

**The 2nd Symposium on  
Neutrinos and Dark Matter in Nuclear Physics**  
*Paris, September 3-9, 2006*

# **Neutrino and Weak Processes in Astro-Nuclear Physics**

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University of Tokyo**

# OUTLINE

- **Neutrino Oscillations:**

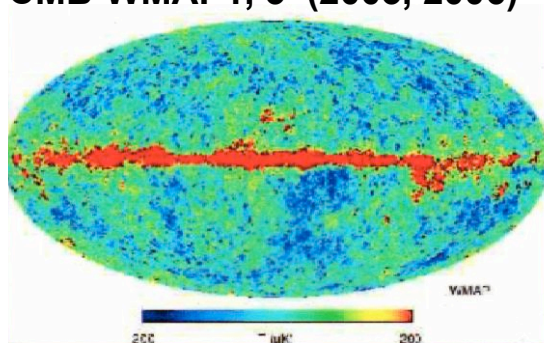
How to determine  $\theta_{13}$  and mass hierarchy **ASTROPHYSICALLY ?**

- **Ultra High-Energy Cosmic Rays (UHECRs) = most likely neutral:**

If neutrinos, what is their **COSMOLOGICAL ORIGIN ?**

- **Cosmological WMAP-1 & 3 data of CMB-Anisotropies:**

CMB-WMAP1, 3 (2003, 2006)



$$\Omega_\nu < 0.022 \quad (95\% \text{ C.L.})$$

Spergel, et al., ApJ (2006), astro-ph/0603449

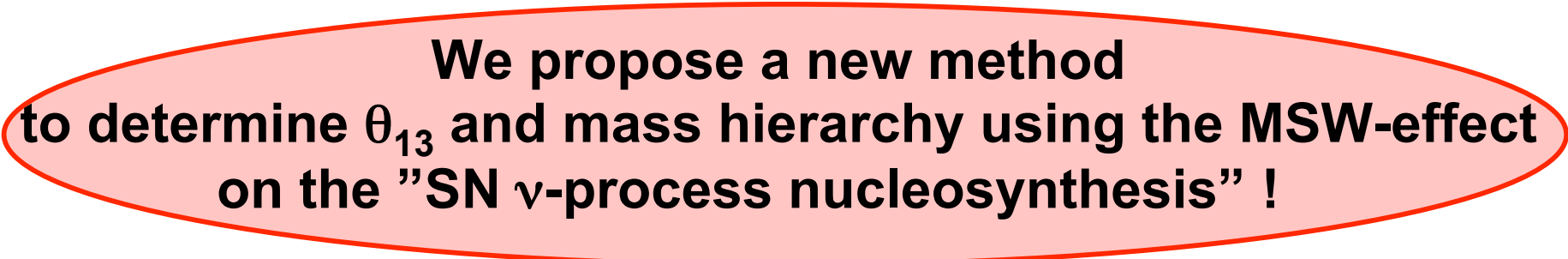
Fukugita, et al., PR D74 (2006), 027302



What is CDM,  $\Omega_{\text{CDM}} = 0.26$ , and what is DARK ENERGY,  $\Omega_\Lambda = 0.7$  ?



**We detected  $\nu$ 's, then NEUTRON STAR once formed in SN1987A !**



**We propose a new method to determine  $\theta_{13}$  and mass hierarchy using the MSW-effect on the "SN  $\nu$ -process nucleosynthesis" !**

Yoshida, Kajino, Yokomakura, Kimura, Takamura, & Hartmann,  
Phys. Rev. Lett. 96 (2006), 091101.

$$\sin^2 2\theta_{12} = 0.816, \quad \sin^2 2\theta_{23} = 1.0, \quad \sin^2 2\theta_{13} < 0.1 ?$$

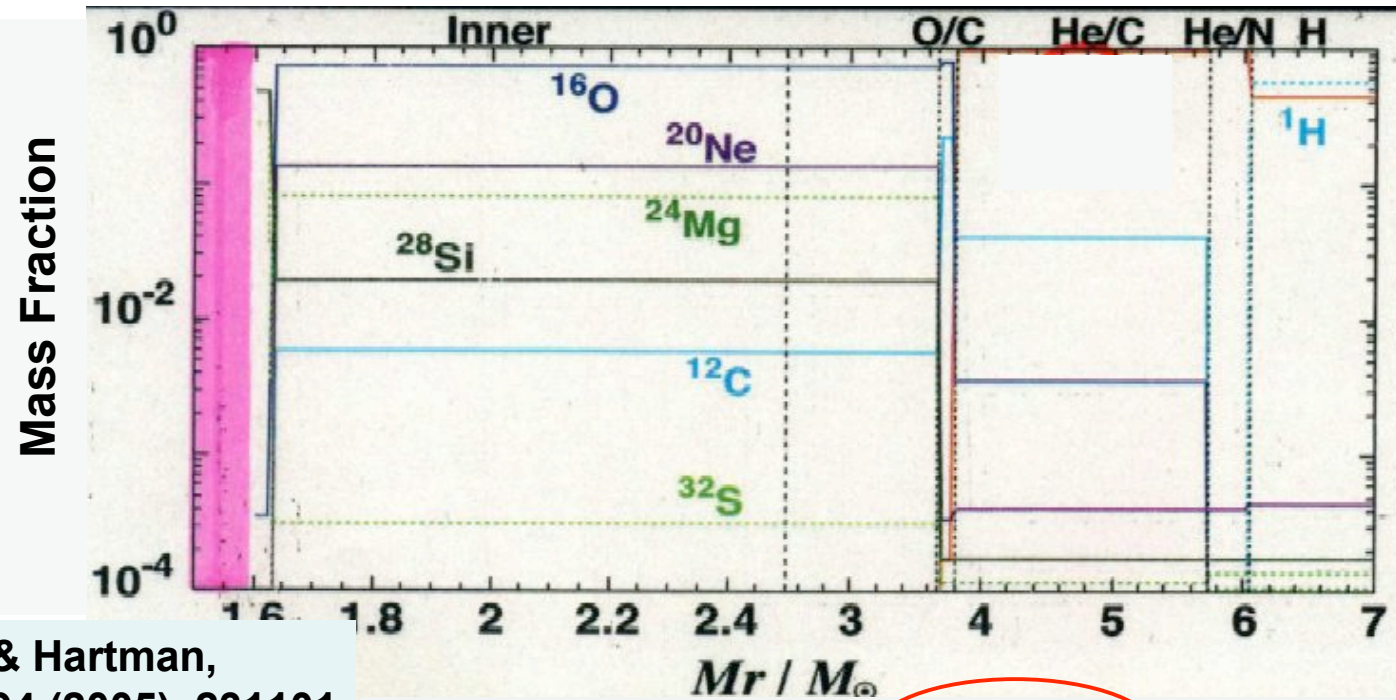
$$\Delta m_{21}^2 = 7.9 \times 10^{-5} \text{ eV}^2, \quad |\Delta m_{13}^2| = 2.4 \times 10^{-3} \text{ eV}^2 ?$$

**SK, SNO, KamLand + Many Experiments**



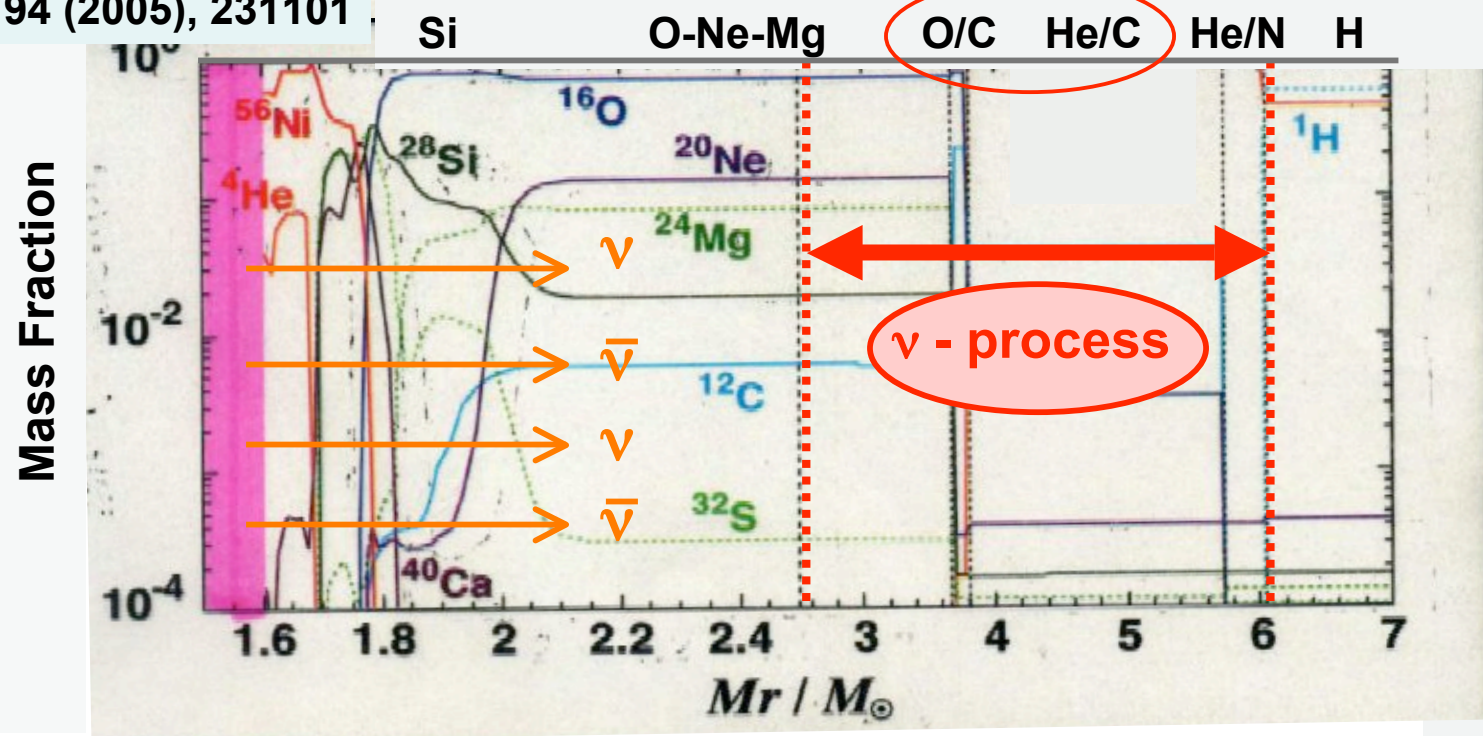
**How important is the  $\nu$ -OSCILLATION (MSW) EFFECT in the outer layers of SN explosions ?**

Before  
Explosion



Yoshida, Kajino & Hartman,  
Phys. Rev. Lett. 94 (2005), 231101

After  
Explosion  
( $\sim 10$  s)

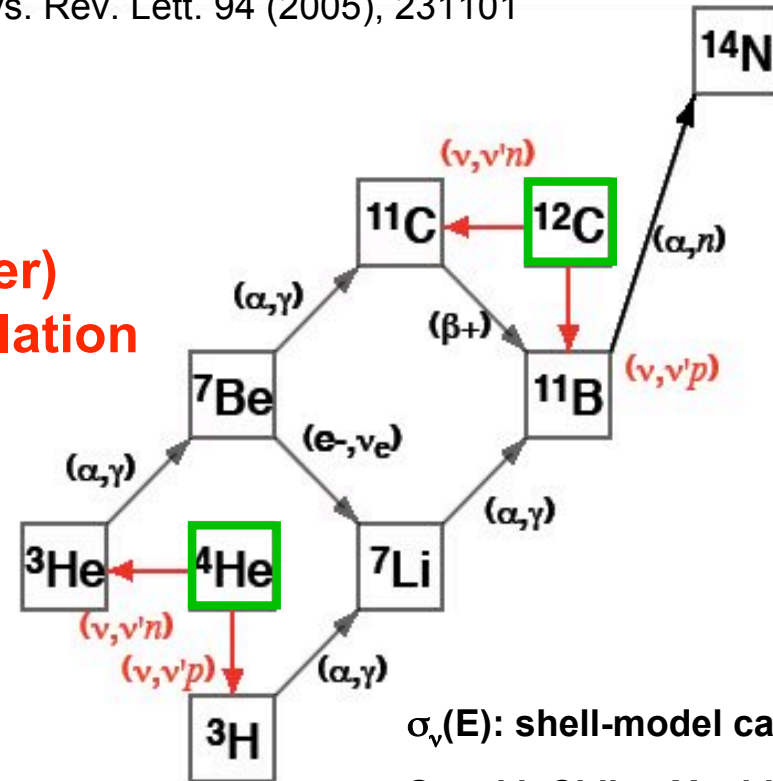
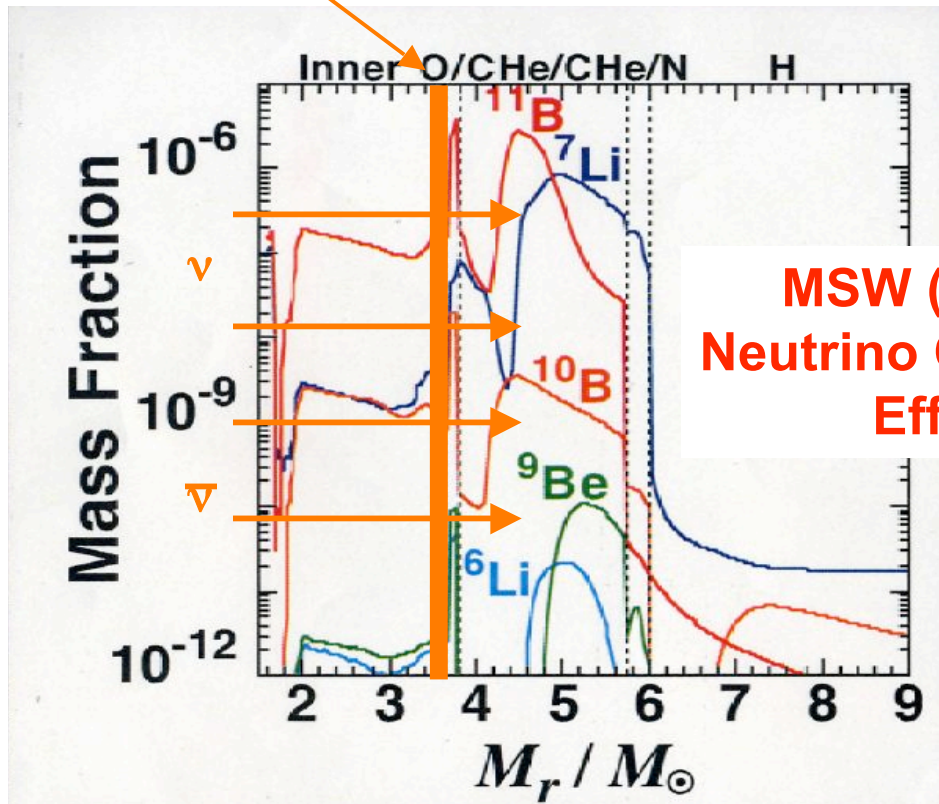




# Supernova $\nu$ -Process & Key Reactions

H-Resonance

Yoshida, Kajino & Hartman,  
Phys. Rev. Lett. 94 (2005), 231101

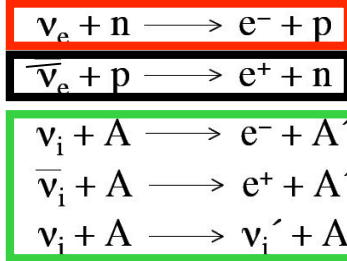
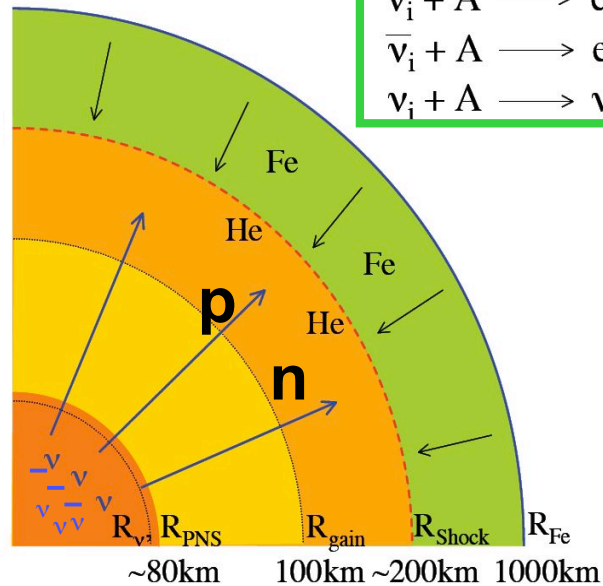


+ Neutrino Oscillation

$$\nu_{\mu\tau}(\bar{\nu}_{\mu\tau}) \longleftrightarrow \nu_e(\bar{\nu}_e)$$



## Collapsing Iron-Core

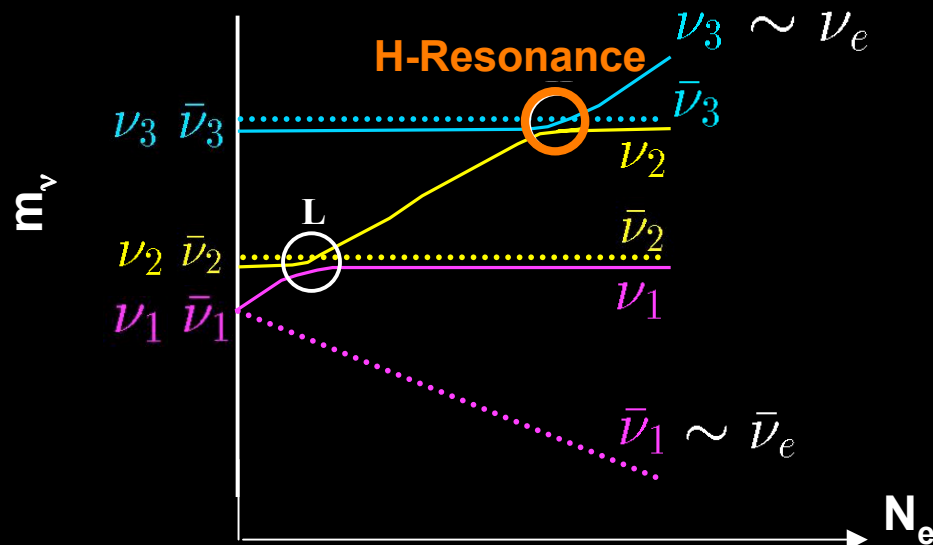


KEY of our  
“NUCLEOSYNTHESIS PROPOSAL”  
is to use the ENERGY HIERARCHY of  
SUPRENOVA  $\nu$ 's.

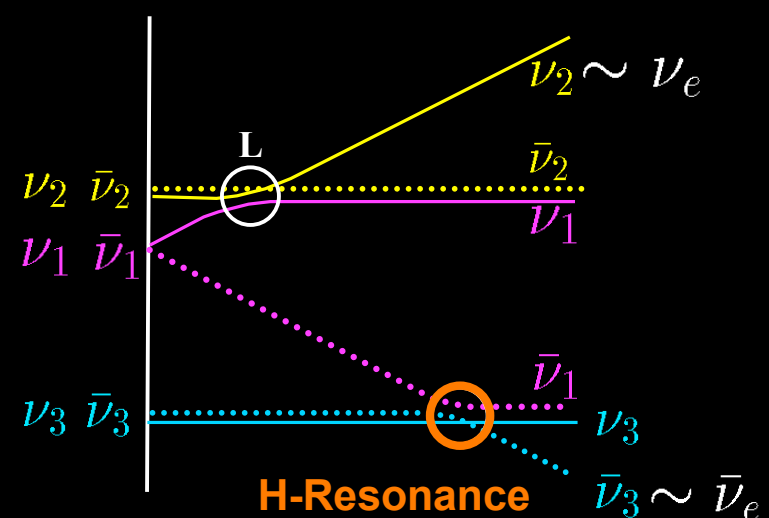
## ENERGY HIERARCHY

$$\begin{aligned} E_{\nu_e} &< E_{\bar{\nu}_e} < E_{\nu_{\mu\tau}, \bar{\nu}_{\mu\tau}} \\ \parallel &\parallel &\parallel \\ 12\text{MeV} &20\text{MeV} &24\text{MeV} \end{aligned}$$

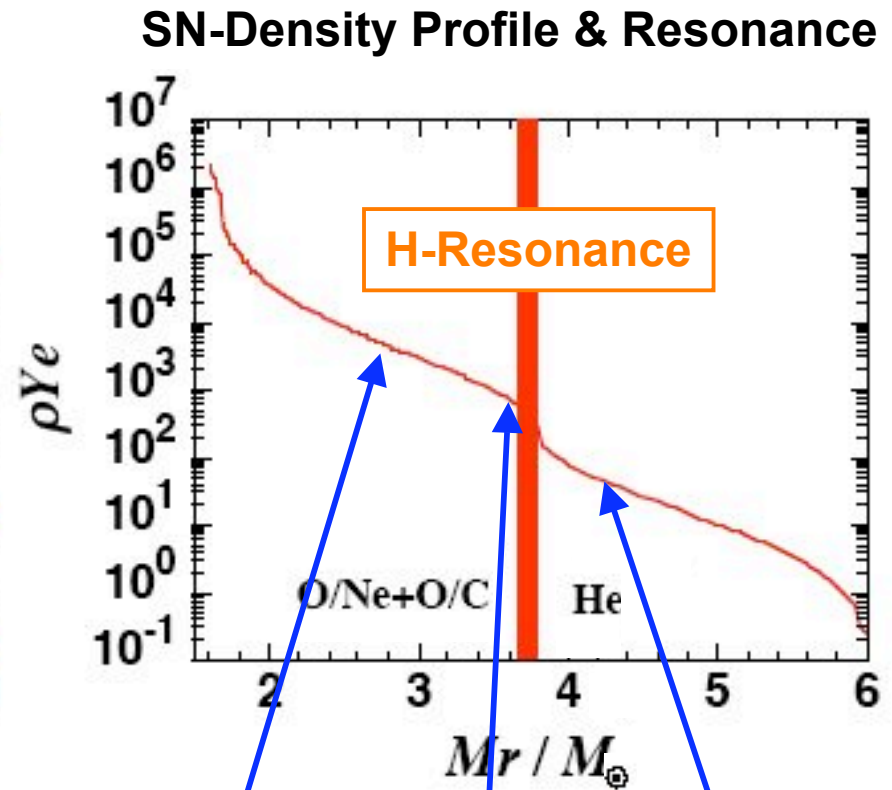
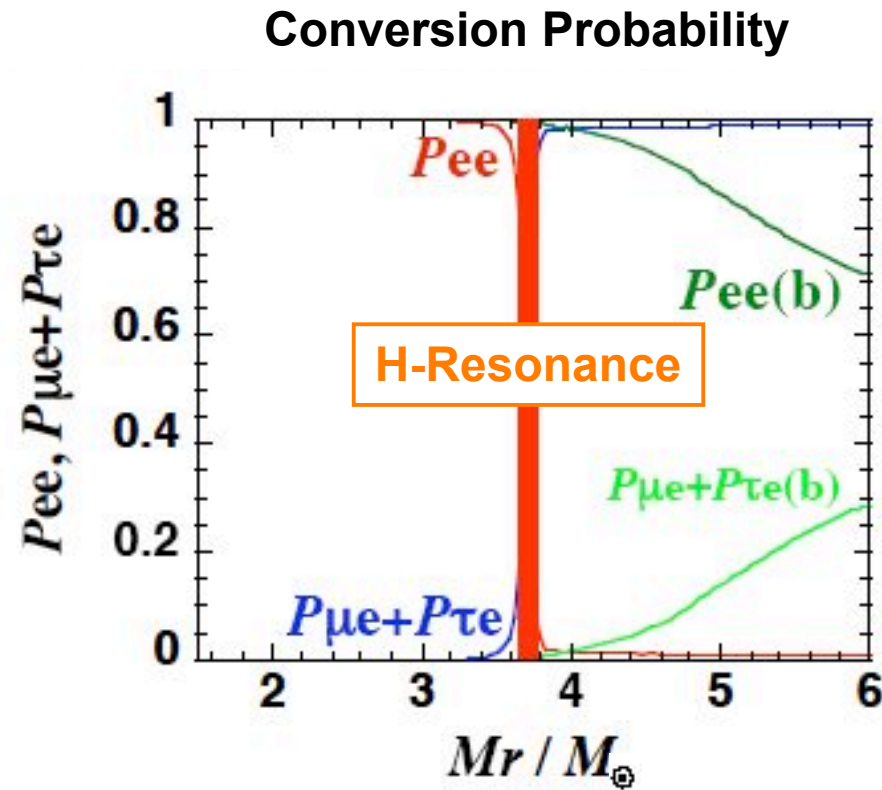
## Normal



## Inverted



# SN-Neutrino Oscillation (MSW) Effect on $\nu$ -Process

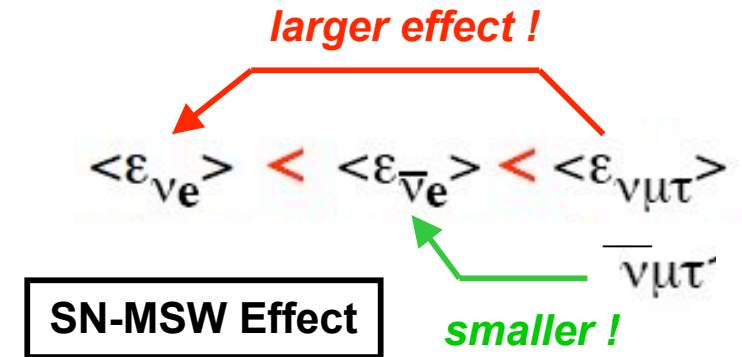
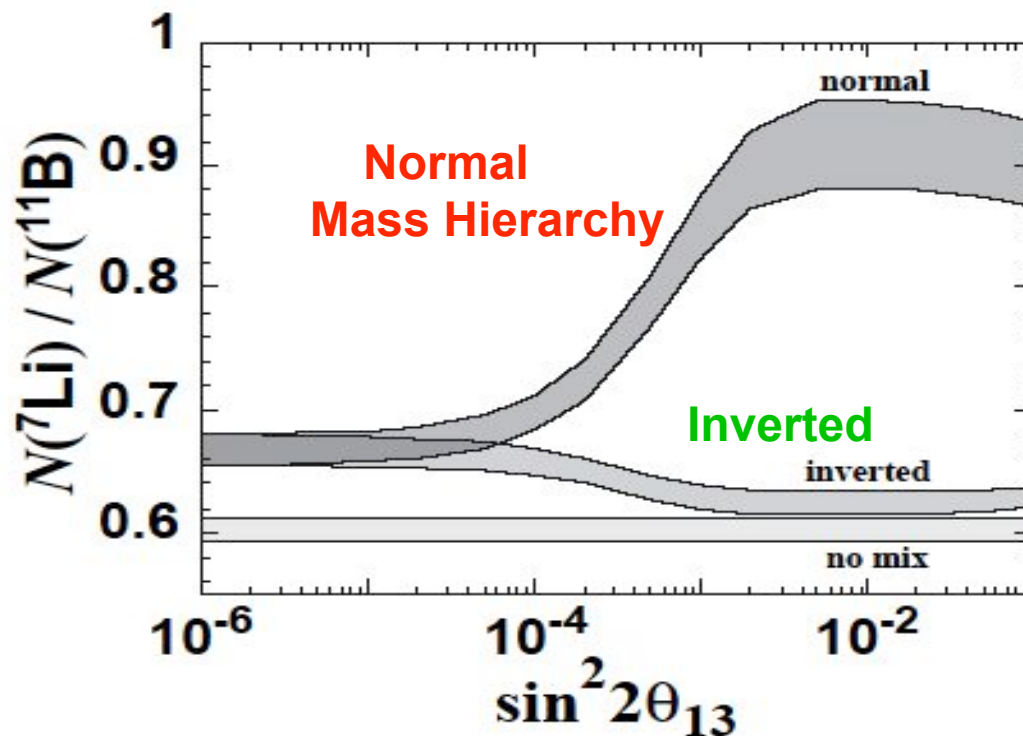
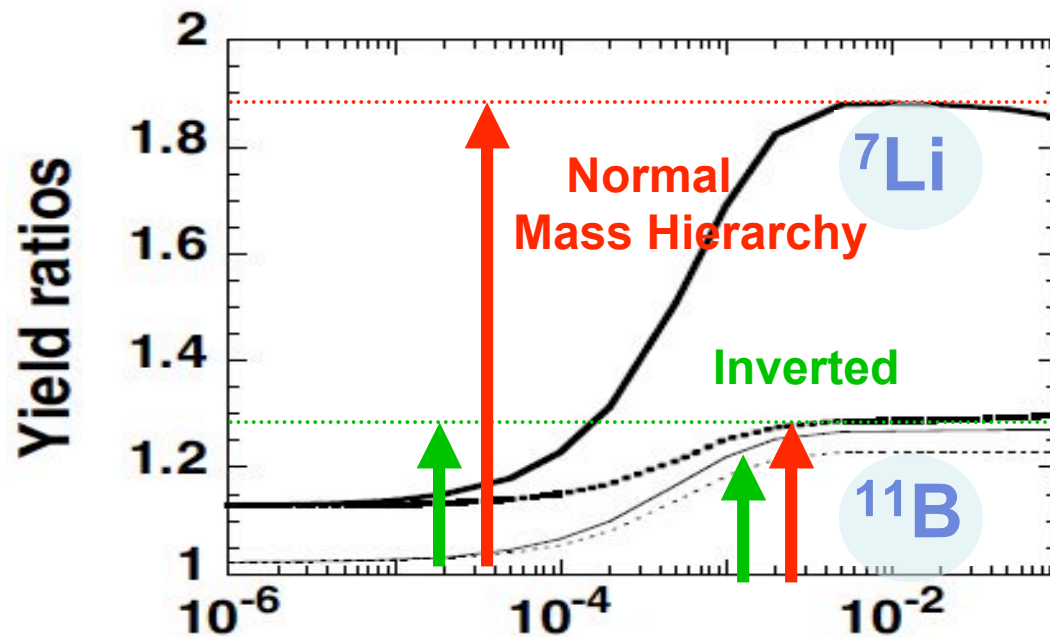


Parameters:  $25M_{\text{solar}}$  SN model (Nomoto)

$$\sin^2 2\theta_{13} = 0.04$$

$$\Delta m_{13}^2 = 2.4 \times 10^{-3} \text{eV}^2 \quad \text{normal}$$

$$E_{\nu e} = 12 \text{MeV}, E_{\bar{\nu} e} = 20 \text{MeV}, E_{\nu \mu \tau, \bar{\nu} \mu \tau} = 24 \text{MeV}$$



We propose a detection of  $^7\text{Li}/^{11}\text{B}$ -abundance ratio in

- Supernova Remnants,
- Meteorites (presolar grains) of almost pure Supernova origin.

Present Observation:

$$(^7\text{Li}/^{11}\text{B})_{\text{METEO}} = 7.5$$

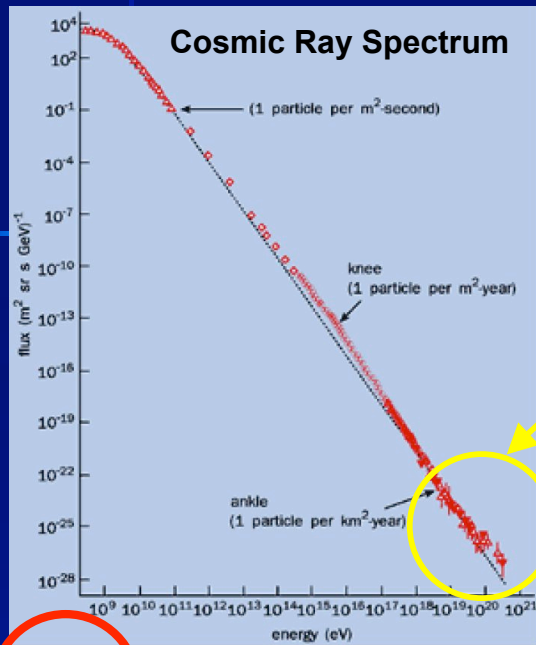
$$(^7\text{Li}/^{11}\text{B})_{\text{SN-}\nu} = ? \text{ (to come)}$$

$$(^7\text{Li}/^{11}\text{B})_{\text{GCR}} = 0.5$$

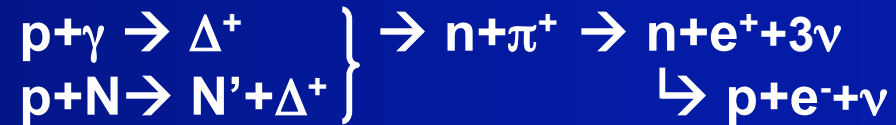
Yoshida, Kajino, Yokomakura, Kimura, Takamura, & Hartmann, PRL 96 (2006) 091101.



# High Energy Neutrinos from GRBs

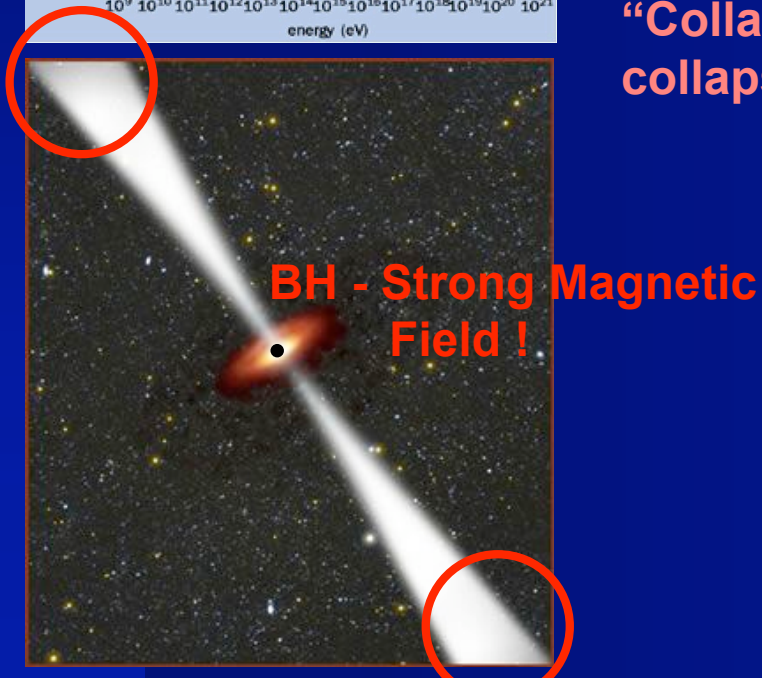


$\nu$ 's, neutral particles, are a candidate for UHECRs, and **GZK- $\nu$ 's** or **extra-Galactic  $\nu$ 's** from **GRBs** have ever been studied.



Central engine of the GRB is still unknown.

“Collapsar” is a viable candidate, which is a core-collapse supernova associated with **BH** formation.



**PROPOSE:-**

UHE- $\nu$ 's are produced by decays of Heavy-Meson Synchrotron Emission.

UHECR  $\otimes$  Strong Magnetic Field in GRBs !

Tokuhsa, Kajino, Ichiki, Famiano & Mathews (2006)

# Theory of Meson Synchrotron Emission

Ginzburg & Syrovatskii (1965), Peskin & Schroeder (1995), Tokuhiisa & Kajino (1999) ApJ 525, L117

$$\mathcal{L} = \frac{1}{2} \{ (\partial_\mu \phi_\pi)^2 - m_\pi^2 \phi_\pi^2 \} + j(x) \phi_\pi(x)$$

$\Phi_\pi$  = 2nd Quantized Meson ( $\pi$ ) Field

$$\hat{\Phi}_\pi = \hat{\Phi}_\pi^{(0)} + i \int d^4 y D_R(x-y) j(y)$$

$$D_R(x-y) \equiv \theta(x^0 - y^0) \int \frac{d^3 p}{(2\pi)^3} \frac{1}{2E_p} \left( e^{-ip \cdot (x-y)} - e^{ip \cdot (x-y)} \right)$$

$j(x)$  = Proton Current in Strong Magnetic Field

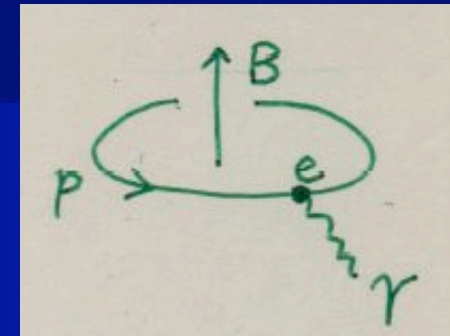
$$j(x) = \sqrt{4\pi} g \sqrt{1-\beta^2} \delta(x - x_0(t))$$

Meson Emission Intensity

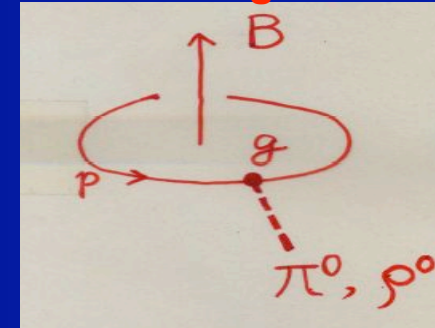
$$\frac{dI_\pi}{dE_\pi} = \frac{g^2}{\sqrt{3}\pi} \frac{E_\pi}{\hbar^2 c} \frac{1}{r_p^2} \int_0^\infty y(x) K_{1/3}(\eta) d\eta$$

$$y(x) = \frac{2}{3} \frac{m_\pi}{m_p} \frac{1}{\chi} \cdot x \cdot \left( 1 + \frac{1}{x^2} \right)^{3/2}$$

Photon Synchrotron.  
Emission  $e^2 := 1$



Meson Synchrotron  
Emission  $g^2 := 1000$



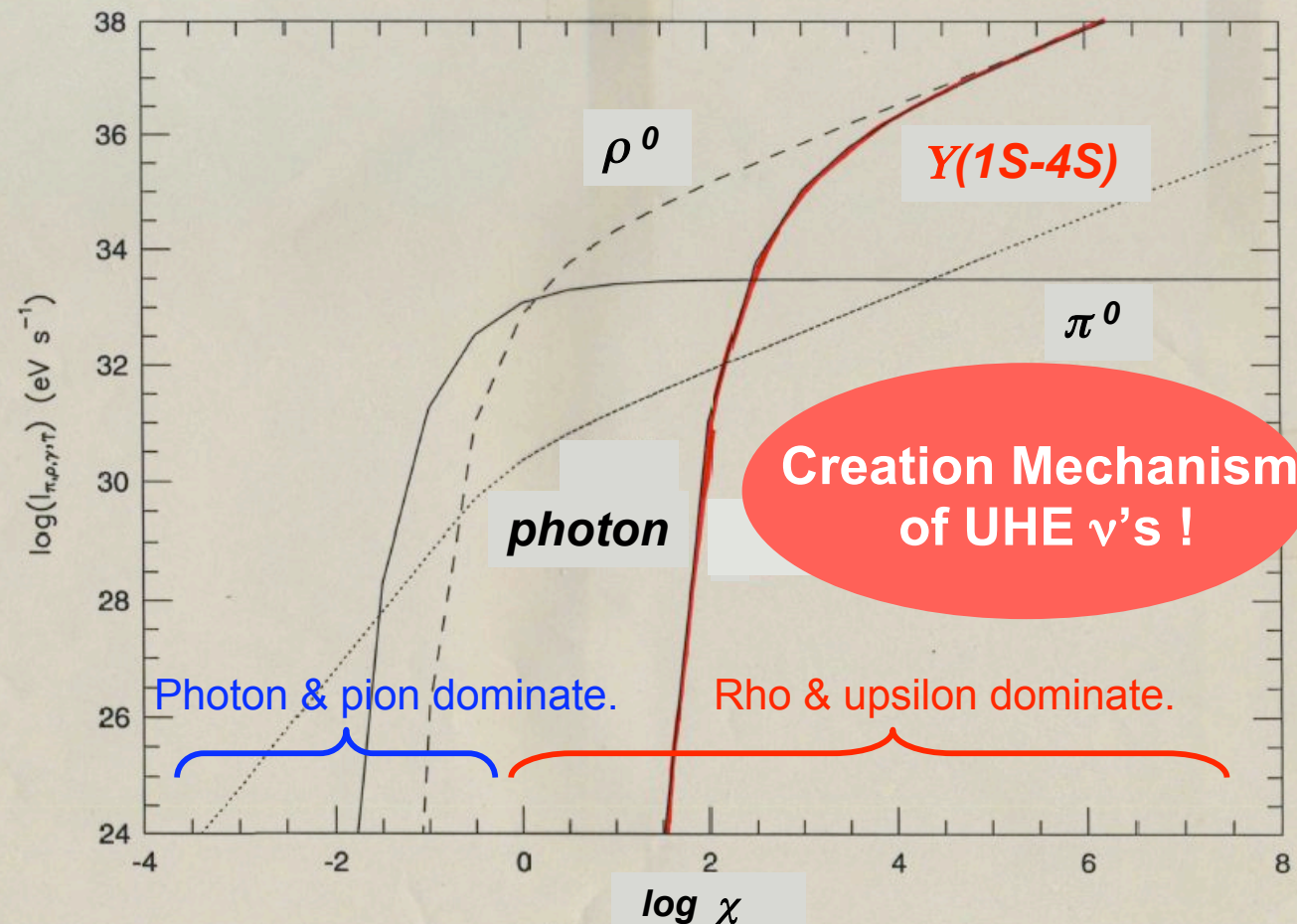
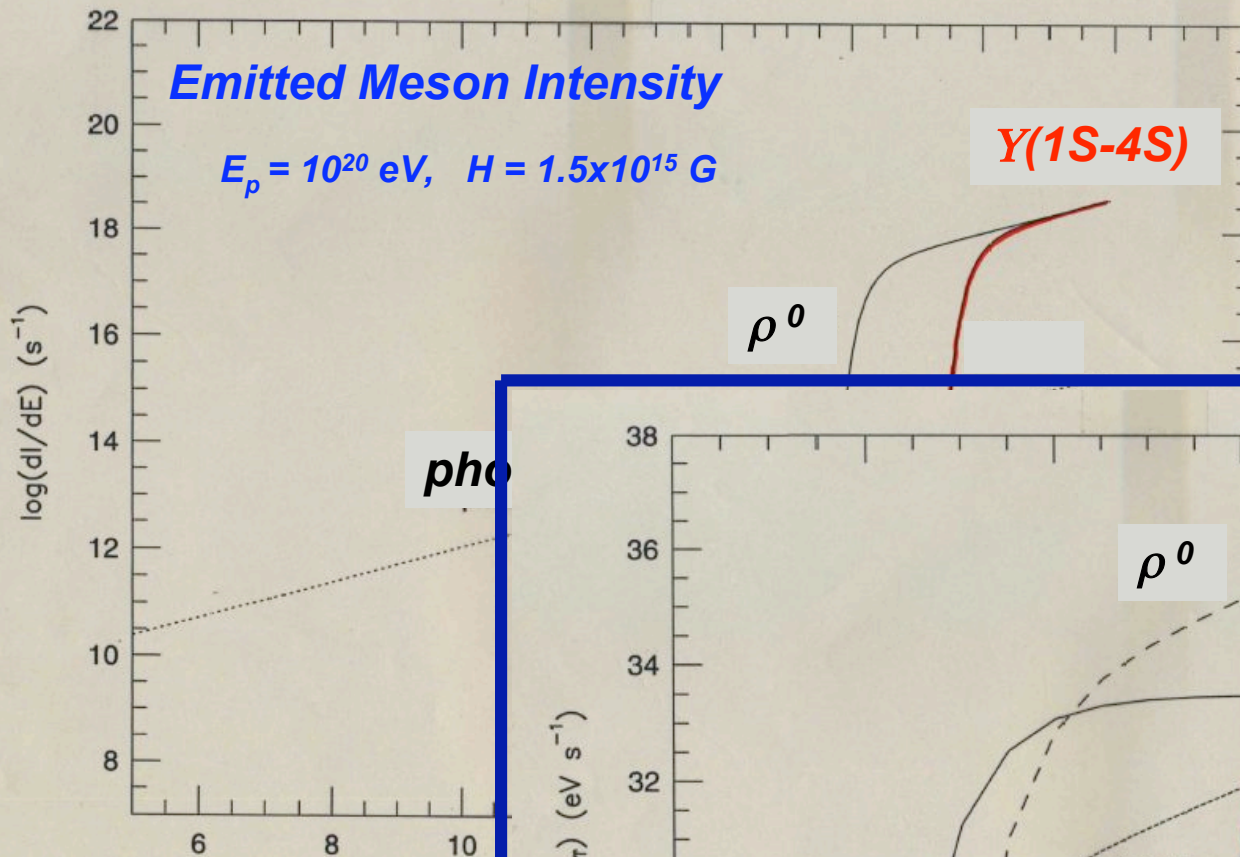
Lorentz factor      magnetic field

$$\chi = \gamma_p \cdot \frac{H}{H_0}$$

$$H_0 = \frac{m_p^2 c^3}{e \hbar} = 1.5 \times 10^{20} \text{ G}$$

Tokuhsa & Kajino (1999)  
ApJ 525, L117

Tokuhsa, Kajino, Ichiki,  
Famiano & Mathews  
(2006)



Lorentz factor      magnetic field

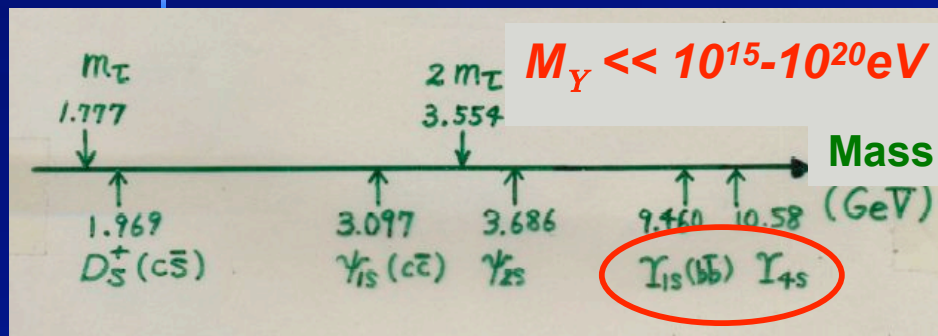
$$\chi = \gamma_p \cdot \frac{H}{H_0}$$

$$H_0 = \frac{m_p^2 c^3}{e \hbar} = 1.5 \times 10^{20} \text{ G}$$



# Three generations of quarks & leptons

$$\begin{matrix} u & c & t \\ d & s & b \end{matrix} \longleftrightarrow \begin{matrix} e & \mu & \tau \\ \nu_e & \nu_\mu & \nu_\tau \end{matrix}$$



$$Y(1S-4S) = b\bar{b}$$

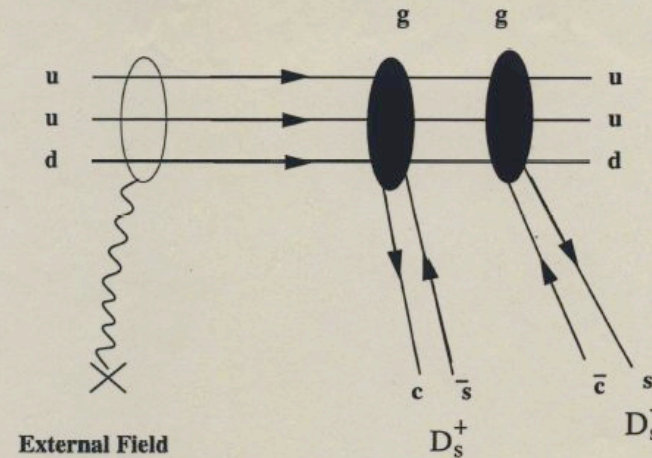
**Upsilon**, a neutral vector meson, is a heavy quarkonium which can decay to lepton pairs:

$$Y(1S-4S) \longrightarrow e^{+-} \mu^{+-} \tau^{+-}$$

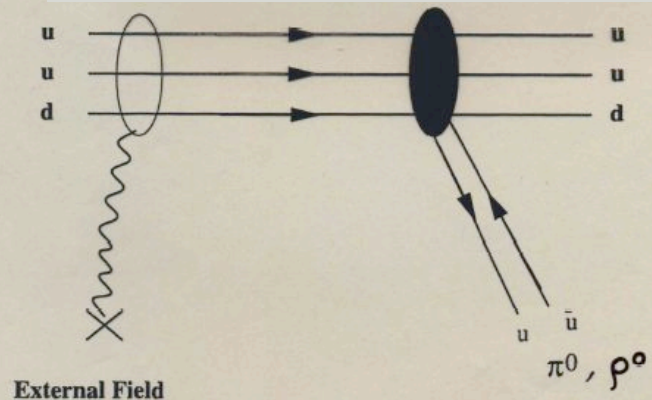
$$\mu^{+-} (2.2 \times 10^{-6} \text{ s}) \text{ Large E.-Loss} \longrightarrow \nu_\mu$$

$$\tau^{+-} (2.9 \times 10^{-13} \text{ s}) \longrightarrow \nu_\tau \text{ \& } \nu_\mu$$

Waxman & Bahcall (1997)

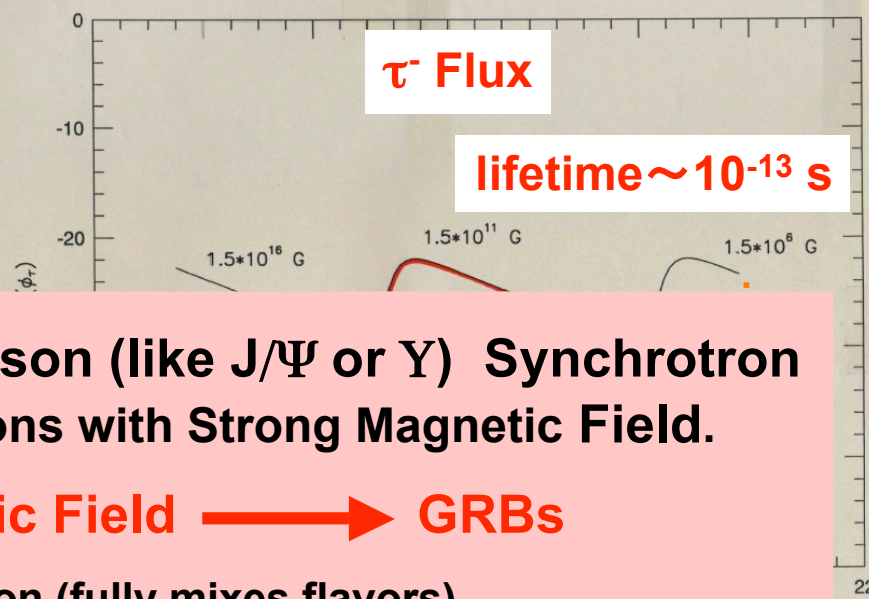
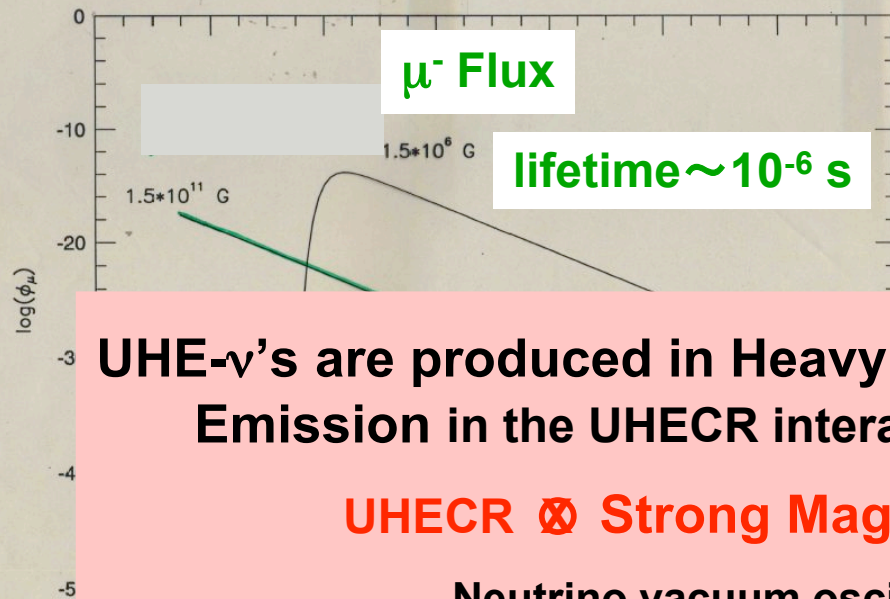


Tokuhisa, Kajino, Ichiki, Famiano & Mathews (2006)



$\pi^0, \rho^0$   
 $b \bar{b}$   
**HEAVY MESON  $\Upsilon$**   
**: DECAYS TO  $e^\pm, \mu^\pm, \tau^\pm$**





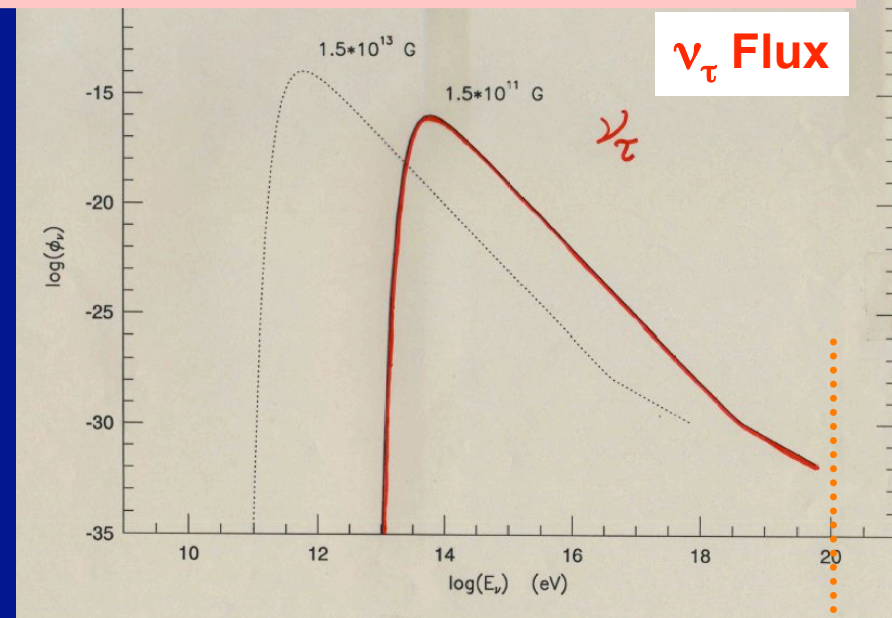
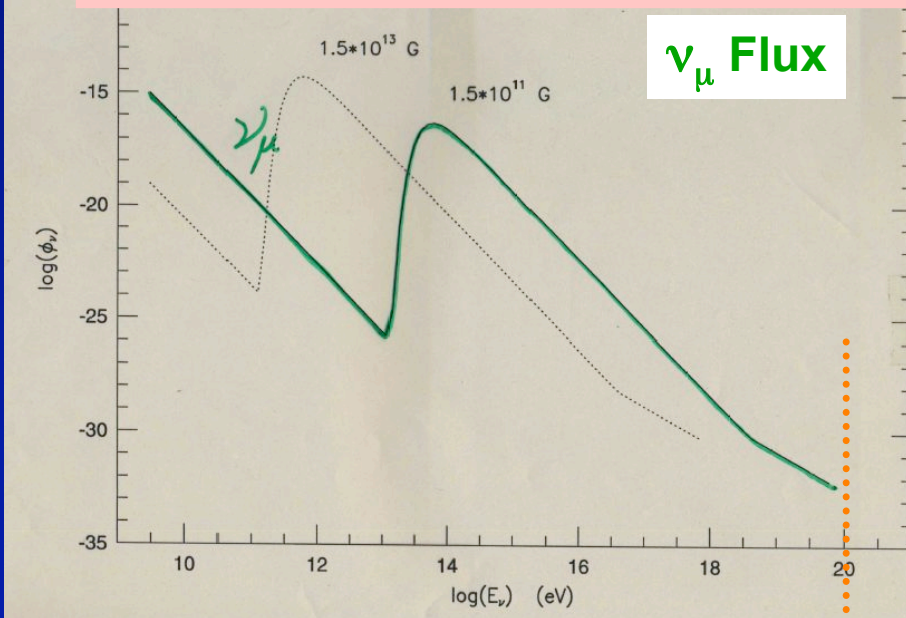
**UHE- $\nu$ 's are produced in Heavy-Meson (like  $J/\Psi$  or  $Y$ ) Synchrotron Emission in the UHECR interactions with Strong Magnetic Field.**

**UHECR  $\otimes$  Strong Magnetic Field  $\longrightarrow$  GRBs**

**Neutrino vacuum oscillation (fully mixes flavors)**

**Structure function of mesons**

**Realistic neutrino energy spectrum**

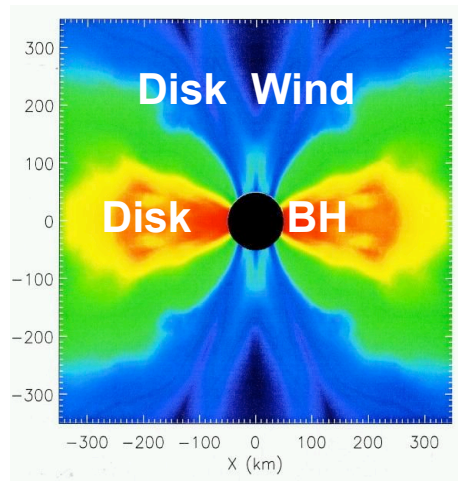


**“Collapsar”, a first generation star, should have affected metal-poor Pop. II stars.**

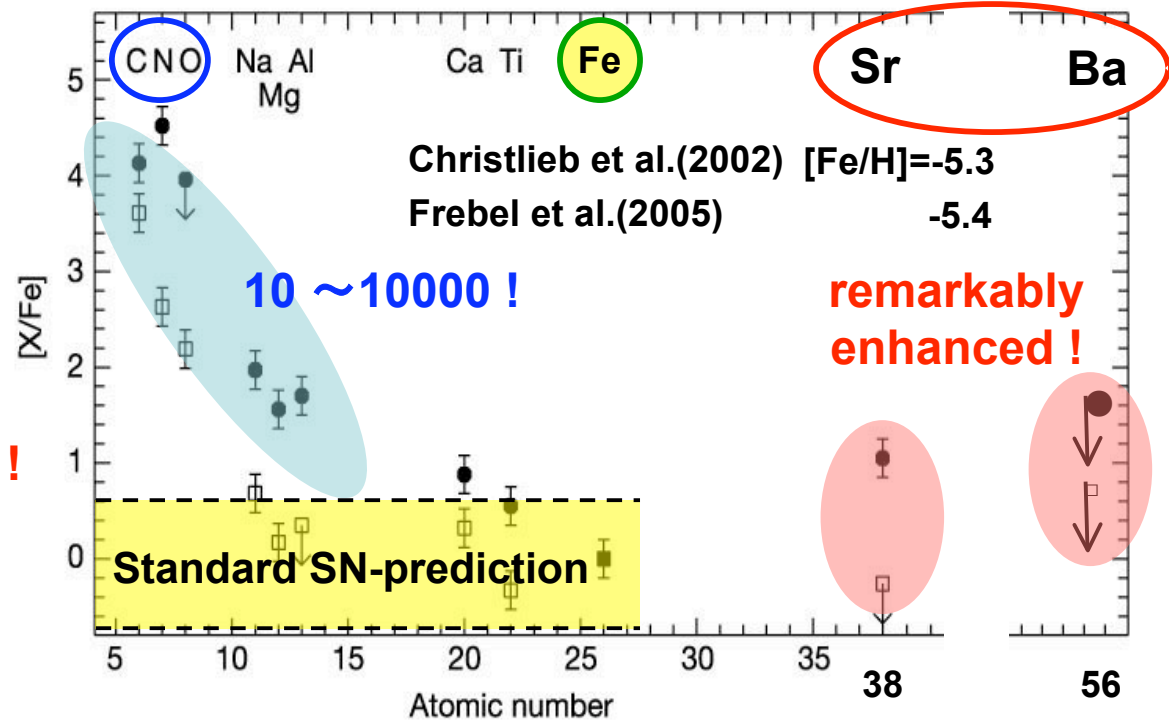
SUBARU TELESCOPE discovered an **oldest Pop. II star** in the Milky Way:  $[\text{Fe}/\text{H}] = -5.4$  (Nature, 2005)!



**No  $\nu$ 's from central BH !**



**Supernova model fails !**



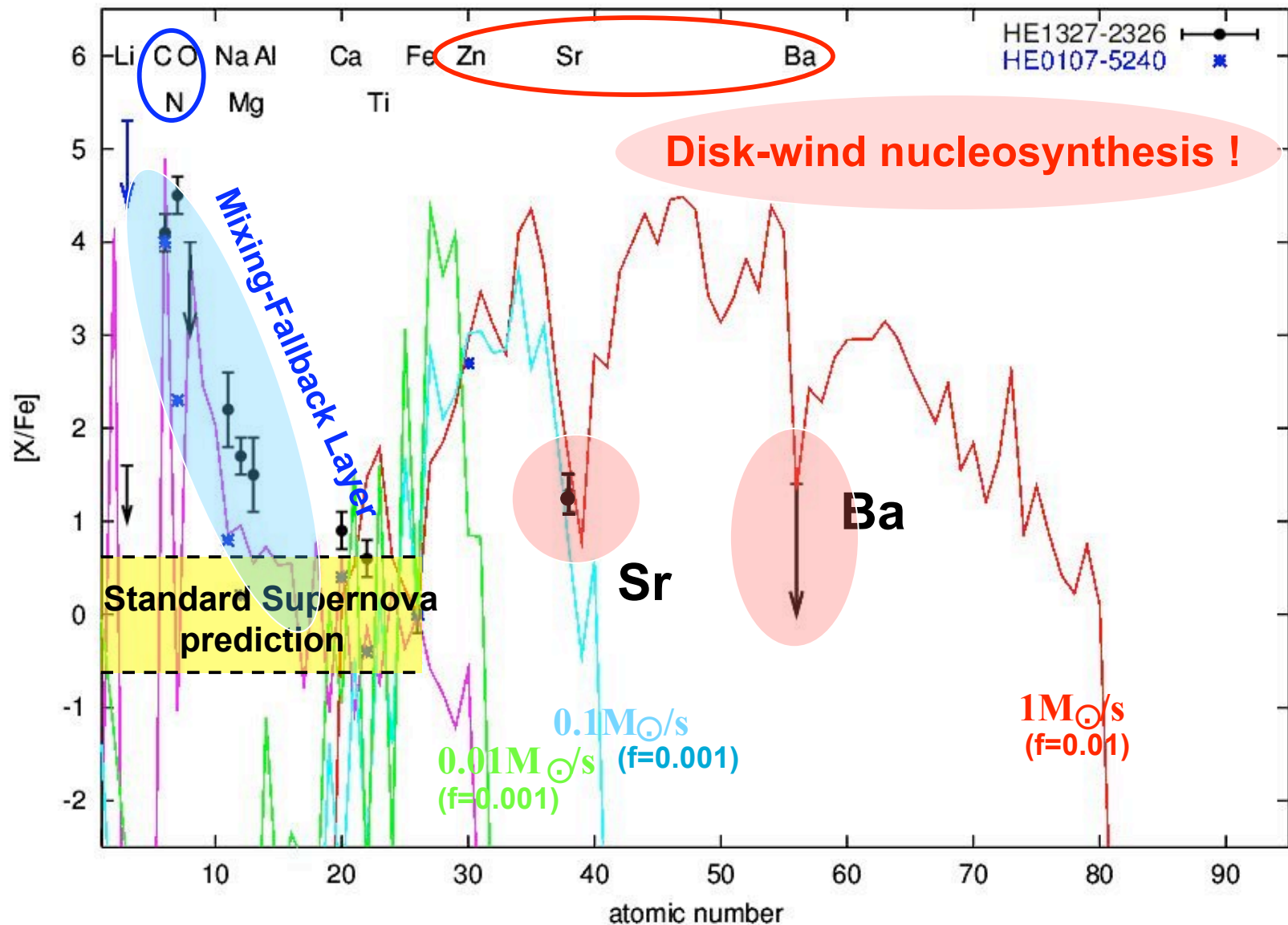
**Explosive outer layer  
Nucleosynthesis with  
Mixing-Fallback for BH  
Umeda & Nomoto (2003)**

**Disk-Wind nucleosynthesis  
of r-process !**

Sasaqui, Kajino et al. (2006)

# Calculated Result

Sasaqui, Kajino, Yoshida, Otsuki & Aoki (2006)



# OUTLINE

## ● Neutrino Oscillations:

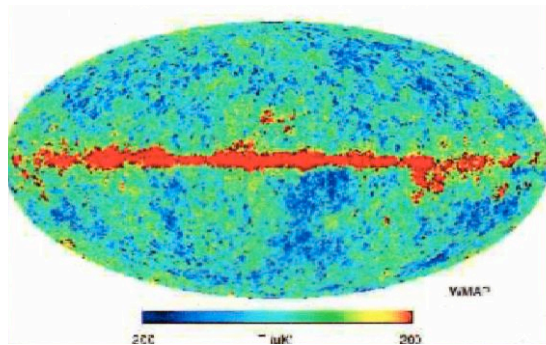
How to determine  $\theta_{13}$  and Mass Hierarchy astrophysically ?

## ● Ultra High-Energy Cosmic Rays (UHECRs) = most likely neutral:

If neutrinos, what is their cosmological origin ?

## ● Cosmological WMAP-1 & 3 data of CMB-Anisotropies:

WMAP1, 3 (2003, 2006)



Universe is likely flat and accelerating!

$$\Omega_B + \Omega_{\text{CDM}} + \Omega_\nu + \Omega_\Lambda = 1$$

$$\Sigma m_\nu < 2.0 \text{ eV (95\% C.L.)}$$

$$\Omega_\nu < 0.022 \text{ (95\% C.L.)}$$

Spergel, et al., ApJ (2006), astro-ph/0603449

Fukugita, et al., PR D74 (2006), 027302

**Fit to scalar + tensor fluctuations needs eleven parameters !**

Neutrino of  $\Omega_\nu < 0.02$ , a hot dark matter, is not a major part of dark matter  
 $\Omega_{\text{DM}} = 0.26$ . It should be cold.

**What is CDM,  $\Omega_{\text{CDM}} = 0.26$ , and what is DARK ENERGY,  $\Omega_\Lambda = 0.7$  ?**



We propose Exchanging-CDM Model in Brane World Cosmology.  
Is accelerating universe model with  $\Omega_\Lambda = 0$  possible ?

## Brane World Cosmology

Motivated by the D-brane solution  
in 10 dim STRING THEORY

Randall-Sundrum II; PRL 83 (1999)

The Universe is embedded  
in a 5 dim spacetime

Brane  
II

4D-Einstein Universe

CDM particles can flow in and  
out between brane and bulk !

CDM particles  
= Lightest SUSY Particles

Ichiki, Garnavich, Kajino, Mathews  
& Yahiro, PRD 68 (2003) 083518

5-th bulk dim. **Z**

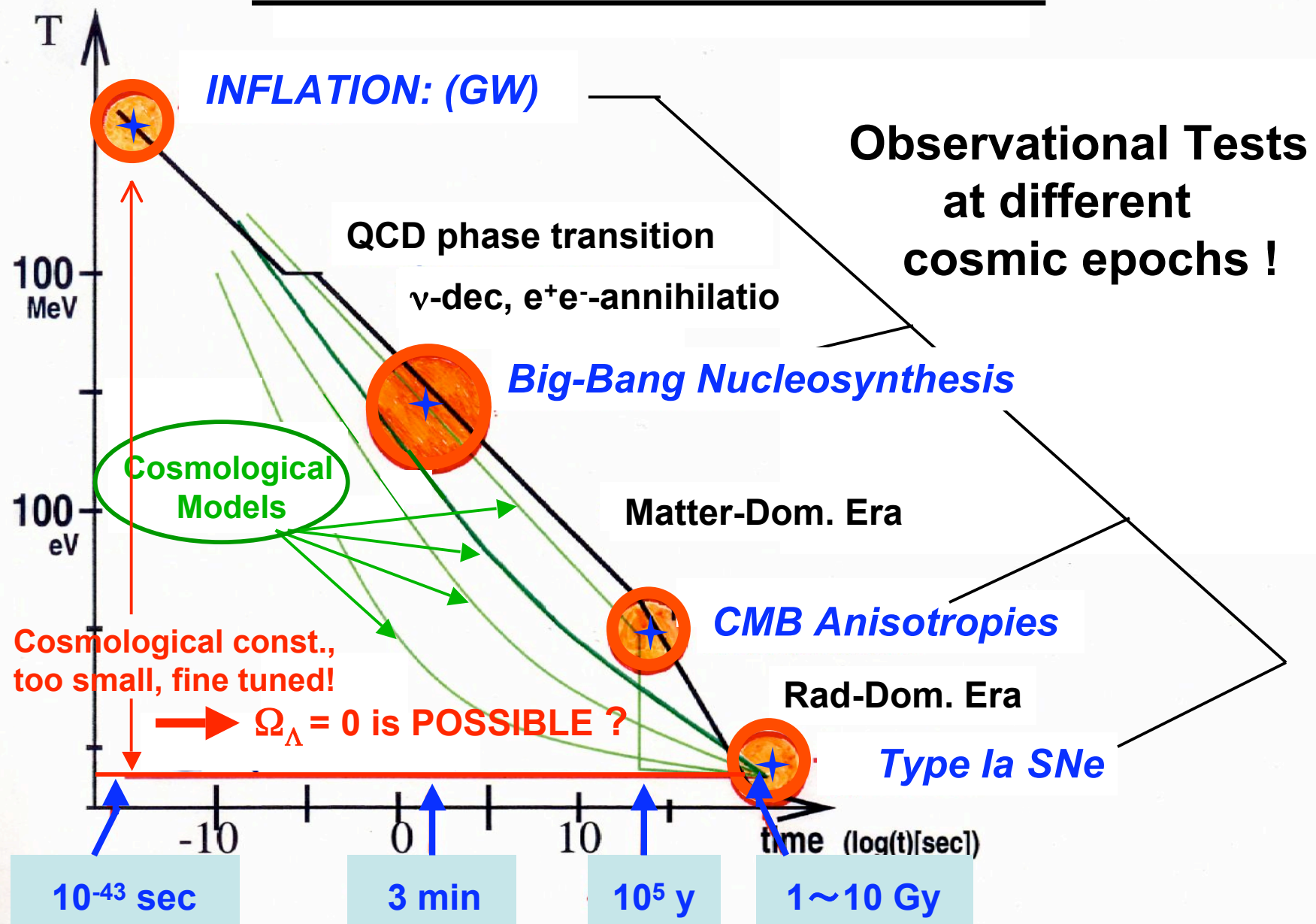
$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}(\bar{\rho} + \rho + \rho_\chi) + \frac{k}{a^2}$$

Dark Radiation term:

$$\dot{\rho}_\chi + 4H\rho_\chi = -\alpha/a^q \times \rho_{cr}H,$$

$q = \text{adjustable parameter}$

# Thermal History of the Universe

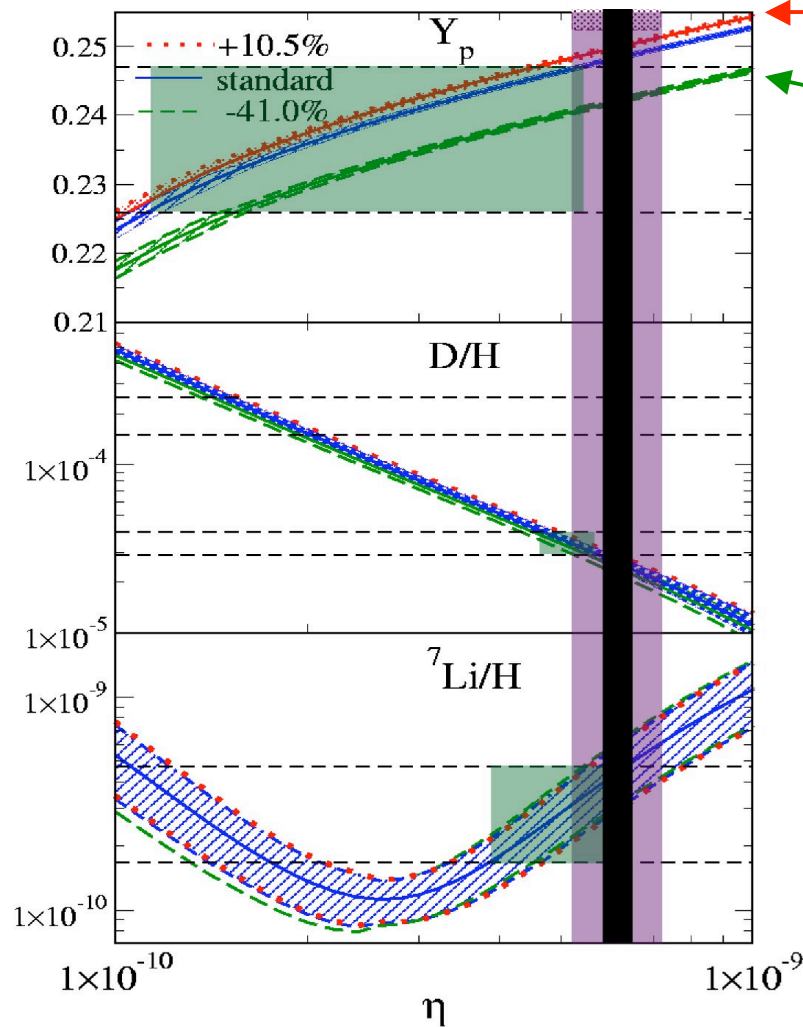


# Big-Bang Nucleosynthesis in Brane Cosmology

Ichiki, Garnavich, Kajino, Mathews & Yahiro, PRD 68 (2003) 083518

$t = 3 \text{ min}$

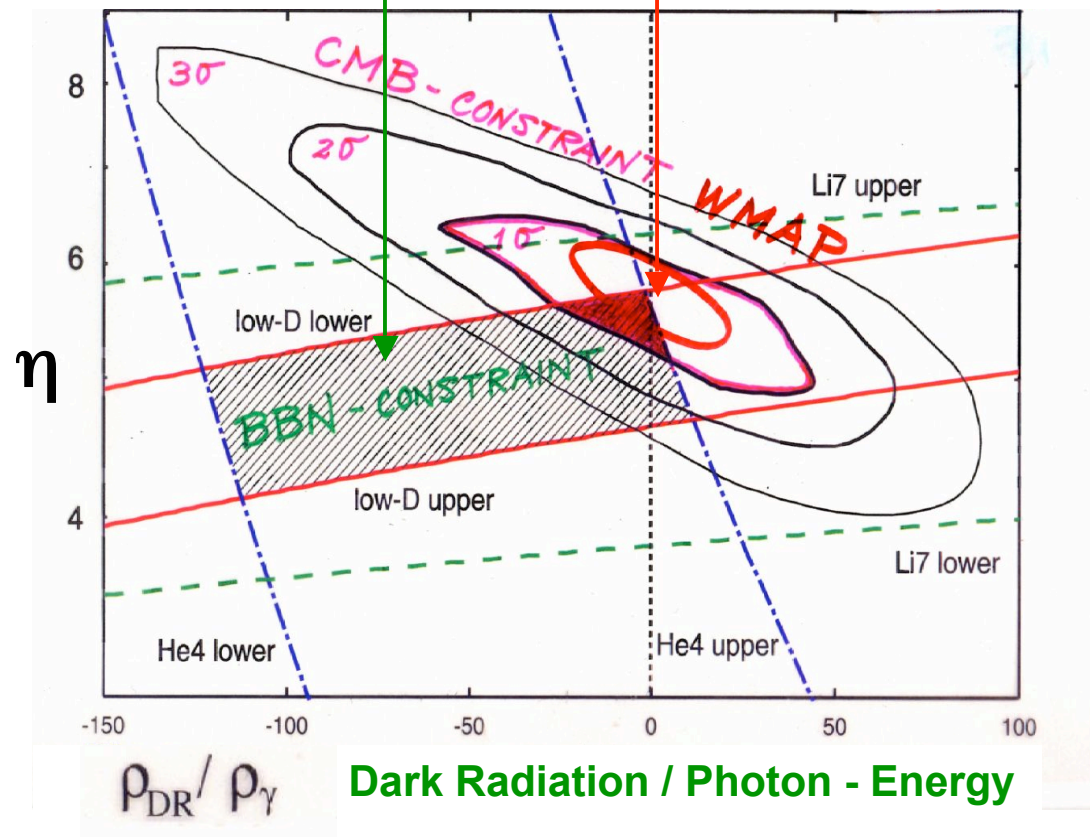
CMB-WMAP



Standard BBN Model

Dark Radiation

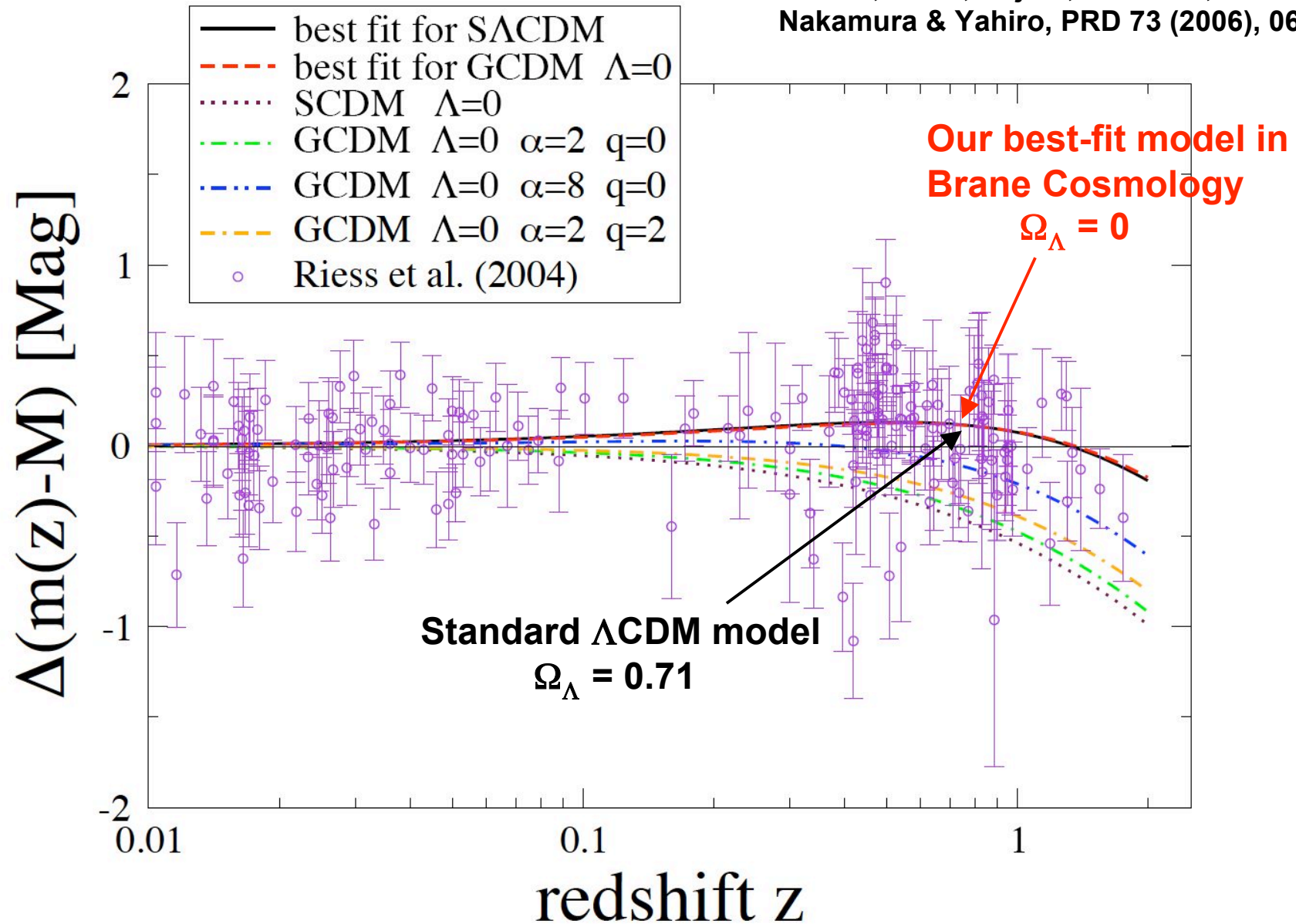
relaxes the tension between the CMB and  ${}^4\text{He}$ .



# Supernova $m$ - $M$ vs. $z$ Relation

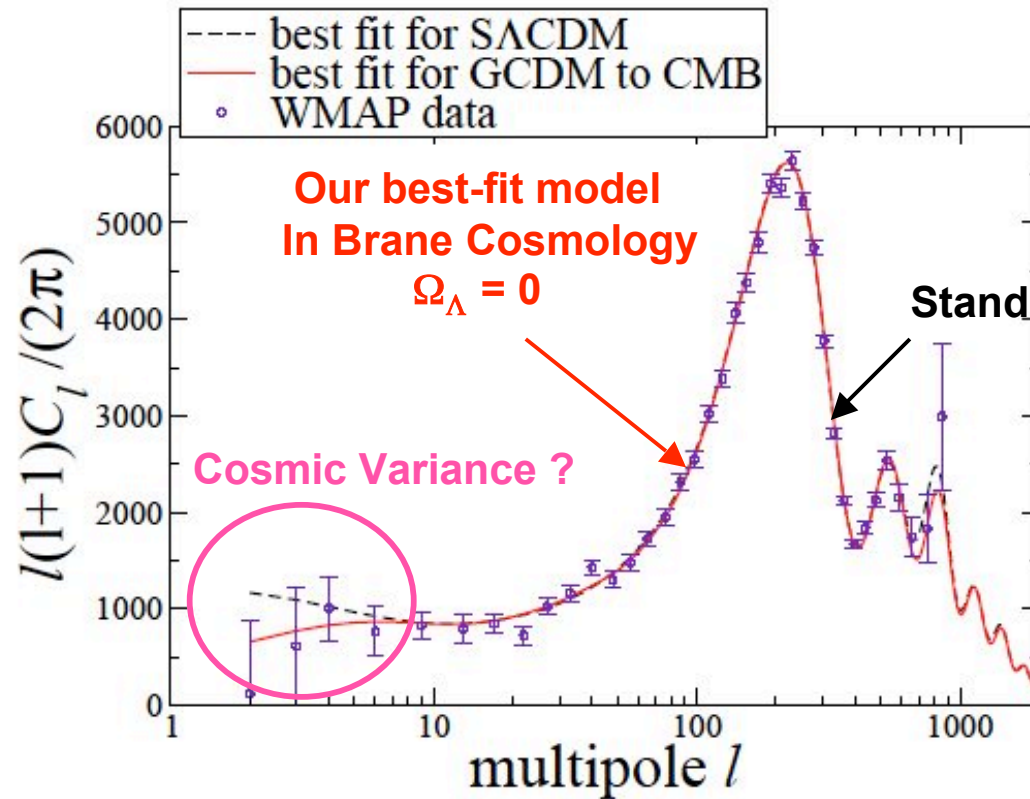
$t = 1 \sim 10$  Gy

Umezū, Ichiki, Kajino, Mathews,  
Nakamura & Yahiro, PRD 73 (2006), 063527





Umezu, Ichiki, Kajino, Mathews,  
Nakamura & Yahiro, PRD 73 (2006), 063527

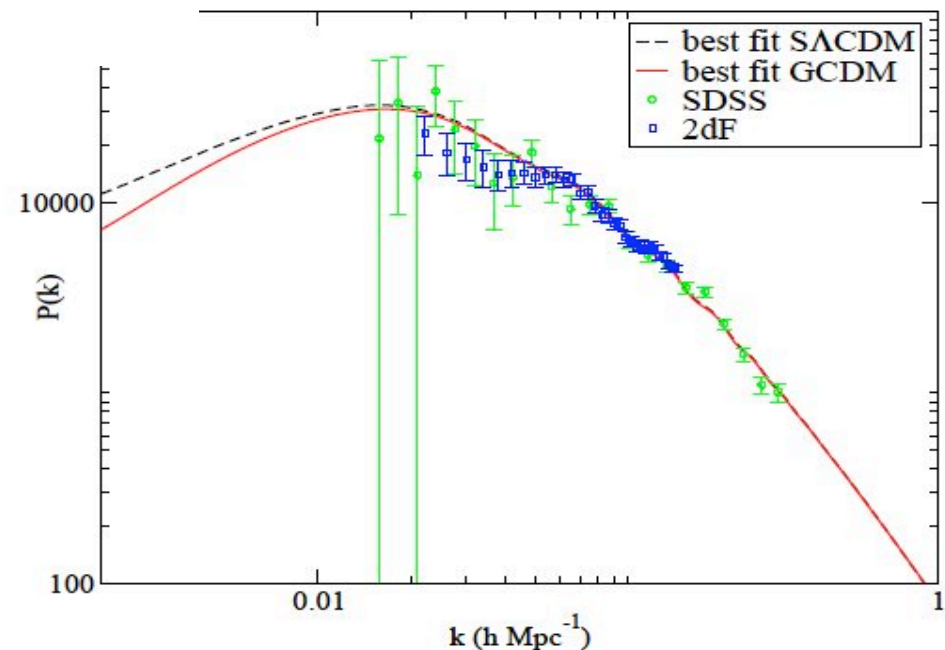


## Matter Power Spectrum

**Only OUR MODEL  
can explain this quenching !**

## CMB Anisotropies

$$t = 3 \times 10^5 \text{ y}$$



# Summary

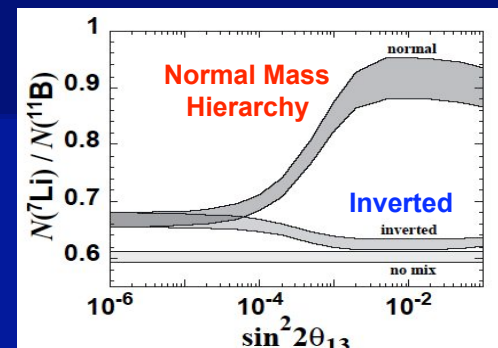
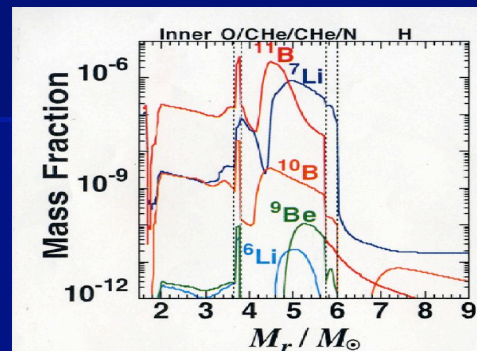
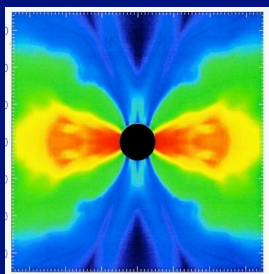
- The  $\nu$ -process in core-collapse supernovae provides unique tool to determine the unknown oscillation parameter  $\theta_{13}$  and mass hierarchy of active neutrinos.

**MSW (matter)**

**$\nu$  - oscillation effect !**



Upsilon  
 $\rightarrow e^+ \mu^+ \tau^+$   
 $\rightarrow \nu_\mu \nu_\tau$

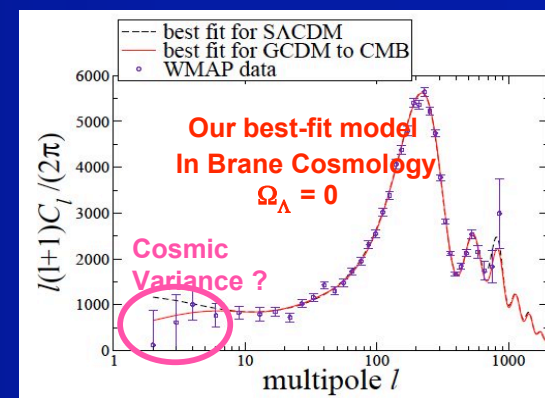


- UHE- $\nu$ 's are produced from heavy-meson (upsilon) synchrotron emission by UHECR hadronic interactions with strong magnetic field in the GRBs.

**Vacuum  $\nu$ -oscillation effect !**

- $\nu$ 's take a tiny fraction of cosmic mass.

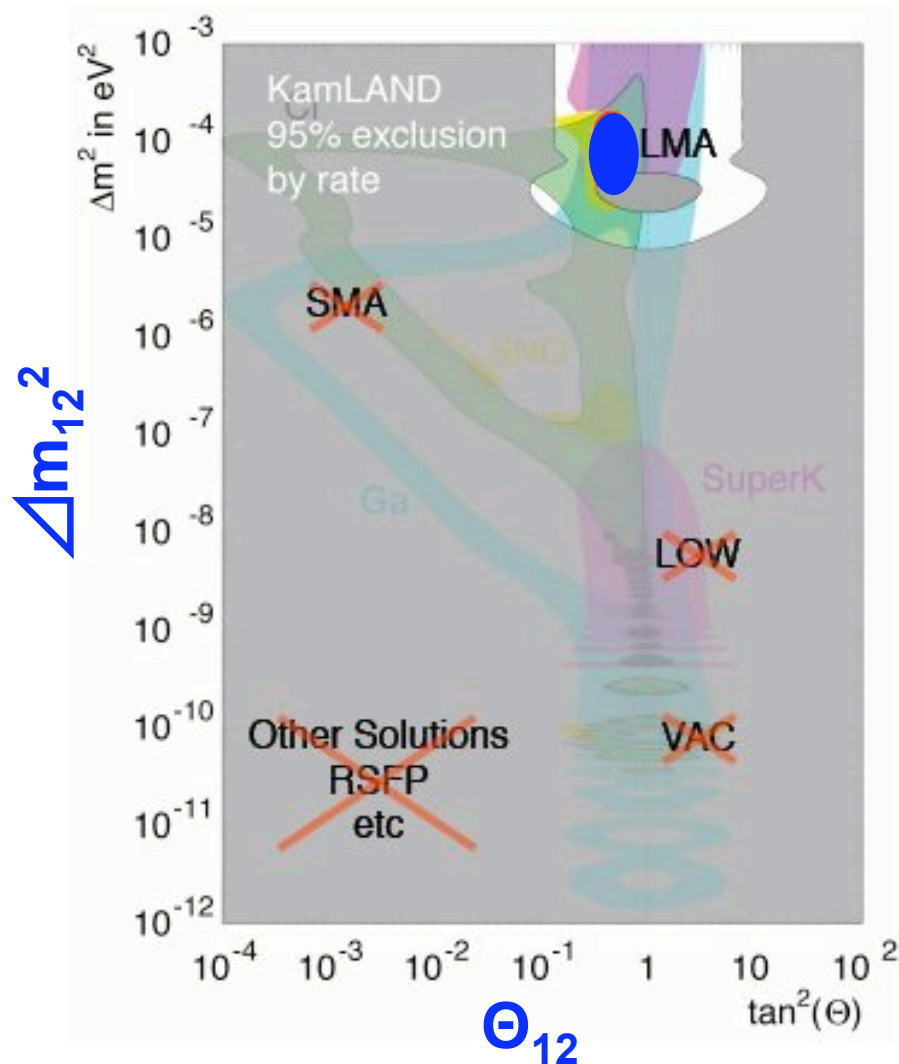
Brane world cosmology with  $\Omega_\Lambda = 0$  can explain accelerating cosmic expansion if dark matter particles can be exchanged between the brane and the bulk.



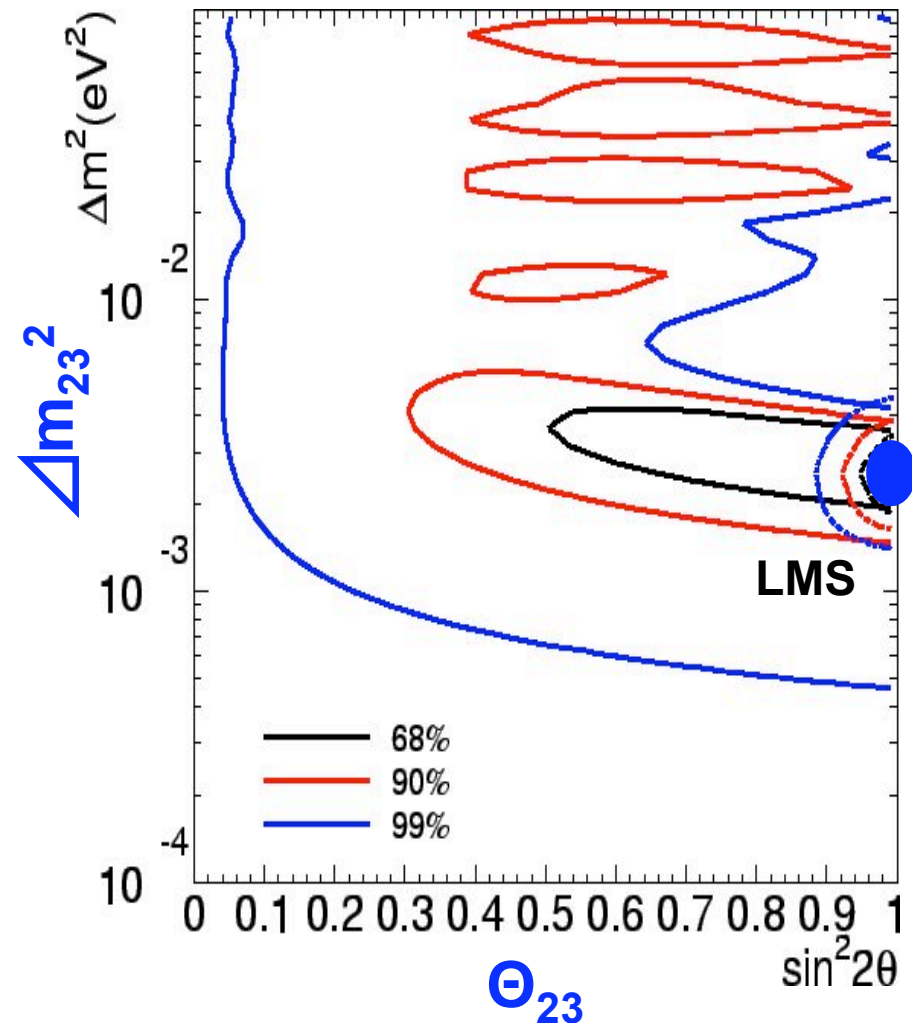


# “KNOWN” Neutrino Oscillation Parameters

Super-K, SNO, KamLand (reactor  $\nu$ ) determined  $\Delta m_{12}^2$  and  $\theta_{12}$  uniquely.

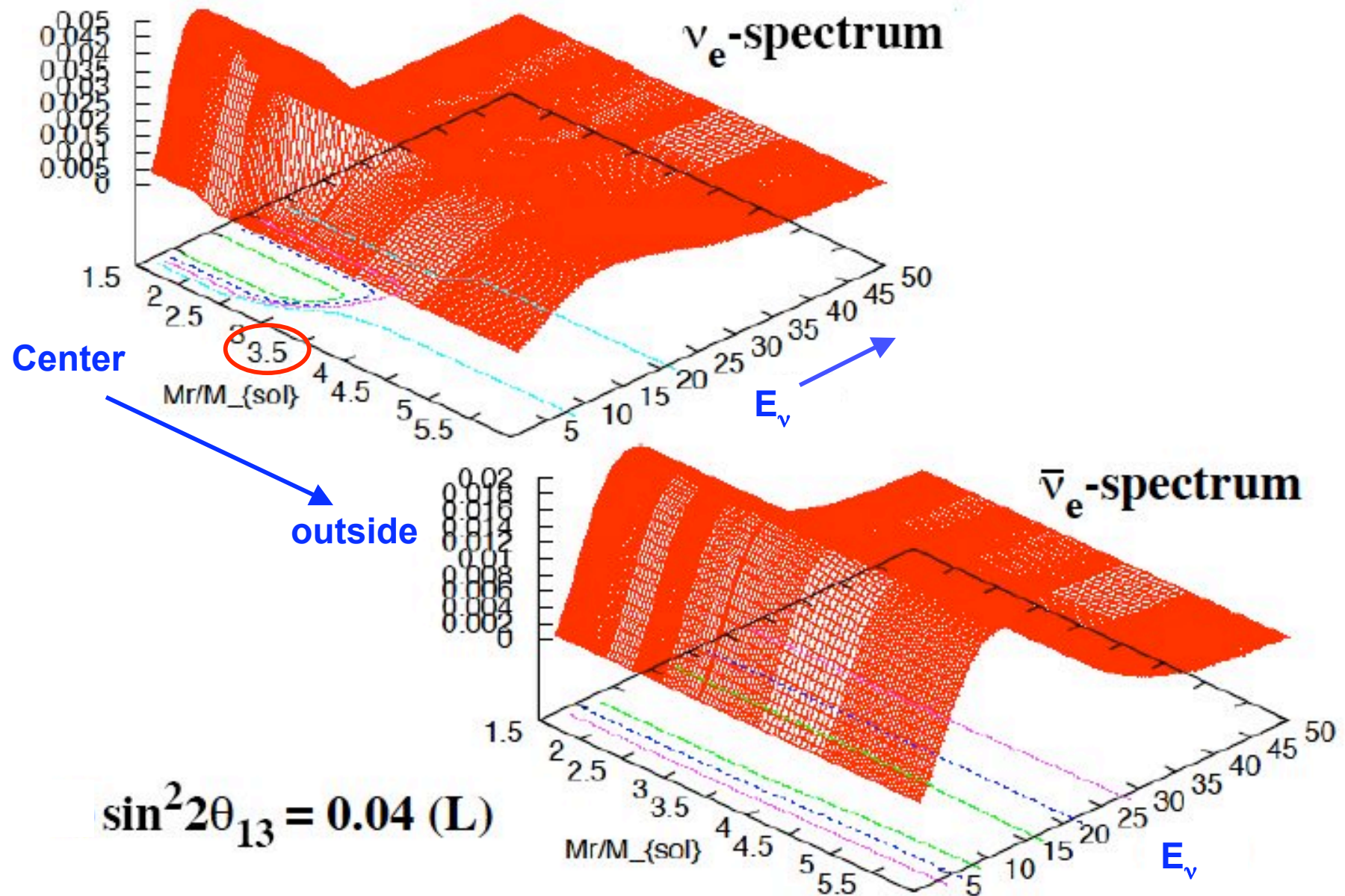


Super Kamiokande (atmospheric  $\nu$ ) determined  $\Delta m_{23}^2$  and  $\theta_{23}$  uniquely.





# Neutrino Oscillation (MSW Effect) through propagation



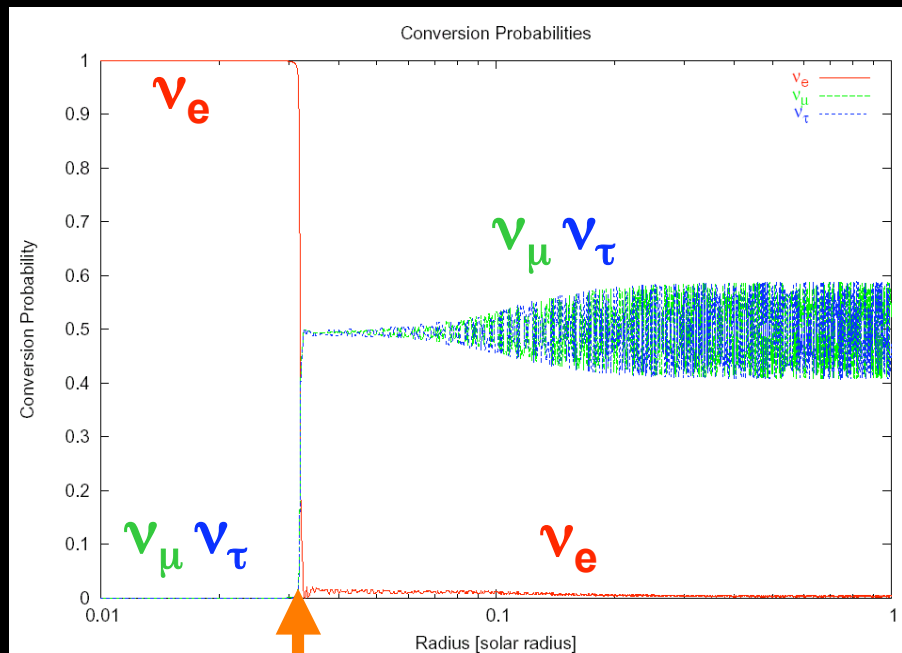
# Neutrino Oscillation (MSW Effect) through propagation

Kawagoe, Kajino, Suzuki, Sumiyoshi, Yamada (2006)

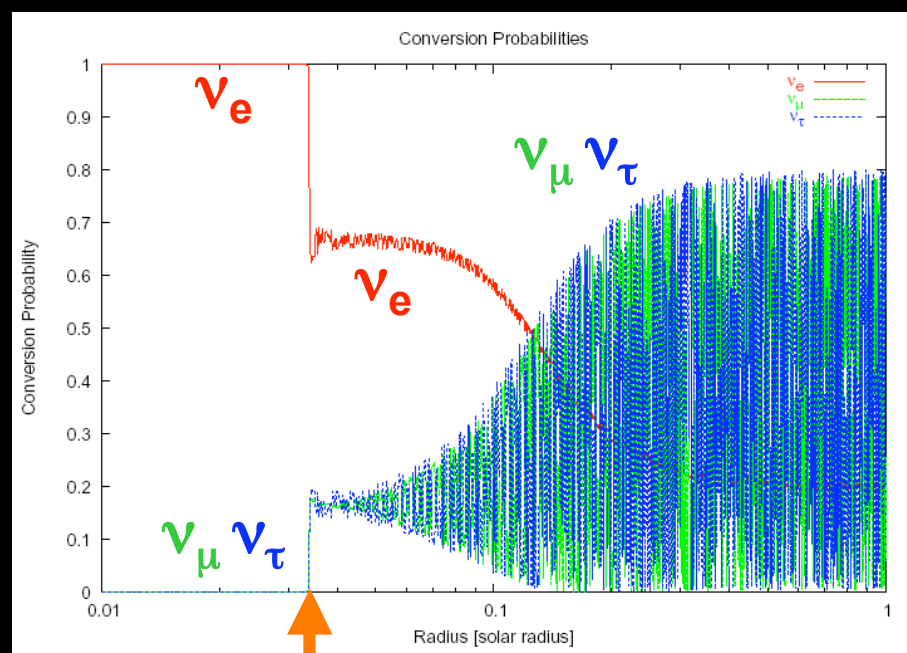
Normal Hierarchy

$E_\nu = 5.6 \text{ MeV}$

Adiabatic

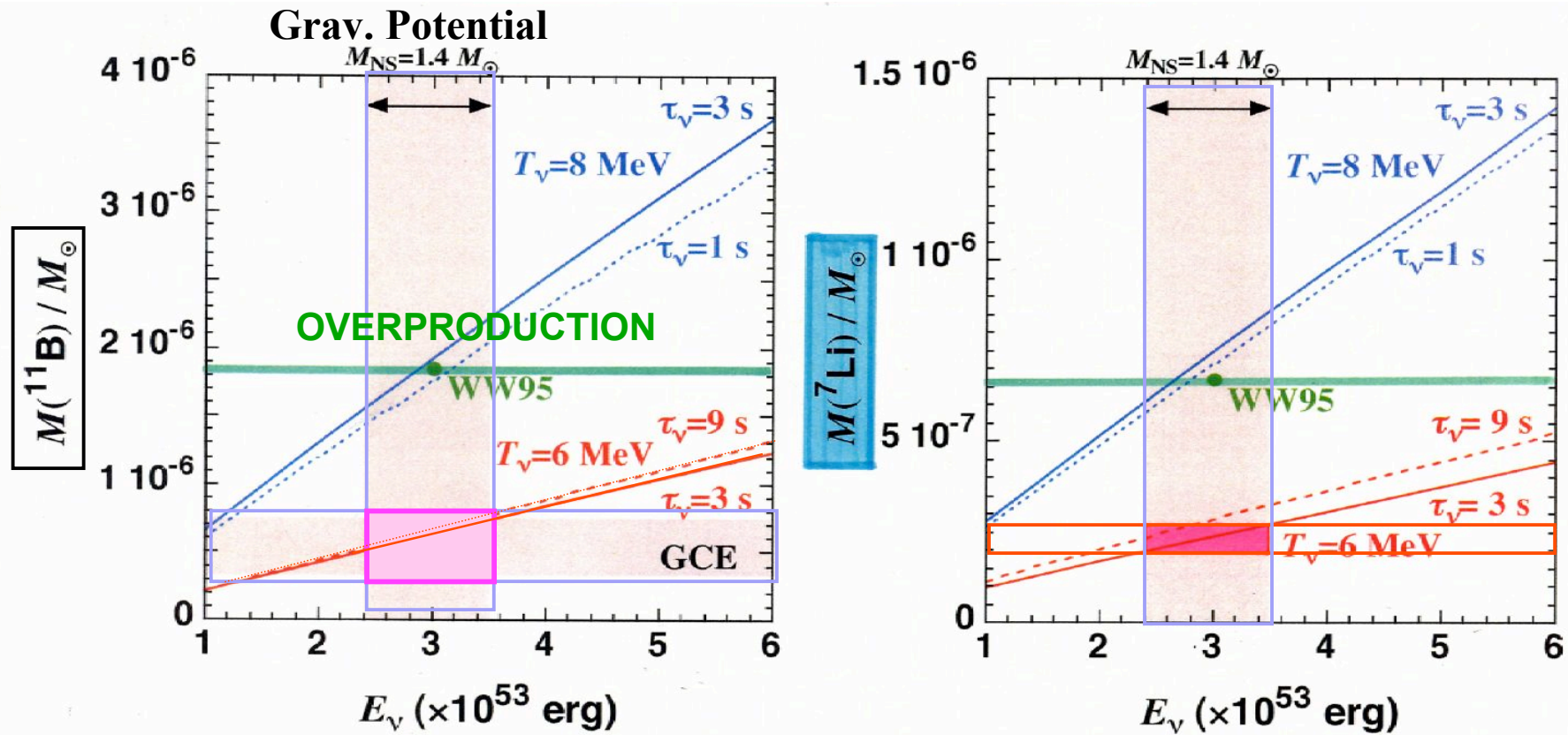


Non-Adiabatic



# Supernova $\nu$ -Process

Yoshida, T., Kajino, T., & Hartmann, D. H.  
2005, PRL 94, 231101



GCE constraints on  $^{11}\text{B}$   
Meteoritic  $^{11}\text{B}/^{10}\text{B}$

Prediction of  $^7\text{Li}$

Lower neutrino temperature, consistent with recent theoretical calculation of neutrino transfer (Thomas-Janka et al. 2004)



## Lepton Decay Mode to Neutrinos

	Mass (MeV)	Life (sec)	Decay Mode
$e^-$	0.511	$> 4.3 \times 10^{23}$ yr	
$\mu^-$	105.7	$2.197 \times 10^{-6}$	$e^- \bar{\nu}_e \nu_\mu$ ( $\approx 100\%$ )
$\tau^-$	1777.1	$2.9 \times 10^{-13}$	$e^- \bar{\nu}_e \nu_\tau$ (17.8%) $\mu^- \bar{\nu}_\mu \nu_\tau$ (17.4%)

## Meson Decay Mode to Three Flavor Lepton Pairs

	Quarks	I	$J^{PC}$	Mass (MeV)	Life (sec)	Decay Mode
$\pi^0$	$u\bar{u} - d\bar{d}$	1	$1^{-+}$	134.98	$8.4 \pm 0.6 \times 10^{-17}$	$2\gamma$ 98.8%
$\pi^+$	$u\bar{d}$	1	$0^-$	139.6	$2.197 \times 10^{-6}$	$e^- \bar{\nu}_e \nu_\mu$ 99.9%
$\rho^0$	$u\bar{u} - d\bar{d}$	1	$1^{--}$	$768.5 \pm 0.6$	$\Gamma = 150.7 \pm 1.2$ MeV	$\pi\pi \approx 100\%$
$D_s^+ (D_s^-)$	$c\bar{s} (s\bar{c})$	0	$0^-$	$1968.5 \pm 0.6$	$(0.467 \pm 0.017) \times 10^{-12}$	$\tau^+ \nu_\tau$ $7 \pm 4\%$
$J/\psi(1S)$	$c\bar{c}$	0	$1^{--}$	$3096.88 \pm 0.04$	$\Gamma = 87 \pm 5$ keV	$\mu^+ \mu^-$ $6.01 \pm 0.19\%$
$J/\psi(2S)$	$c\bar{c}$	0	$1^{--}$	$3686.00 \pm 0.09$	$\Gamma = 277 \pm 31$ keV	$\mu^+ \mu^-$ $(7.7 \pm 1.7) \times 10^{-3}\%$
$\Upsilon(1S)$	$b\bar{b}$	0	$1^{--}$	$9460.37 \pm 0.21$	$\Gamma = 52.5 \pm 1.8$ keV	$\tau^+ \tau^-$ $(2.67^{+0.14}_{-0.16})\%$
$\Upsilon(4S)$	$b\bar{b}$	?	$1^{--}$	$10580 \pm 4$	$\Gamma = 10 \pm 4$ MeV	$e^+ e^-$ $(2.8 \pm 0.7) \times 10^{-5}\%$

$e^\pm, \mu^\pm, \tau^\pm \sim 3\%$

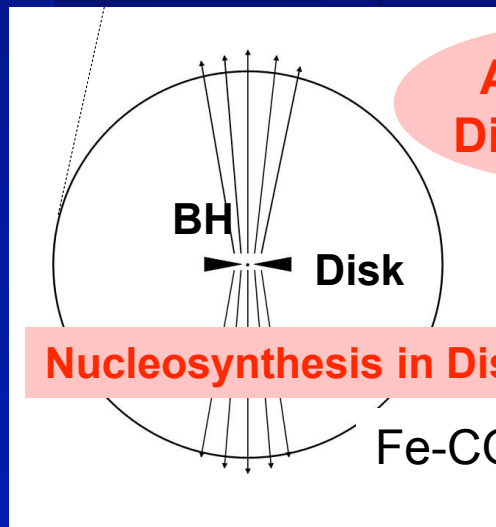
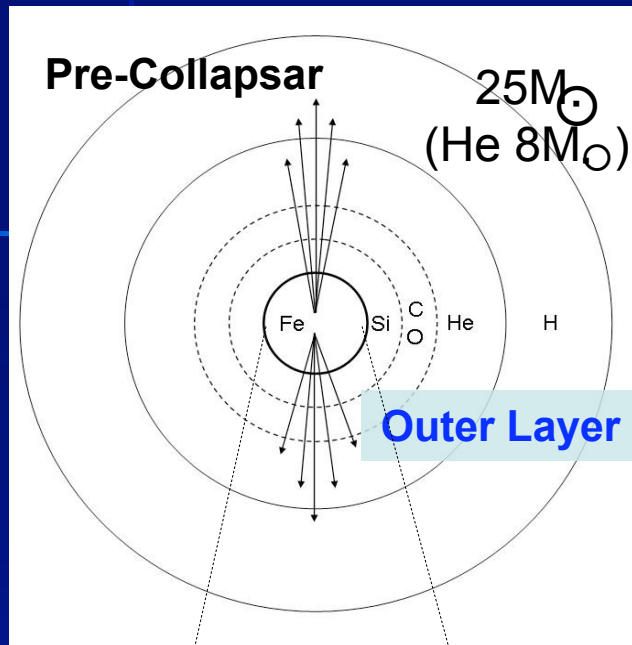
Table 2.1: Data of MESONS, Review of Particle Physics 1996



# Two Modes of Nucleosynthesis in Collapsar

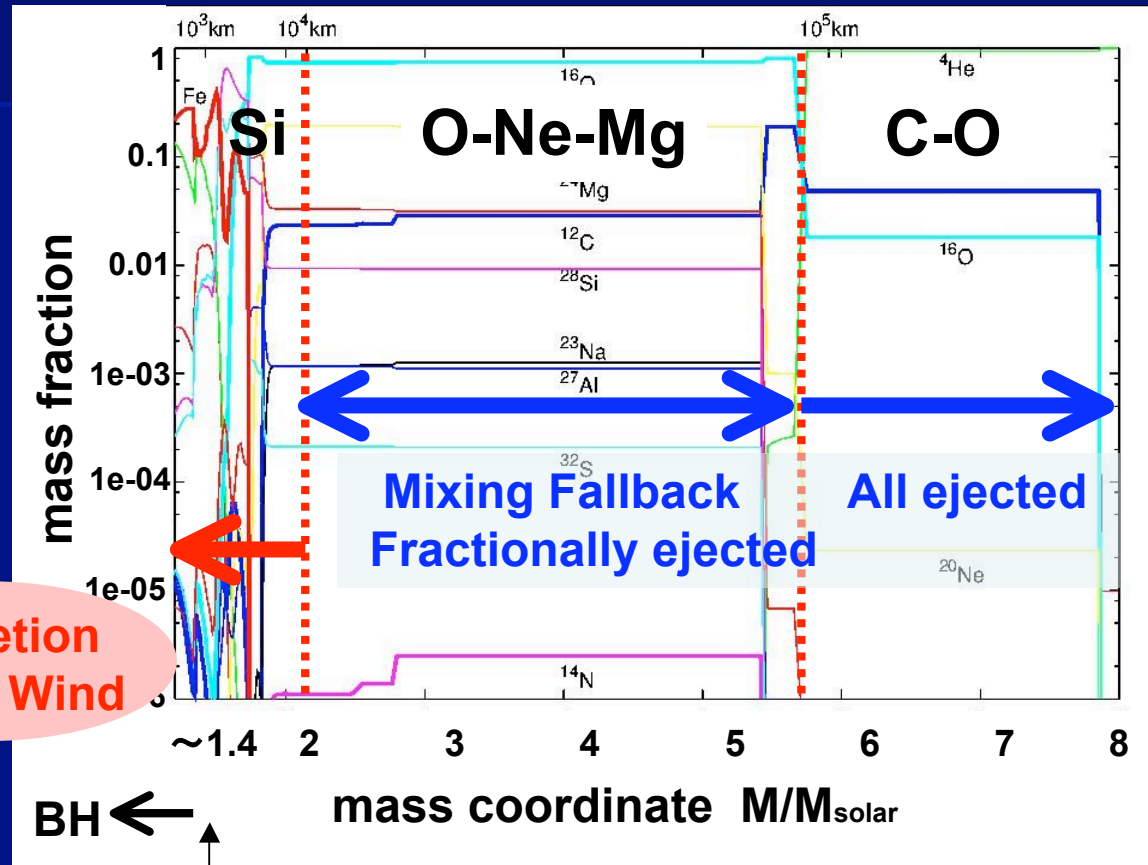
Nucleosynthesis in outer layer

+ Explosive Disk-Wind nucleosynthesis



Accretion  
Disk + Wind

Nucleosynthesis in Disk-Wind !



Yoshida, Sasaqui & Kajio (2006)

Umeda & Nomoto (2003)

# Brane World Cosmology

Motivated by the D-brane solution  
in 10 dim STRING THEORY

Randall-Sundrum II; PRL 83 (1999)

The Universe is embedded  
in a 5 dim spacetime  $AdS_5$ .

Brane  
||  
4D-Einstein Universe

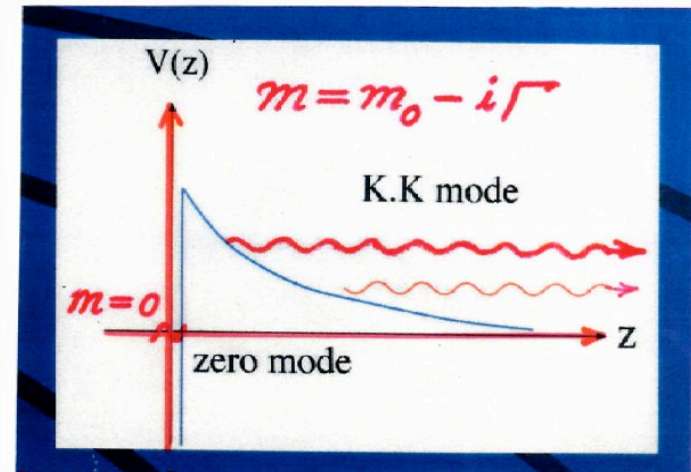
Quantized matter fields in  $AdS_5$   
leads to quasilocalized eigenstates  
on the 4 dim brane.

CDM Particle **SUSY !?**

5-th dimension, compactified.

Massive particle can tunnel into  $z$  !

Dubovsky, Rubakov, & Tinyakov (2000)



**We proposed Disappearing SUSY-CDM Model ! (2003)**

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## Disappearing LSP (Lightest SUSY Particle) CDM Model Is a likely possibility !

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LSP = Lightest Supersymmetric Particle

$$m_0 \sim 1 \text{ TeV} \text{ vs. } m_B \sim 1 \text{ GeV}$$

Fermion:

$$\Gamma = m_0(m_0/2k)^{2gv/k-1} \pi/\Gamma_f(gv/k+1/2)^2$$

v = vacuum expectation value

g = coupling const.

Scalar Particles (Bosons):

$$\Gamma = (\pi/16) m_0^3/k^2$$

$$k = (-\Lambda_5/6)^{-1/2}$$

- ***LSPs (CDM) disappear at cosmological time !***
- ***BARYONS do not !***

**Largest  $\Gamma$  for largest  $m_0$**

## Modified Friedmann Equation

$$H^2 = \frac{8\pi G_N}{3} \rho - \frac{k}{a^2} + \frac{\Lambda_4}{3} + \cancel{\frac{\kappa_5^4}{36} \rho^2} - E$$

$$\rho = \rho_M + \rho_R + \rho_{DM}$$

$$\rho_{DM} = C e^{-\Gamma t} / a^3$$

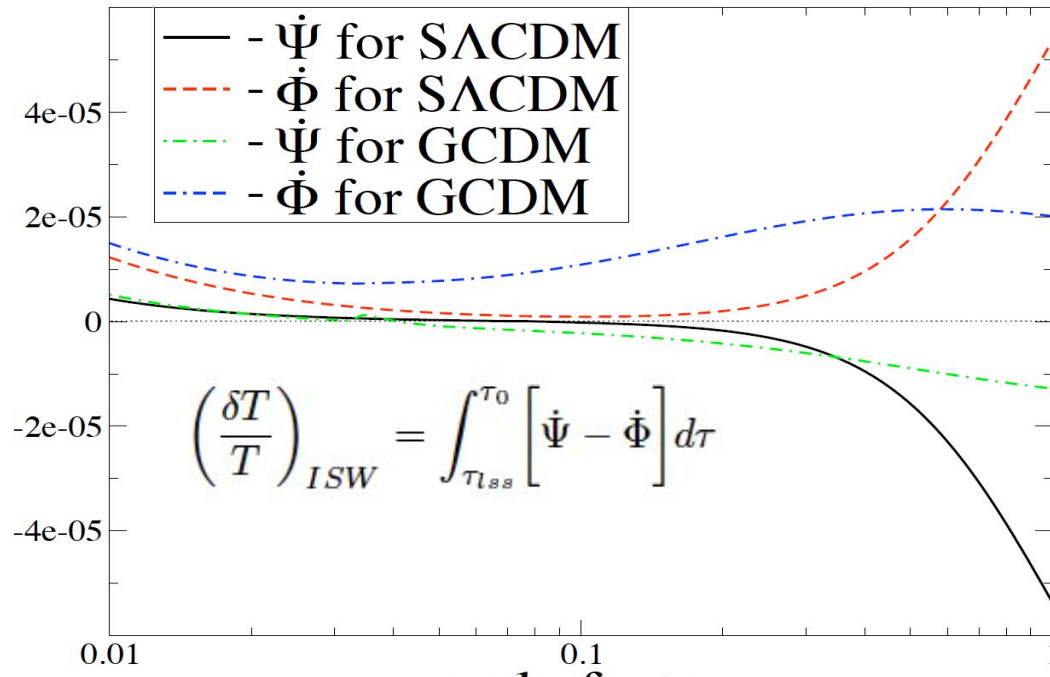
E = “Dark Radiation” or  
Electric part of the bulk  
Weyl tensor

$$\frac{dE}{dt} + 4HE = \Gamma \rho_{DM}$$

Ichiki, Garavich, Kajino, Mathews & Yahiro  
PRD 68 (2003), 083518



# LATE Integrated Sachs-Wolf effect



Umezu, Ichiki, Kajino, Mathews,  
Nakamura & Yahiro, PRD 73 (2006), 063527

Parameter sets for various fits.

scale factor

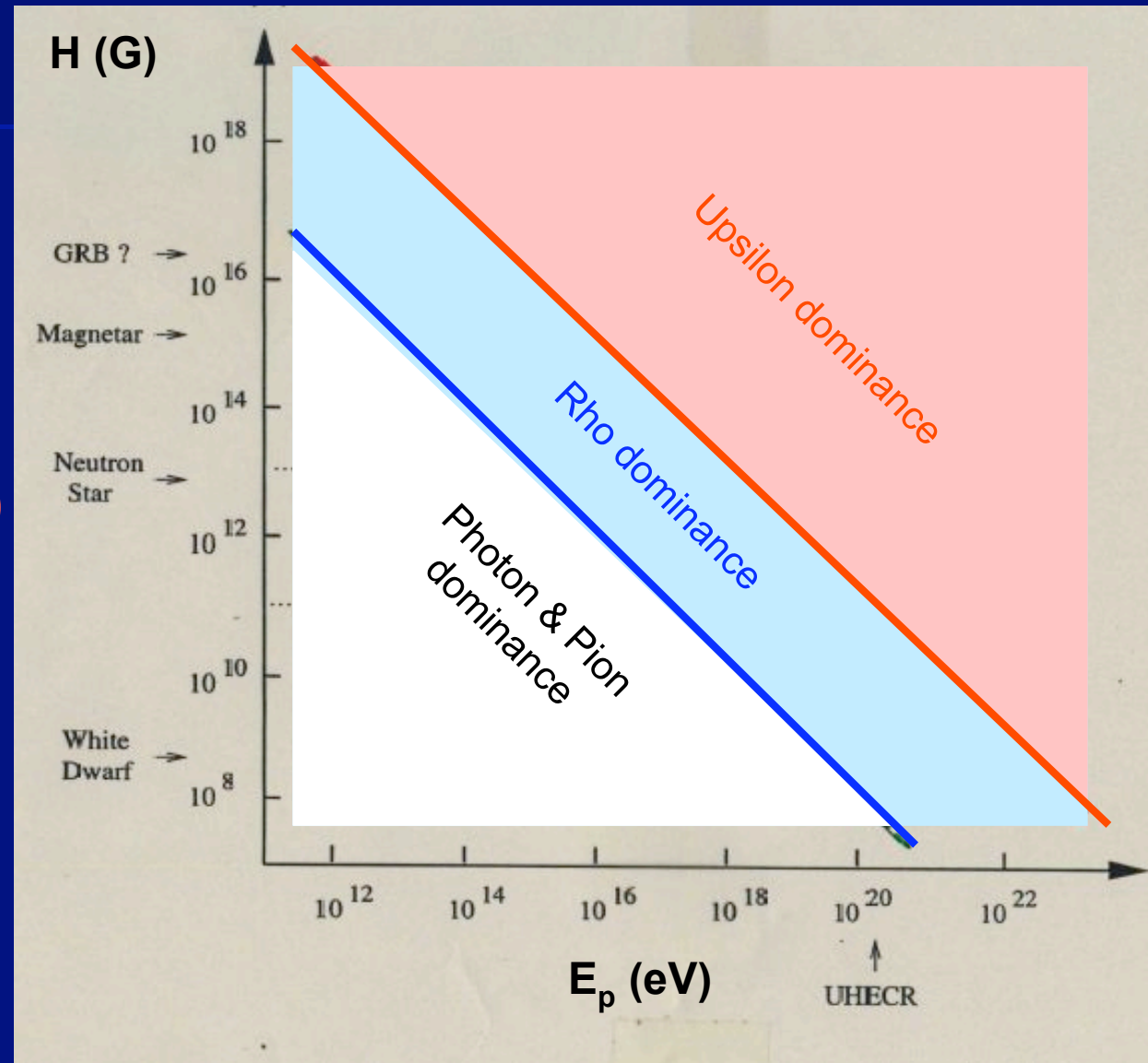
Fit	$\alpha$	$q$	$\Omega_b h^2$	$\Omega_{DM} + \Omega_{DR}$ $\Omega_{DM} + \Omega_\Lambda$	$\Omega_{DM}$	$\Omega_{DR}$ $\Omega_\Lambda$	$h$	$z_{re}$	$n_s$	$\tau$	$b$	$\chi_r^2$
SN Ia Only												
Best Fit GCDM	11.0	0.006	0.022	0.93	3.31	-2.38	0.58	-	-	-	-	1.23
Best Fit SΛCDM	-	-	0.022	0.97	0.26	0.71	0.71	-	-	-	-	1.24
CMB Only												
Best Fit GCDM	2.14	2.92	0.029	0.93	1.91	-0.98	0.64	29.1	1.18	0.533	-	1.02
Best Fit SΛCDM	-	-	0.023	0.94	0.23	0.71	0.71	14.9	0.97	0.13	-	1.01
SN Ia + CMB												
Best Fit GCDM	8.45	0.023	0.023	0.95	3.14	-2.19	0.71	15.0	0.97	0.133	-	1.04
Best Fit SΛCDM	-	-	0.023	0.96	0.25	0.71	0.70	13.3	0.96	0.111	-	1.04
SN Ia + CMB + P(k)												
Best Fit GCDM	8.33	0.037	0.024	0.95	3.05	-2.44	0.71	15.3	0.98	0.140	2.1	1.03
Best Fit SΛCDM	-	-	0.023	0.95	0.24	0.71	0.70	13.7	0.97	0.117	1.05	1.03

Meson synchrotron emission is an important process in UHECR-hadrons interactions in strong magnetic field of the GRBs., which serves for :-

1. Energy Loss Mechanism !

2. Creation Mechanism of UHE neutrinos !

$$\chi \equiv \gamma_p \cdot \frac{H}{H_0} > 0.01 \sim 0.1$$



# Collapsar is a viable candidate for the Central Engine of GRBs

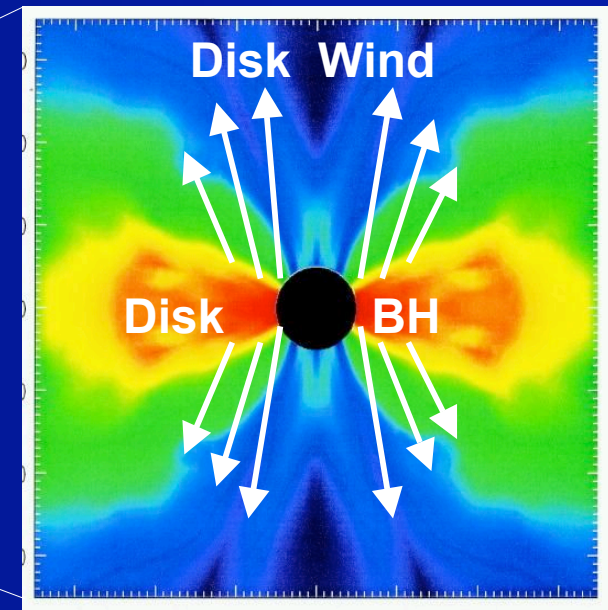
GRB (image)



$\nu$ 's are not emitted from the central BH !

GRB is a cosmological activity at high redshift in the early galaxy.

Collapsar Model  
McFadyen & Woosley (1999)



Collapsar is a core-collapse supernova of the first-generation massive star formed from primeval zero metal gas.

→ **Nucleosynthetic Signature**