

# Physique au LHC: théorie

## *Ecole doctorale Orsay*

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- SUSY au LHC

1. BSM, SUSY et le MSSM
2. Le spectre de Higgs dans le MSSM
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# 1. SUSY and the MSSM

The SM has many attractive theoretical/experimental features:

- Based on gauge principle, unitary, perturbative, renormalisable . . .
- Once  $M_H$  fixed: everything is predictable with great accuracy.
- And has passed all experimental tests up to now.

But the model has too many shortcomings:

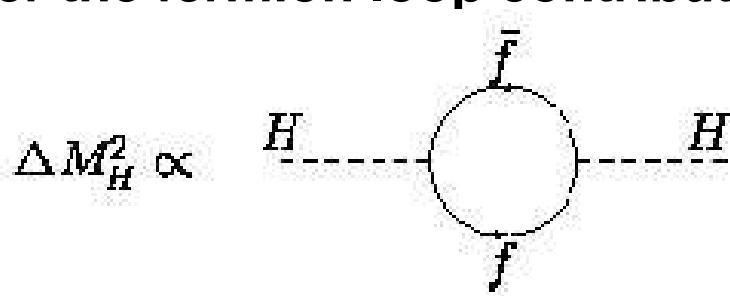
- Too many free parameters (19!) in the model, put by hand...
- No satisfactory explanation for  $\mu^2 < 0$  (put ad hoc).
- Does not include the fourth fundamental force, gravity, ..
- Does not say anything about the masses of the neutrinos.
- No real unification of the three gauge interactions.
- Does not explain the baryon asymmetry in the universe.
- There is no stable, weak, massive particle for dark matter.

And above all that, there is the hierarchy or naturalness problem.

# 1. BSM & SUSY: the hierarchy problem

## Radiative corrections to the Higgs boson mass in the SM

Let us first consider the fermion loop contribution to  $M_H^2$



Using a cut-off  $\Lambda$  (see excercises later) one obtains:

$$\Delta M_H^2 = N_f \frac{\lambda_f^2}{8\pi^2} \left[ -\Lambda^2 + 6m_f^2 \log \frac{\Lambda}{m_f} - 2m_f^2 \right] + \mathcal{O}(1/\Lambda^2)$$

We have thus a quadratic divergence,  $\Delta M_H^2 \sim \Lambda^2$ .

Divergence is independent of  $M_H$ , and does not disappear if  $M_H = 0$ :

The choice  $M_H = 0$  does not increase the symmetry of  $\mathcal{L}_{\text{SM}}$ .

If we fix the cut-off  $\Lambda$  to  $M_{\text{GUT}}$  or  $M_P$ :  $\Rightarrow M_H \sim 10^{14}$  to  $10^{17}$  GeV!

The Higgs boson mass prefers to be close to the very high scale:

This is the hierarchy problem.

# 1. BSM & SUSY: the hierarchy problem

But we want a light Higgs ( $M_H \lesssim 1$  TeV) for unitarity etc... reasons.

We need thus to make:  $M_H^2|^{\text{Physical}} = M_H^2|^0 + \Delta M_H^2 + \text{counterterm}$

And adjust this counterterm with a precision of  $10^{-30}$  (30 digits)

This fine-tunning would be very unnatural...

In SM, besides fermion loops, there are also contributions to  $M_H$  from the massive gauge bosons and from the Higgs boson itself:

$$\Rightarrow \Delta M_H^2 \propto [3(M_W^2 + M_Z^2 + M_H^2)/4 - \sum m_f^2](\Lambda^2/M_W^2)$$

We can adjust the unknown  $M_H$  so that the quadratic divergence disappears (would be a prediction for Higgs mass,  $M_H \sim 200$  GeV). However: does not work at two-loop level or at higher orders....

Summary: the problem of the quadratic divergences to  $M_H$  is there.

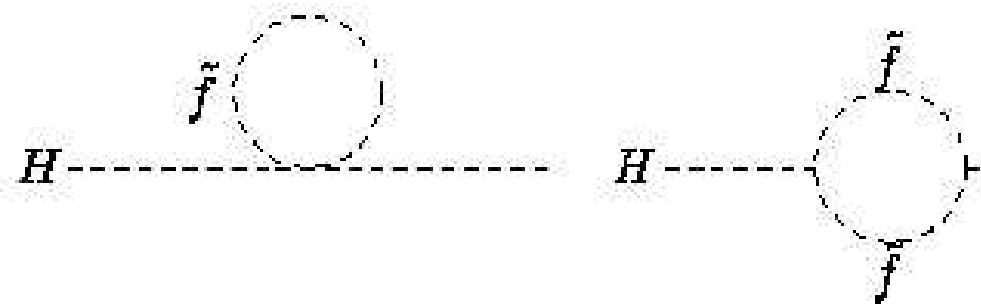
Photon and fermion masses protected by gauge and chiral symmetry,

.... but here is no symmetry which protects  $M_H$  in the SM.

# 1. BSM & SUSY: the hierarchy problem

Imagine now that you have additional scalar particles:

Add the contributions of scalar fermion partner loops to  $\Delta M_H^2$



- $\lambda_f^2 = -\lambda_S$ .
- $N_S = N_f$  (nb: 2 scalars).
- $m_1 = m_2 = m_S$ .
- Add f+S contributions.

$$\Delta M_H^2|^{\text{tot}} = \frac{\lambda_f^2 N_f}{4\pi^2} \left[ (m_f^2 - m_S^2) \log\left(\frac{\Lambda}{m_S}\right) + 3m_f^2 \log\left(\frac{m_S}{m_f}\right) \right]$$

The quadratic divergences have disappeared in the sum!! (same job for W/Z/H). Logarithmic divergence still there, but contribution small.

No divergences at all if in addition  $m_S = m_f$  (exact SUSY)!

⇒ Symmetry fermions–scalars → no divergence in  $\Lambda^2$

“Supersymmetry” no divergences at all:  $M_H$  is protected!

Note that if  $M_S \gg 1 \text{ TeV}$  the fine tuning problem is back!!!

# 1. BSM & SUSY: SUSY

SUSY: symmetry relating fermions  $s=\frac{1}{2}$  and bosons  $s=0,1$

$$Q|\text{fermion}\rangle = |\text{boson}\rangle, \quad Q|\text{boson}\rangle = |\text{fermion}\rangle$$

is the most attractive extension of SM also for other reasons

- Links internal and space–time symmetries: larger for S matrix..
  - If SUSY is gauged  $\Rightarrow s = \frac{3}{2}, 2 \Rightarrow$  link with 4th force, gravity...
  - Naturally present in Superstrings (theory of everything?).
  - The spectrum of superparticles fixes unification of couplings and  $P$ .
  - Possibility of unifying the fermion Yukawa couplings at  $M_{\text{GUT}}$ .
  - The LSP can have the right relic density and solve the DM problem.
  - Radiative breaking of the EW symmetry:  $\mu^2 > 0$  at  $M_{\text{GUT}}, < 0$  at  $M_{\text{EW}}$
- · · and all this at once · · · But we need  $M_{\text{SUSY}} \sim \mathcal{O}(\text{TeV})!$

otherwise, back to the hierarchy, dark matter and unification problems · · ·

# 1. BSM & SUSY: SUSY

**Drawback: no satisfactory way to break SUSY spontaneously**

**Solution: SUSY-breaking occurs in a hidden sector of particles with no (or very tiny) couplings to the visible sector of the MSSM.**

**If mediating interaction is flavor-blind, universal breaking terms.**

**Examples: gravity (mSUGRA), gauge (GMSB) mediation ...**

**Many breaking schemes but none is fully satisfactory at the moment:**

⇒ **Explicit breaking by hand** (also with several possibilities...).

- We need SUSY breaking at low energy to solve the problems:
  - Quadratic divergences in the Higgs sector.
  - Unification of the coupling constants of  $SU(3)_C \times SU(2)_L \times U(1)_Y$ .
  - Dark Matter problem (existence of a massive stable particle), etc.
- In the breaking, we still need to preserve: gauge invariance, renormalizability, and no quadratic divergence (soft SUSY-breaking).

⇒ **“Low energy SUSY” ≡ effective theory at low energy.**

# 1. BSM & SUSY: the MSSM

The MSSM is the most economic low energy SUSY extension of SM

It is based on the following assumptions:

- **Minimal gauge group:**  $G_{\text{SM}} = \text{SU}(3)_C \times \text{SU}(2)_L \times \text{U}(1)$ .

The SM spin-1 gauge bosons [B,  $W_{1-3}$  and  $g_{1-8}$ ] and their spin- $\frac{1}{2}$  gaugino partners [ $\tilde{b}$ ,  $\tilde{w}_{1-3}$ ,  $\tilde{g}_{1-8}$ ] are in vector superfields.

Superfields	$\text{SU}(3)_C$	$\text{SU}(2)_L$	$\text{U}(1)_Y$	Particle content
$\hat{G}^a$	8	1	0	$G^\mu, \tilde{g}$
$\hat{W}^i$	1	3	0	$W_i^\mu, \tilde{\omega}_i$
$\hat{B}$	1	1	0	$B^\mu, \tilde{b}$

Charged winos mix with higgsinos to form the two charginos  $\chi_{1,2}^\pm$   
Bino and neutral wino mix with higgsinos to form 4 neutralinos  $\chi_{1,2,3,4}^0$

Gluinos do not mix with anybody....

# 1. BSM & SUSY: the MSSM

- **Minimal particle content:**
  - Three fermion generations [as in SM no  $\nu_R \dots$ ] and their spin=0 SUSY partners, the sfermions  $\tilde{f}_L, \tilde{f}_R$ , combined in chiral supermultiplets.
  - No chiral anomalies ( $\sum_f Q_f \equiv 0$ ) and fermion mass generation in a SUSY invariant way (no conjugate  $H^*$  field for u-quarks), we need:  
**two chiral superfields with  $Y = +1$  and  $Y = -1$**

Superfield	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	Particle content
$\hat{Q}$	3	2	$\frac{1}{3}$	$(u_L, d_L), (\tilde{u}_L, \tilde{d}_L)$
$\hat{U}^c$	$\bar{3}$	1	$-\frac{4}{3}$	$\bar{u}_R, \tilde{u}_R^*$
$\hat{D}^c$	$\bar{3}$	1	$\frac{2}{3}$	$\bar{d}_R, \tilde{d}_R^*$
$\hat{L}$	1	2	-1	$(\nu_L, e_L), (\tilde{\nu}_L, \tilde{e}_L)$
$\hat{E}^c$	1	1	2	$\bar{e}_R, \tilde{e}_R^*$
$\hat{H}_1$	1	2	-1	$(H_1, \tilde{h}_1)$
$\hat{H}_2$	1	2	1	$(H_2, \tilde{h}_2)$

# 1. BSM & SUSY: the MSSM

- R-parity conservation:

To eliminate terms violating B and L numbers (and proton decay):

Discrete and multiplicative symmetry called R-parity or  $R_p$ :

$$R_p = (-1)^{2s+3B+L}$$

Then  $R = +1$  for all ordinary SM particles

$R = -1$  for all the SUSY particles

The consequences of  $R_p$  conservation are very important:

- SUSY particles always produced in pairs.
- SUSY particles decay into an odd number of SUSY particles.
- The lightest SUSY particle (LSP) is absolutely stable.

# 1. BSM & SUSY: the MSSM

At this stage, we have a globally supersymmetric Lagrangian.

- Everything is specified by SUSY and gauge invariance.
- No additional parameter compared to SM.
- Only freedom, the choice of the Superpotential.

The most general Superpotential compatible with SUSY, gauge invariance, renormalizability and R-parity conservation is:

$$W = \sum_{i,j=\text{gen}} Y_{ij}^u \hat{u}_R^i \hat{H}_2 \cdot \hat{Q}^j + Y_{ij}^d \hat{d}_R^i \hat{H}_1 \cdot \hat{Q}^j + Y_{ij}^l \hat{l}_R^i \hat{H}_1 \cdot \hat{L}^j + \mu \hat{H}_1 \cdot \hat{H}_2$$

- $Y_{ij}^{u,d,l}$  denote the Yukawa couplings among the three generations (and which simply a generalisation of the SM Yukawa interaction).
- $\mu$  supersymmetric Higgs–higgsino parameter with dimension of mass (it is thus a supersymmetric parameter, see later....).

# 1. BSM & SUSY: the unconstrained MSSM

- **Soft SUSY breaking:**

To explicitly break Supersymmetry without reintroducing the quadratic divergences (the so-called soft SUSY-breaking), we add by hand a collection of soft terms (of dimension two and three):

$$\begin{aligned}\mathcal{L}_{\text{gaugino}} &= \frac{1}{2} \left[ M_1 \tilde{b} \tilde{b} + M_2 \sum_{a=1}^3 \tilde{w}^a \tilde{w}_a + M_3 \sum_{a=1}^8 \tilde{g}^a \tilde{g}_a + \text{h.c.} \right] \\ \mathcal{L}_{\text{sf.}} &= \sum_i m_{\tilde{Q},i}^2 \tilde{Q}_i^\dagger \tilde{Q}_i + m_{\tilde{L},i}^2 \tilde{L}_i^\dagger \tilde{L}_i + m_{\tilde{u},i}^2 |\tilde{u}_{R,i}|^2 + m_{\tilde{d},i}^2 |\tilde{d}_{R,i}|^2 + m_{\tilde{l},i}^2 |\tilde{l}_{R,i}|^2 \\ \mathcal{L}_{\text{Higgs}} &= m_2^2 H_2^\dagger H_2 + m_1^2 H_1^\dagger H_1 + B\mu(H_2 \cdot H_1 + \text{h.c.}) \\ \mathcal{L}_{\text{tr.}} &= \sum_{i,j} \left[ A_{ij}^u Y_{ij}^u \tilde{u}_{R,i} H_2 \cdot \tilde{Q}_j + A_{ij}^d Y_{ij}^d \tilde{d}_{R,i} H_1 \cdot \tilde{Q}_j + A_{ij}^l Y_{ij}^l \tilde{l}_{R,i} H_1 \cdot \tilde{L}_j + \right]\end{aligned}$$

A rather complicated and problematic potential indeed!

- Too many parameters and thus not very predictive.
- Leads generically to a problematic phenomenology.

# 1. BSM & SUSY: the unconstrained MSSM

In the most general case (mixing and phases): 105 free parameters!

- complex gaugino masses  $M_1, M_2, M_3$  : 6
- $3 \times 3$  hermitian mass matrices  $m_{\tilde{F}}$  : 45
- $3 \times 3$  complex trilinear coupling matrices  $A_f$  : 54
- $2 \times 2$  matrix for the bilinear B coupling : 4
- Higgs masses squared,  $m_{H_1}^2, m_{H_2}^2$  : 2

111–6 (due to constraints from symmetries and Higgs sector)=105.

For “generic” sets of these parameters, leads to severe problems:

- large flavor changing neutral currents [FCNC]
- unacceptable amount of additional CP–violation
- color and/or charge breaking minima
- an incorrect value of the Z boson mass, etc.....

We need more constrained MSSMs

# 1. BSM & SUSY: the phenomenological MSSM

A phenomenologically viable MSSM is defined by assuming:

- all soft SUSY-breaking parameters are real (no new CP viol).
- Mass and trilinear cpls. for sfermions diagonal (no FCNC)
- 1st/2d sfermion generation universality (no pb. with Kaons)

Phenomenological MSSM (pMSSM) with 22 free parameters:

$\tan \beta$ : the ratio of the vevs of the two-Higgs doublet fields.

$m_{H_u}^2, m_{H_d}^2$ : the Higgs mass parameters squared.

$M_1, M_2, M_3$ : the bino, wino and gluino mass parameters.

$m_{\tilde{q}}, m_{\tilde{u}_R}, m_{\tilde{d}_R}, m_{\tilde{l}}, m_{\tilde{e}_R}$ : 1st/2d generation sfermion mass para.

$m_{\tilde{Q}}, m_{\tilde{t}_R}, m_{\tilde{b}_R}, m_{\tilde{L}}, m_{\tilde{\tau}_R}$ : third generation sfermion mass para.

$A_t, A_b, A_\tau$ : the third generation trilinear couplings.

$A_u, A_d, A_e$ : the first/second generation trilinear couplings.

# 1. BSM & SUSY: the constrained MSSM

In fact:

- You can trade  $m_{H_u}^2, m_{H_d}^2$  with more "physical"  $\mu$  and  $M_A$  (in fact:  $\mu^2$  and  $B\mu$  can be determined from ESWB, see later).
- $A_u, A_d, A_e$  in general not relevant for phenomenology.  
(enter only in "light" flavor physics:  $(g - 2)_\mu$ , neutron edm, ....).
- If you focus on a given sector (Higgs, gauginos, sfermions):  
only few parameters to deal with and model indep. analyses....  
⇒ **phenomenologically more viable model than general MSSM**
- You can also use common soft-SUSY breaking terms in many cases  
( $m_{\tilde{q}} = m_{\tilde{u}_R} = m_{\tilde{d}_R}; m_{\tilde{Q}}, m_{\tilde{t}_R}, m_{\tilde{b}_R}; A_t, A_b, A_\tau$ ; etc..)  
and one ends with an even more restrictive set of parameters,  $\lesssim 10$ .  
⇒ **much more predictive model than general MSSM**

# 1. BSM & SUSY: the constrained MSSM

Almost all problems of MSSM solved at once if soft SUSY-breaking parameters obey a set of universal boundary conditions at  $M_{\text{GUT}}$ .

Underlying assumption: SUSY-breaking occurs in a hidden sector communicating with visible sector through gravitational interactions.

⇒ Universal soft terms emerge if interactions are “flavor-blind”:

Besides  $g_{1,2,3}$  unification which fix the scale  $M_{\text{GUT}} \sim 2 \cdot 10^{16} \text{ GeV}$ :

Unification of gaugino, scalar masses and trili. couplings at  $Q = M_{\text{GUT}}$

Universal gaugino masses:  $M_1 = M_2 = M_3 \equiv m_{1/2}$

Universal scalar masses:  $M_{\tilde{Q}_i} = M_{\tilde{L}_i} = M_{H_i} \equiv m_0$

Universal trilinear couplings:  $A_{ij}^u = A_{ij}^d = A_{ij}^l \equiv A_0 \delta_{ij}$

Also:  $B$  and  $\mu^2$  from requiring of EWSB and minimization of  $V_{\text{Higgs}}$

$$\mu^2 = \frac{1}{2} [\tan 2\beta (m_{H_u}^2 \tan \beta - m_{H_d}^2 \cot \beta) - M_Z^2]$$

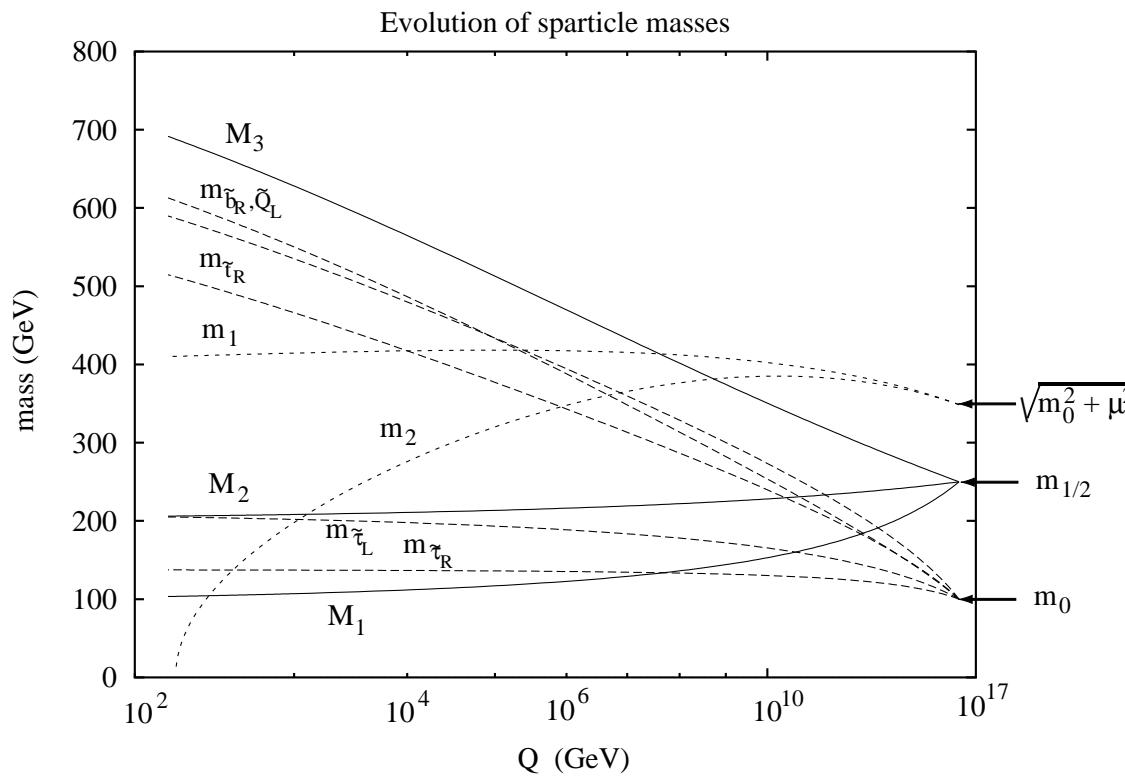
$$B\mu = \frac{1}{2} \sin 2\beta [m_{H_u}^2 + m_{H_d}^2 + 2\mu^2]$$

# 1. BSM & SUSY: the constrained MSSM

Only 4.5 param:  $\tan \beta$ ,  $m_{1/2}$ ,  $m_0$ ,  $A_0$ ,  $\text{sign}(\mu)$

All soft breaking parameters at  $M_S$  are obtained through RGEs.

With  $M_{\text{GUT}} \sim 2 \cdot 10^{16} \text{ GeV}$  and  $M_{\text{SUSY}} \sim \sqrt{m_{\tilde{t}_L} m_{\tilde{t}_R}}$ :



Radiative EWSB occurs since  $M_{H_2}^2 < 0$  at scale  $M_Z$  ( $t/\tilde{t}$  loops)

⇒ EWSB more natural in MSSM ( $\mu^2 < 0$  from RGEs) than in SM!

# 1. BSM & SUSY: the constrained MSSM

In GMSB, SSB transmitted to MSSM fields via SM gauge interactions.

- Hidden sector for SUSY-break. contains messengers fields,  $n_{\hat{q}}/n_{\hat{l}}$  quark-lepton-like pairs coupled to a gauge singlet chiral superfield  $\hat{S}$ .
- The spotential is  $W = \lambda \hat{S} \hat{q} \hat{\bar{q}} + \lambda \hat{S} \hat{l} \hat{\bar{l}}$  with  $\hat{S}$  havings vevs.  $s$  and  $f_S$
- SSB are generated by (1 or 2) loop corrections at scale  $M_{\text{mes}} = \lambda s$

$$M_G(M_{\text{mes}}) = \frac{\alpha_G(M_{\text{mes}})}{4\pi} \Lambda g\left(\frac{\Lambda}{M_{\text{mes}}}\right) \sum_m N_R^G(m)$$

$$m_s^2(M_{\text{mes}}) = 2\Lambda^2 f\left(\frac{\Lambda}{M_{\text{mes}}}\right) \sum_{m,G} \left(\frac{\alpha_G(M_{\text{mes}})}{4\pi}\right)^2 N_R^G(m) C_R^G(s)$$

$A_f(M_{\text{mes}}) \simeq 0$  (generated at two-loops).

with  $\Lambda = f_s/s$ ,  $G = U(1), SU(2), SU(3)$ ,  $m$  and  $s$  label messengers and scalars;  $f/g$  are one/two loop functions;  $N/C$  are Dynkin/Casimirs..

Thus, in the GMSB model there are six basic input parameters

$$\tan\beta, \text{ sign}(\mu), M_{\text{mes}}, \Lambda, n_{\hat{q}}, n_{\hat{l}}$$

plus the mass of the very light gravitino (which is the LSP).

# 1. BSM & SUSY: the constrained MSSM

In AMSB, SUSY breaking occurs also in hidden sector (e.g. extra dims) and is transmitted to visible sector via (e.g. super-Weyl) anomalies.

Gaugino, scalar masses and trilinear couplings are simply related to the scale dependence of the gauge and matter kinetic functions.

In terms of gravitino mass  $m_{3/2}$ ,  $\beta$  functions for  $g_a$  and  $Y_i$  couplings and anomalous dimensions  $\gamma_i$  of chiral superfields, SSB terms are:

$$M_a = \frac{\beta_{g_a}}{g_a} m_{3/2}, \quad A_i = \frac{\beta_{Y_i}}{Y_i} m_{3/2}$$

$$m_i^2 = -\frac{1}{4} \left( \sum_a \frac{\partial \gamma_i}{\partial g_a} \beta_{g_a} + \sum_k \frac{\partial \gamma_i}{\partial Y_k} \beta_{Y_k} \right) m_{3/2}^2$$

RG invariant equations valid at any scale (make a predictive model).

( $\mu^2$  and  $B\mu$  terms are obtained as usual by requiring EWSB).

However, picture spoiled by tachyonic sleptons  $m_{\tilde{L}}^2 < 0$  in general!

⇒ add a non anomalous contribution to soft masses  $c_i m_0^2$  to  $m_i^2$

In minimal AMSB with a universal  $m_0$ ,  $c_i = 1$ , the inputs are:

$m_0$ ,  $m_{3/2}$ ,  $\tan \beta$ ,  $\text{sign}(\mu)$  and  $c_i$

## 2. The MSSM Higgs spectrum

In MSSM with two Higgs doublets  $H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix}$  and  $H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix}$ .

- To cancel the chiral anomalies introduced by the new  $\tilde{h}$  field.
- Give separately masses to d and u fermions in SUSY invariant way.

The terms contributing to scalar potential  $V_H$  come from 3 sources:

D terms (scalar inter.), F terms (Superpotential) and soft-SUSY breaking

$$V_H = \bar{m}_1^2 |H_1|^2 + \bar{m}_2^2 |H_2|^2 - \bar{m}_3^2 \epsilon_{ij} (H_1^i H_2^j + h.c.) + \frac{g_2^2 + g_1^2}{8} (|H_1|^2 - |H_2|^2)^2 + \frac{1}{2} g_2^2 |H_1^* H_2|^2$$

with  $\bar{m}_1^2 = |\mu|^2 + m_1^2$ ,  $\bar{m}_2^2 = |\mu|^2 + m_2^2$ ,  $\bar{m}_3^2 = B\mu$

- Develop in terms of components  $H_1 = (H_1^0, H_1^-)$ ,  $H_2 = (H_2^+, H_2^0)$
- Now require  $V_H^{\min}$  breaks  $G_{SM} \rightarrow U(1)_{QED}$  (neutral component).

$$\langle 0 | \text{Re}(H_1^0) | 0 \rangle = v_1, \quad \langle 0 | \text{Re}(H_2^0) | 0 \rangle = v_2, \quad \tan \beta = v_2/v_1, \quad v_1^2 + v_2^2 = v^2$$

The relevant part of the scalar potential is then simply given by:

$$V_H = \bar{m}_1^2 |H_1^0|^2 + \bar{m}_2^2 |H_2^0|^2 + \bar{m}_3^2 (H_1^0 H_2^0 + h.c.) + \frac{M_Z^2}{4v^2} (|H_1^0|^2 - |H_2^0|^2)^2$$

## 2. The Higgs spectrum: scalar potential

Some remarks on this scalar potential:

$$V_H = \overline{m}_1^2 |H_1^0|^2 + \overline{m}_2^2 |H_2^0|^2 + \overline{m}_3^2 (H_1^0 H_2^0 + h.c.) + \frac{M_Z^2}{4v^2} (|H_1^0|^2 - |H_2^0|^2)^2$$

- Quartic couplings fixed in terms of the gauge couplings, only 3 free parameters:  $\overline{m}_1^2, \overline{m}_2^2, \overline{m}_3^2$  (6 para and a phase in a general 2HDM).
- $m_{1,2}^2 + |\mu|^2$  real, only  $B\mu$  can be complex. But any phase in  $B\mu$  can be absorbed in phases of  $H_1, H_2 \Rightarrow V_H$  (MSSM) conserves CP.
- If  $B\mu$  is zero, all other terms are positive and thus  $V_H = 0$  only if  $\langle H_1^0 \rangle = \langle H_2^0 \rangle = 0$ . To have SSB (without CCB), we need  $\overline{m}_{1,2,3} \neq 0$   
⇒ Connection of gauge symmetry breaking and SUSY breaking!!

More precisely: in SM, SSB takes place with ad hoc choice  $\mu^2 < 0$ .

In MSSM,  $m_{H_i}^2 > 0$  at  $M_{GUT}$  but  $t/\tilde{t}$  in RGE make  $m_{H_i}^2 < 0$  at  $M_Z$ : radiative breaking of the electroweak symmetry (i.e. through RC).

⇒ Symmetry breaking more natural and elegant than in SM.

## 2. The Higgs spectrum: Higgs masses

To obtain the physical Higgs fields and their masses from potential  $V_H$ , develop  $H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix}$  and  $H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix}$  into real (CP-even+charged H) and imaginary (CP-odd H+Goldstones) and diagonalize  $2 \times 2$  mass matrices

$$\mathcal{M}_{ij}^2 = \frac{1}{2} \partial^2 V_H / \partial H_i \partial H_j \Big|_{\langle \text{Re}(H_{1,2}^0) \rangle = v_{1,2}, \langle \text{Im}(H_{1,2}^0) \rangle = 0, \langle H_{1,2}^\pm \rangle = 0}$$

The obtained physical masses and mixing angle are (see excercise):

$$M_A^2 = -\bar{m}_3^2 (\tan \beta + \cot \beta) = -2\bar{m}_3^2 / \sin 2\beta$$

$$M_{h,H}^2 = \frac{1}{2} \left[ M_A^2 + M_Z^2 \mp \sqrt{(M_A^2 + M_Z^2)^2 - 4M_A^2 M_Z^2 \cos^2 2\beta} \right]$$

$$M_{H^\pm}^2 = M_A^2 + M_W^2$$

The mixing angle  $\alpha$  which rotates the CP-even fields ( $-\frac{\pi}{2} \leq \alpha \leq 0$ )

$$\tan 2\alpha = \frac{2\mathcal{M}_{12}}{\mathcal{M}_{11} - \mathcal{M}_{22}} = \frac{-(M_A^2 + M_Z^2) \sin 2\beta}{(M_Z^2 - M_A^2) \cos 2\beta} = \tan 2\beta \frac{M_A^2 + M_Z^2}{M_A^2 - M_Z^2}$$

While the mixing angle for the CP-odd and charged fileds is simply  $\beta$ .

## 2. The Higgs spectrum: Higgs masses

We have an important constraint on the lightest MSSM h boson mass:

$$M_h \leq \min(M_A, M_Z) \cdot |\cos 2\beta| \leq M_Z$$

besides some other (also important) relations for H,A and  $H^\pm$ :

$$M_H > \max(M_A, M_Z) \text{ and } M_{H^\pm} > M_W$$

If we send  $M_A$  to infinity, we will have for Higgs masses and  $\alpha$ :

$$M_h \sim M_Z |\cos 2\beta|, \quad M_H \sim M_{H^\pm} \sim M_A, \quad \alpha \sim \frac{\pi}{2} - \beta$$

This is the decoupling regime: all Higgses are heavy except for h.

The h boson is lighter than  $M_Z$  and should have been seen at LEP2  
(we have  $\sqrt{s}_{\text{LEP2}} \sim 200 \text{ GeV} > M_h + M_Z \sim 180 \text{ GeV}$ ).

So what happened in this case? Maybe the MSSM is already ruled out?  
No! This relation holds only at first order (tree-level) and there are  
strong couplings involved, in particular the  $htt$  and  $h\tilde{t}\tilde{t}$  couplings.

⇒ Calculation of radiative corrections to  $M_h$  necessary.

## 2. The Higgs spectrum: Higgs masses

Radiative corrections very important in the MSSM Higgs sector!

A large activity for the RC calculation in the last 15 years.

- Dominant corrections are due to top (s)quark at one-loop level

$$\Delta M_h^2 = \frac{3g^2}{2\pi^2} \frac{m_t^4}{M_W^2} \log \frac{m_t^2}{m_{\tilde{t}}^2}$$

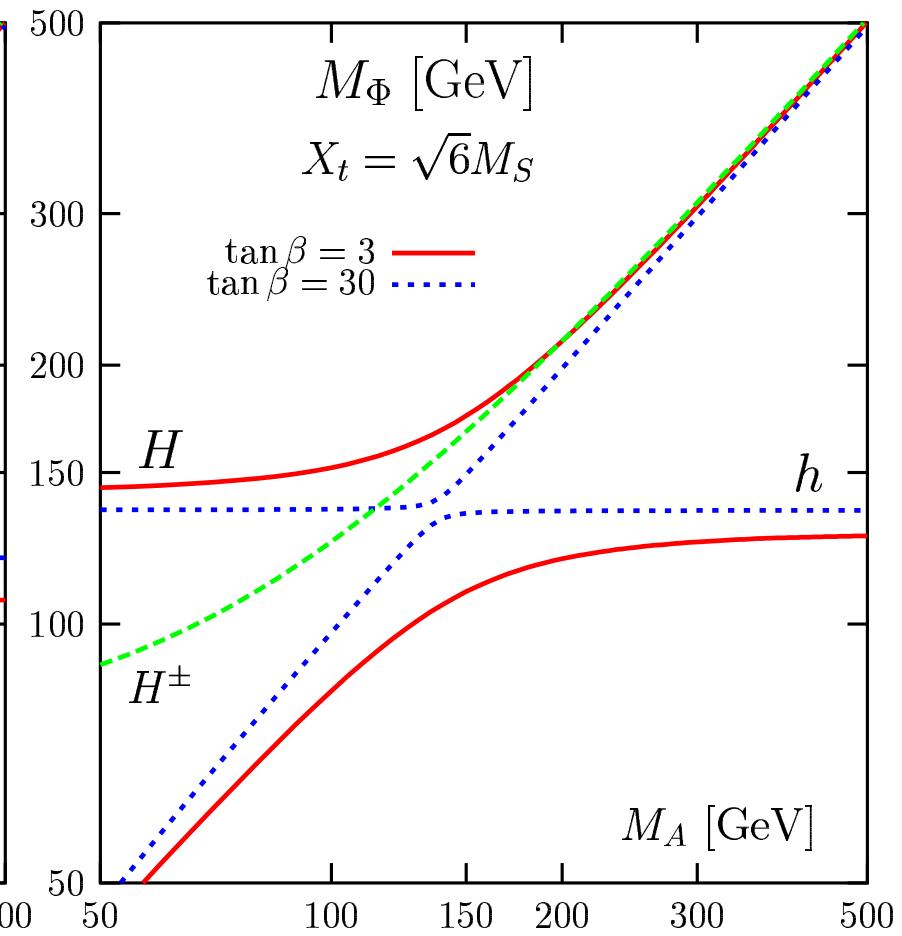
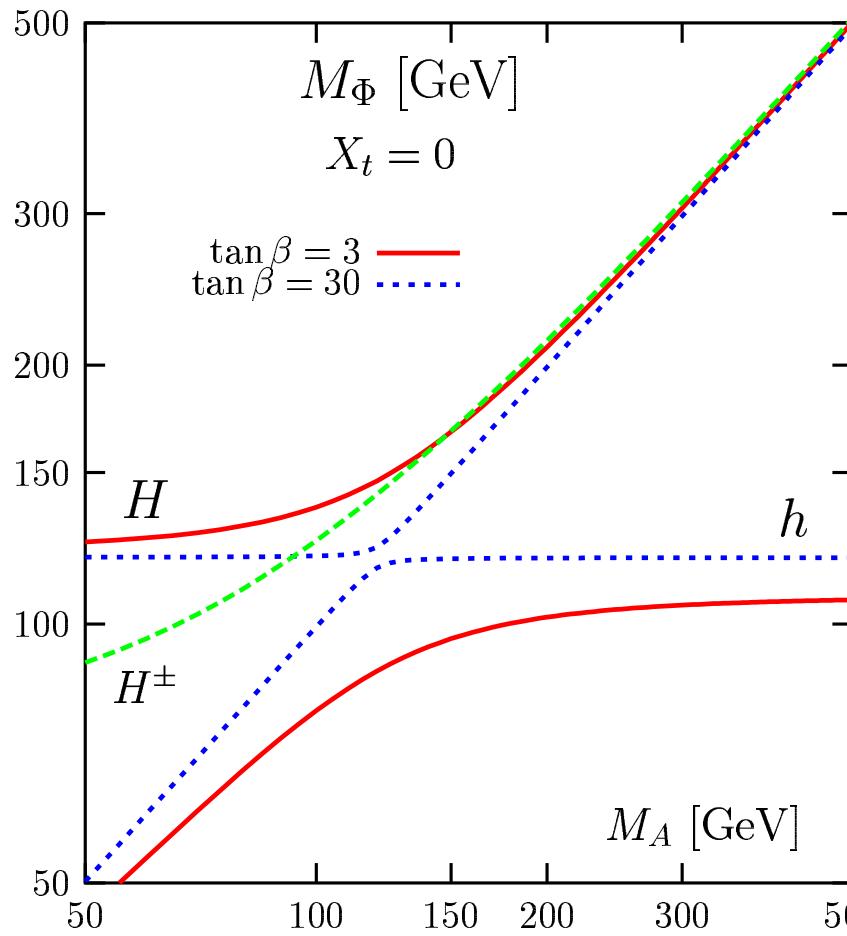
It depends on  $m_t^4$  and  $\log(m_{\tilde{t}}^2/m_t^2)$ , and is large:  $\frac{M_h^{\max} \rightarrow M_Z + 40}{\text{GeV}}$

This explains why the  $h$  boson has not been observed at LEP2.

- The full one-loop corrections have been calculated:
  - the parameters  $\mu$ ,  $A_t$  and  $A_b$  appear at the subleading level.
  - the  $h$  boson mass is maximal (minimal) for  $A_t \sim 2M_{\tilde{Q}}(0)$ .
- Approximate calculation for the dominant two-loop radiative corrections (in the effective potential approach; see SH again):
  - dominant QCD RC large but absorbed by  $m_t|^{\text{pole}} \rightarrow m_t|^{MS}$ .
  - Yukawa corrections rather small in the limit  $M_h = 0$ .

## 2. The Higgs spectrum: Higgs masses

- Using full 1-loop and the 2-loop RC in effective potential approach:
  - $\mathcal{O}(\alpha_t \alpha_S)$ : including squark mixing and gluino loops.
  - $\mathcal{O}(\alpha_t^2)$ : including mixing and  $\mathcal{O}(\alpha_b \alpha_S), \mathcal{O}(\alpha_\tau \alpha_S)$ .



# 3. SUSY spectrum and constraints

## Determination of spectrum:

- RGEs (two loops, numerics)
- EWSB and  $V_{\text{soft}}$  (iterations)
- Masses, couplings, RC

## Sophisticated RGE programs:

- example of SuSpect  
**(Kneur, Moultsaka, AD)**
- other programs also exist:  
**(Isajet, SoftSUSY, Spheno, ...)**

## Viable parameter space:

- choose inputs, param. scan
- impose known constraints  
**(Th, Experimental, DM, ...)**

Low energy input:  $\alpha(M_Z), \alpha_S(M_Z), M_t^{\text{pole}}, M_\tau^{\text{pole}}, m_b^{\overline{\text{MS}}}(m_b); \tan\beta(M_Z)$

Radiative corrections  $\Rightarrow g_{1,2,3}^{\overline{\text{DR}}}(M_Z), Y_\tau^{\overline{\text{DR}}}(M_Z), Y_b^{\overline{\text{DR}}}(M_Z), Y_t^{\overline{\text{DR}}}(M_Z)$

*First iteration: no SUSY radiative corrections.*

One- or two-loop RGE with choice:  $g_1 = g_2 \cdot \sqrt{3/5}$   
 $M_{\text{GUT}} \sim 2 \cdot 10^{16} \text{ GeV}$

Choice of SUSY-breaking model (mSUGRA, GMSB, AMSB, or pMSSM).

Fix your high-energy input (mSUGRA:  $m_0, m_{1/2}, A_0, \text{sign}(\mu)$ , etc...).

Run down all parameters with RGE to  $m_Z$  and  $M_{\text{EWSB}}$  scales

*First iteration: guess for  $M_{\text{EWSB}}$ .*

EWSB:  $\mu^2, \mu B = F_{\text{non-linear}}(m_{H_u}, m_{H_d}, \tan\beta, V_{\text{loop}})$

$V_{\text{loop}} \equiv$  Effective potential at 1-loop with all masses.

*First iteration:  $V_{\text{loop}}$  not included*

Check of consistent EWSB ( $\mu$  convergence, no tachyons, simple CCB/UFB, etc...)

Diagonalization of mass matrices and calculation of masses / couplings

Radiative corrections to the physical Higgs, sfermions, gaugino masses.

*First iteration: no radiative corrections.*

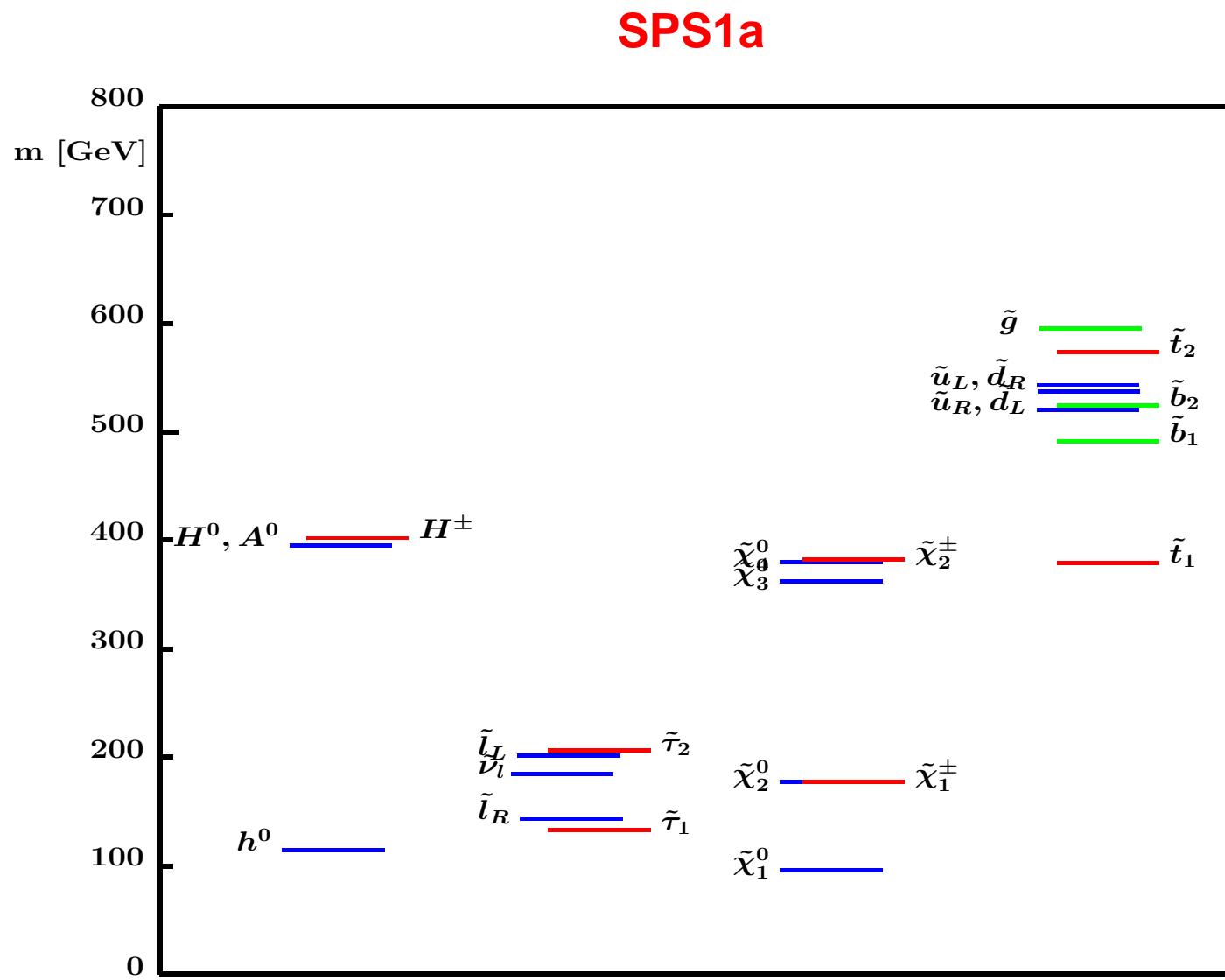
Check of a reasonable spectrum:

- no tachyonic masses (from RGE, EWSB or mix),
- information provided on fine-tuning, CCB/UFB conditions,
- calculation of MSSM contributions to:  $\Delta\rho, (g-2), b \rightarrow s\gamma$ .

### 3. SUSY spectrum: Theoretical constraints

- No RGE problems:
  - Perturbative couplings/No Landau poles
  - Non tachyonic sfermions (in particular for 3d generation)
  - Consistent unification of gauge couplings
- Proper implementation of EWSB:
  - Non tachyonic A boson or  $\mu$  parameter
  - Convergent/stable value of  $\mu$  after several iterations
  - Vacuum non CCB nor UFB
- Reasonnable SUSY spectrum:
  - Non tachyonic sfermions from mixing
  - Higgs masses not NaN
  - The LSP is the lightest neutralino  $\chi_1^0$

### 3. SUSY spectrum: example of spectrum



### 3. SUSY spectrum: direct experimental constraints

#### Bounds from $\tilde{P}$ searches:

- **Bounds from LEPI/LEPII:**

$$m_{\tilde{\chi}_1^\pm} \gtrsim 104 \text{ GeV}$$

$$m_{\tilde{f}} \gtrsim 100 \text{ GeV}$$

with  $\tilde{f} = \tilde{t}_1, \tilde{b}_1, \tilde{l}^\pm, \tilde{\nu}$

- **Bounds from the Tevatron:**

$$m_{\tilde{g}} \gtrsim 300 \text{ GeV}$$

$$m_{\tilde{q}_{1,2}} \gtrsim 260 \text{ GeV}$$

with  $\tilde{q} = \tilde{u}, \tilde{d}, \tilde{s}, \tilde{c}, \tilde{b}$

- **Possible refinements:**

- (almost) stable  $\tilde{\chi}_1^+$  at LEPII

- degenerate  $\tilde{t}_1, \tilde{\tau}_1$  with LSP

- $\tilde{t}_1$  with large  $\Delta m$  at Tevatron

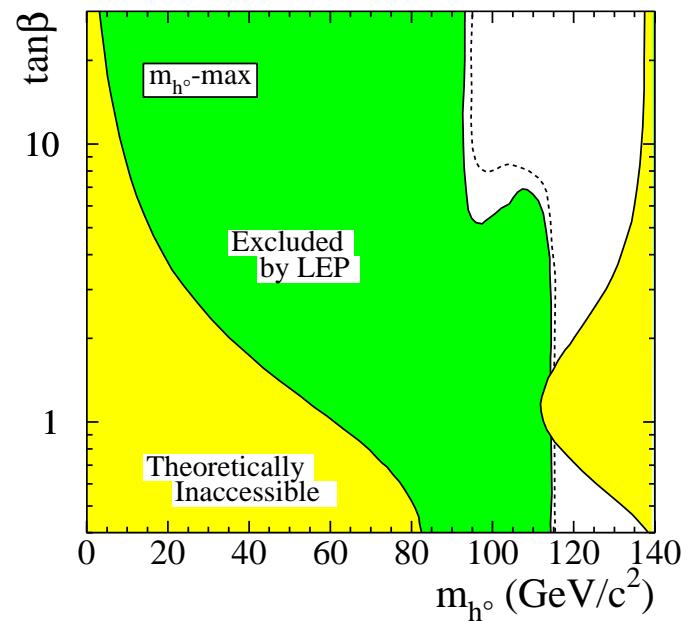
#### Bounds from Higgs searches at LEPII:

$$M_A \gg M_Z \Rightarrow M_h > 114 \text{ GeV}$$

$$M_A \sim M_Z \Rightarrow M_h, M_A \gtrsim 92 \text{ GeV}$$

- Slightly depend on  $m_t, H$  mixing, ...

- Include a  $\Delta^{\text{th}} M_h \sim 3 \text{ GeV}$  error.



(Excluded boundary to be fitted)

Note: include  $1.7\sigma$  Higgs signal??

### 3. SUSY spectrum: indirect experimental constraints

- High precision electroweak measurements: agree with SM  
Large  $(\tilde{t}, \tilde{b})$  mass splitting might generate large contributions:  
 $\Delta^{\text{SUSY}} \rho = \Pi_{ZZ}(0)/M_Z^2 - \Pi_{WW}(0)/M_W^2 \lesssim 2.2 \cdot 10^{-3}$   
**(loose constraints from direct SUSY contributions to  $Z b\bar{b}$  vertex)**
- The  $(g - 2)_\mu$  constraint:  $2.5\sigma$  away from SM (only  $e^+ e^-$  data)  
Might be accounted for by  $\tilde{\mu}-\chi^0$  and  $\tilde{\nu}_\mu-\chi^\pm$  loop contributions  
 $1.06 \cdot 10^{-9} \leq \frac{1}{2} g_\mu^{\text{SUSY}} \leq 4.36 \cdot 10^{-9}$   
**(OK with SM if +  $\tau$  data:  $-5.7 \cdot 10^{-10} \leq \frac{1}{2} g_\mu^{\text{SUSY}} \leq 4.7 \cdot 10^{-9}$ )**
- The  $b \rightarrow s\gamma$  constraint: experimental value agrees with SM  
Strong constraints on the  $t-H^\pm$  and  $\tilde{t}-\chi^\pm$  loop contributions  
 $2.65 \cdot 10^{-4} \leq B(b \rightarrow s\gamma) \leq 4.45 \cdot 10^{-4}$   
**(might be alleviated with a small amount of flavor violation)**
- The  $b \rightarrow s\ell^+\ell^-$  constraint: not very stringent in mSUGRA yet

### 3. SUSY spectrum: the dark matter constraint

- WMAP measurement of temperature anisotropies in CMB, ...

$$\Omega_{\text{DM}} h^2 \simeq 0.113 \pm 0.009 \Rightarrow 0.09 \leq \Omega_{\text{DM}} h^2 \leq 0.14 \text{ at 99% CL}$$

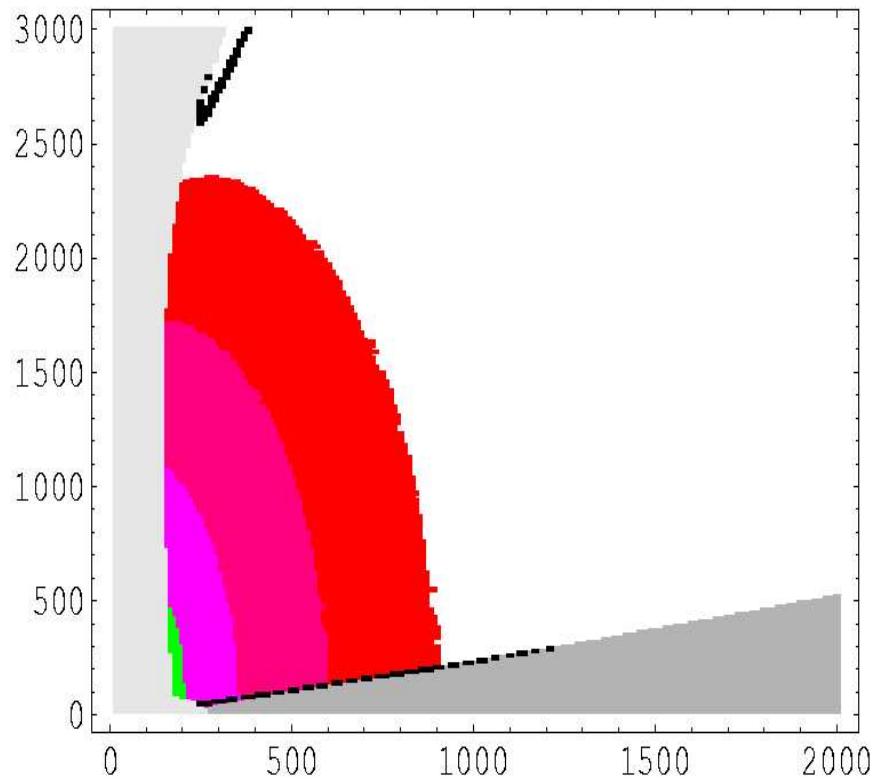
- In the MSSM, LSP neutralino  $\chi_1^0$  is best candidate for CDM
  - electrically neutral and (often maybe too) weakly interacting
  - stable if R-parity is conserved
  - massive:  $m_{\chi_1^0} \gtrsim 50 \text{ GeV}$  in constrained models (mSUGRA)
- Calculation of  $\Omega_{\chi_1^0} h^2 \propto \langle v \sigma(\chi\chi \rightarrow \text{SM part.}) \rangle^{-1}$  complicated:
  - Many final states ( $\Phi = h, H, A, H^\pm; f = \ell, q; V = W, Z, \gamma$ )  
 $\chi_1^0 \chi_1^0 \rightarrow f\bar{f}, VV, \Phi_i \Phi_j, \Phi_i V$  etc....
  - Several channels are present; for example in  $\chi_1^0 \chi_1^0 \rightarrow f\bar{f}$ :  
 **$t$ -channel**  $\tilde{f}$ ,  **$s$ -channel**  $Z$  and  **$s$ -channel**  $A, h, H$  exchanges
  - Co-annihilation processes with NLSP taken into account:  
 $\chi_1^0 + \tilde{P} \rightarrow X + Y$  and  $\tilde{P} + \tilde{P}^{(*)} \rightarrow X + Y$  if  $m_{\tilde{P}} \sim m_\chi$

### 3. SUSY spectrum: an example of a scan

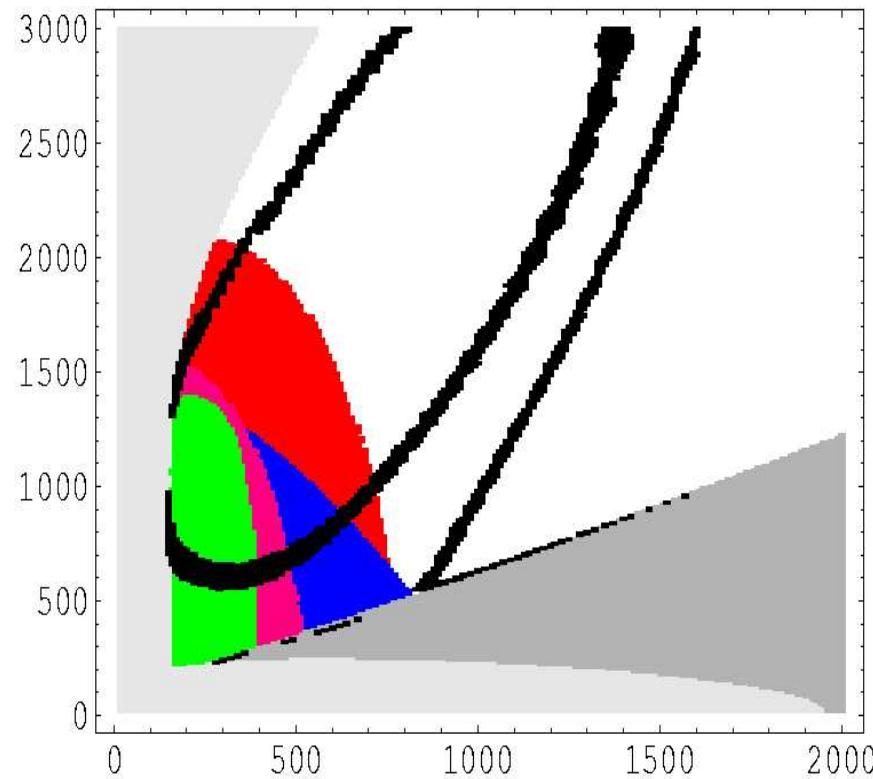
An  $(m_{1/2}, m_0)$  scan with  $A = 0, \mu > 0, m_t = 172.5$  GeV:

$m_0$

$\tan \beta = 10$



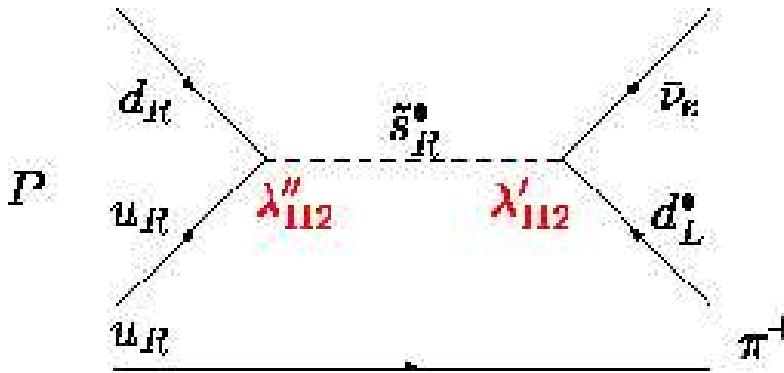
$\tan \beta = 50$



Generically, four (known) regions with the required amount of DM:  $m_{1/2}$   
bulk region (excluded), focus point, co-annihilation,  $A/h$  pole regions

## 4. Extensions of MSSM: Rp violation

To avoid fast P decay, we do not need both L and B conservation



In most general W, include  $\Delta L=1$  or  $\Delta B=1$  interactions:

$$W_{\Delta L=1} = \frac{1}{2} \lambda_{ijk} L_i L_j \bar{e}_k + \lambda'_{ijk} L_i Q_j \bar{d}_k + \mu'_i L_i H_u$$

$$W_{\Delta B=1} = \frac{1}{2} \lambda''_{ijk} \bar{u}_i \bar{d}_j \bar{d}_k$$

P decay modes and experimental limits on  $\beta$  and  $L$  imply  $\lambda''_{ijk} \ll 1$ .

- However, at least 45 new parameters in the general case.
- no stable LSP and thus no SUSY DM candidate...
- But, rich phenomenology (e.g. s channel sfermion production)
- enters in neutrino phenomenology and addresses small  $\nu$  masses

## 4. Extensions of the MSSM: CP violation

One can allow for some CP-violating parameters, in particular:

- Complex  $M_1, M_2, M_3$  (some phases rotated away) and  $\mu$
- Complex trilinear  $A_f$  couplings, in particular  $A_t$ .

The MSSM Higgs sector stays CP-conserving at the tree-level but complex parameters enter at the one-loop level through  $\mu$  and  $A_t$ .

- CP violation is needed for (direct) baryogenesis in MSSM
- However, many new parameters will enter in the general case
- Complicates the determination of spectrum but less fine-tunning!
- Strongly constrained by data ( $n_{\text{edm}} \dots$ ) and needs cancelations
- No sign yet of any additionnaly from CP in B-factories etc...

One can also allow for flavor non-diagonal interactions, however:

- Parameters strongly constrained from FCNC, K, B physics...
- Only adds complications/parameters (no theory motivation)...

## 4. Extensions of the MSSM: NMSSM

The  $\mu$  problem:  $\mu$  enters EWSB and the determination of  $M_Z$ .

It must be of order SUSY-breaking parameters such as  $M_{H_1}, M_{H_2}$ .

But  $\mu$  is a SUSY preserving parameter, comes from  $W \propto \mu \hat{H}_1 \hat{H}_2$ ,  
and, a priori, no reason for having  $\mu \propto M_Z, M_{\text{SUSY}} \ll M_{\text{GUT}}$ ....

Solution:  $\mu$  is related to a vev of an additional field  $S$  with  $\langle S \rangle = s$

**NMSSM: introduce a gauge singlet superfield  $\hat{S}$  into superpotential**

$$W = W_{\text{MSSM}} + \lambda \hat{H}_1 \hat{H}_2 \hat{S} + \frac{1}{3} \kappa \hat{S}$$

Extended spectrum in NMSSM compared to MSSM:

- one additional neutralino state:  $\Rightarrow \chi_{1,\dots,5}^0$
  - two additional Higgs particles  $\Rightarrow H_1, H_2, H_3, A_1, A_2, H^+, H^-$
- $\Rightarrow$  less constrained and fine tuned model, richer phenomenology...

Ex: upper bound on h mass is  $M_h^{\text{NMSSM}} = M_h^{\text{MSSM}} + 20\text{--}40 \text{ GeV}$ .

LEP searches bounds are not valid and h lighter than 100 GeV.

## 4. Extensions of the MSSM: ESSM

An even more extended model with richer phenomenology is the  $E_6$ SSM

- based on low-energy matter content of 27 repr. of the  $E_6$  group
- there are also two additional non Higgs scalar doublets.

It has a very elegant solution to the  $\mu$  problem of the MSSM

$E_6 \rightarrow SO(10) \times U(1)_\psi \rightarrow SU(5) \times U(1)_\psi \times U(1)_\chi \rightarrow G_{SM} \times U(1)'$   
extra  $U(1)'$  allows for  $\lambda S H_1 H_2$  interaction which generates effective  $\mu$

The model has very nice features:

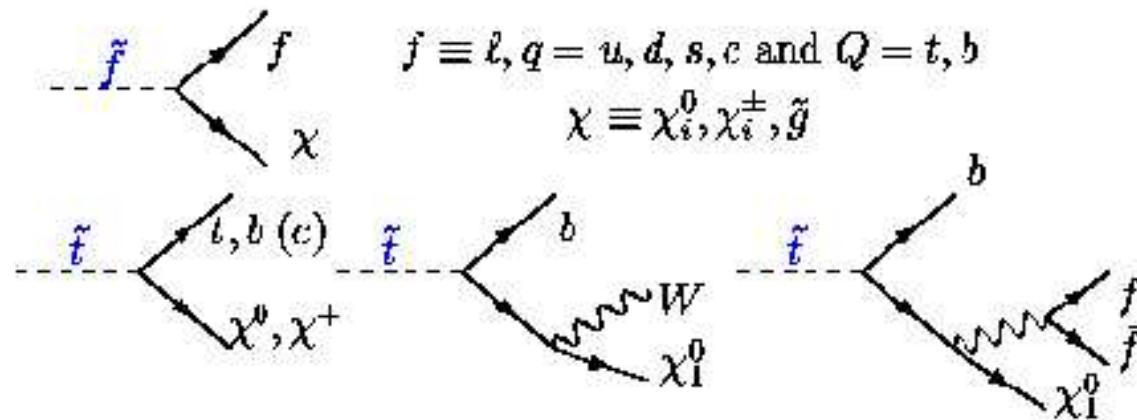
- gives a solution to the  $\mu$  problem with less fine-tuning as in NMSSM
- gauge coupling unification at  $M_{GUT}$  with a reasonable  $\alpha_s$  value
- a full unification of all forces including gravity possible is at  $M_P$

.... and very rich phenomenology:

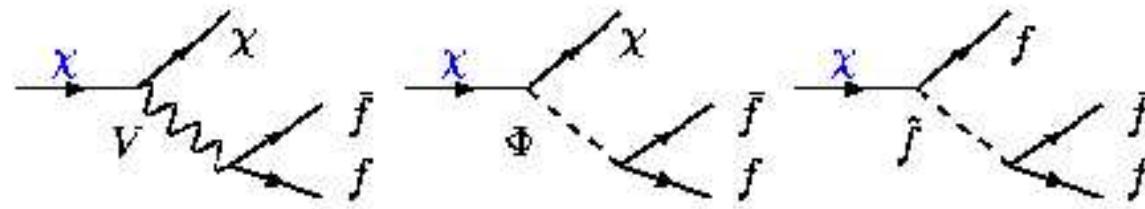
- extended Higgs sector and possibility of a light  $Z'$  gauge boson
- extra light matter in anomaly representation of dimension 27 of  $E_6$

# 5. Decays and Production of sparticles

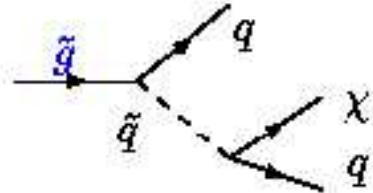
## Squarks and Sleptons



## Charginos and neutralinos



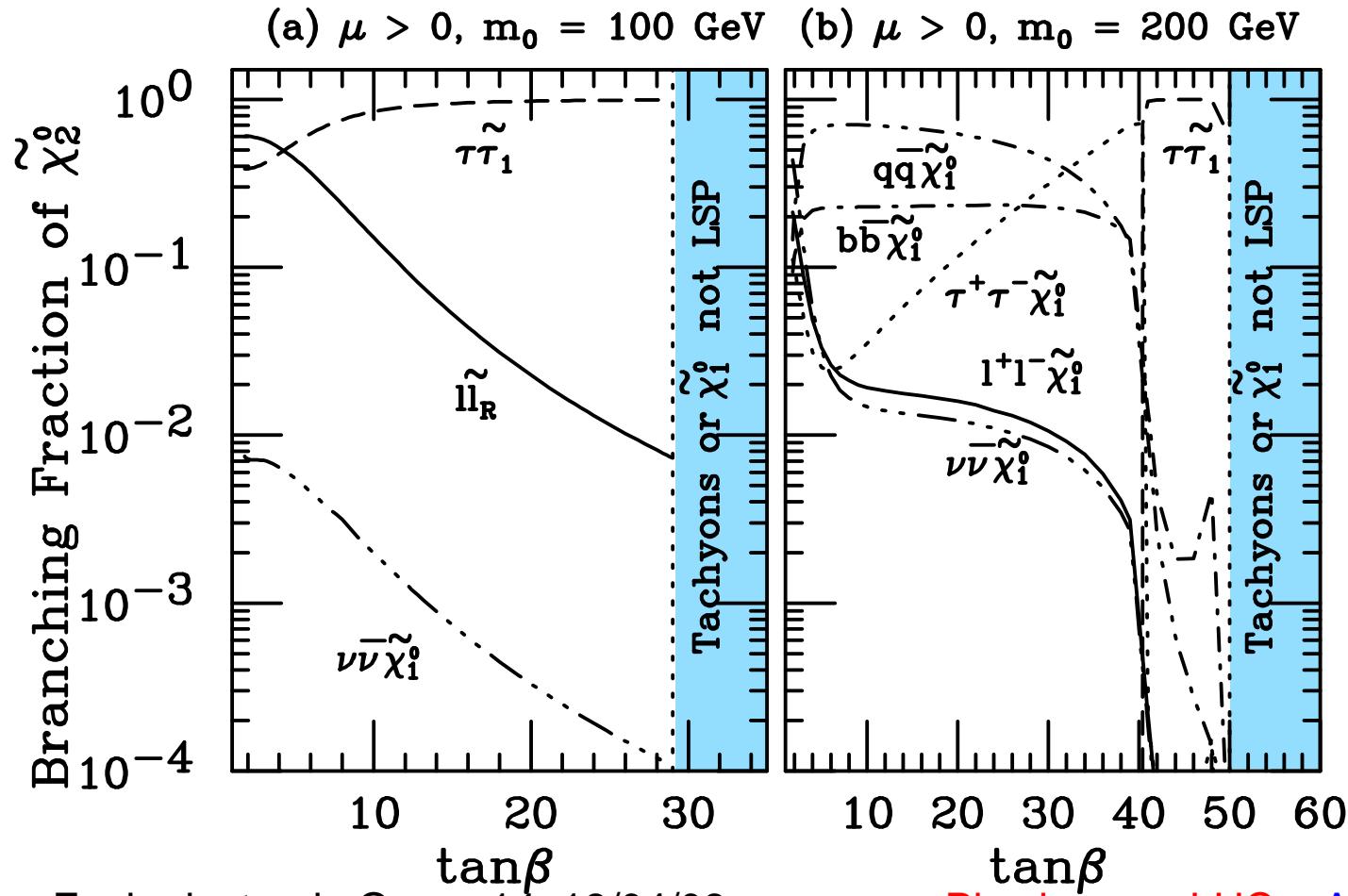
## Gluinos



## 5. Decays: possible decays of sparticles

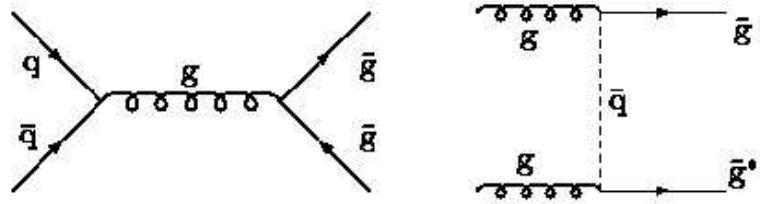
- Possibility of cascade decays:  $\tilde{q} \rightarrow q + \chi_2^0 \rightarrow q + \chi_1^0 f\bar{f}$ .
- Signature in usual MSSM:  $E_T$  from escaping  $\chi_1^0$  LSPs.
- In GMSB, signature is due to NLSP  $(\chi_1^0, \tilde{\tau}_1) \rightarrow \tilde{G} + (\gamma, \tau)$ .

Example of final state decay in mSUGRA:  $\chi_2^0$

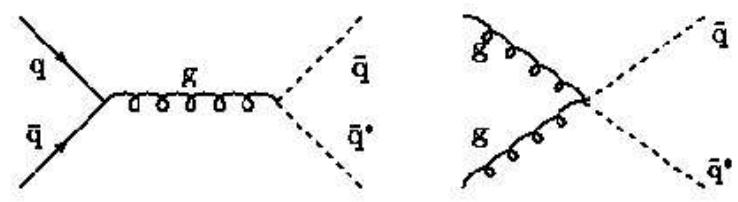


# 5. Production of SUSY particles

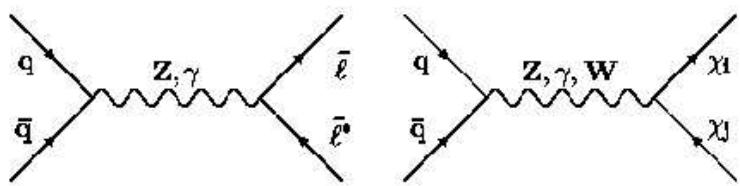
- Gluino production



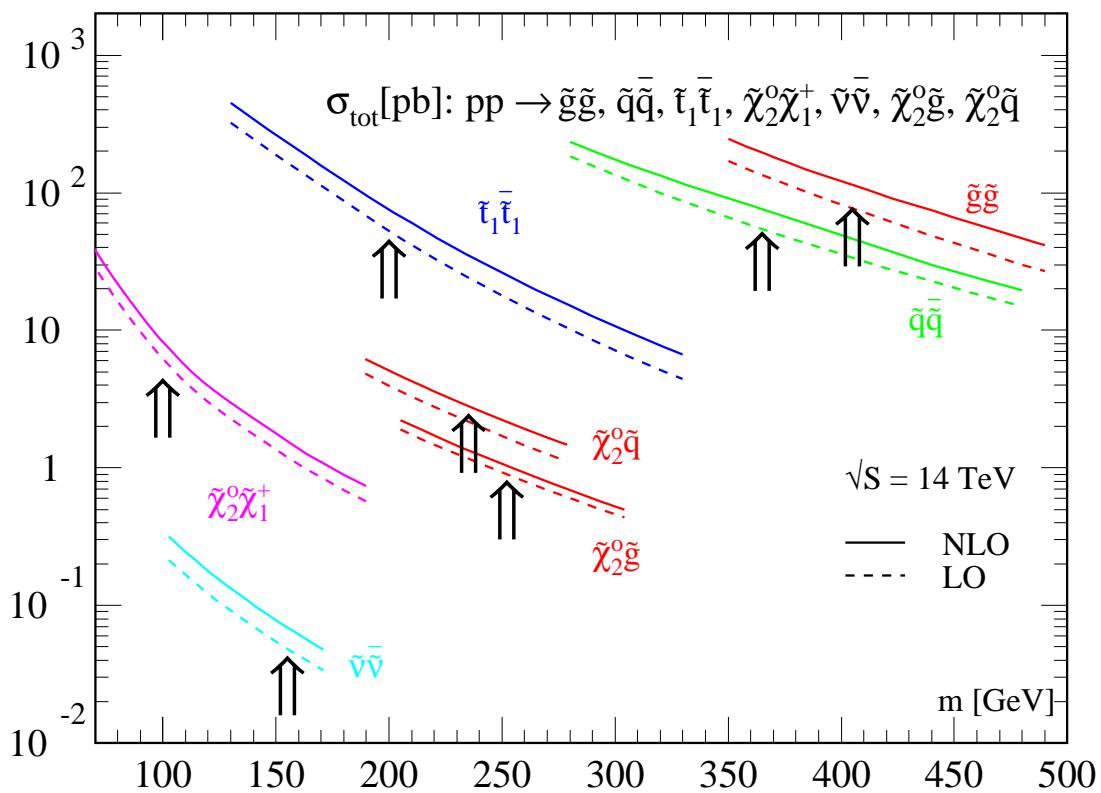
- Squark production



- $\chi/\tilde{\ell}$  production

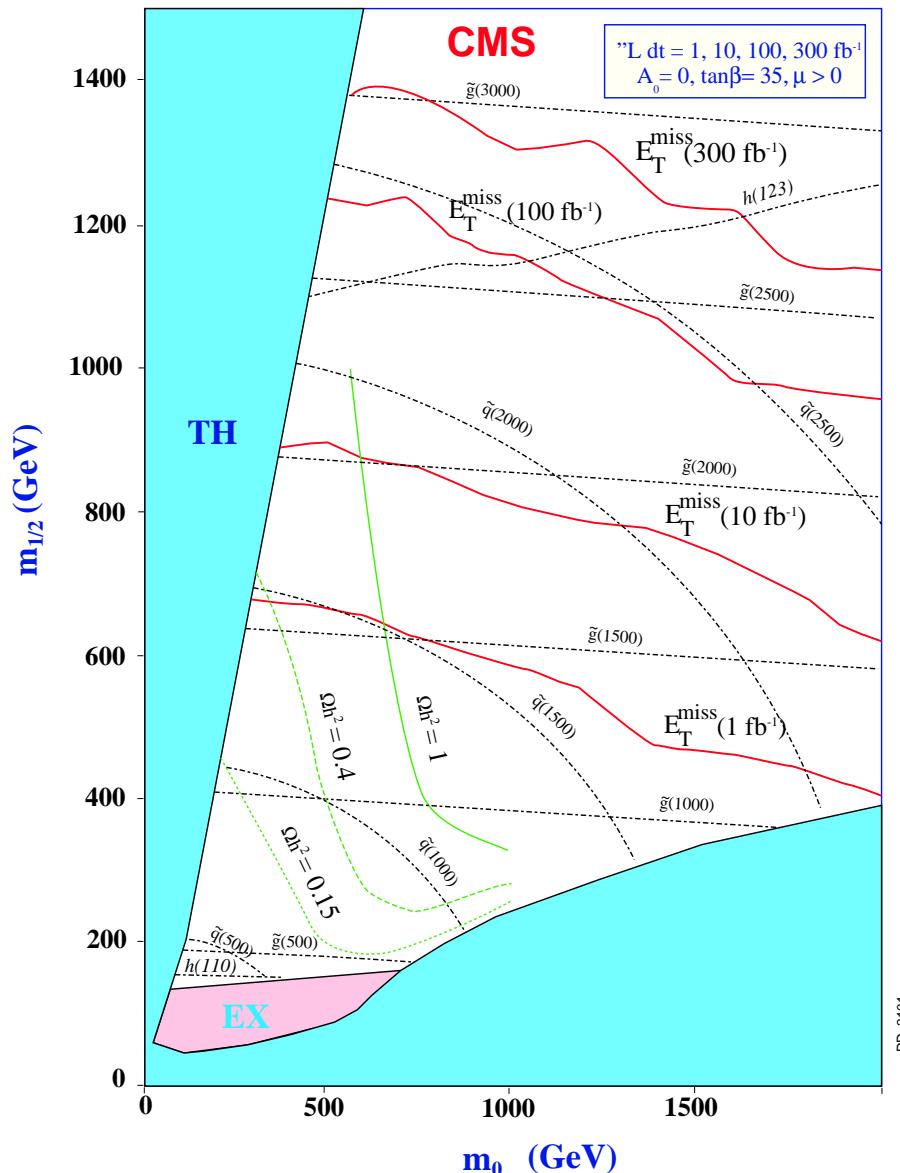


## Cross sections at the LHC



# 5. Sparticle discovery reach at the LHC

The CMS  $\tilde{q}, \tilde{g}$  mass reach in  $E_T^{\text{miss}} + \text{jets}$  inclusive channel  
for various integrated luminosities



# 6. SUSY Higgs Decays and Production

Higgs decays (and cross sections) strongly depend on couplings

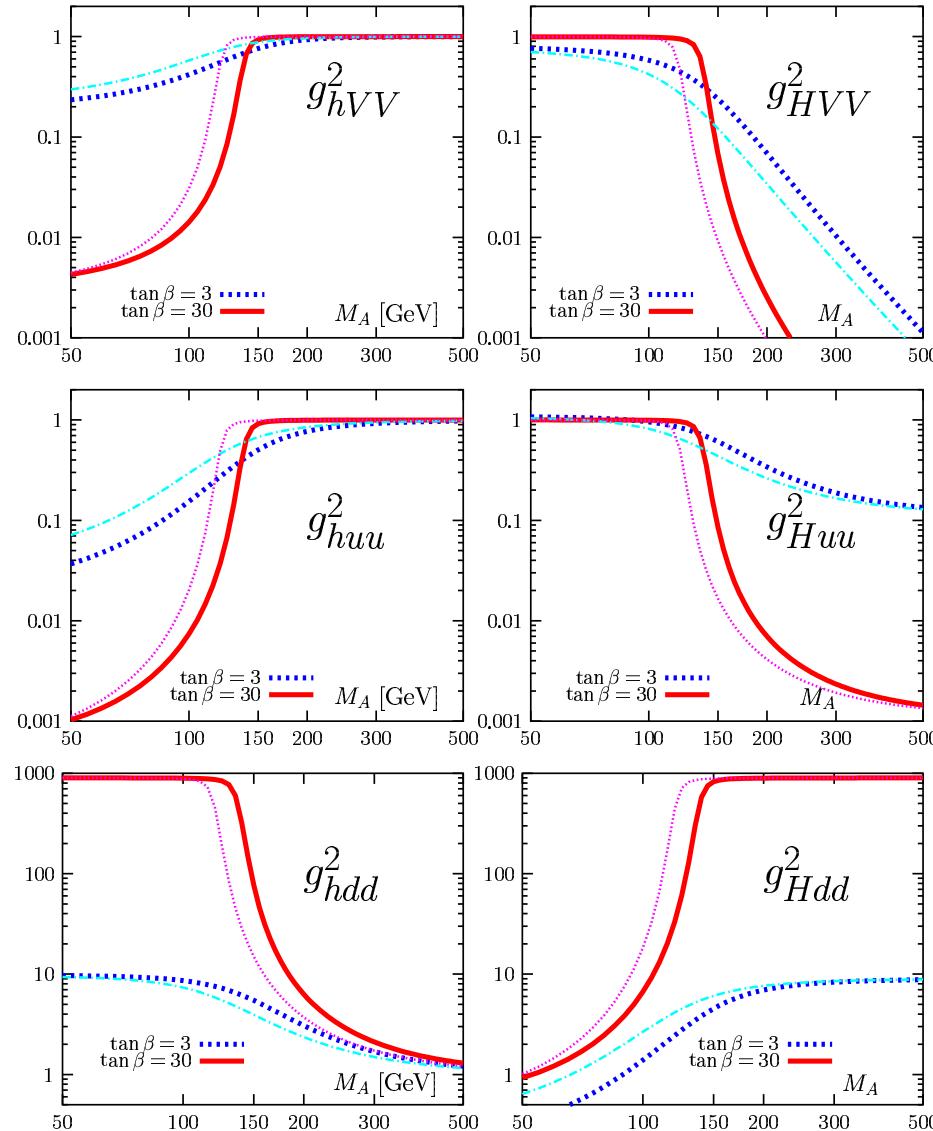
Couplings in terms of  $H_{\text{SM}}$  and their values in decoupling limit:

$\Phi$	$g_{\Phi \bar{u} u}$	$g_{\Phi \bar{d} d}$	$g_{\Phi VV}$
$h$	$\frac{\cos \alpha}{\sin \beta} \rightarrow 1$	$\frac{\sin \alpha}{\cos \beta} \rightarrow 1$	$\sin(\beta - \alpha) \rightarrow 1$
$H$	$\frac{\sin \alpha}{\sin \beta} \rightarrow 1/\tan \beta$	$\frac{\cos \alpha}{\cos \beta} \rightarrow \tan \beta$	$\cos(\beta - \alpha) \rightarrow 0$
$A$	$1/\tan \beta$	$\tan \beta$	0

- The couplings of  $H^\pm$  have the same intensity as those of  $A$ .
- Couplings of  $h, H$  to  $VV$  are suppressed; no  $AVV$  couplings (CP)
- For  $\tan \beta > 1$ : cplgs to  $d$  enhanced, cplgs to  $u$  suppressed.
- For  $\tan \beta \gg 1$ : couplings to  $b$  quarks  $b (m_b \tan \beta)$  very strong.
- For  $M_A \gg M_Z$ :  $h$  couples like the SM Higgs boson and  $H$  like  $A$ .

# 6. Higgs decays: SUSY Higgs couplings

Including radiative corrections just as in the case of the Higgs masses:



## 6. Higgs decays: channels

### General features in Higgs decays

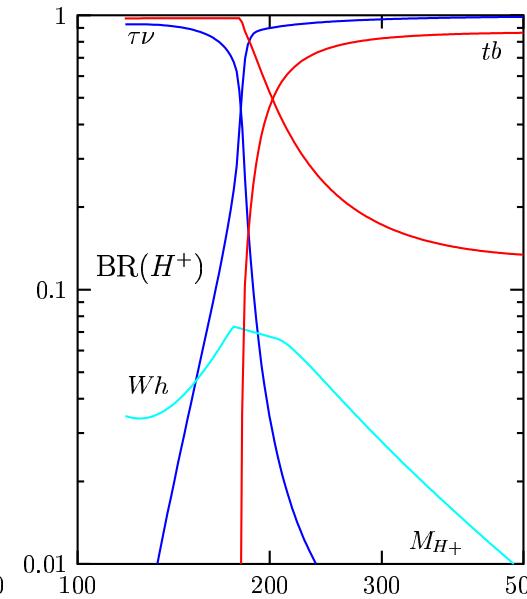
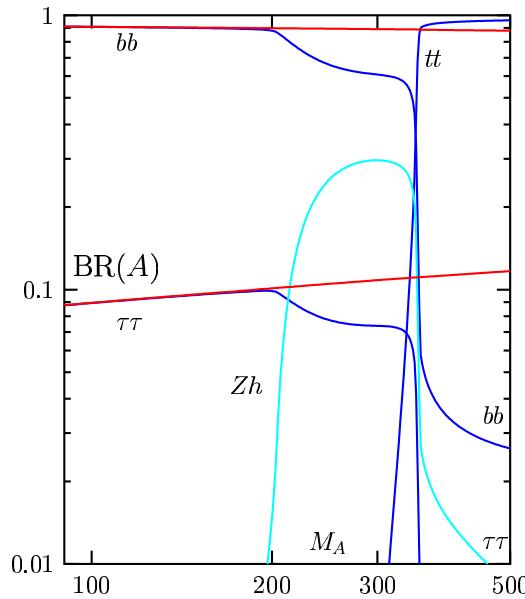
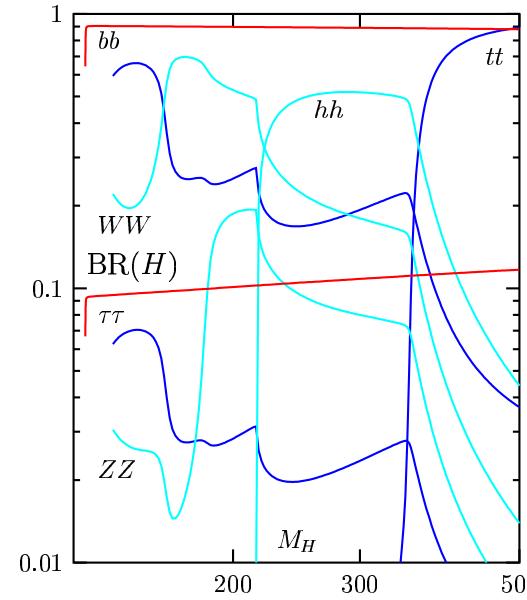
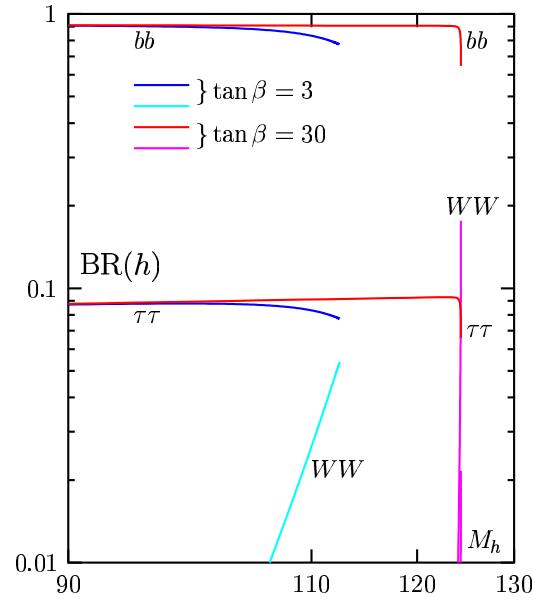
- $h$ : same as  $H_{\text{SM}}$  in general (in particular in decoupling limit)  
 $h \rightarrow b\bar{b}$  and  $\tau^+\tau^-$  potentially enhanced ( $\tan \beta \gtrsim 3$ ).
- $A$ : only  $b\bar{b}$ ,  $\tau^+\tau^-$  and  $t\bar{t}$  decays (no  $VV$ ,  $hZ$  suppressed).
- $H$ : same as  $A$  in general ( $WW$ ,  $ZZ$ ,  $hh$  decays suppressed).
- $H^\pm$ :  $\tau\nu$  and  $tb$  decays (depending if  $M_{H^\pm} <$  or  $> m_t$ ).

### Possible new effects

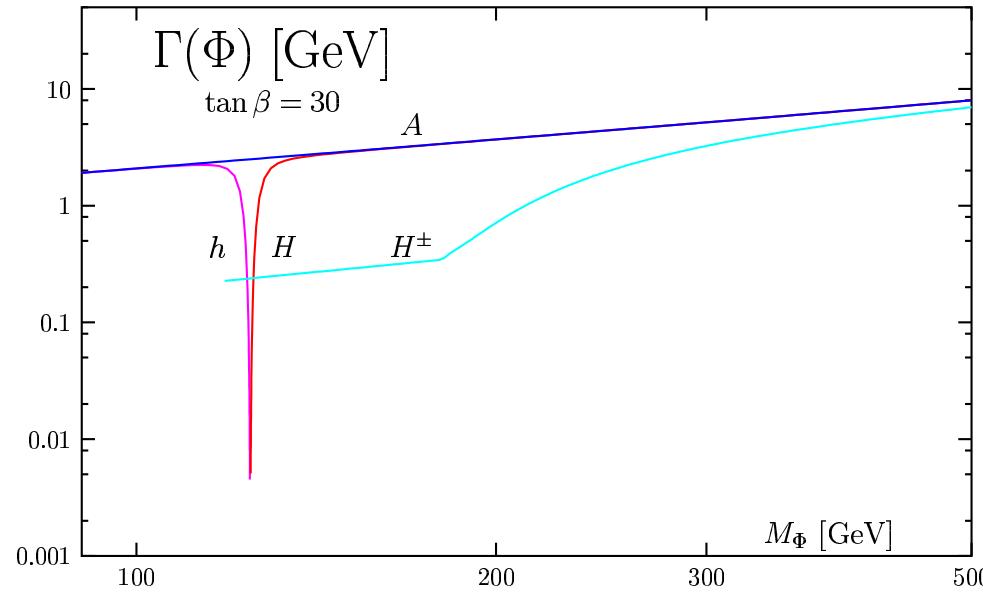
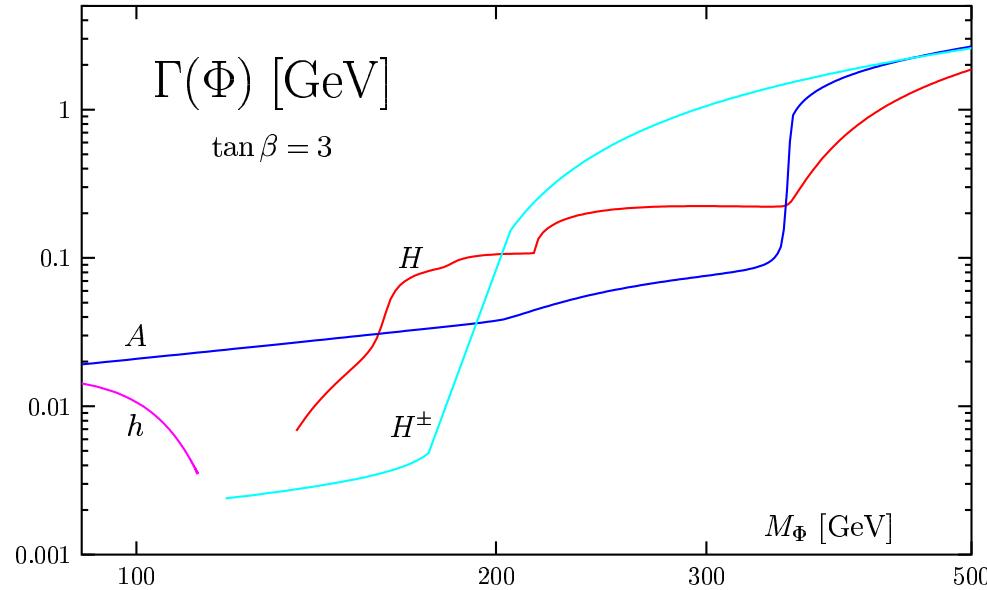
- Although suppressed, decays into  $V\Phi$  and/or  $VV$  possible.
- 3-body decays important ( $h \rightarrow WW^*$ ,  $H/A \rightarrow tt^*$ ,  $H^+ \rightarrow tb^*$ ...)
- SUSY particle loops might be important ( $h/A/H \rightarrow b\bar{b}$ ,  $h \rightarrow gg$ ).
- Decays into sparticles if kinematically allowed significant:  
 $h \rightarrow \chi_1^0 \chi_1^0$  still possible in non universal MSSMs.  
 $H, A \rightarrow \chi_i^+ \chi_j^-$ ,  $\chi_i^0 \chi_j^0$  and  $H^\pm \rightarrow \chi_i^0 \chi_j^\pm$  important for low  $\tan \beta$ .

Total decay widths: Small compared to SM (no  $V_L$  contribution).

## 6. Higgs Decays: BRs



## 6. Higgs decays: total widths

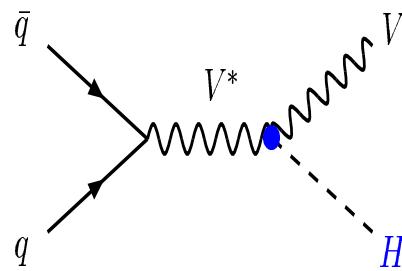


# 6. Higgs production at LHC

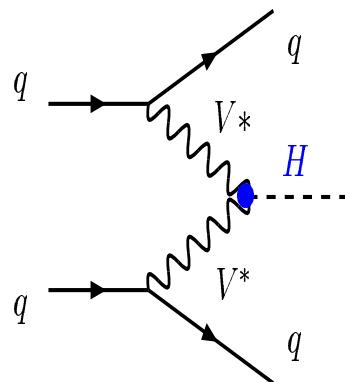
## SM production mechanisms

[assuming heavy sparticles]

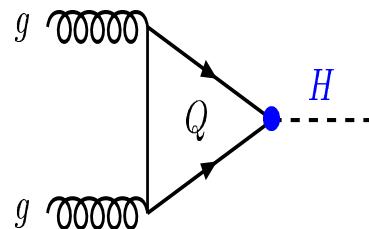
Higgs-strahlung



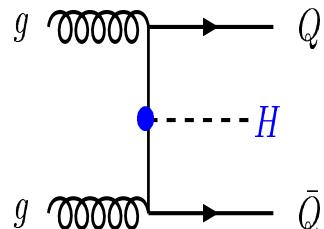
Vector boson fusion



gluon-gluon fusion



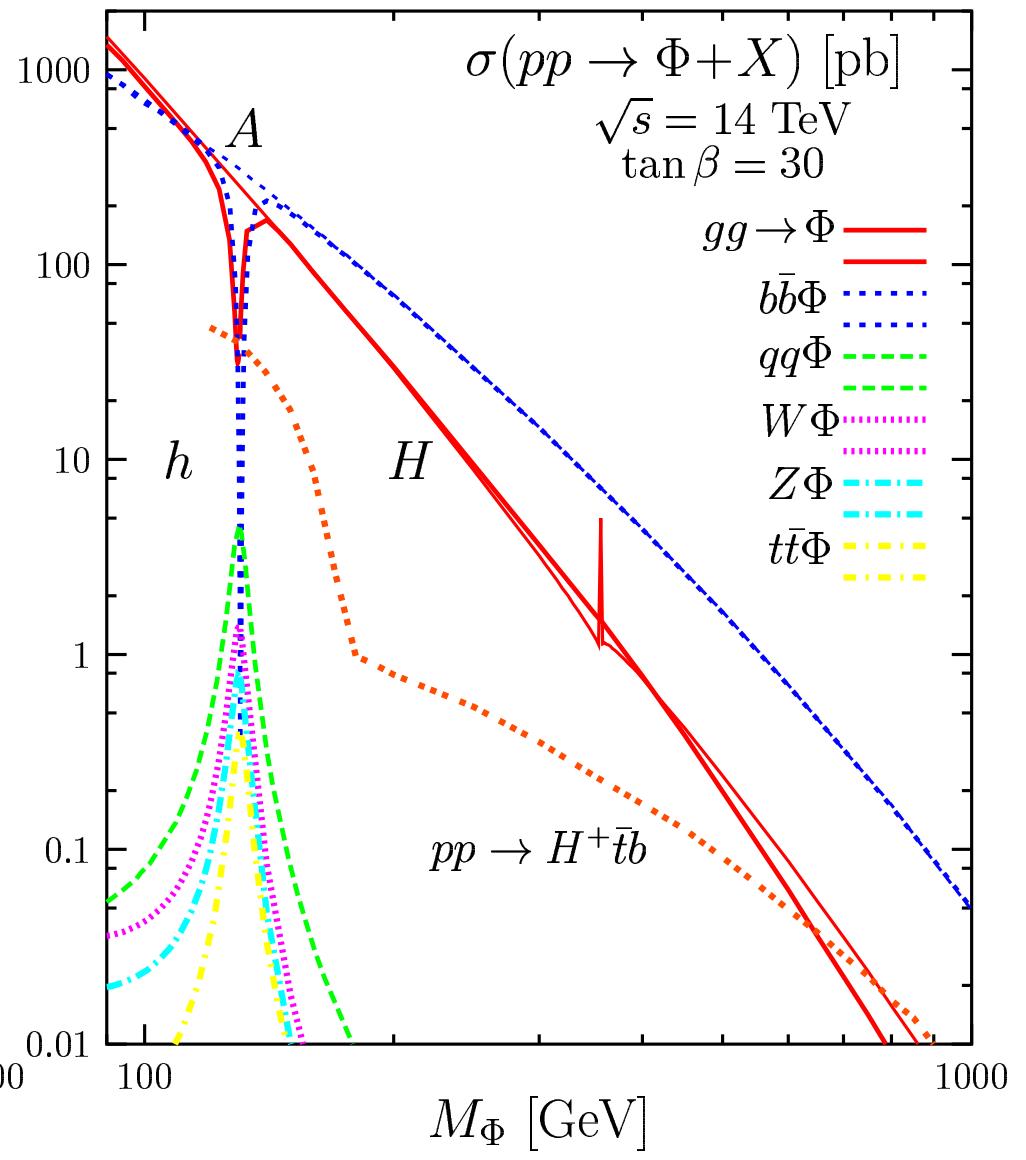
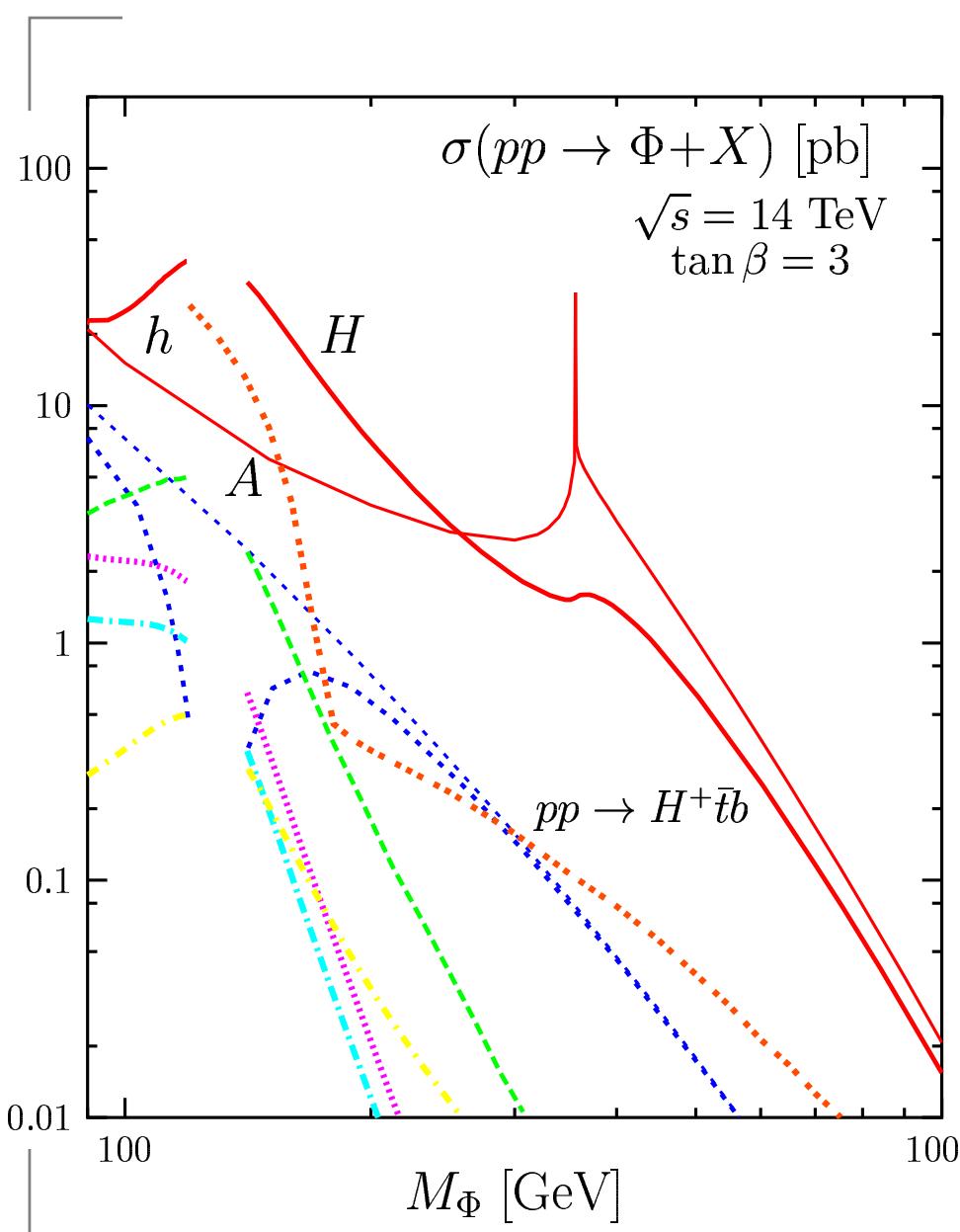
in association with  $Q\bar{Q}$



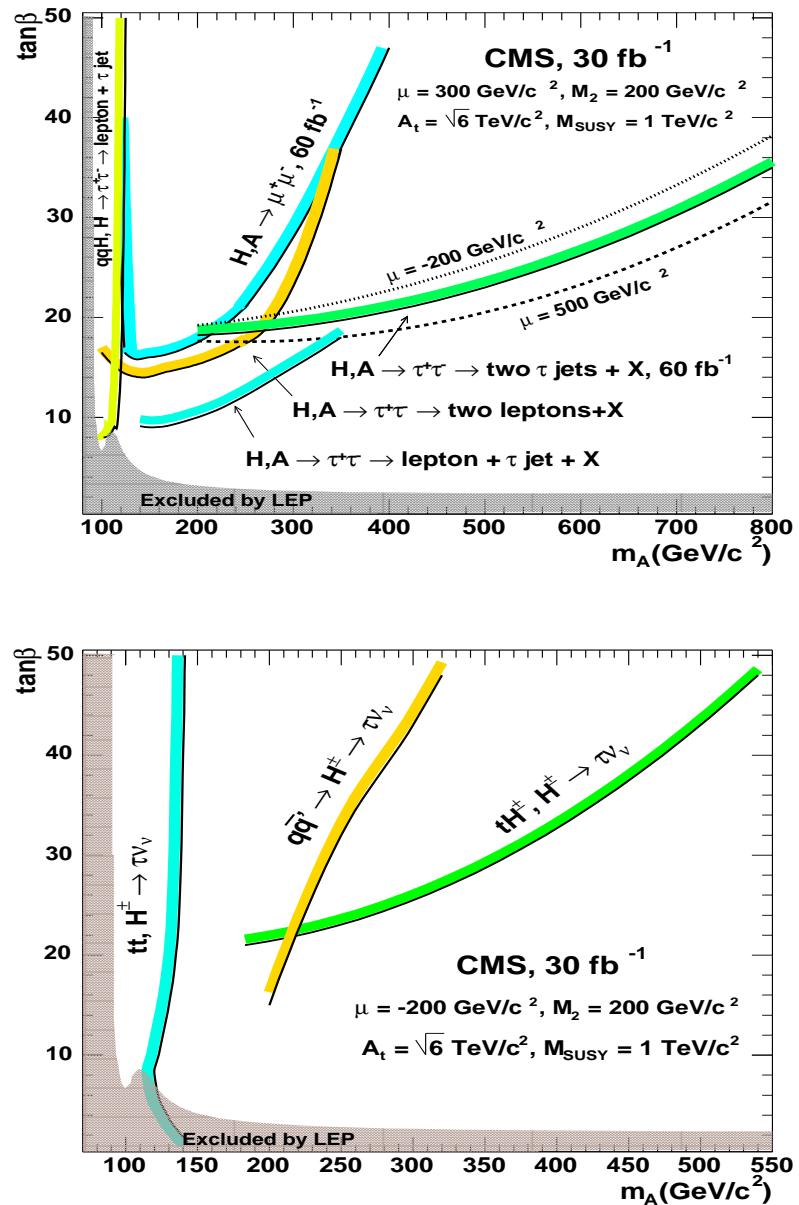
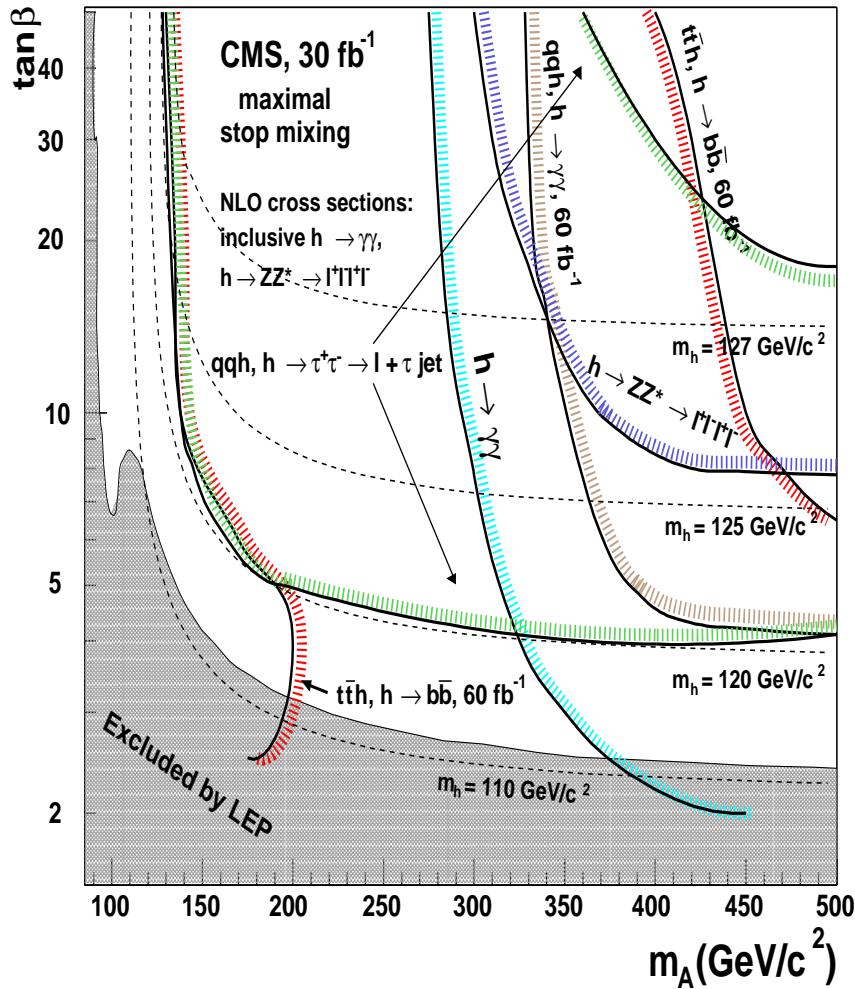
## What is different in MSSM

- All work for CP-even  $h, H$  bosons.
  - in  $\Phi V$ ,  $q\bar{q}\Phi$   $h/H$  complementary
  - $\sigma(h) + \sigma(H) = \sigma(H_{SM})$
  - additional mechanism:  $q\bar{q} \rightarrow A+h/H$
- For  $gg \rightarrow \Phi$  and  $pp \rightarrow tt\Phi$ 
  - include the contr. of b-quarks
  - dominant contr. at high  $\tan\beta$ !
- For pseudoscalar  $A$  boson:
  - CP: no  $\Phi A$  and  $q\bar{q}A$
  - $gg \rightarrow A$  and  $pp \rightarrow bbA$  dominant.
- For charged Higgs boson:
  - $M_H \lesssim m_t$ :  $pp \rightarrow t\bar{t}$  with  $t \rightarrow H^+ b$
  - $M_H \gtrsim m_t$ : continuum  $pp \rightarrow t\bar{b}H^-$

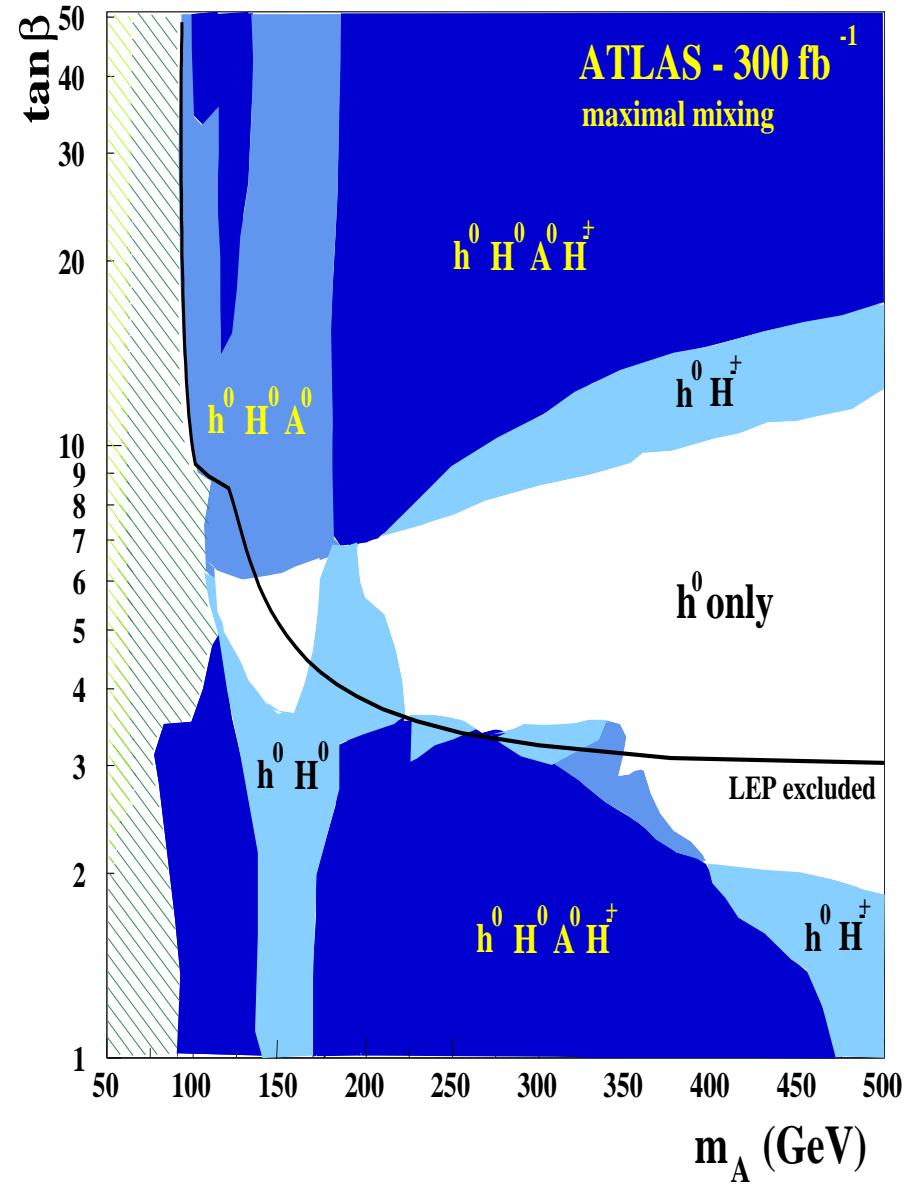
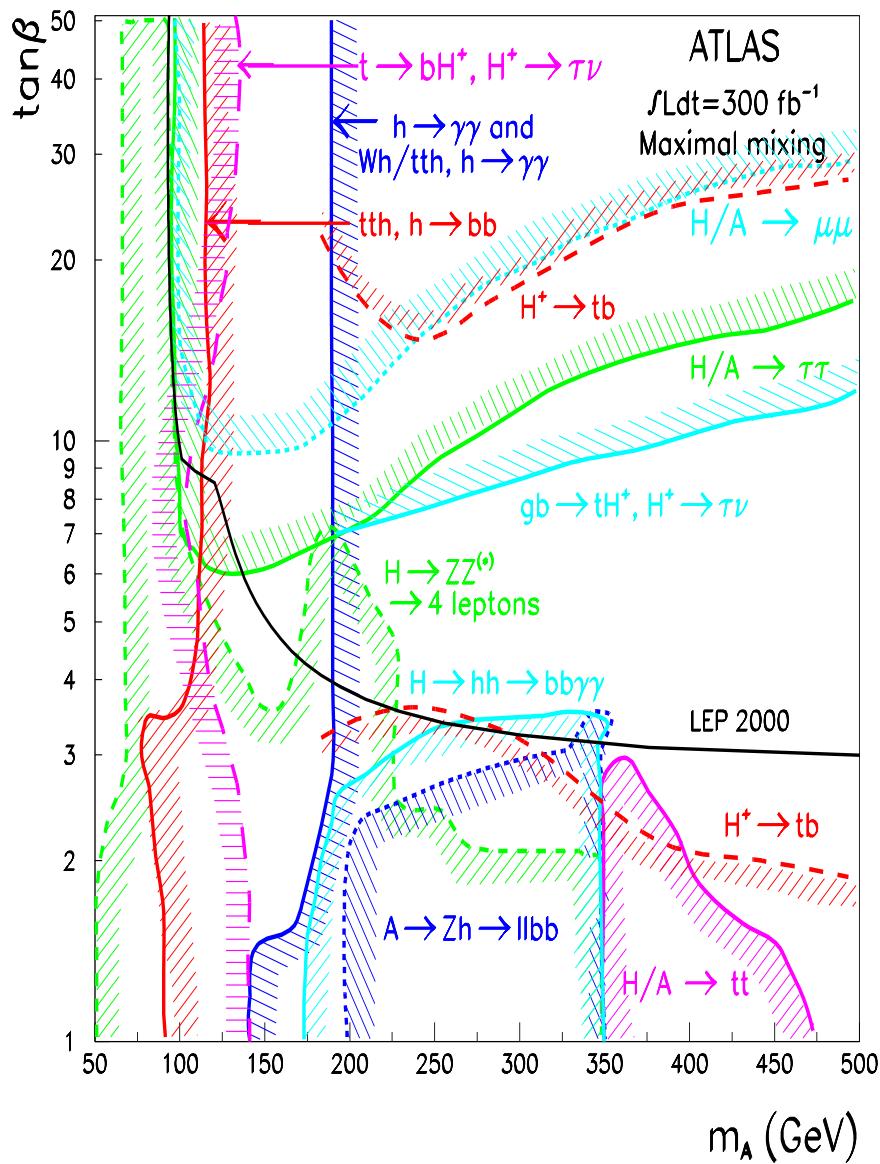
## 6. Higgs production: cross sections



# 6. Higgs production: detection



## 6. Higgs production: detection



## 7. Higgs in non minimal scenarios

However: life can be much more complicated even in the MSSM

- There are scenarii where searches are different from the SM case:
  - The intense coupling regime:  $h, H, A$  almost mass degenerate....
- SUSY particles might play an important role in production/decay:
  - light  $\tilde{t}$  loops might make  $\sigma(gg \rightarrow h \rightarrow \gamma\gamma)$  smaller than in SM.
  - Higgses can be produced with sparticles ( $pp \rightarrow \tilde{t}\tilde{t}^*h, \dots$  ).
  - Cascade decays of SUSY particles into Higgs bosons....
- SUSY decays, if allowed, might alter the search strategies:
  - $h \rightarrow \chi_1^0 \chi_1^0, \tilde{\nu} \tilde{\nu}$  are still possible in non universal models...
  - Decays of  $A, H, H^\pm$  into  $\chi_i^\pm, \chi_i^0$  are possible but can be useful...

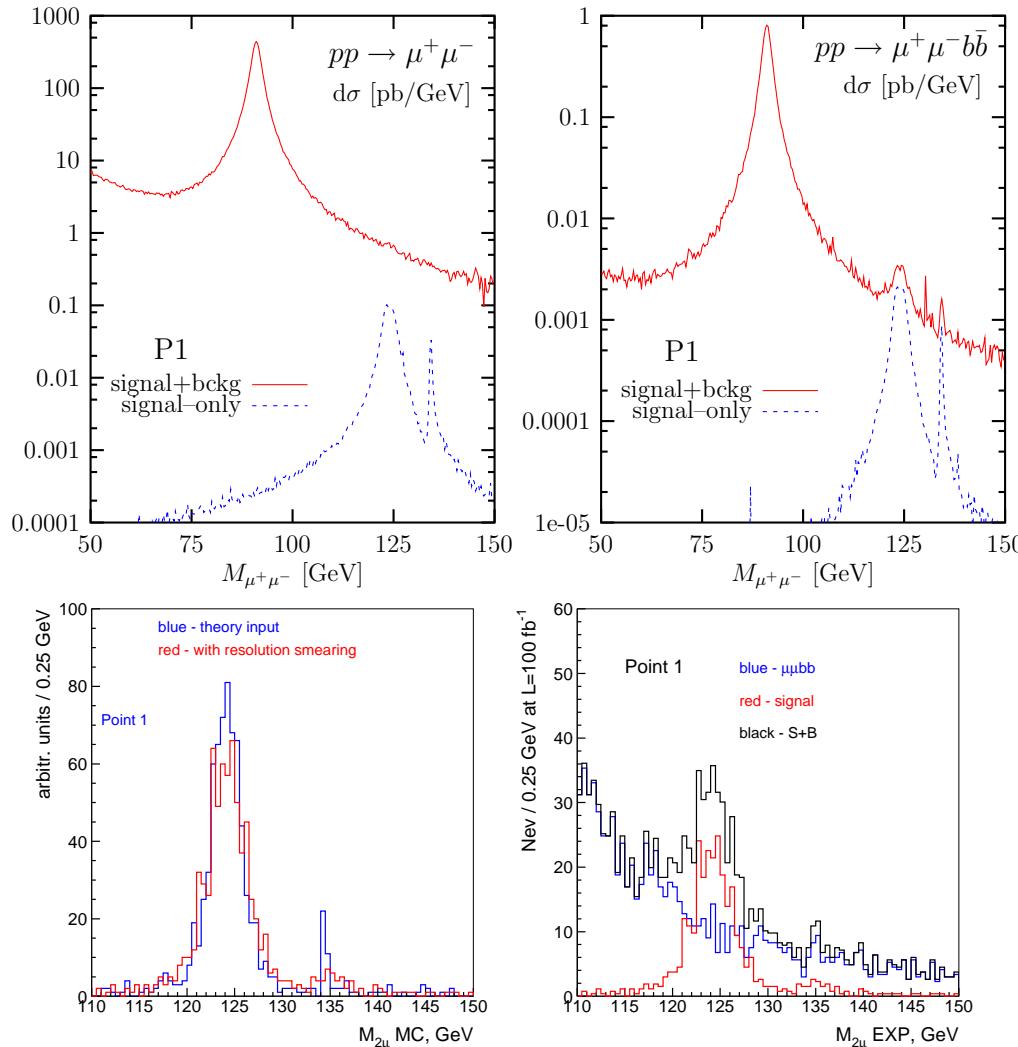
Life can be even more complicated in extensions of the MSSM

- CP violation in the Higgs sector which changes the spectrum.
- NMSSM with an additional Higgs singlet and difficult Higgs decays.

Be prepared for the unexpected!

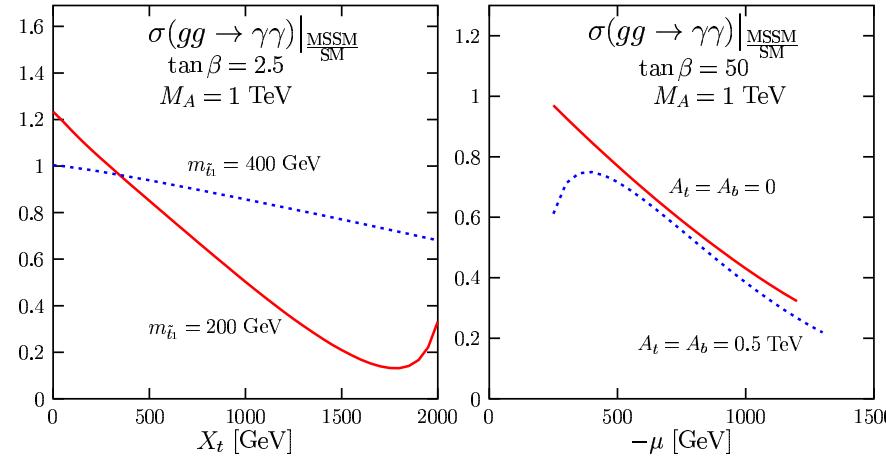
## 7. Higgs in non minimal scenarios

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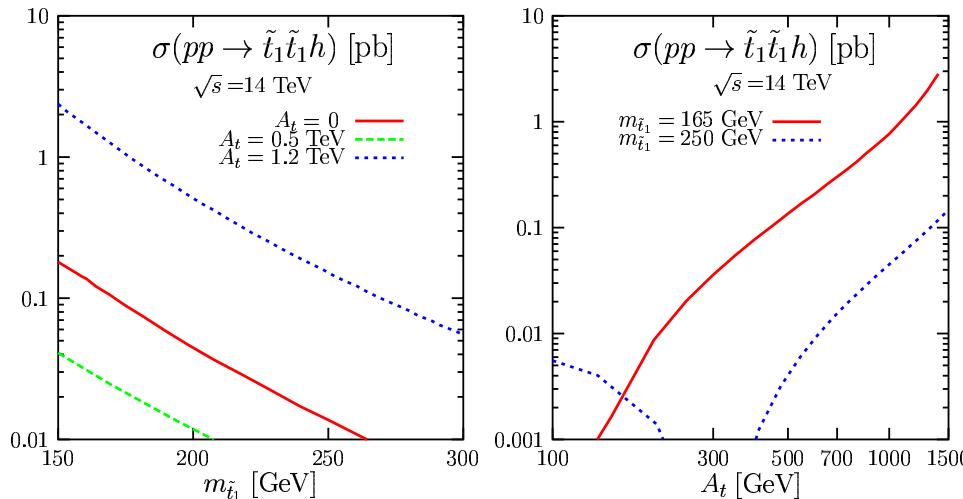


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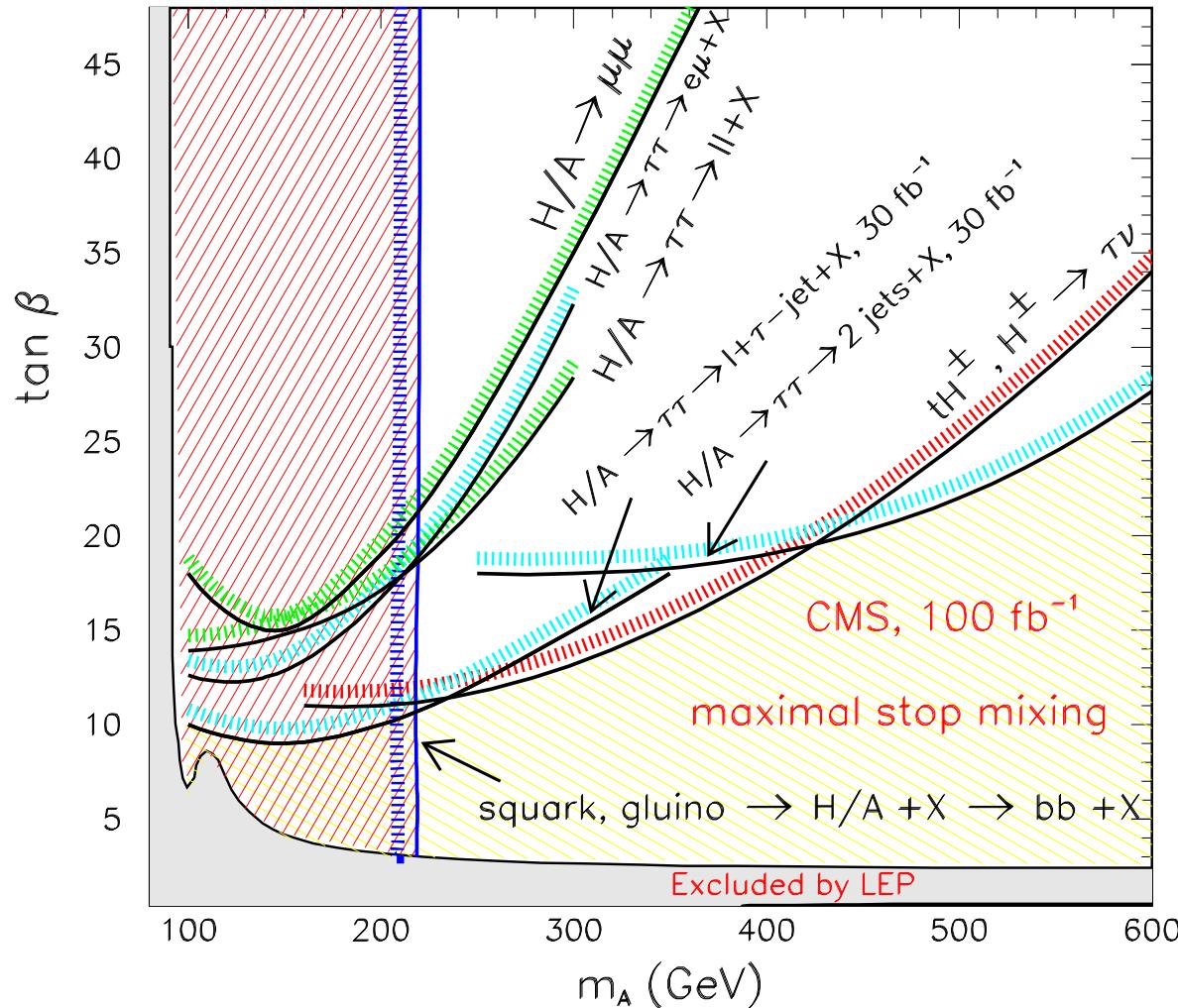


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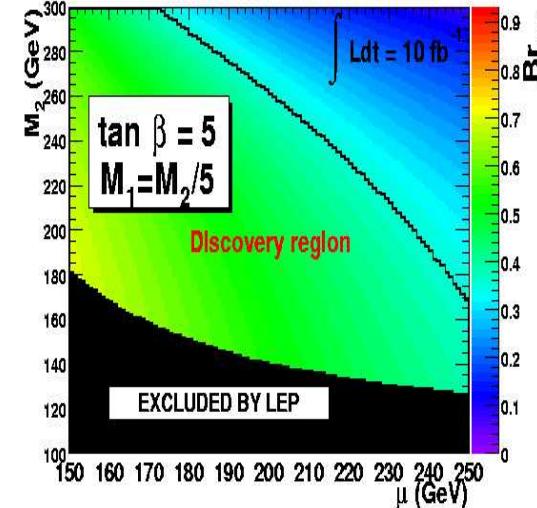
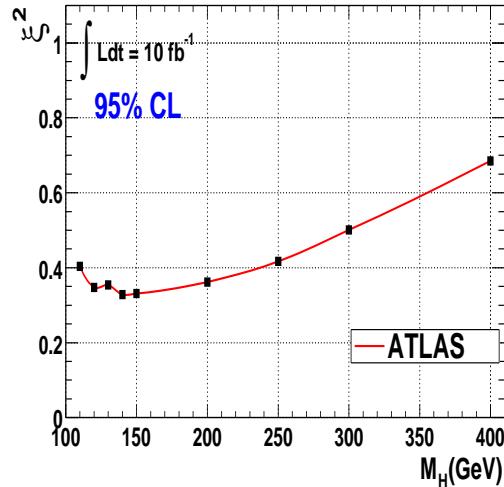
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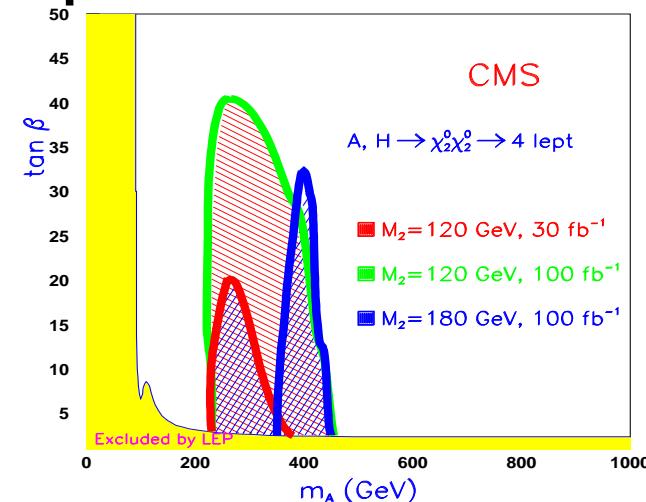
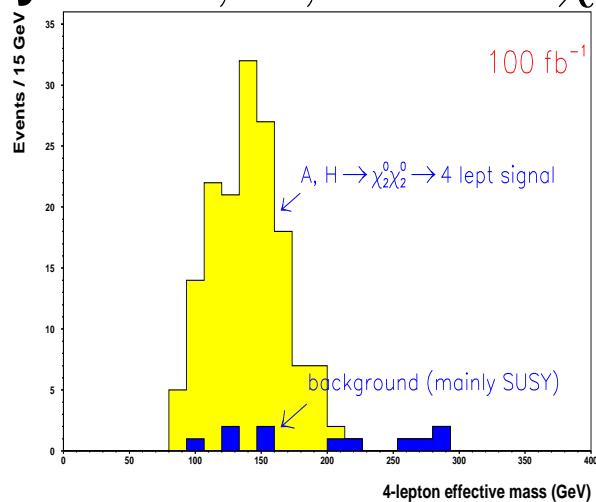


## 7. Higgs in non minimal scenarios

- SUSY decays, if allowed, might alter the search strategies:
  - $h \rightarrow \chi_1^0 \chi_1^0, \tilde{\nu} \tilde{\nu}$  are still possible in non universal models...



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## 7. Higgs in non minimal scenarios: CP–violation

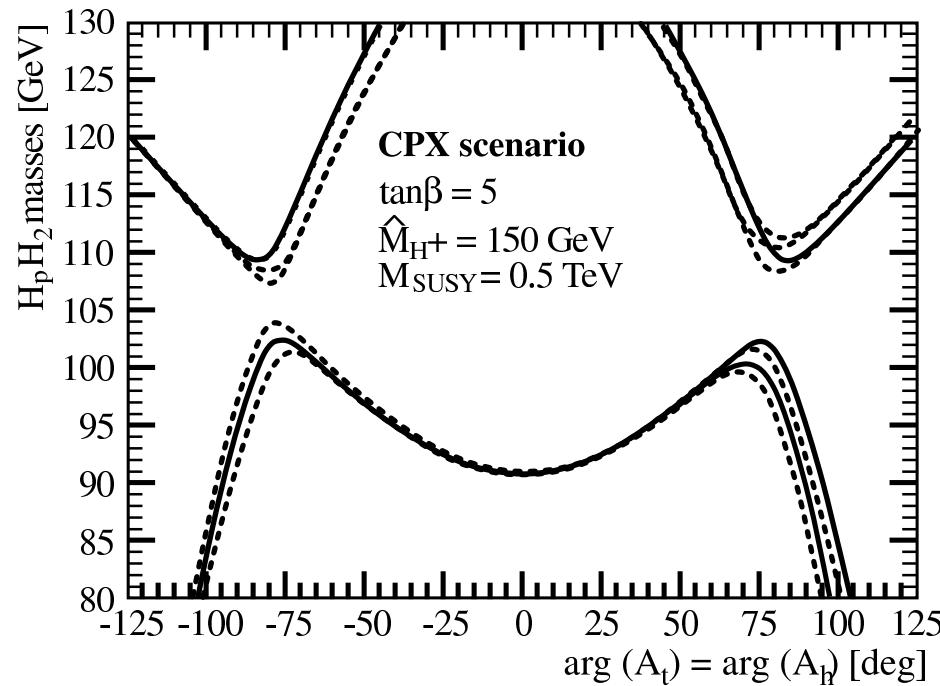
Life can be even more complicated in extensions of the MSSM

We can allow for some amount of CP–violation in eg.  $M_i$ ,  $\mu$  and  $A_f$

Higgs sector: CP–conserving at tree level  $\Rightarrow$  CP–violating at one–loop

Good to address the issue of baryogenesis at the electroweak scale....

- $h, H, A$  are not CP definite states and  $h_1, h_2, h_3$  CP mixtures
- determination of Higgs spectrum slightly more complicated,
- possibility of a light  $h_1$  that has escaped detection at LEP2.



Carena et al, Choi+Drees et al, Pilaftsis et al, Ellis et al, Haber+Gunion, Krawczyk et al, Osland et al, Heinemeyer et al, Moretti et al, .....

## 7. Higgs in non minimal scenarios: CP-violation

The CPX scenario:

(Carena et al, Ellis et al, )

$h_1$  light but weak cplgs to  $W, Z$

$h_2 \rightarrow h_1 h_1$  decays allowed

$h_3$  couplings to  $VV$  reduced...

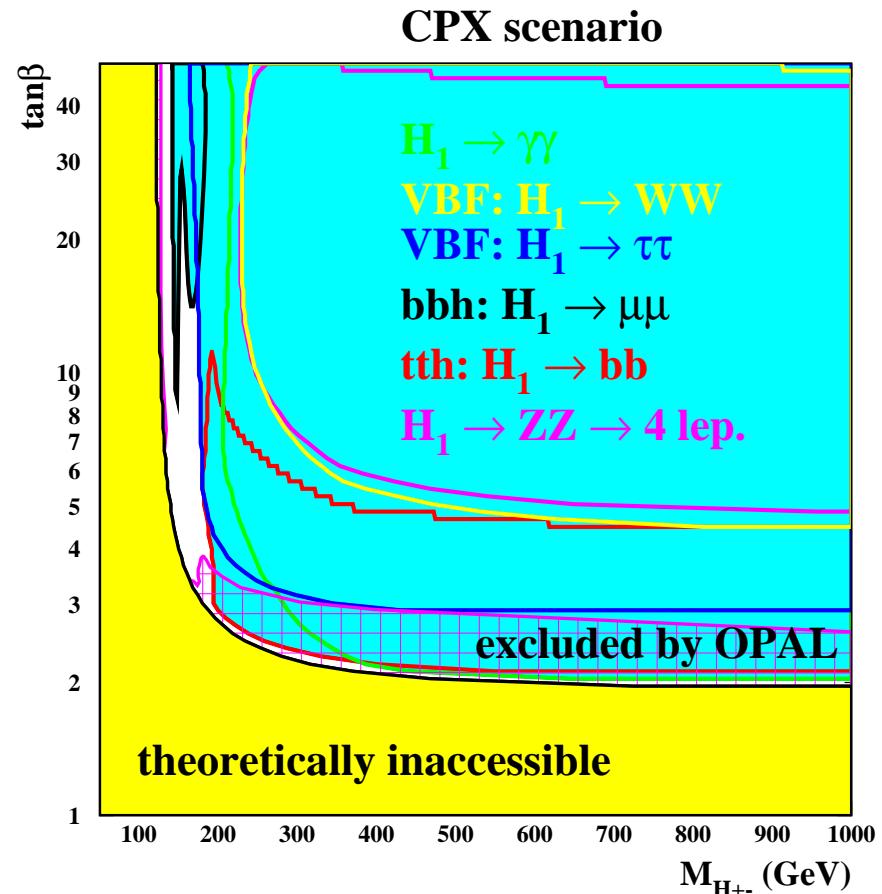
All Higgses escape detection

Still, there is the possibility

$t \rightarrow H^+ b$  with  $H^+ \rightarrow h W^*$

(Godbole, Guchait, Roy).

M. Schumacher →



Regions of MSSM parameter space not covered by ATLAS/CMS:  
more work is still needed....

## 7. Higgs in non minimal scenarios: the NMSSM

The next-to-minimal SSM is becoming the “standard” MSSM these days..

MSSM problem:  $\mu$  is SUSY-preserving but  $\mathcal{O}(M_Z)$ ; a priori no reason

Solution,  $\mu$  related to the vev of singlet field,  $\langle S \rangle \propto \mu$  Kim+Nilles

NMSSM: introduce a gauge singlet in Superpotential:  $\lambda \hat{H}_1 \hat{H}_2 \hat{S} + \frac{1}{3} \hat{S}$

Nilles et al, Frere et al, Ellis et al, Drees, Ellwanger et al, King et al, ...

SUSY spectrum extended by  $\chi_5^0$  and two neutral Higgs particles  $h_3, a_2$

- additional parameters enter in Higgs masses and couplings
  - less constrained model, more flexibility, ....
- the bound on lightest Higgs boson mass is higher than in MSSM
  - less fine-tuning is needed to cope with LEP..
- possibility of a light Higgs which has escaped detection at LEP2
  - possibility of a light Higgs which has escaped detection at LEP2
    - rich phenomenology: low energy constraints, DM, ....
- Note: constrained NMSSM, less freedom than in mSUGRA ...

## 7. Higgs in non minimal scenarios: the NMSSM

The NMSSM with universal boundary conditions at GUT scale:

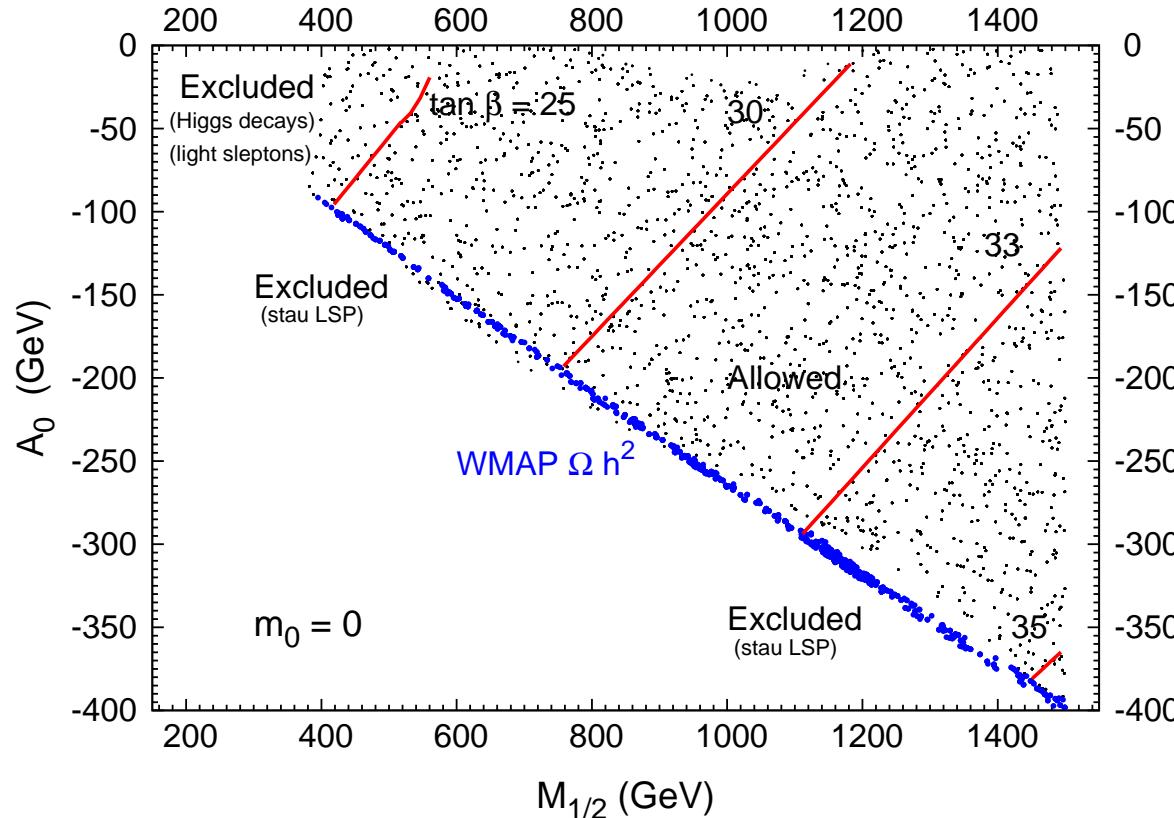
In principle:  $M_{1/2}$ ,  $m_0$ ,  $A_0$ ,  $\lambda$ ,  $\tan \beta$  as free parameters

With constraints: proper EWSB+LEP Higgs+low energy+ WMAP

only one cNMSSM free parameter:  $m_0 \sim 0$  and  $\lambda \lesssim 0.01$

The parameters  $A_0$  and  $\tan \beta$  are related to  $M_{1/2}$

Ellwanger,  
Teixeira,  
AD (2008)

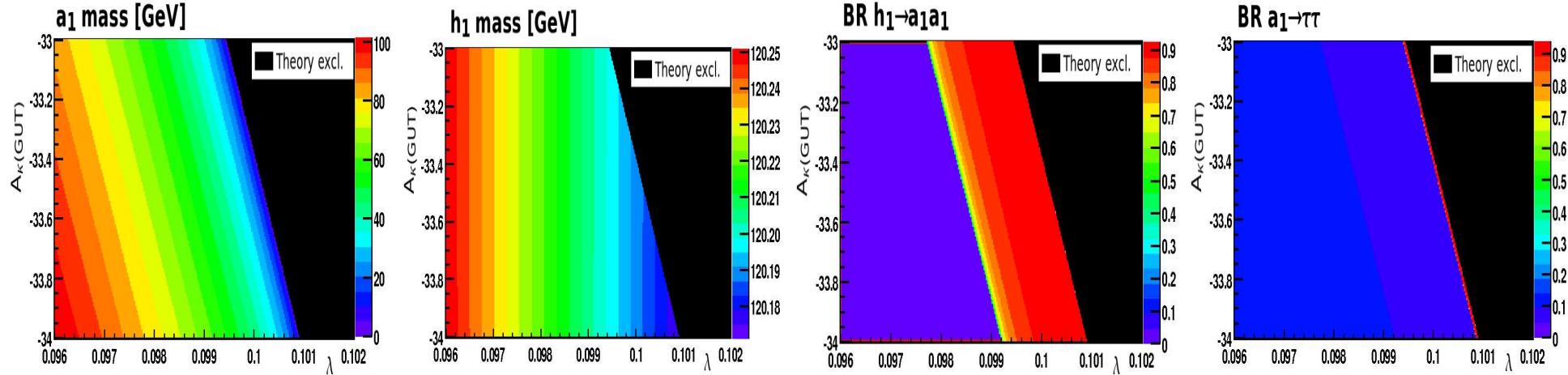


## 4. Production in NMSSM

But life can be even more complicated with LHC Higgs searches:

the possibility of missing all Higgs bosons is not yet ruled out!

(Ellwanger, Hugonie, Gunion, Moretti; King..., Nevzorov..., Barger...)



Recently, some benchmark scenarios for NMSSM Higgs searches have been proposed: AD, Drees, Rottlander, M. Schumacher, et al., ....

- **$h_1$  is SM-like and  $a_1$  light:**  $h_1 \rightarrow a_1 a_1$  with  $a_1 \rightarrow b\bar{b}$  and/or  $\tau^+ \tau^-$
- **$h_2$  is SM-like and  $h_1$  light:**  $h_2 \rightarrow h_1 h_1$  with  $h_1 \rightarrow b\bar{b}$
- **All Higgs are light (NMSSM ICR): reduced couplings to VV, etc...**

## 7. Higgs in non minimal scenarios: NMSSM

Higgs → Higgs+Higgs → 4b, 2b2 $\tau$

searches very difficult at the LHC:

$pp \rightarrow qq \rightarrow W^*W^*qq \rightarrow h_1qq$

—  $h_1 \rightarrow a_1a_1 \rightarrow b\bar{b}\tau\tau \times 500$ .

— total background.

(Ellwanger..., Baffioni+D.Zerwas)

Higgs → Higgs+Higgs → 4 $\tau$  → 4 $\ell$ X

also difficult but detection possible

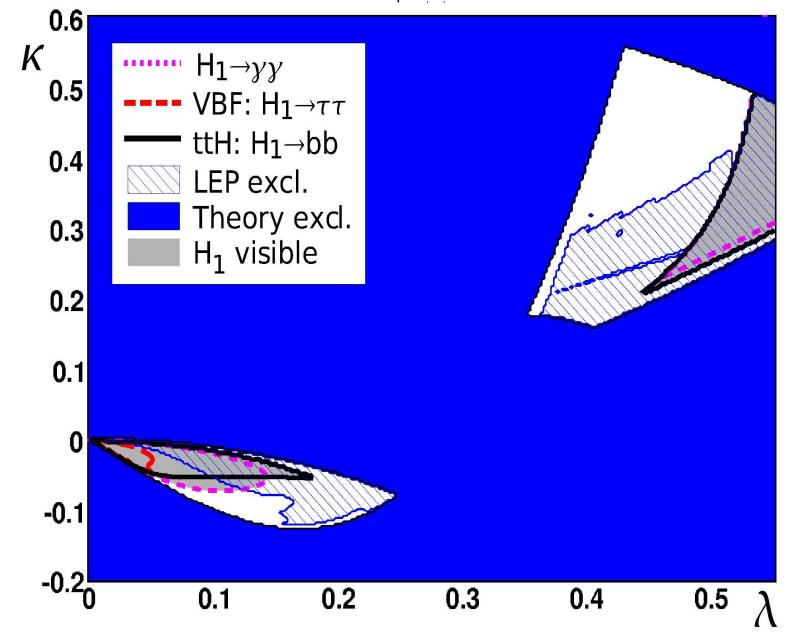
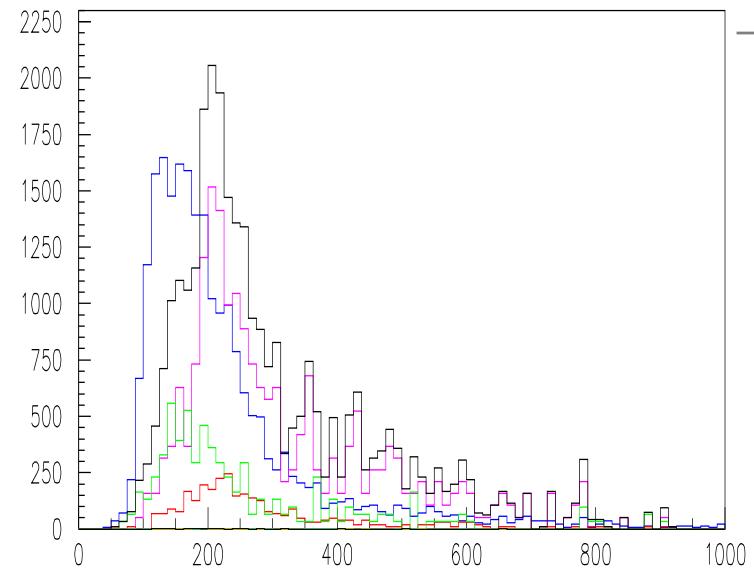
(Nikitenko .., Schumacher+Rottlander)

Example of scan for light  $h_1$

using VBF + all  $h_1$  decay channels

(same for all Higgsses can be done)

(Schumacher+Rottlander)

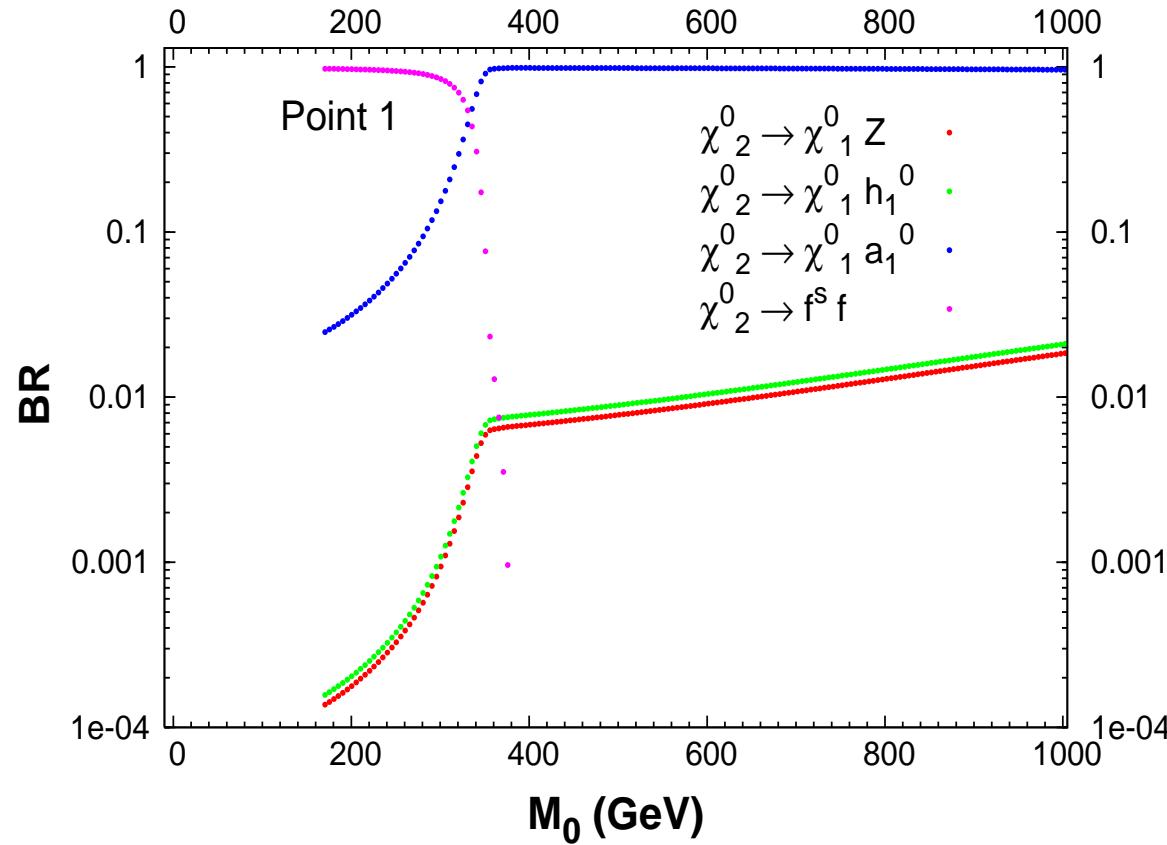


## 7. Higgs in non minimal scenarios

A possible rescue in both the CPV MSSM and NMSSM might come from SUSY particle cascade decays into Higgs bosons. In particular:

$$pp \rightarrow \tilde{q}\tilde{q}, \tilde{g}\tilde{g}, \tilde{g}\tilde{q} \rightarrow \chi + X \text{ with } \chi_2^0 \rightarrow \chi_1^0 + \text{Higgs}$$

Example for one of the NMSSM benchmark points with light  $a_1$ :



Ellwanger ea

## 7. Invisible Higgs??

There are many scenarios in which a Higgs boson would decay invisibly

- In MSSM, Higgs  $\rightarrow \chi_1^0 \chi_1^0, \tilde{\nu} \tilde{\nu}$ , etc.. as already discussed.
- In MSSM with  $R_p$ : Higgs  $\rightarrow J J$  could be dominant. Valle ea
- The SM when minimally extended to contain a singlet field (which decouples from f/V),  $H \rightarrow S S$  can be dominant Bij, Wells ea,..
- In large extra dimensions H mixing with graviscalars. Gunion ea

... or very different couplings to fermions and bosons...

- Radion mixing in warped extra dimension models: suppressed f/V couplings and Higgs decays to radions Hewett+ Rizzo, Gunion ea
- Presence of new quarks which alter production Moreau ea

... Many possible surprises/difficult scenarios.....