



**Accelerators based compact sources  
of quasi-monochromatic radiation  
for phase-contrast X-ray imaging**

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# Participation of IAP in LIA IDEATE



## Institute of Applied Physics National Academy of Sciences of Ukraine (Sumy, Ukraine)

The LIA IDEATE covers R&D and optimisation of innovative technologies for the experiments at the particle accelerators and development of accelerator techniques.

### Research program and projects

- R&D of detector technologies
- Accelerator techniques
- Experimental platforms
- R&D on instrumentation for medical applications
- Developments for flavour physics
- Developments for nuclear physics
- Developments for hadron physics
- Pedagogical activities

Phase-contrast X-ray imaging

# Phase-contrast X-ray imaging

**Phase-contrast X-ray imaging (PCI)** is a general term for different technical methods that use information concerning changes in the phase of an X-ray beam that passes through an object in order to create its images.

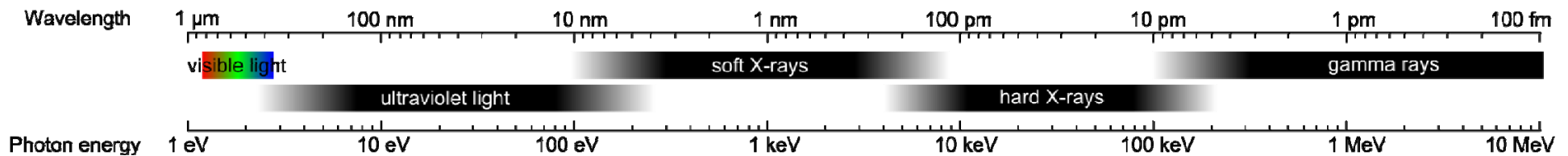
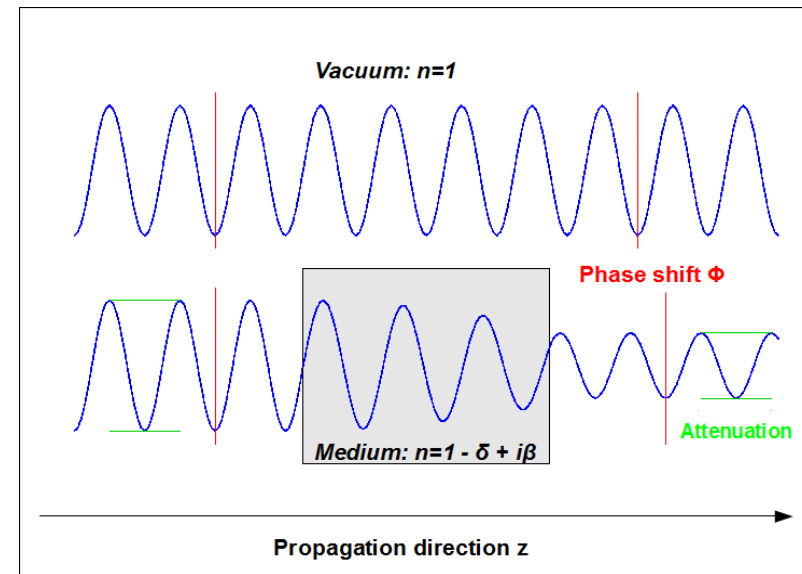
$$\Psi(z) = E_0 e^{inkz} = E_0 e^{i(1-\delta)kz} e^{-\beta kz}$$

the phase shift

an exponential decay factor decreasing the amplitude of the wave

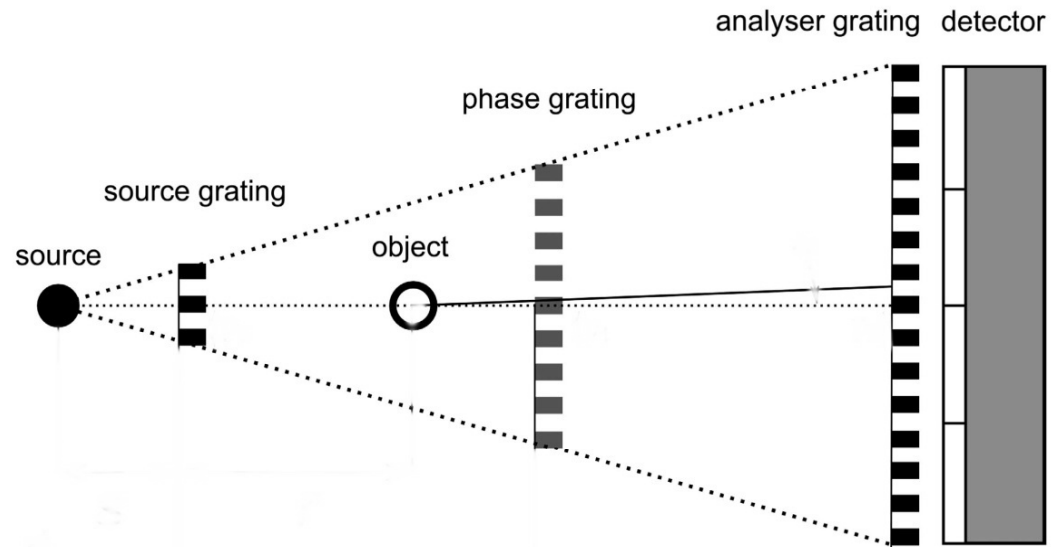
$$\delta \propto k^{-2}$$

$$\beta \propto k^{-4}$$



# Phase-contrast X-ray imaging. Experimental realisation

- Crystal interferometry
- Grating Bense-Hart
- Analyzer-based imaging
- Propagation-based imaging
- Edge-illumination
- Grating-based imaging  
(Talbot interferometry)

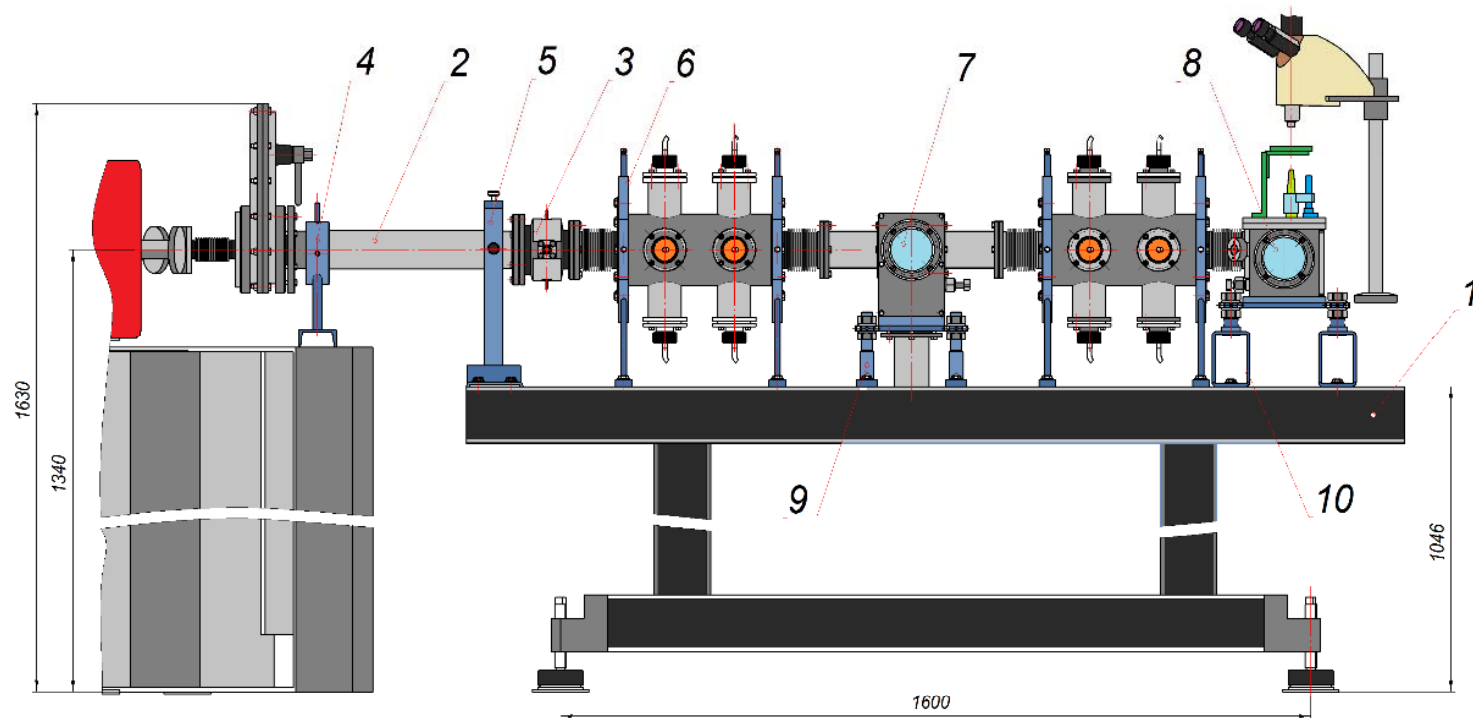


## Required characteristic of radiation for X-ray phase contrast

Energy range	$\Delta E/E$	Source size	Size on the object	Flux on the object	Coherence
> 10 keV	3%	small	50 cm	> $10^{(9)}$ ph/s	yes

# Accelerators based compact source of quasi-monochromatic X-ray at IAP NASU

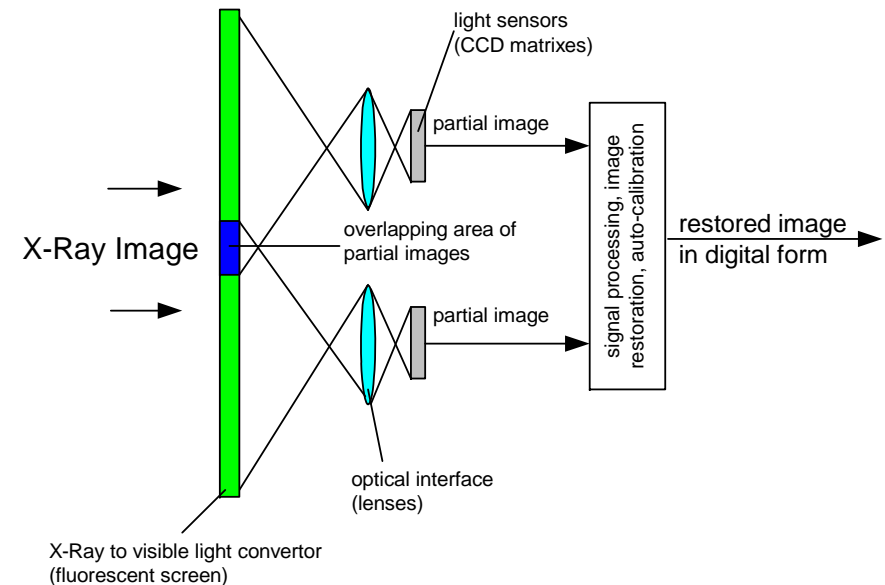
3D model and a general view of the  
quasimonochromatic X-ray source with ion  
excitation.



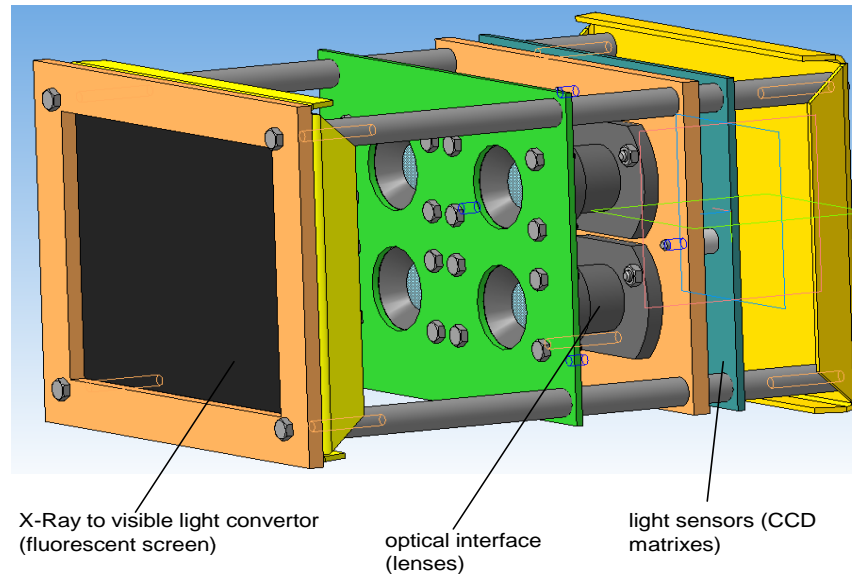
# Multimatrix X-Ray detector for phase contrast imaging experiments

## Basic parameters

Sensitive Area	90x60mm
Optical Configuration	2x2 cells
DQE(0)	0.44
Optical Resolution	up to 12 $\mu\text{m}/\text{mm}$
Dynamic Range	equal to 14bits
Energy of detected X-Ray quantum	9-100keV (for different conversional screens)
Frame rate	15-150 FPS
External digital interface	Gigabit Ethernet

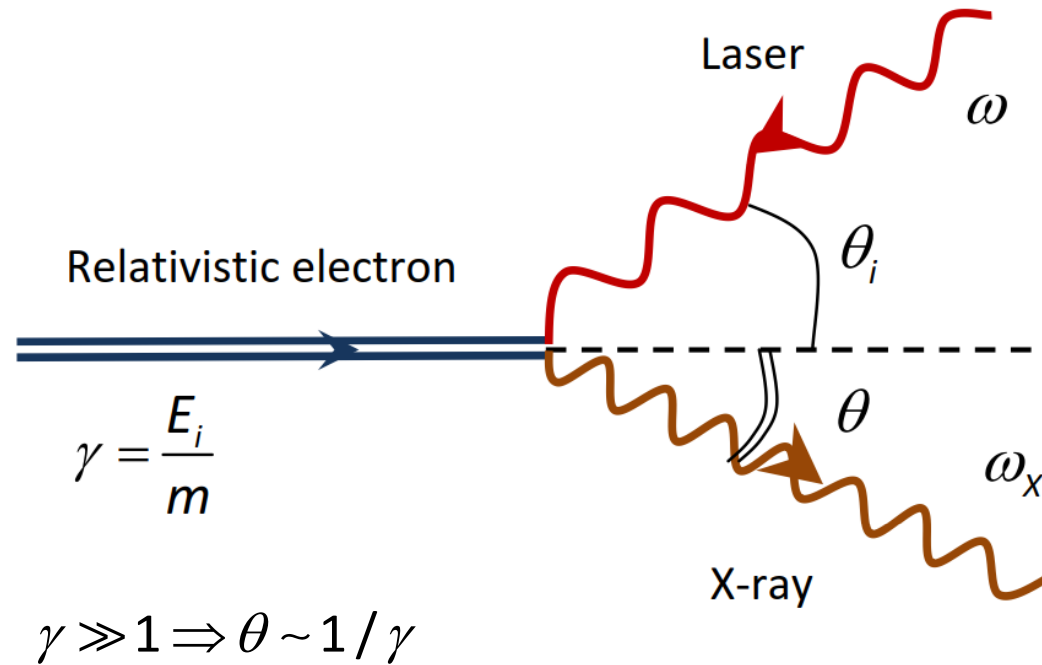


Optical scheme of the detector



3D CAD Drawing of the Multimatrix Hybrid X-Ray Detector

## Compton backscattering process



Energy of X-ray photons, which are emitted by a relativistic electron in collision with the laser pulse

$$\hbar\omega_x \approx \hbar\omega \frac{2\gamma^2(1 + \cos\theta_i)}{1 + \gamma^2\theta^2}$$



## X-ray sources based on Compton backscattering

	Type	Energy [KeV]	Flux ( @ 10% bandwidth)	Source size ( $\mu\text{m}$ )
*PLEIADES (LLNL) [11,12]	Linac	10-100	$10^7$ (10 Hz)	18
*Vanderbilt [13,14]	Linac	15-50	$10^8$ (few Hz)	30
*SLAC [15]	Linac	20-85		
*Waseda University [16,17]	Linac	0.25-0.5	$2.5 \cdot 10^4$ (5 Hz)	
*AIST, Japan [18]	Linac	10-40	$10^6$	30
*Tsinghua University [19]	Linac	4.6	$1.7 \cdot 10^4$	
*LUCX (KEK) [20]	Linac	33	$5 \cdot 10^4$ (12.5 Hz)	80
+ UTNL, Japan [21,22]	Linac	10-40	$10^9$	
MIT project [23]	Linac	3-30	$3 \cdot 10^{12}$ (100 MHz)	2
MXI systems [24]	Linac	8-100	$10^9$ (10Hz)	
SPARC –PLASMONX [25]	Linac	20-380	$2 \cdot 10^8$ - $2 \cdot 10^{10}$	0.5-13
Quantum Beam (KEK) [26,27]	Linac		$10^{13}$	3
*TERAS (AIST) [28]	Storage ring	1-40	$5 \cdot 10^4$	2
*Lyncean Tech [29,30,31]	Storage ring	7-35	$\sim 10^{12}$	30
Kharkov (SNC KIPT) [32]	Storage ring	10-500	$2.6 \cdot 10^{13}$ (25 MHz)	35
TTX (THU China) [33,34]	Storage ring	20-80	$2 \cdot 10^{12}$	35
ThomX France [35]	Storage ring	50	$10^{13}$ (25 MHz)	70

ThomX - Conceptual Design Report



## The spectral line broadening

Estimation of spectral line broadening for the parameters of ThomX source

$$\omega_{x0} = \omega \frac{2\gamma^2 (1 + \cos \theta_i)}{1 + \gamma^2 \theta^2}$$

Electron energy dispersion  $\Delta\gamma / \gamma \sim 0.6\%$

$$\omega_x(\gamma) \approx \omega \frac{2(\gamma + \Delta\gamma)^2 (1 + \cos \theta_i)}{1 + \gamma^2 \theta^2} = \omega_{x0} \left( 1 + \frac{2\Delta\gamma}{\gamma} \right) \Rightarrow \frac{\Delta\omega_x(\gamma)}{\omega_{x0}} = \frac{2\Delta\gamma}{\gamma} \sim 10^{-3}$$

Spectral width of pulsed laser  $\Delta\omega / \omega = 2\pi / \omega\tau \approx 0.35\%$

$$\omega_x(\omega) \approx \omega_{x0} \left( 1 + \frac{\Delta\omega}{\omega} \right) \Rightarrow \frac{\Delta\omega_x(\omega)}{\omega_{x0}} = \frac{\Delta\omega}{\omega} \sim 10^{-3}$$

$\frac{\Delta\omega_x(\gamma)}{\omega_{x0}} \sim \frac{\Delta\omega_x(\omega)}{\omega_{x0}}$
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The same energy width corresponds of X-ray emission angle  $\theta \sim 1$  mrad

$$\frac{\Delta\omega_x}{\omega_x} = \sqrt{\left( \frac{2\Delta\gamma}{\gamma} \right)^2 + \left( \Delta\theta_i \tan \frac{\theta_i}{2} \right)^2 + \left( \frac{\Delta\omega}{\omega} \right)^2} + \text{Nonlinear\_Effects}$$

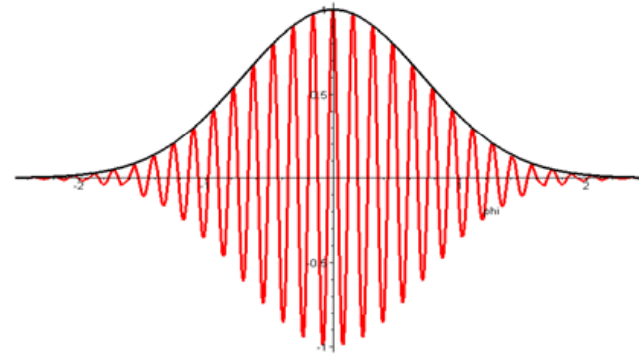
## Compton backscattering process. Accounting of a pulse character of the laser field

Conservation law  $p_i + \hbar k = p_f + \hbar k_x$

Four-potential of pulsed laser wave

$$A_{pul}^{\mu}(\varphi) = g\left(\frac{\varphi}{\omega\tau}\right) A_{mon}^{\mu}(\varphi)$$

Quasi-monochromatic condition  $N_{pul} = \frac{\omega\tau}{2\pi} \gg 1$



Here  $\varphi$  is the laser-wave phase,  $A_{mon}^{\mu}(\varphi)$  is four-potential of plane monochromatic wave, the function  $g(\varphi/\omega\tau)$  is envelope function of the four-potential of an external wave, that allows us to take into account the pulsed character of a laser field.

Klein -Nishina formula can be summarized in the case, when an external laser field has a pulsed character. The energy of X-ray photon has a finite spectral width even at the fixed emission angle. The differential probability of one-photon Compton backscattering :

$$\frac{dW}{dW_{KN}} = N_{pul} \frac{\tau}{\tau_e} \int_0^{\tau_e/\tau} d\xi \cdot g(\xi) \int_{-\infty}^{\infty} d\xi' \cdot g(\xi') \cos\left(\tau(\omega_x + E_f - E_i - \omega)(\xi' - \xi)\right)$$

## Compton backscattering process. Accounting of a pulse character of the laser field

For the ThomX project typical laser parameters are:  $\hbar\omega=1.23$  eV,  $\tau=1$  ps, and the electron beam parameters are:  $E_i=50$  MeV ( $\gamma\approx 100$ ),  $\tau_e=20$  ps.

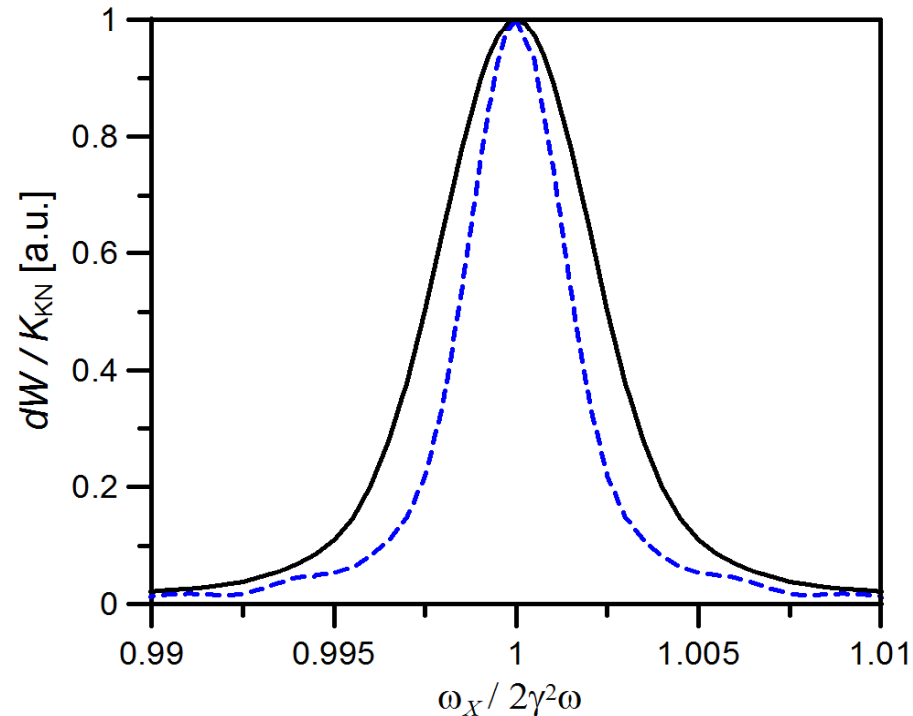


Figure. Broadening of X-ray spectrum caused by a pulsed character of laser field for the ThomX typical laser pulse and the electron beam parameters. The emission angle  $\theta=1/\gamma$ .

Solid line corresponds to the envelope function in the form of Gaussian function

$$g(\xi) = \exp(-\xi^2), \text{ dotted line corresponds to Lorentz function } g(\xi) = (1 + \xi^2)^{-1}.$$

**Thank you for attention!**