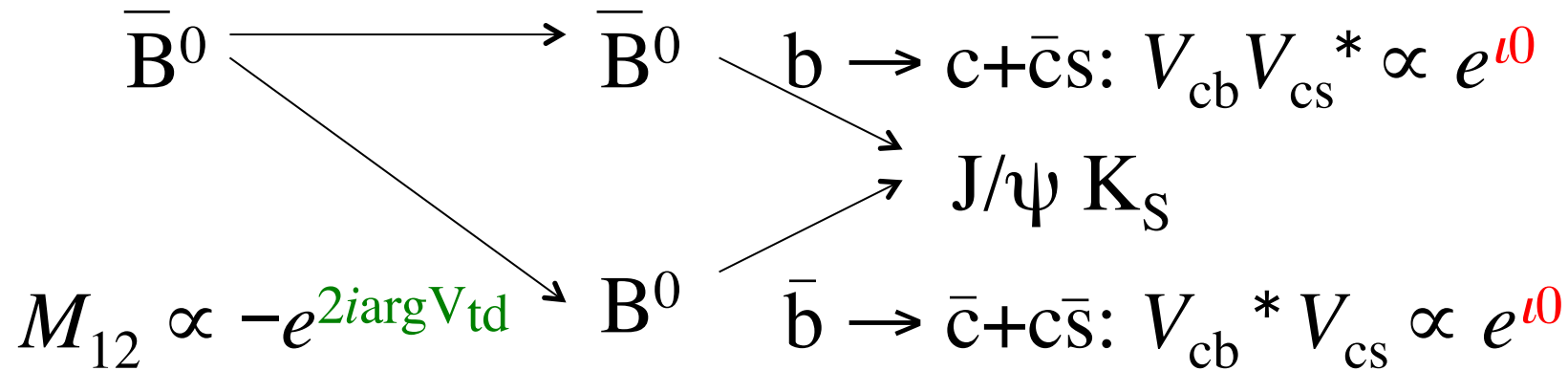
# Current Status of $V_{CKM}$



# Current Status of $V_{CKM}$

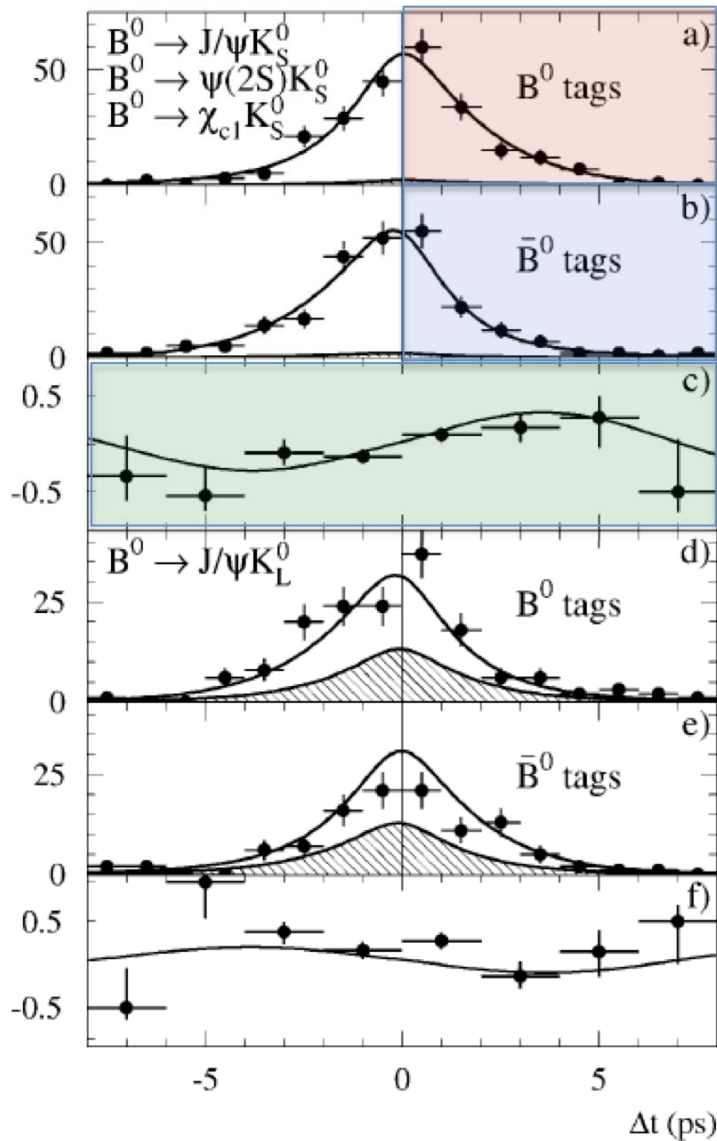


# Current Status of $V_{CKM}$



two processes interfere  $\rightarrow$  CPV  $\propto \sin 2 \arg V_{td}$

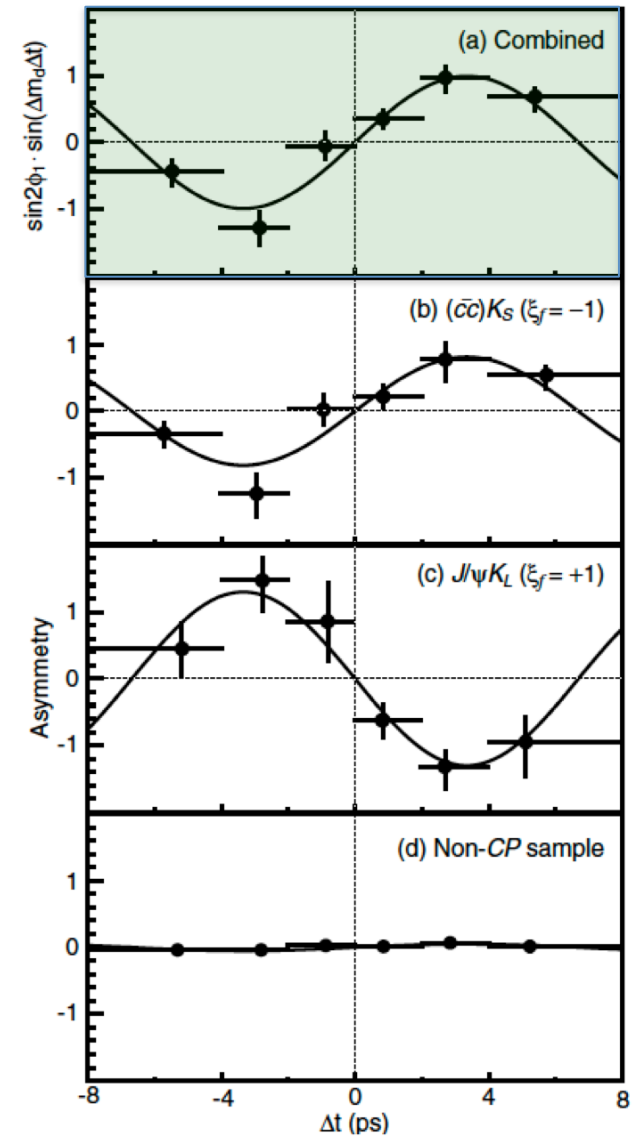
# Current Status of $V_{CKM}$



$$\bar{B}^0_{t=0} \rightarrow J/\psi K_S(t)$$

$$B^0_{t=0} \rightarrow J/\psi K_S(t)$$

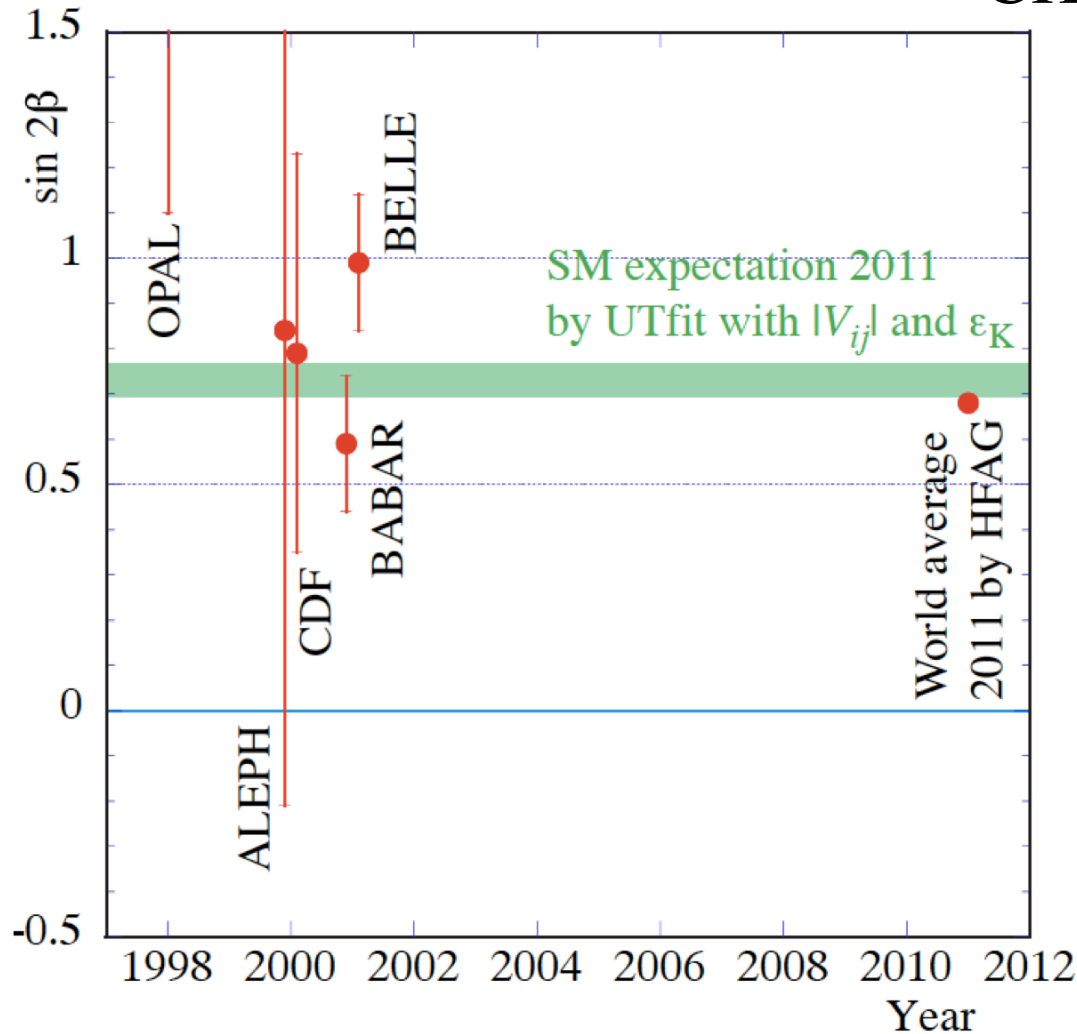
Time dependent  
CP asymmetries



BABAR: Phys. Rev. Lett. 87, 091801 (2001)

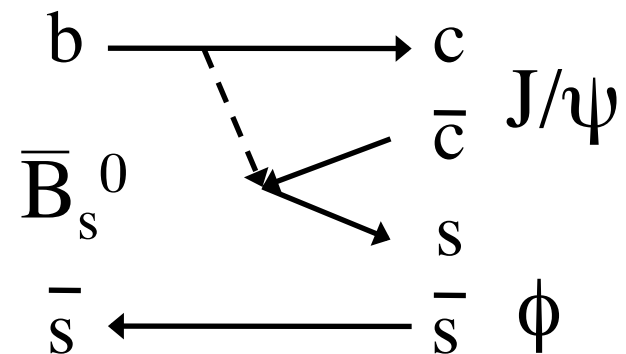
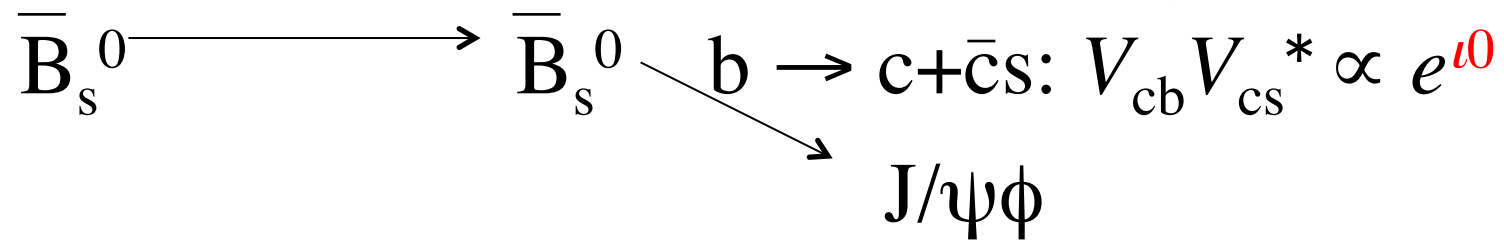
BELLE: Phys. Rev. Lett. 87, 091802 (2001)

# Current Status of $V_{CKM}$



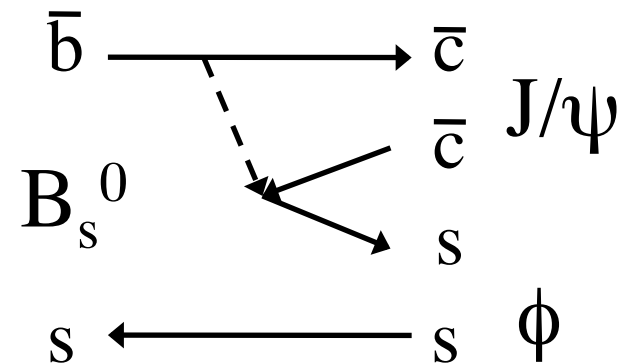
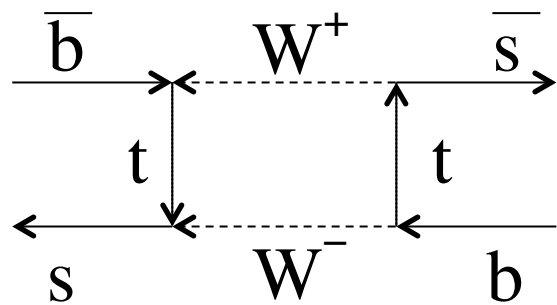
two processes interfere  $\rightarrow$  CPV  $\propto$  sin  $2\arg V_{td}$   
 $0.679 \pm 0.020$  (HFAG 2012)

# Current Status of $V_{CKM}$

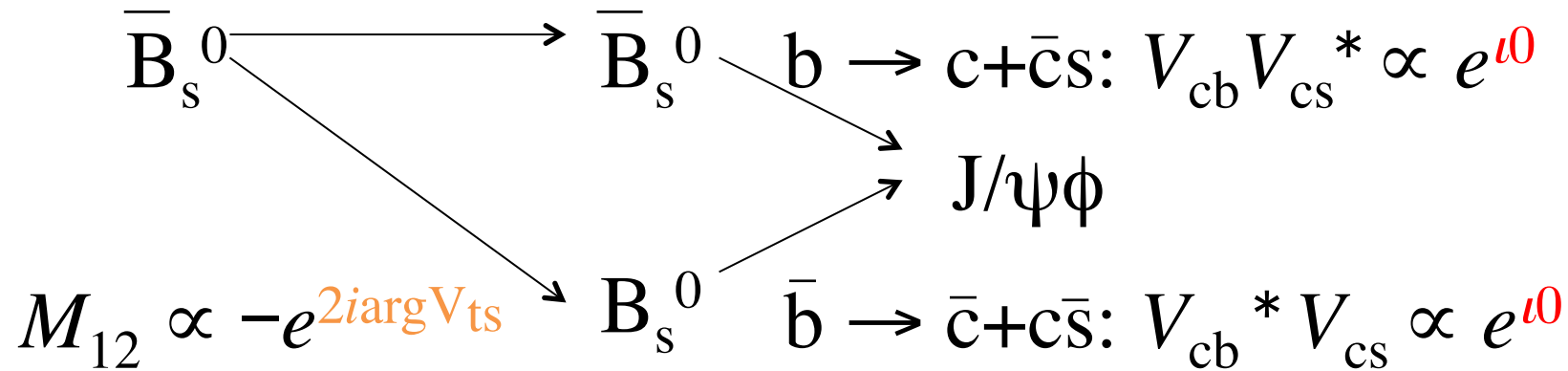


# Current Status of $V_{CKM}$

$\bar{B}_s^0 \rightarrow B_s^0 \rightarrow J/\psi K_S \text{ or } J/\psi \phi$   
 $M_{12} \propto -e^{2i \arg V_{td}}$  or  $-e^{2i \arg V_{ts}}$   
 $\bar{b} \rightarrow \bar{c} + c \bar{s}: V_{cb}^* V_{cs} \propto e^{i\theta}$



# Current Status of $V_{CKM}$

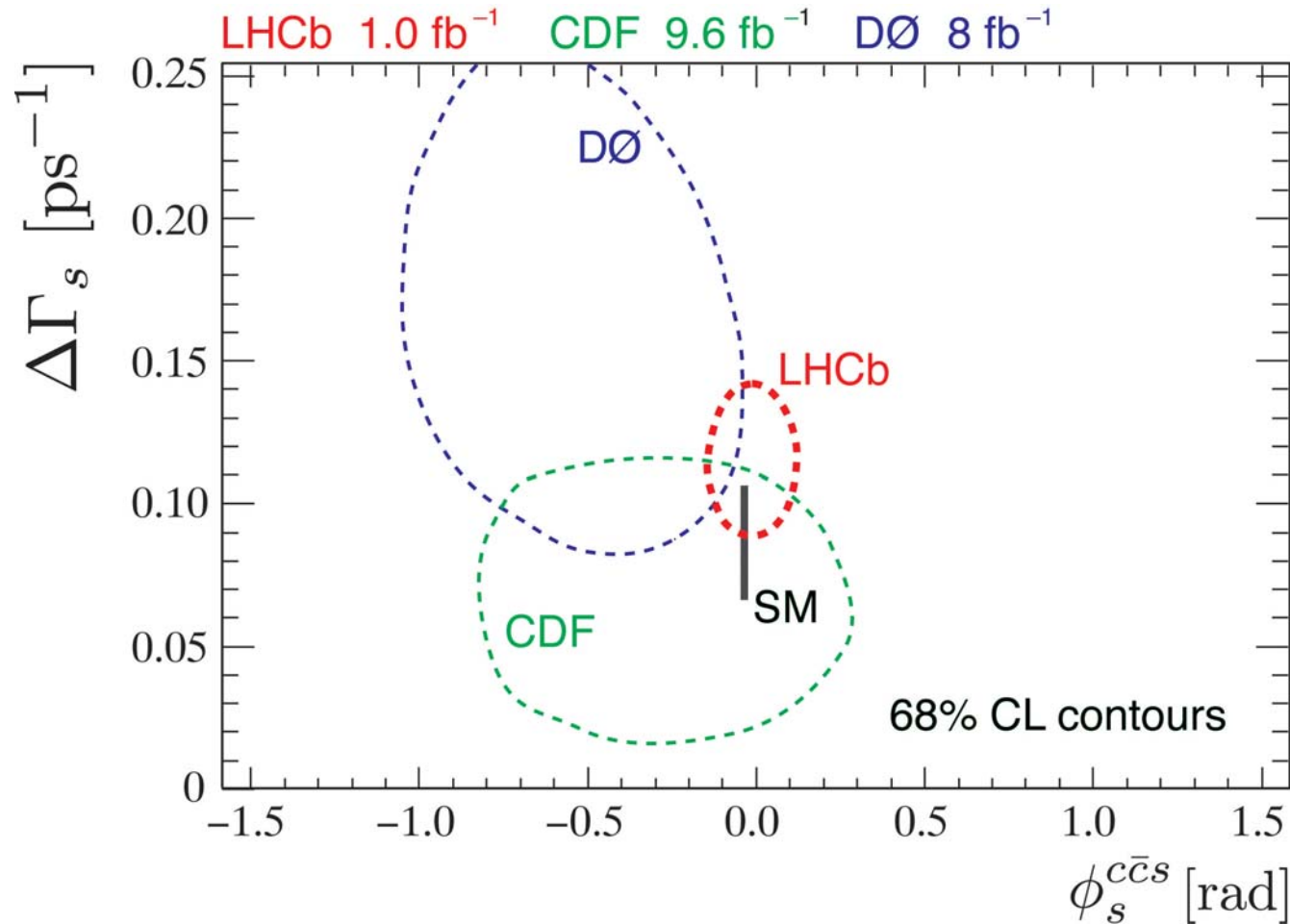


two processes interfere  $\rightarrow$  CPV  $\propto \sin 2\arg V_{ts}$

not yet well measured



# Current Status of $V_{CKM}$



two processes interfere  $\rightarrow$  CPV  $\propto$   $\sin 2\arg V_{ts}$

$$-0.044^{+0.090}_{-0.085} \quad (\text{HFAG 2012})$$

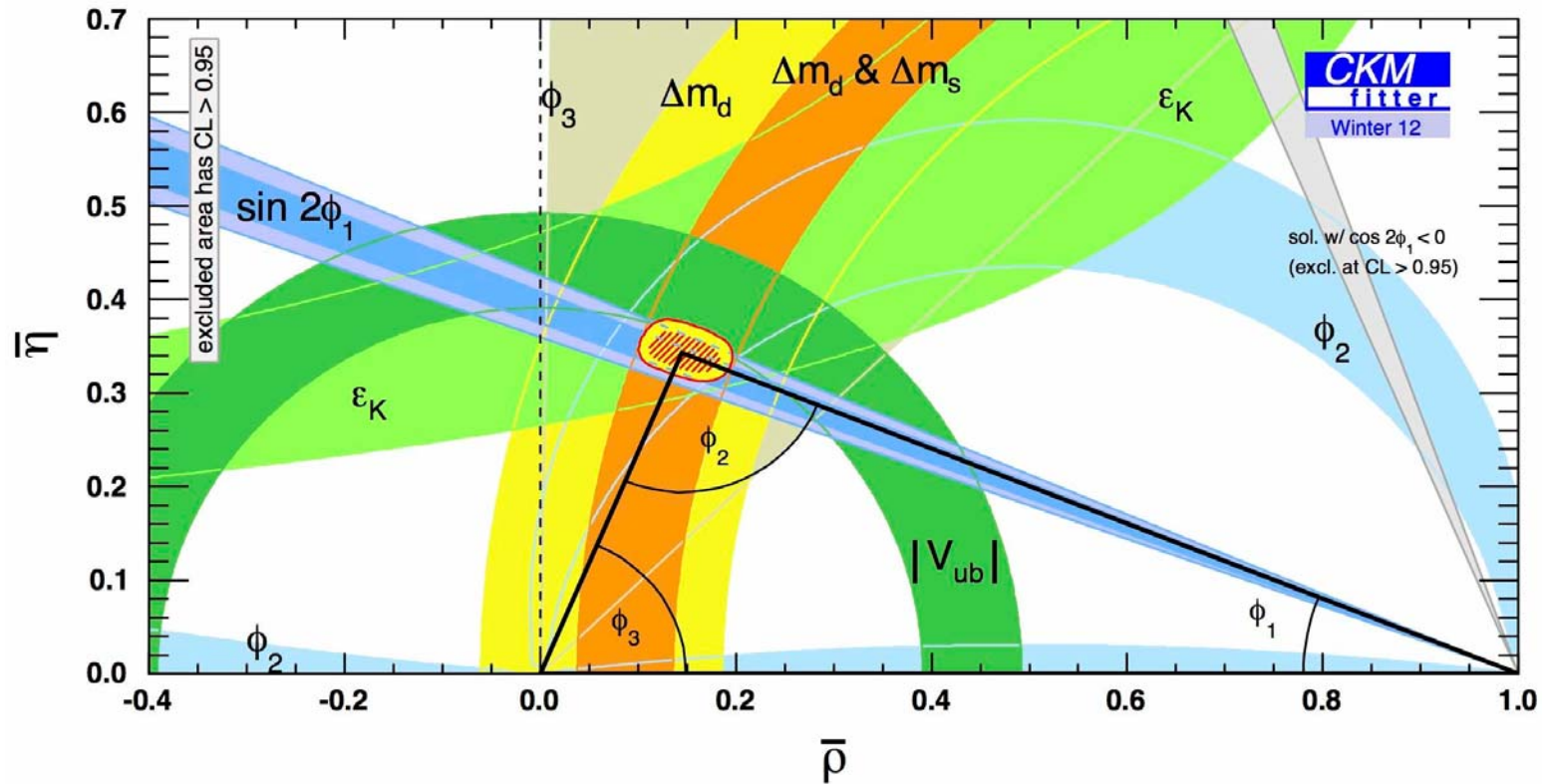
# Current Status of $V_{\text{CKM}}$

$$\approx \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda - iA^2\lambda^5\eta & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \hat{\rho} - i\hat{\eta}) & -A\lambda^2 - iA\lambda^4\eta & 1 \end{pmatrix} \quad \begin{aligned} \hat{\rho} &= \rho \left(1 - \frac{\lambda^2}{2}\right) \\ \hat{\eta} &= \eta \left(1 - \frac{\lambda^2}{2}\right) \end{aligned}$$

$A$  from  $|V_{cb}|$ ,  $\rho$  and  $\eta$  from  $\left\{ \begin{array}{l} |V_{ub}| \text{ and } \arg V_{ub} \\ |V_{tb}| \text{ and } \arg V_{tb} \\ |V_{ub}| \text{ and } |V_{tb}| \\ |V_{td}| \text{ and } \arg V_{ub} \end{array} \right.$

many solutions  
 i.e.  
 consistency  
 can be checked

# Current Status of $V_{CKM}$



- BABAR completed in 2008 and Belle completed in 2010  
 $\sim 1.2 \text{ ab}^{-1}$  data, i.e.  $\sim 1.3 \times 10^9 \text{ BB}$
- CDF and D0 completed in 2011,  $\sim 20 \text{ fb}^{-1}$  data
- LHCb running, 7 TeV in 1010+2011 ( $1 \text{ fb}^{-1}$ ), 8 TeV in 2012

# Current Status of $V_{CKM}$

- To look for New Physics, extraction of  $(\lambda, A, \rho, \eta)$  with the processes totally dominated by the SM
  - tree decays
    - $\lambda$  and  $A$  are already from the tree decay modes
    - $(\rho, \eta)$  from the tree decays:
      - $|V_{ub}/V_{cb}|$  from the semileptonic decays
      - $\arg V_{ub}$  from  $B \rightarrow DK^*$  (interference between  $b \rightarrow c$  and  $b \rightarrow u$ )

$B^\pm \rightarrow$  “D”  $K^\pm$ , with “D”  $\rightarrow K^+\pi^-$  and  $K^-\pi^+$   
 with “D”  $\rightarrow K^+K^-$  or  $\pi^+\pi^-$   
 with “D”  $\rightarrow \underline{K}_S\pi^+\pi^-$  Dalitz plot

$B^0 \rightarrow$  “D”  $K^{*0}$  and “D”  $K^{*0}$  with “D” decays

}  
 BABAR  
 Belle  
 LHCb

Time dependent CP asymmetries  
 of  $B_s(t=0) \rightarrow D_s^\pm K^\mp$  vs CP conjugated state

LHCb

# Current Status of $V_{CKM}$

- To look for New Physics, extraction of  $(\lambda, A, \rho, \eta)$  with the processes totally dominated by the SM
  - tree decays
    - $\lambda$  and  $A$  are already from the tree decay modes
    - $(\rho, \eta)$  from the tree decays:
      - $|V_{ub}/V_{cb}|$  from the semileptonic decays
      - $\arg V_{ub}$  from  $B \rightarrow DK^*$  (interference between  $b \rightarrow c$  and  $b \rightarrow u$ )

$B^\pm \rightarrow$  “D”  $K^\pm$ , with “D”  $\rightarrow K^+\pi^-$  and  $K^-\pi^+$

Can you demonstrate these?

$B^0 \rightarrow$  “D”  $K^{*0}$  and “D”  $K^{*0}$  with “D” decays

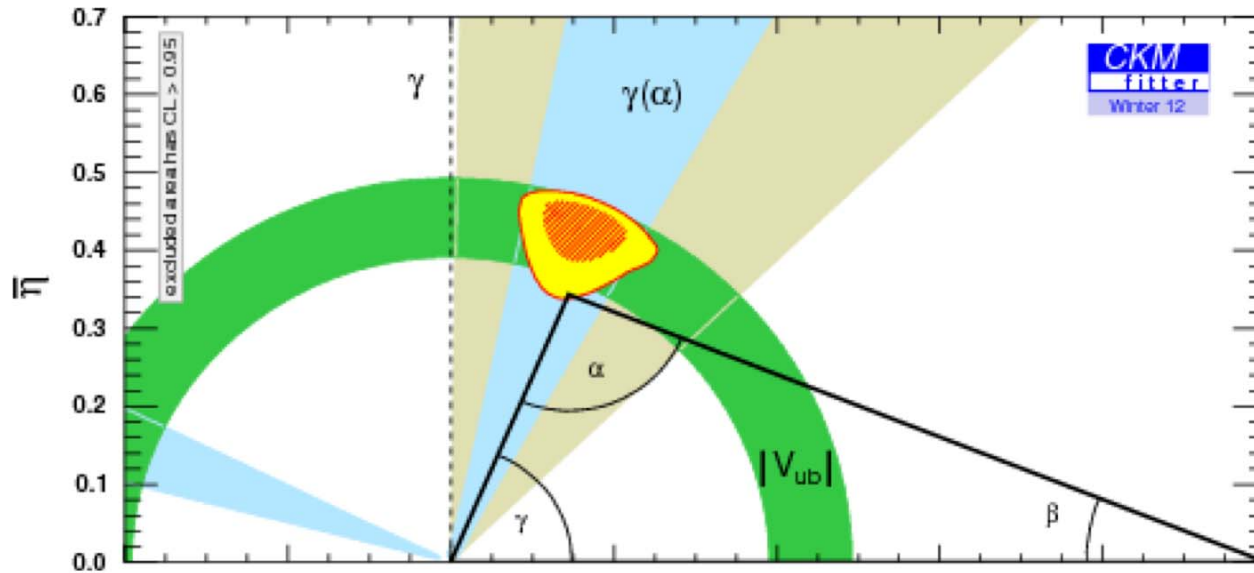
Time dependent CP asymmetries  
of  $B_s(t=0) \rightarrow D_s^\pm K^\mp$  vs CP conjugated state

LHCb

# Current Status of $V_{\text{CKM}}$

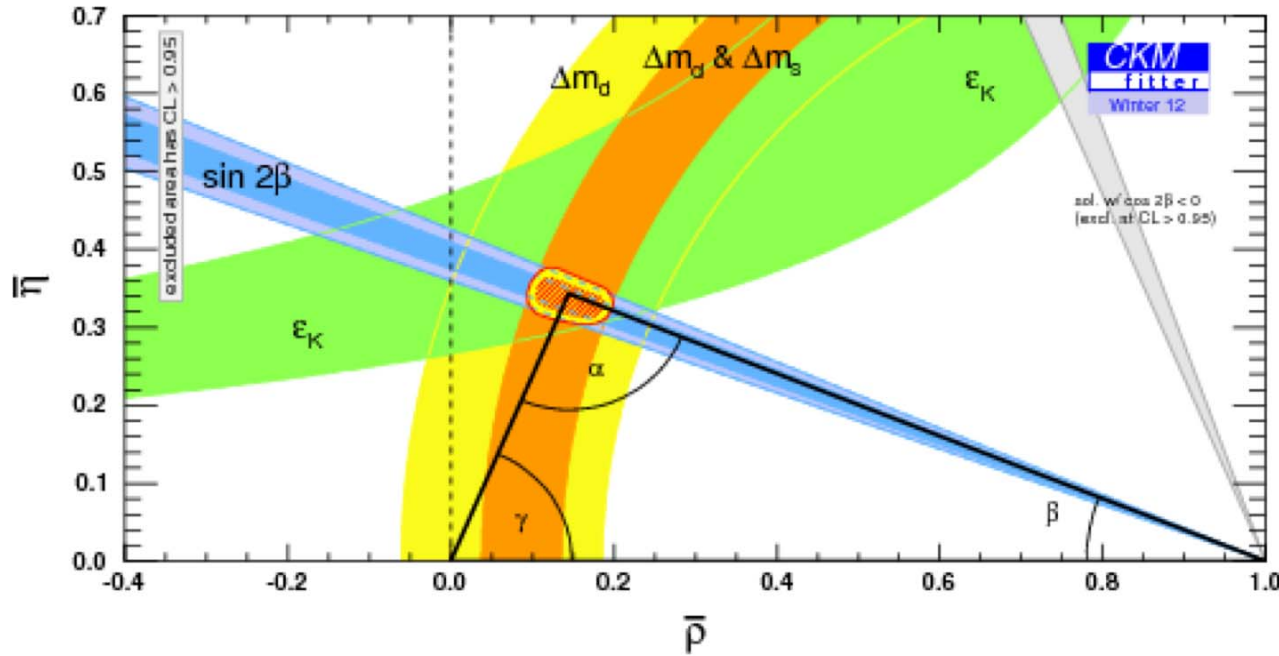
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- Should be compared with  $(\rho, \eta)$  from the loop processes:
  - $|V_{td}|$  from  $\Delta m_d$  and  $\arg V_{td}$  from CPV in  $B_d \rightarrow J/\psi K_S$
  - Combination of  $\varepsilon_K$  with  $|V_{td}|$  or CPV in  $B_d \rightarrow J/\psi K_S$

- To wit



$\rho, \eta$

- Show



$\rho$

# Current Status of $V_{CKM}$

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  - Combination of  $\varepsilon_K$  with  $|V_{td}|$  or CPV in  $B_d \rightarrow J/\psi K_S$
- Further improvement with the LHCb data expected



# Current Status of $V_{CKM}$

- No sign of new physics in  $B \rightarrow \mu^+ \mu^-$   
 Now results dominated by the LHC experiments

95% CL upper limit

Mode	Limit	ATLAS	CMS	LHCb 2010	LHCb 2011	Combined
$B_s^0 \rightarrow \mu^+ \mu^-$ ( $10^{-9}$ )	Bkg Only	23	(3.6)	65	3.4	2.3
	Bkg+SM		8.4		7.2	6.1
	Obs	22	7.7 (7.2)	56	4.5	4.2
$B^0 \rightarrow \mu^+ \mu^-$ ( $10^{-10}$ )	Bkg Only	–	(13)	180	11	7.3
	Bkg+SM	–	16			
	Obs	–	14 (16)	150	10	8.1

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)_{SM} = (3.2 \pm 0.2) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)_{SM} = (1.0 \pm 0.1) \times 10^{-10}$$

# Plan of Lectures

- Direct-search versus Indirect-search
- Early History
- Standard Model Flavour Framework
- More of Weak Decay
- Current Status of  $V_{\text{CKM}}$
- Any Sign of New Physics
- Closer Look
- Epilogue

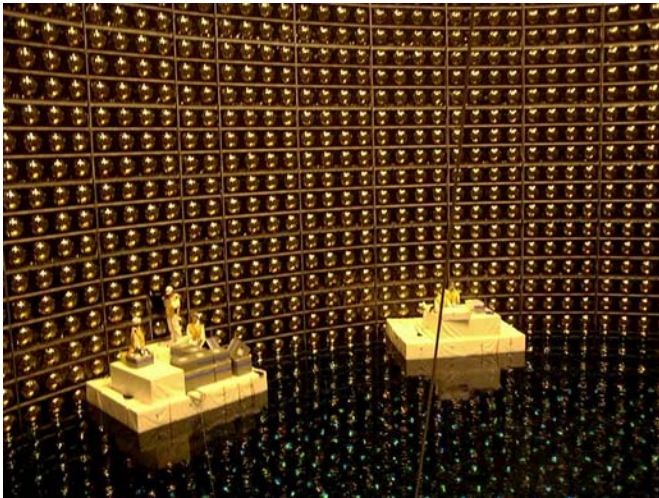
# Any Sign of New Physics?

- There exist solid observations for physics beyond the Standard Model

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- There exist solid observations for physics beyond the Standard Model  
Neutrino oscillations → in the SM,  $m_\nu = 0$  by definition

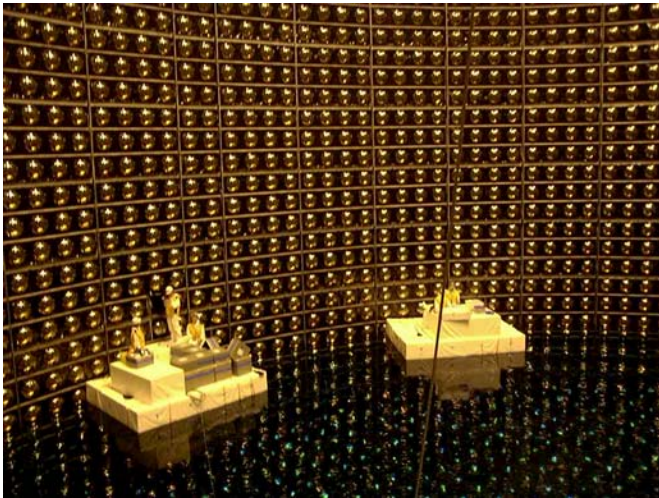
S-KAMIOKANDE



# Any Sign of New Physics?

- There exist solid observations for physics beyond the Standard Model
  - Neutrino oscillations
  - Dark matter → **no candidate particle in the SM**

S-KAMIOKANDE



Bullet Galaxy Clusters



# Any Sign of New Physics?

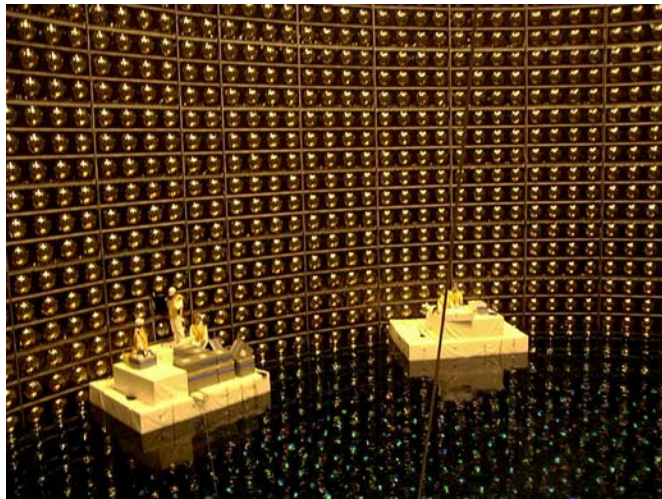
- There exist solid observations for physics beyond the Standard Model

Neutrino oscillations

Dark matter

$N_B / N_\gamma = 10^{-10}$  → the SM CPV not sufficient

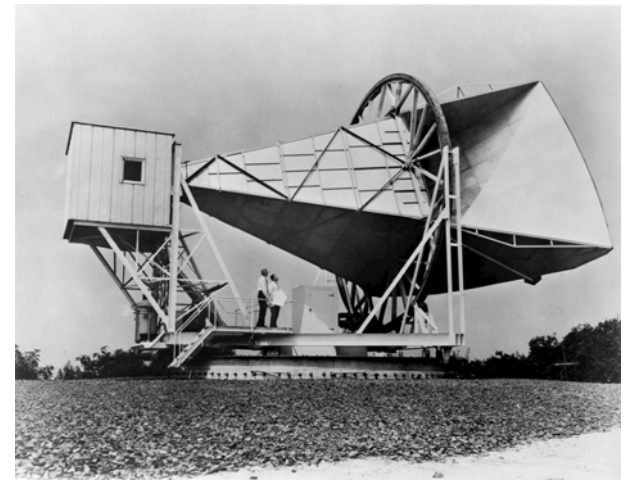
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Bullet Galaxy Clusters



The Horn Antenna  
Bell Telephone Laboratory



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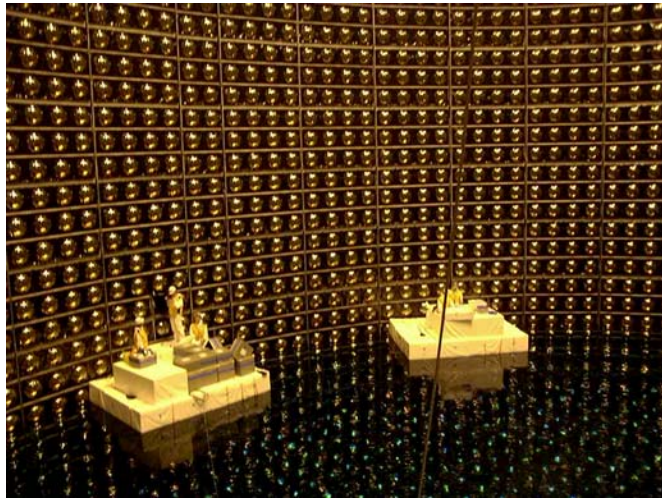
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Neutrino oscillations

Dark matter

$$N_B / N_\gamma = 10^{-10}$$

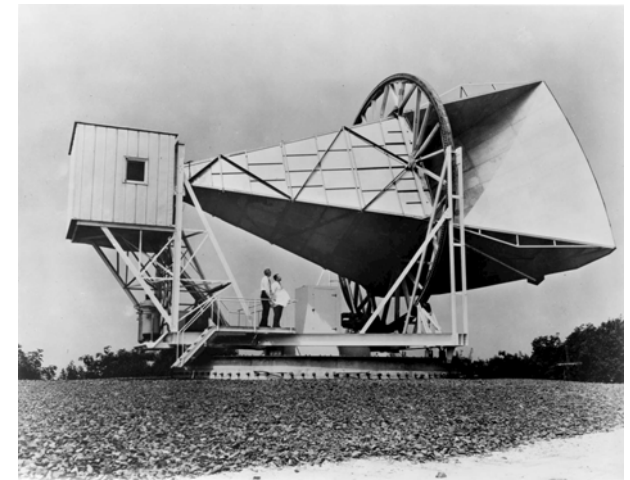
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- And the SM includes no gravity, has too many parameters, requires some fine tunings, etc.

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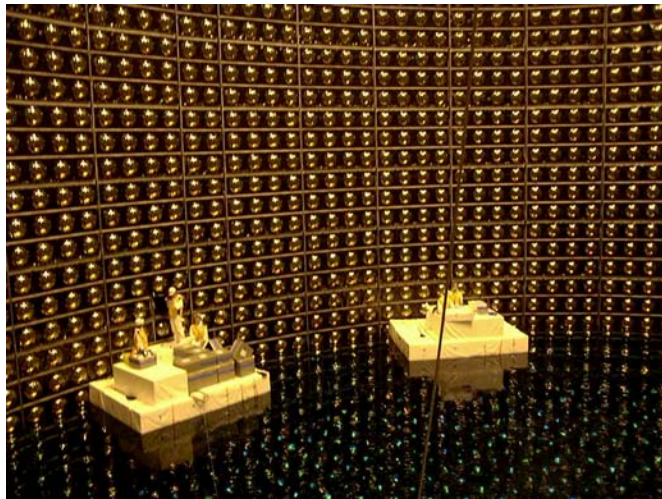
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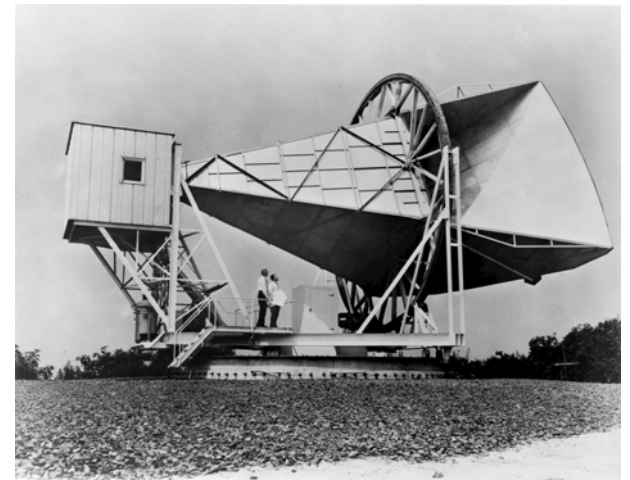
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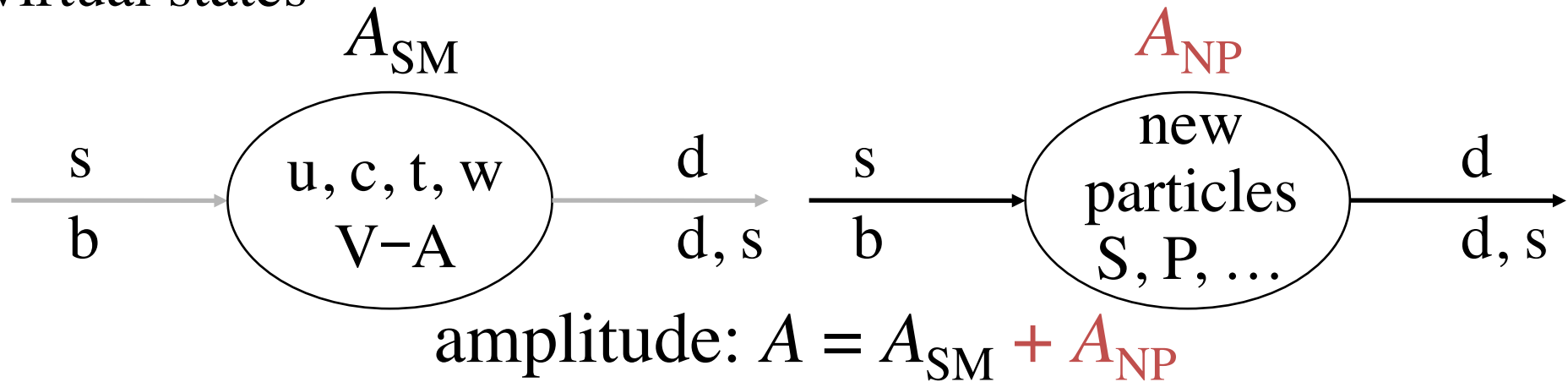


- And the SM includes no gravity, has too many parameters, requires some fine tunings, etc. However, we do not know whether the energy scale for new physics accessible to us...



# Closer Look

In general, new physics can enter in the loop diagrams as virtual states

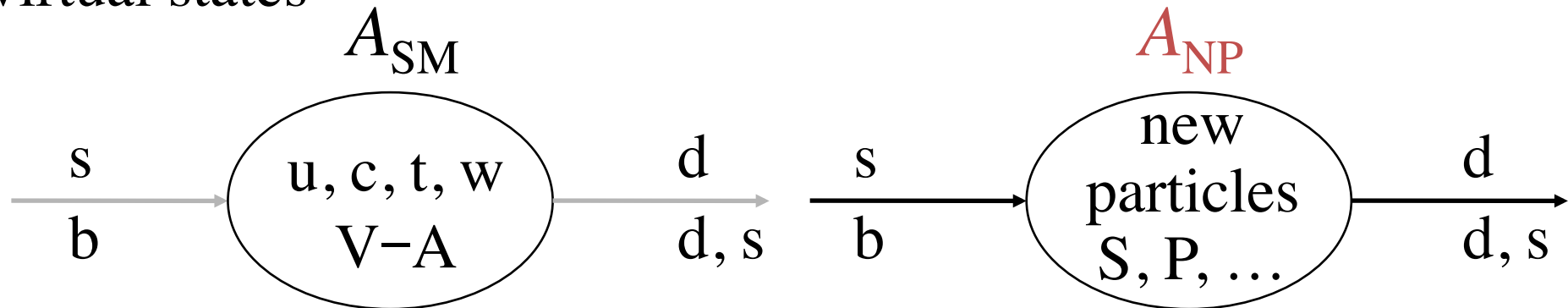


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# Closer Look

In general, new physics can enter in the loop diagrams as virtual states



amplitude:  $A = A_{SM} + A_{NP}$

$|A|$ :

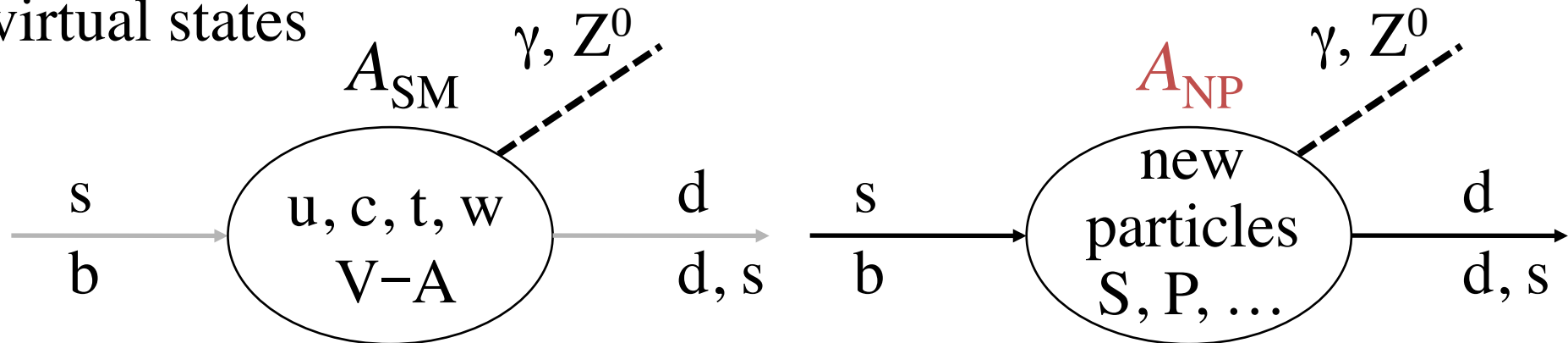
rare decays ( $\Delta F=1$ ),  $\Delta m$  ( $\Delta F=2$ )

$\arg A$ :

CP violation

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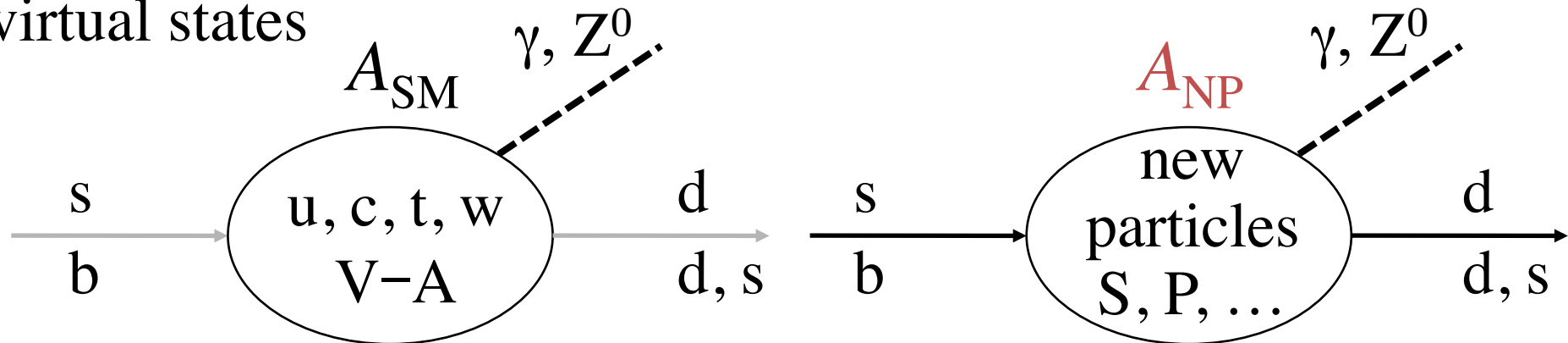
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Lorentz structure of  $A$ : “photon” polarization via

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Lorentz structure of  $A$ : “photon” polarization via

final state angular distribution or mixing-decay CP violation

If coupling  $\approx O(\text{weak})$ , already  $m(\text{NP}) > O(100\text{TeV})$

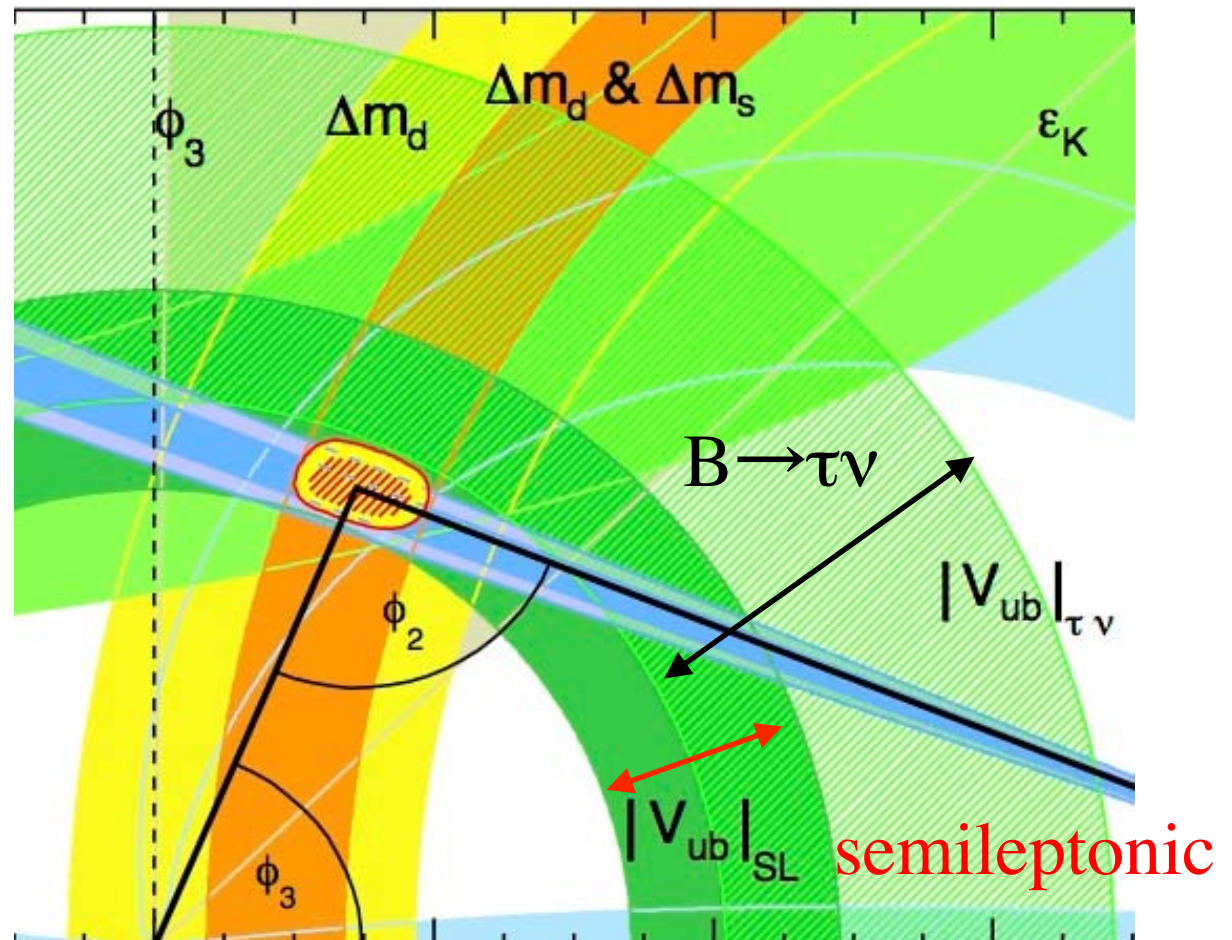
→ Minimal Flavour Violation (same origin for all FSB)?

Should be still visible in the Br. and Lorentz structure

# Closer Look

- If one looks closer, any hint of discrepancies?
  - “ $\sin 2\beta$ ” extracted from CPV in  $B_d \rightarrow J/\psi K_S$  somewhat small
  - $|V_{ub}|$  extracted from  $B \rightarrow \tau \nu$  decays larger than  $|V_{ub}|$  extracted from the **semileptonic** decays.

CPV in  $B_d \rightarrow J/\psi K_S$

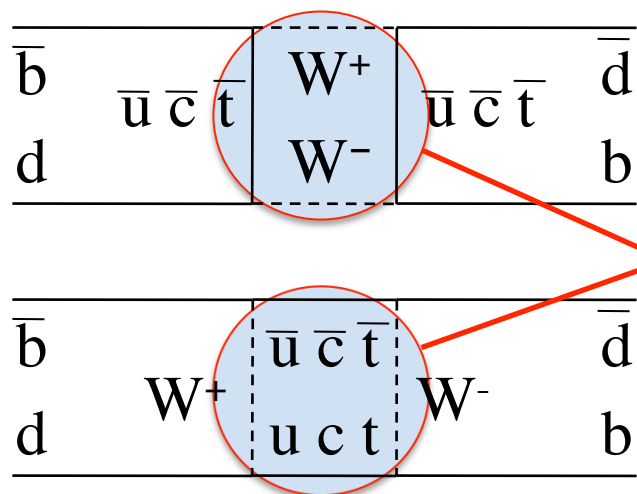


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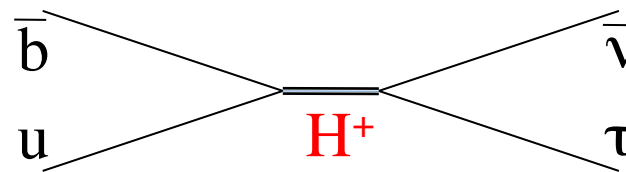
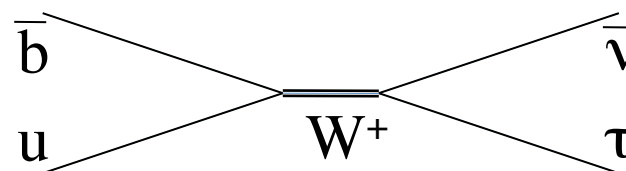
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  1. Problem with extracting  $|V_{ub}/V_{cb}|$  due to the hadronic uncertainties

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- This could be due to
  1. Problem with extracting  $|V_{ub}/V_{cb}|$  due to the hadronic uncertainties
  - OR
  2. New Physics in  $B^0$ - $\bar{B}^0$  oscillations and charged Higgs in  $B \rightarrow \tau \nu$



+ new particles





# Closer Look

$|V_{cb}|$  and  $|V_{ub}|$

Errors are **dominated by the theoretical uncertainties** in the strong interaction for the semileptonic decays.

⇒ can be reduced by studying the decay kinematics,  
e.g. lepton momentum, hadronic-mass distribution, etc.  
with **higher statistics in a clean environment**

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**Case for Super B Factories:**

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$|V_{ub}|$  from  $B^\pm \rightarrow \tau^\pm \nu$  error still **statistics limited**.

Recent Belle:  $(1.14 \pm 0.23) \times 10^{-4}$ , only  $1.3\sigma$  away from SM

**Another case Super B Factories**

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Another case Super B Factories

$\text{Br}(B \rightarrow D^{(*)} \tau \nu)$  by BABAR: larger than SM by  $\sim 3.4\sigma$ ,  
also due to charged Higgs? (but only complicated ones)

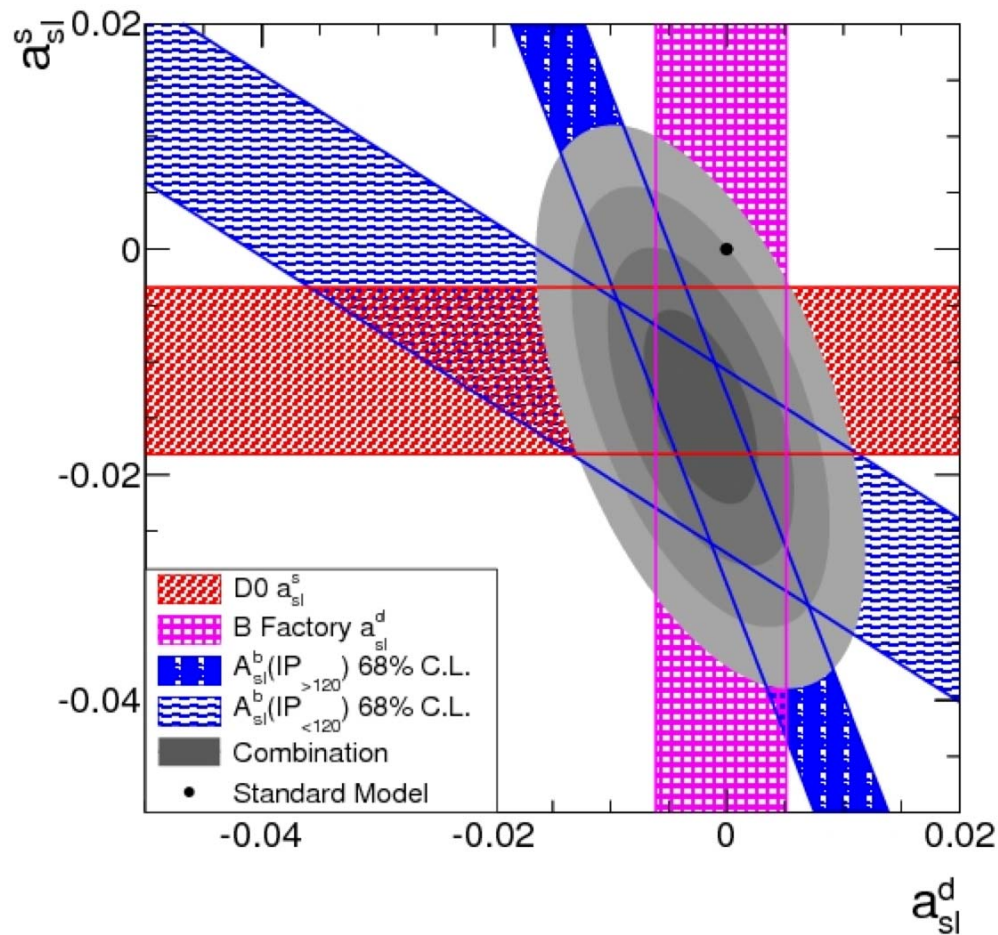
**Looking forward to the Belle analysis**

# Closer Look

- CPV in the  $B_s$  system: used to be “almost” untouched territory:  
Started with CDF and D0

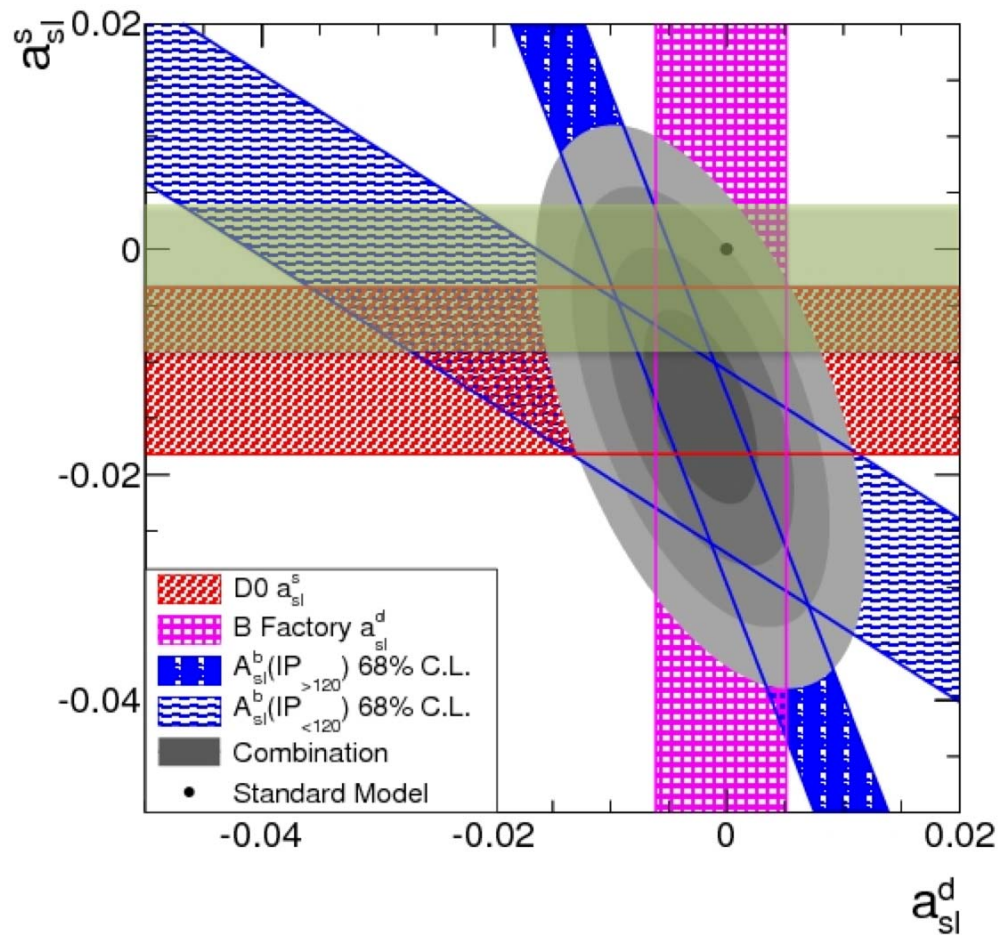
# Closer Look

- CPV in the  $B_d-\bar{B}_d$  and  $B_s-\bar{B}_s$  oscillations: SM small  
D0 measures possibly large CPV for  $B_s$



# Closer Look

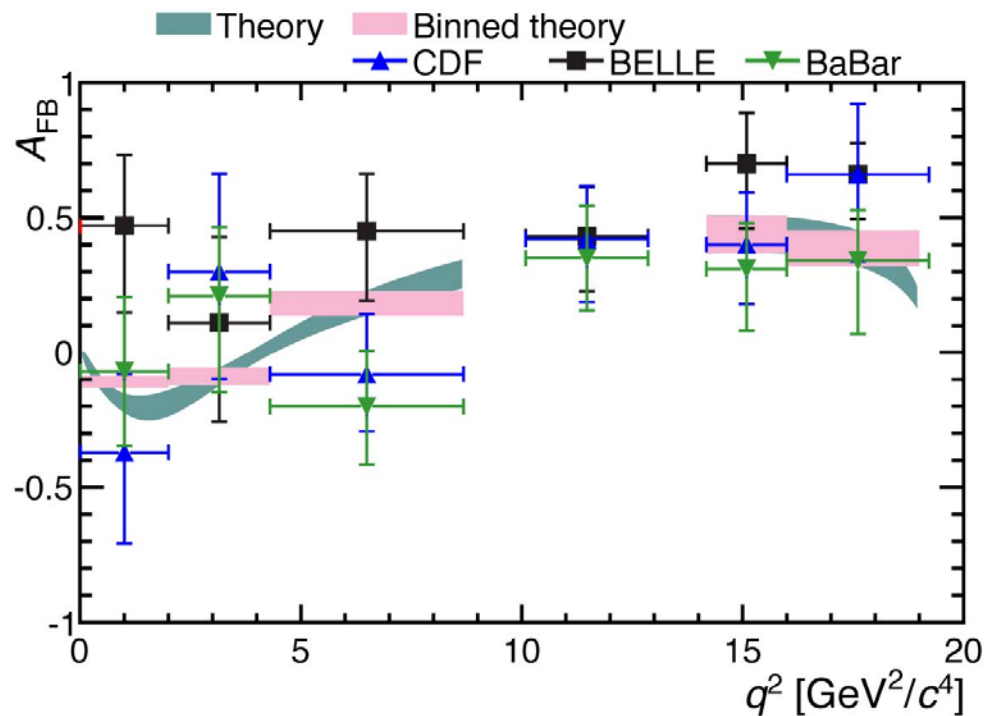
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Not confirmed by  
by LHCb  $1 \text{ fb}^{-1}$  data  
Much more data  
in future

# Closer Look

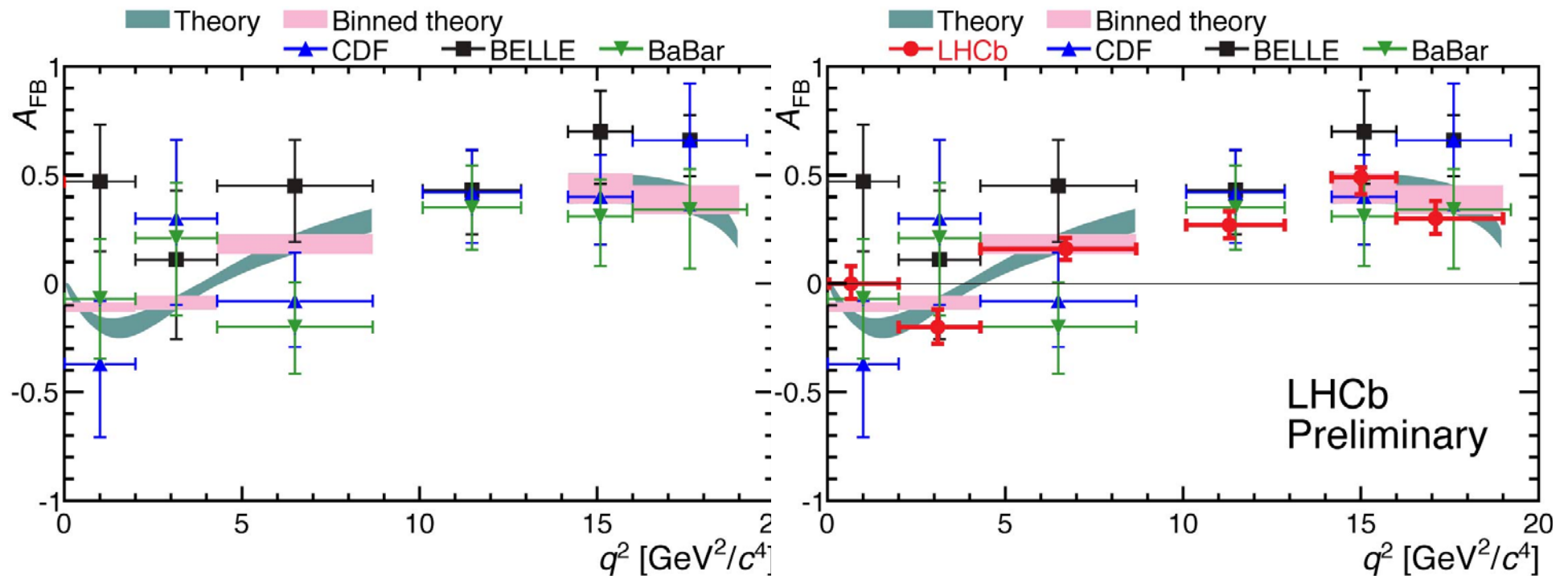
- Lorentz structure of electroweak penguin current with  $B \rightarrow K^{*0} \mu^+ \mu^-$  decays:  
example:  $A_{FB}$  of the muon pairs v.s.  $m^2(\mu^+ \mu^-)$   
BABAR+BELLE+CDF: inconclusive





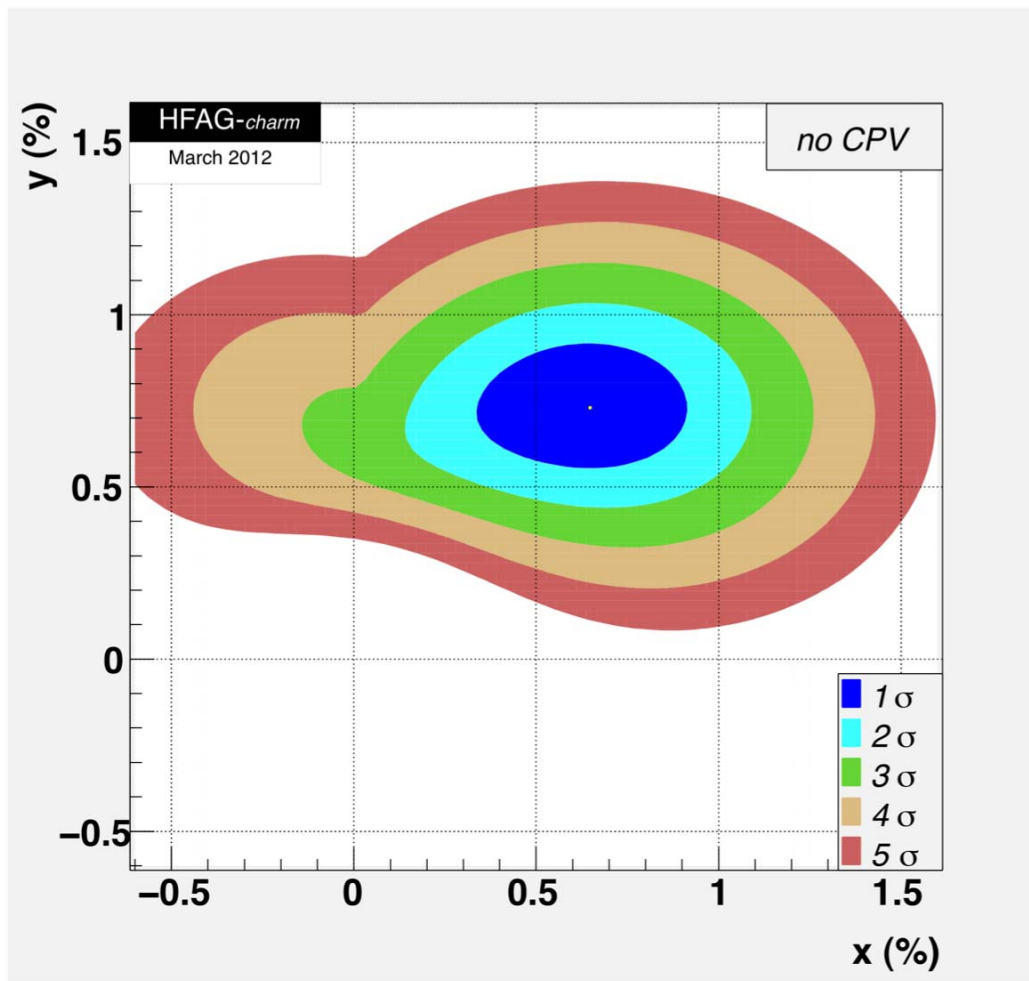
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LHCb ( $1 \text{ fb}^{-1}$ ) good agreement with SM



# Closer Look

- Up-type quarks: D-meson system:  
 $\bar{D}$ -D mixing observed, SM prediction difficult



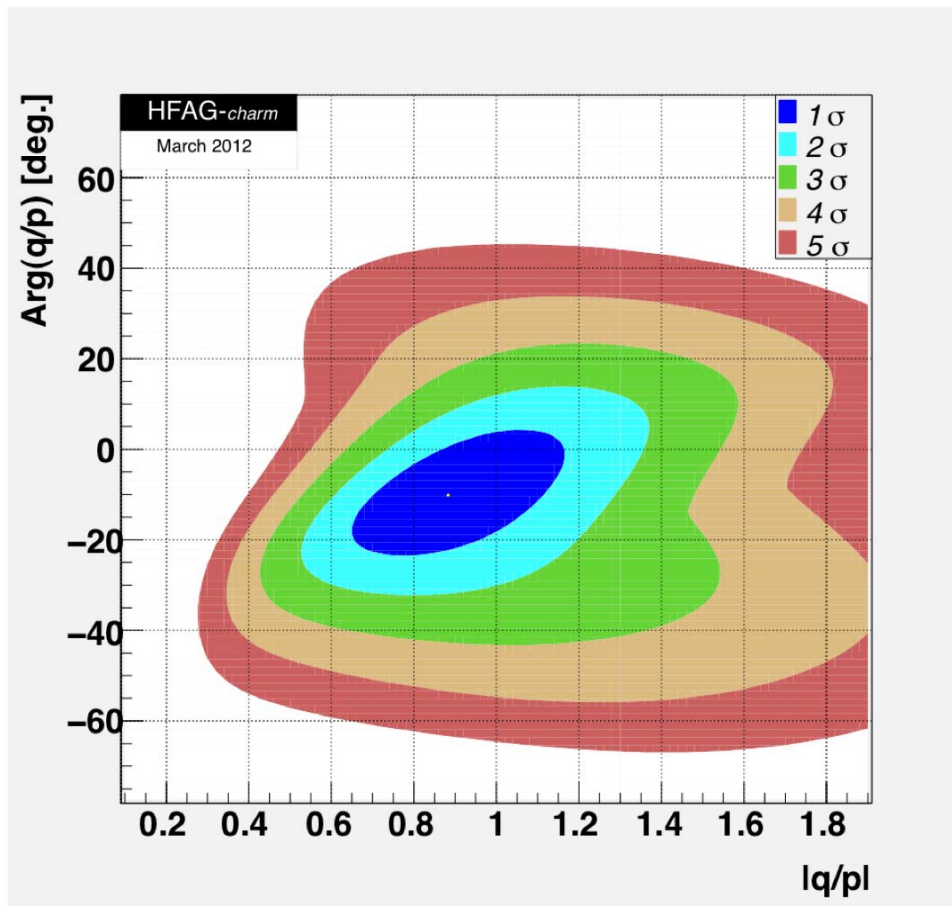
$$x = \Delta m / \bar{\Gamma}$$

$$y = \Delta \Gamma / \bar{\Gamma}$$

No mixing:  $x = y = 0$

# Closer Look

- Up-type quarks: D-meson system:  
 $\bar{D}$ -D mixing observed, SM prediction difficult  
CPV in  $\bar{D}$ -D oscillations not seen, small in SM



No CPV in oscillations

$$|p/q|=1$$

$$\arg(p/q) = 0$$

# Closer Look

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CPV in the decay amplitudes: ???

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$$\Delta A_{\text{CP}} = A_{\text{CP}}(\text{K}^+\text{K}^-) - A_{\text{CP}}(\pi^+\pi^-)$$

$$\text{LHCb} \quad -0.82 \pm 0.24 \quad (0.62 \text{ fb}^{-1})$$

$$\text{CDF} \quad -0.62 \pm 0.23$$

$$\text{Belle} \quad -0.87 \pm 0.41$$

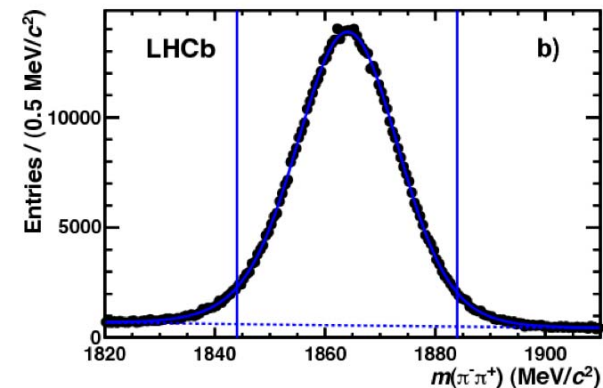
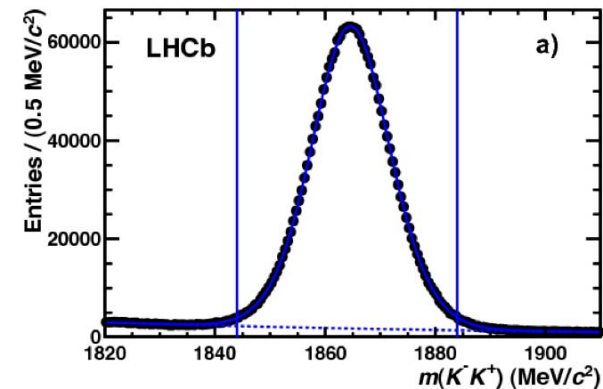
SM expectation was  $O(10^{-3})$

could be stretched to  $\sim 5 \times 10^{-3}$  ?

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More data with LHCb will be interesting  
c.f. very clean tagged D signal



# And Bigger Picture

- Kaon physics  $K^+ \rightarrow \pi^+ \nu \nu$ ,  $K_L^0 \rightarrow \pi^0 \nu \nu$   
testing of MFV
- Charged lepton flavour violation search  
SUSY?
- And even more fundamental...  
Quark-lepton flavour unification?  
Origin of flavour structure?

# Plan of Lectures

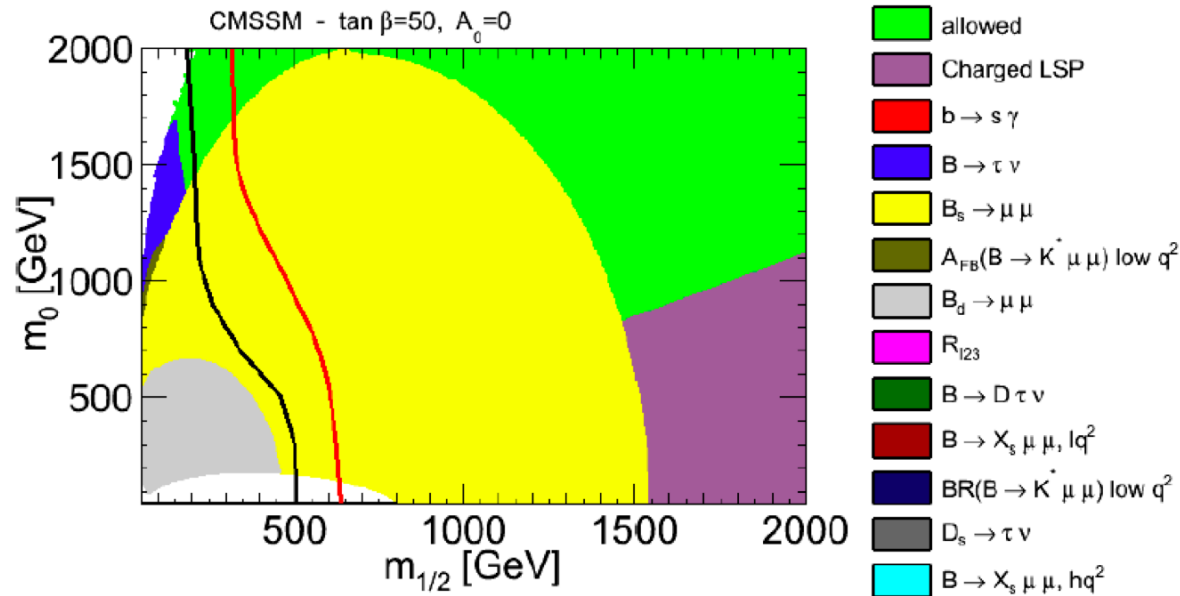
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- **Epilogue**



# Epilogue

## Synergy between the direct and indirect search

### Implications



Black line: CMS exclusion limit with  $1.1 \text{ fb}^{-1}$  data

Red line: CMS exclusion limit with  $4.4 \text{ fb}^{-1}$  data

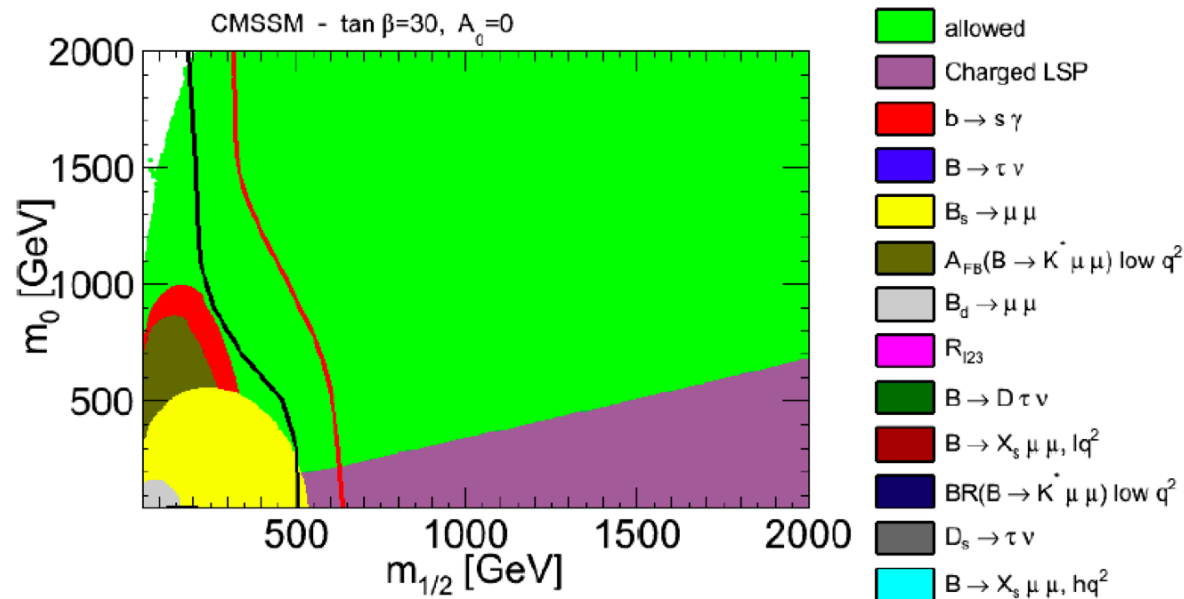
New LHCb limits for  $BR(B_s \rightarrow \mu^+ \mu^-)$  and  $BR(B_d \rightarrow \mu^+ \mu^-)$

SuperIso v3.2+

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# Epilogue

By the ~~middle of 2012.~~ end of 2017

ATLAS CMS high $p_T$ physics	BSM
LHCb flavour physics	Only SM
Particle Physics	




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By the ~~middle of 2012~~ end of 2017

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Particle Physics				

Oh, no more space left...

# Epilogue

In any case,



**Exciting time is ahead of us all.**