

# Ultra-light scalar Dark Matter probed with the SDSS Lyman- $\alpha$ forest

*arxiv:1703.09126*

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**FKPPL Project « LYAWDM » :**

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*Combine analysis of SDSS quasars with cosmological simulations to study particle physics models (neutrinos, WDM, Fuzzy Dark Matter)*

# Fuzzy dark matter (FDM)

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- eg. Hu et al. PRL 2000, Marsh Phys. Rep. 2016, Hui et al. PRD 2017 ...
- **Lowest possible mass for DM ?**
  - Fermions : Tremaine-Gunn  $m \gtrsim \text{few } 100 \text{ eV}$ .
  - Bosons : down to  $\sim 10^{-24} \text{ eV}$
- **de Broglie wavelength for DM large** enough so that wave effects smooth density fluctuations on scales relevant to structure formation or DM halo dynamics

$$\frac{\lambda_{\text{dB}}}{2 \text{ kpc}} \sim \left( \frac{10^{-22} \text{ eV}}{m} \right) \left( \frac{10 \text{ km/s}}{v} \right)$$

- **A way to solve the CDM « small scale crisis » (DM cores in dwarfs, halo abundance...)**
- Theory motivation ?
  - pseudoscalar Axion-Like-Particles (ALPs) generic prediction in string compactification
  - relic field from misalignment mechanism similar to QCD axions with  $m \sim \mu\text{eV}$

# Structure formation in FDM

- Linear perturbations : FDM  $\sim$  fluid with effective sound speed

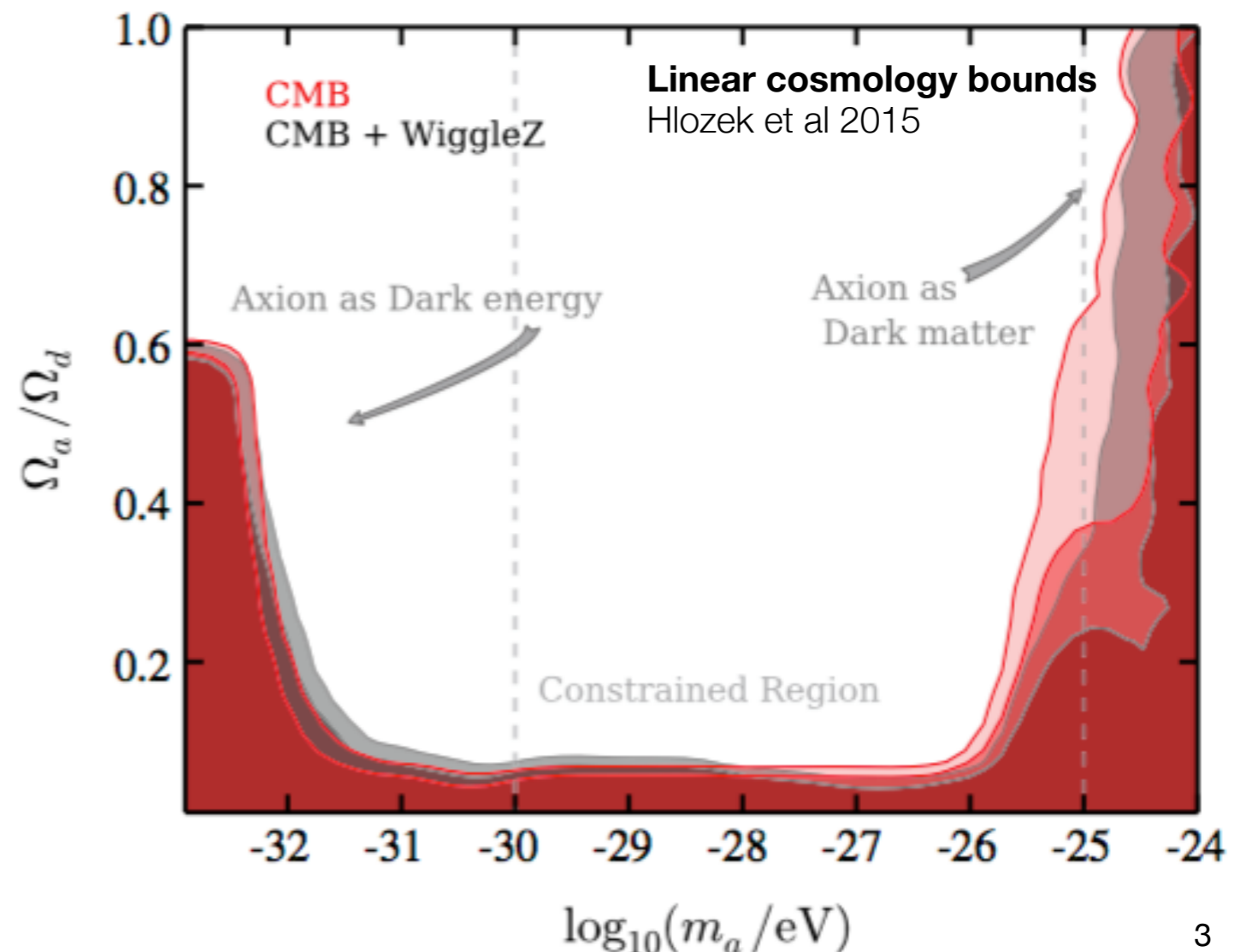
Related Jeans scale : 
$$k_J = 67 a^{1/4} \left( \frac{\Omega_a h^2}{0.12} \right)^{1/4} \left( \frac{m_a}{10^{-22} \text{ eV}} \right)^{1/2} \text{ Mpc}^{-1}$$

- Cut-off in matter power spectrum  $P(k)$  for scales smaller than Jeans scale at equality**

Linear cosmology probes  
exclude  $m_a \sim 10^{-24} - 10^{-25} \text{ eV}$

Larger masses  $\sim 10^{-22} \text{ eV}$   
constrained by non linear probes  
eg.

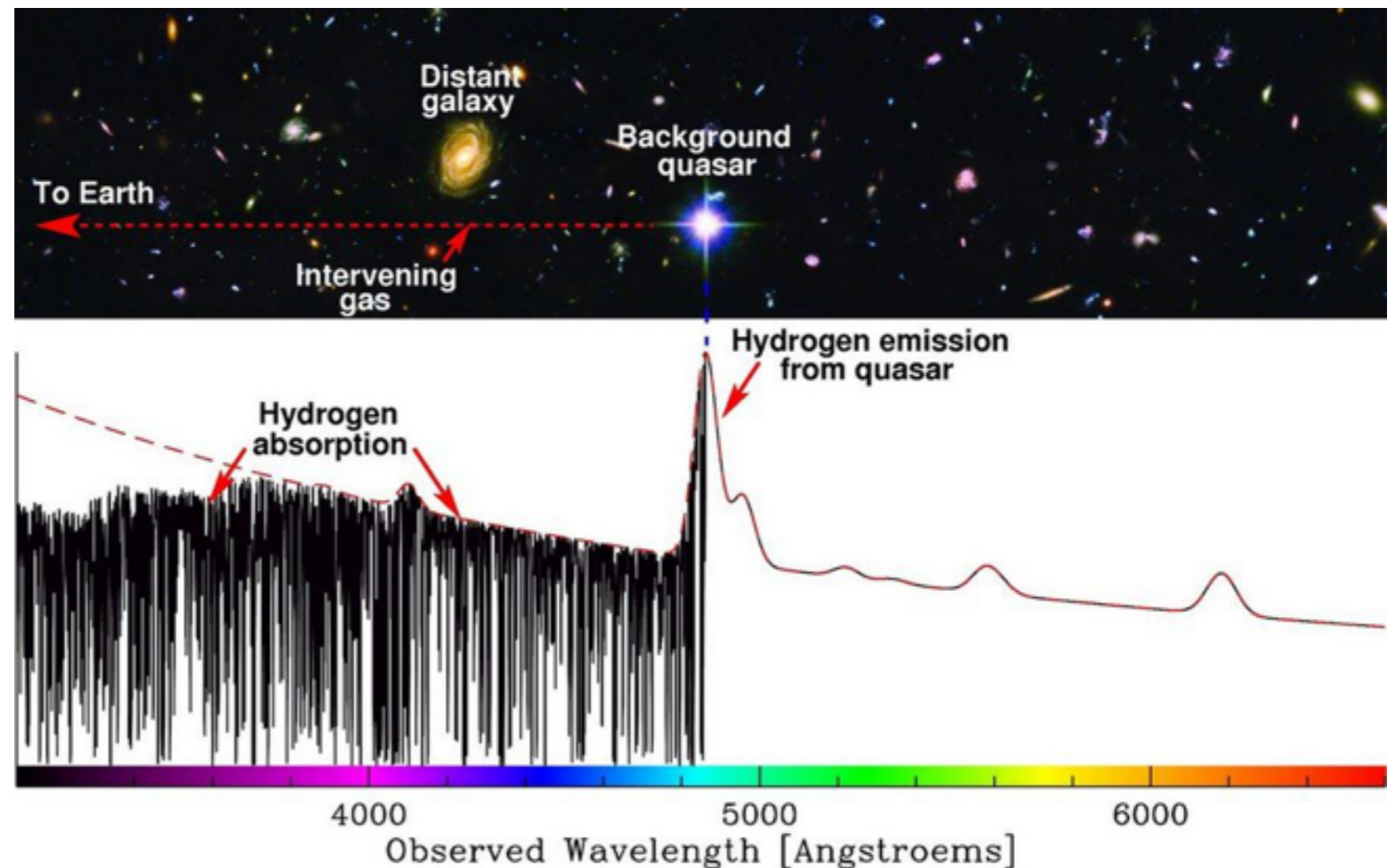
galaxy luminosity function  
**Lyman- $\alpha$  forest**



# The SDSS Lyman- $\alpha$ forest

**Measure fluctuations of Lyman- $\alpha$  flux transmitted by the neutral intergalactic medium (IGM)**

$\Rightarrow$  closely related to the small-scale matter power spectrum



**SDSS DR9 catalog** : 60000 quasar spectra

$\Rightarrow$  flux power spectra with near-% precision

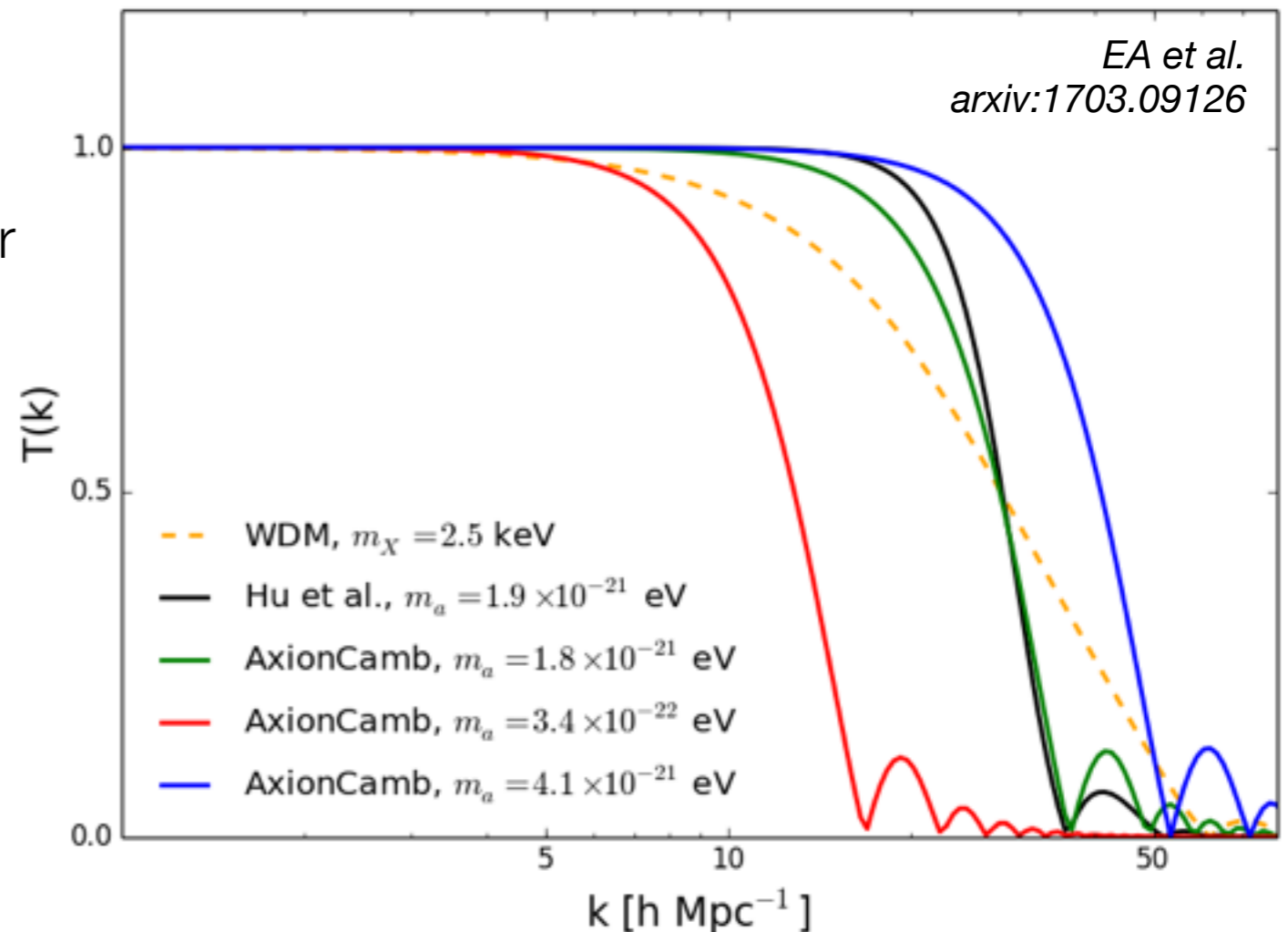
- $z=2.4-4.2$
- scales down to  $\approx$  Mpc

# Constraining FDM with the Lyman- $\alpha$ forest

- **Similar to WDM /  $\sum m_\nu$  bounds**
- **Linear power spectrum @z=30**
  - From AxionCAMB Boltzmann solver
  - WDM-FDM scaling law, such that  $T(k_c)=0.5$  :

$$m_X = 0.79 \left( \frac{m_a}{10^{-22} \text{ eV}} \right)^{0.42} \text{ keV}$$

- Shape different from WDM
- **Non-linear evolution + hydrodynamics of IGM : GADGET simulations**
  - resolution  $768^3$  particles  $25 \text{ h}^{-1} \text{ Mpc}$
- Predict flux power spectrum  $P_{1D}(k)$  and compare with data



## Model parameters :

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$\Omega_M, \sigma_8, n_s, h, m_a$

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$T_{0,\gamma}$  (IGM heating),  $\alpha, \beta$  (opt. depth)

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$a_{si}$ , noise, splicing

# Bounds on the FDM mass

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- **Based on SDSS quasars only :**

$m_a > 2.0 \times 10^{-21} - 2.3 \times 10^{-21} \text{ eV}$  depending on the method

- **Including high-resolution spectra** (XQ100+HIRES+MIKE)

$m_a > 2.9 \times 10^{-21} \text{ eV}$

- See also Irsic et al. arXiv:1703.04683 :

$m_a > 2.0 \times 10^{-21} - 3.7 \times 10^{-21} \text{ eV}$

different systematics

- **Current limitation : IGM modeling**

- **Average IGM parameters** : temperature and optical depth vs  $z$  :  $(T_0, \gamma)$  and  $(\alpha, \beta)$  free parameters.
- **IGM fluctuations of non-gravitational origin** (discrete ionizing sources, reionization-induced inhomogeneities, feedback eg. galactic outflows...) : simple parameterizations for related deviations of  $P(k, z)$ , with amplitudes left as free parameters.

# Validity of the N-body approximation for FDM ?

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Non-linear (newtonian) regime :

**Schrödinger equation  $\Rightarrow$  Madelung equation :**

*wavefunction : amplitude<sup>2</sup> =  $\rho$ ;  $\nabla(\text{phase}) = v$*

$$\partial_t \vec{v} + H \vec{v} + \frac{1}{a} (\vec{v} \cdot \nabla) \vec{v} = -\frac{1}{a} \nabla \left[ \phi - \frac{\hbar^2}{2m_a^2 a^2} \left( \frac{\nabla^2 \sqrt{\rho}}{\sqrt{\rho}} \right) \right]$$

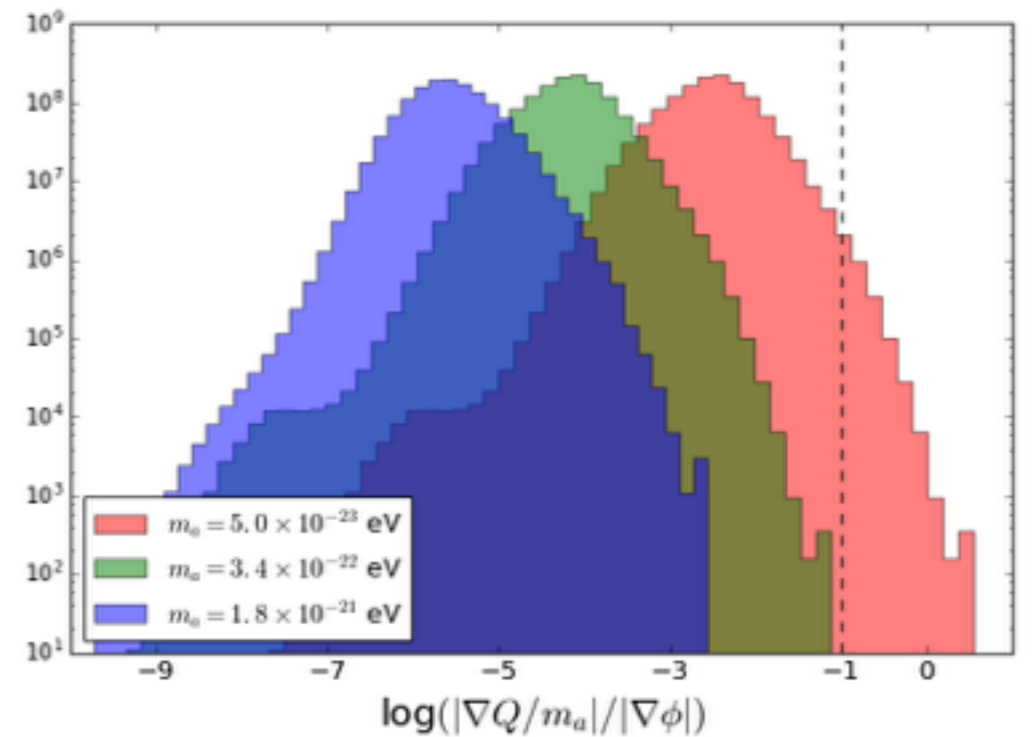
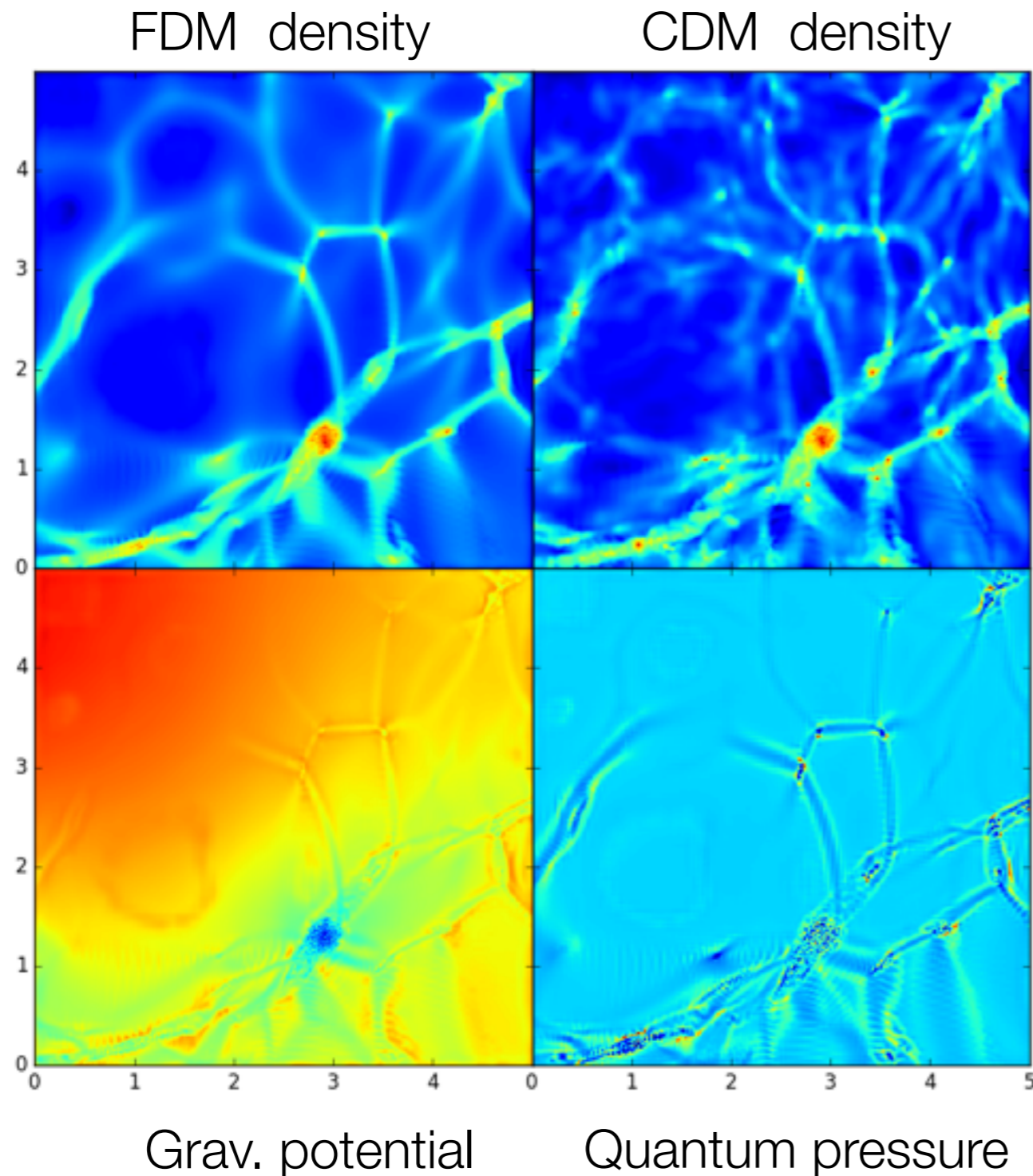
« **Quantum pressure** » **Q**

N-body (GADGET) codes solve the Euler-Poisson system

$\nabla Q$  hard to compute (small scale variations)

**Use standard N-body  $\Leftrightarrow$  neglect  $\nabla Q$  wrt gravitation force  $\nabla \phi$**

# FDM : « Quantum force » vs gravitational force



⇒ **N-body ok at the scales considered here at least for  $m_a \gtrsim 10^{-22}$  eV**



# Summary

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- **Fuzzy Dark Matter = axion-like particle with  $m_a \sim 10^{-22}$  eV :**  
**a possible solution to the « small scale CDM crisis »**  
**with interesting phenomenology**
- **Lyman- $\alpha$  forest currently provides the strongest constraints :**  
 **$m_a \gtrsim 2-3 \times 10^{-21}$  eV**
- If taken seriously, it closes this interesting FDM window.
- Need to :
  - Improve modeling of the IGM physics
  - Take into account the « quantum pressure » in the NL regime for low masses



# Homogenous evolution of the FDM fluid

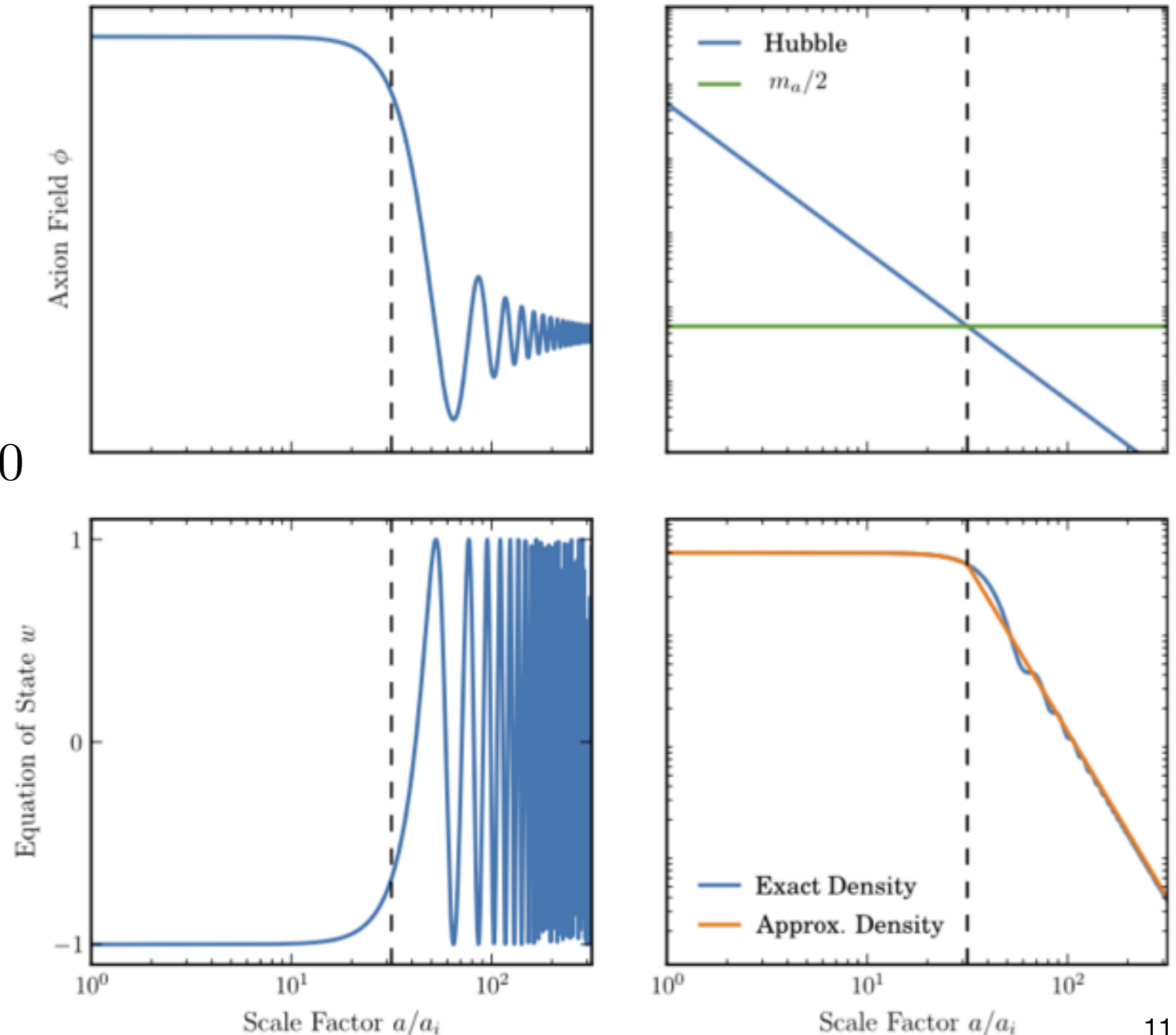
D.J.E. Marsh / Physics Reports 643 (2016) 1-79

- **Classical field**  
(occupation nb  $\gg 1$ )
- Klein Gordon equation  
(no interactions)

$$\ddot{\Psi}_0 + 3H(z) \dot{\Psi}_0 + m_a^2 \Psi_0 = 0$$

$H > m_a$  : DE regime

$H < m_a$  : DM regime



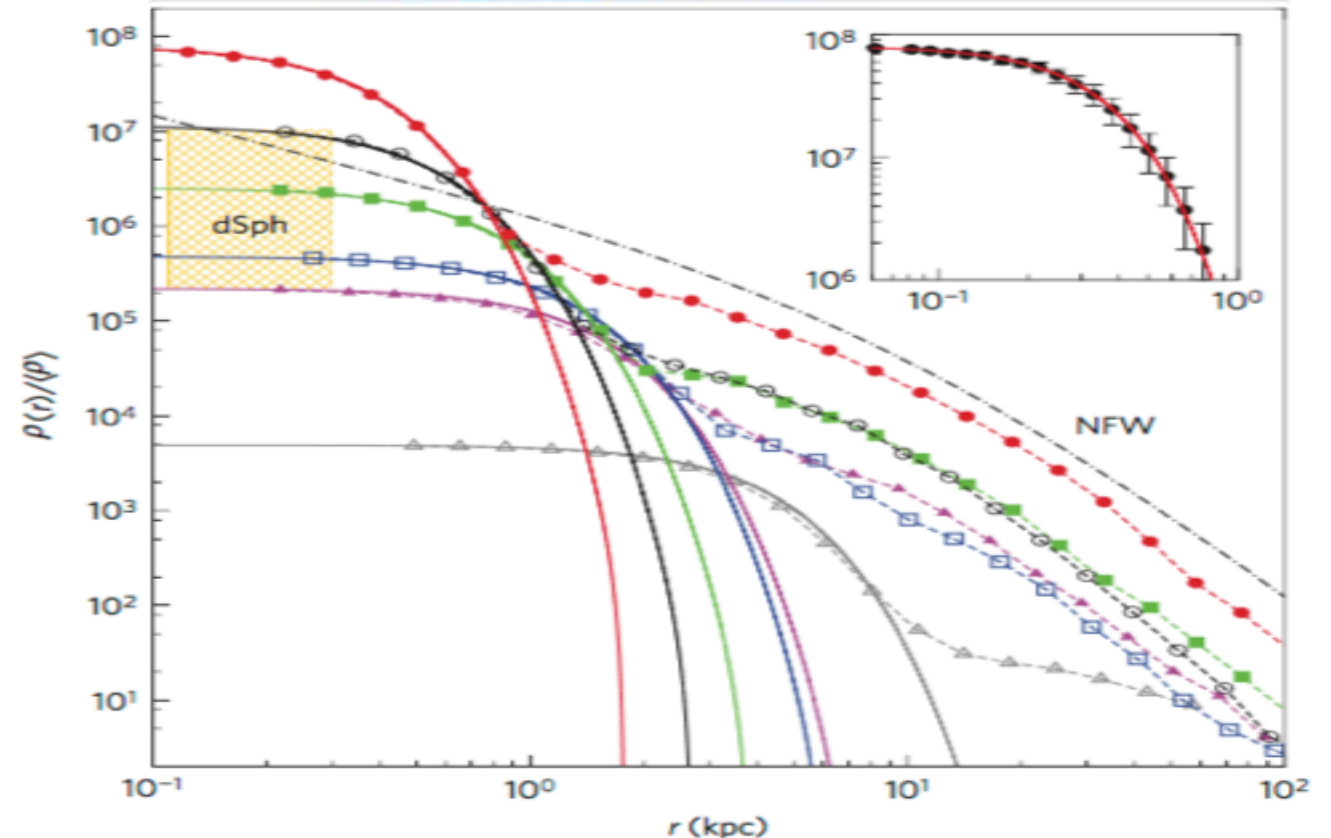
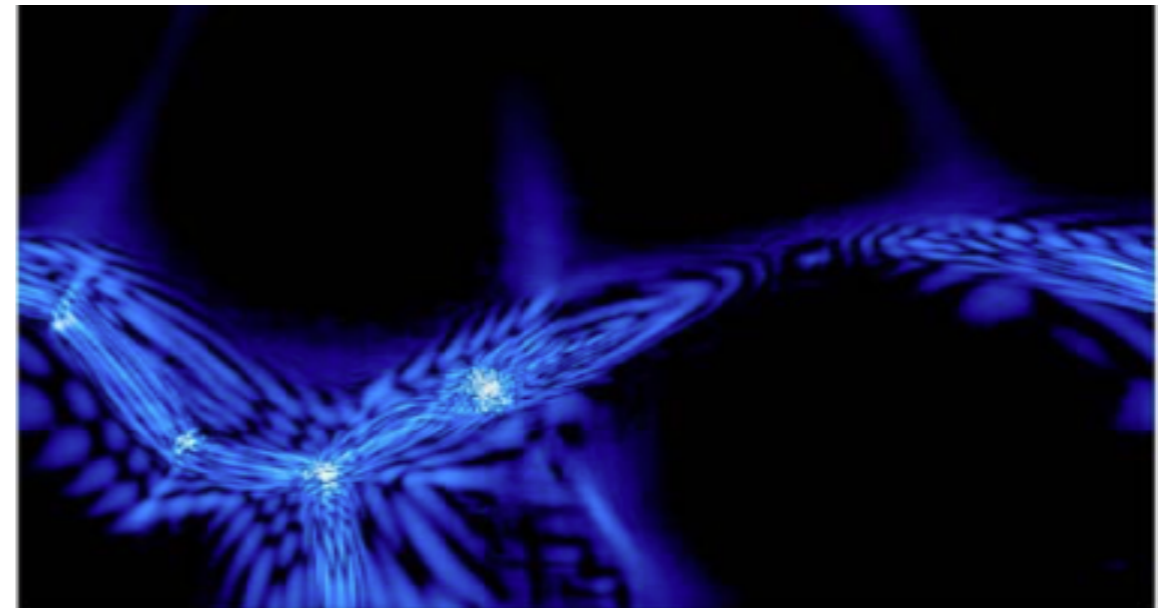
# Small-scale FDM halo properties

- Non-linear, non-relativistic : Schrödinger-Poisson system

$$\left[ i \frac{\partial}{\partial \tau} + \frac{\nabla^2}{2} - aV \right] \psi = 0$$

$$\nabla^2 V = |\psi|^2 - 1,$$

- Pure FDM cosmological simulations in ~few Mpc boxes (eg. Schive et al. Nature Phys. 2014)
- Key prediction: **solitonic core**
- Fit dwarf kinematics with  $m_a \sim 10^{-22}$  eV
- No « Catch 22 » wrt the Warm Datter Matter scenario



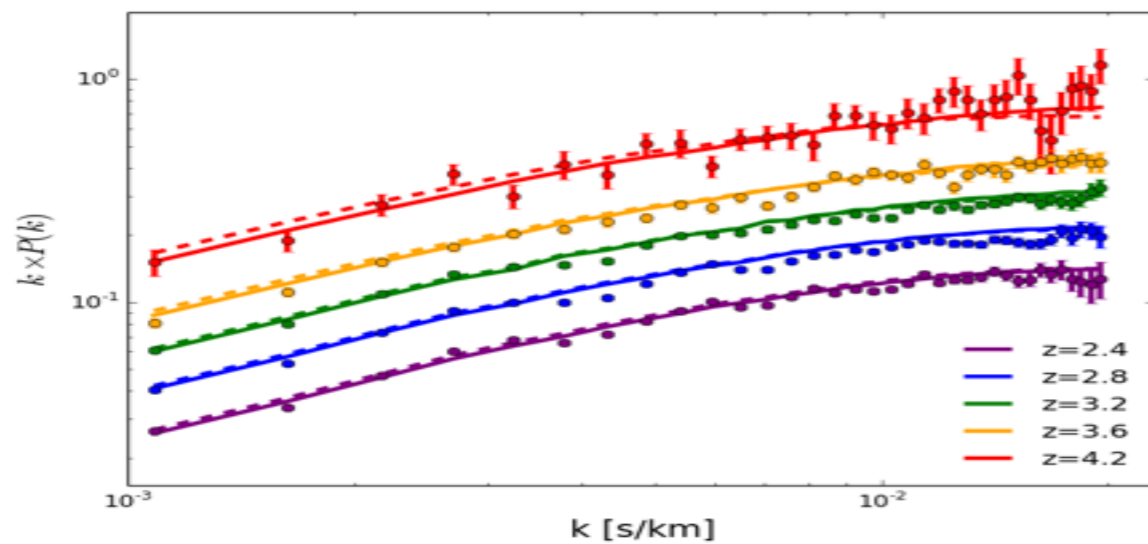
# $P_{1D}(k)$ predictions in SDSS window

Similar feature as for WDM

**WDM-FDM scaling law** best adapted to the measured SDSS flux power spectra :

require  $\chi^2(m_a) = \chi^2(m_X)$

$$m_X = 0.715 \times \left( \frac{m_a}{10^{-22} \text{ eV}} \right)^{0.558} \text{ keV}$$



Flux spectra with  $\tau_{\text{eff}} = 0.0025 (1+z)^{3.7}$

