

The proton radius from atomic/molecular spectroscopy : Current status and perspectives

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4 research axes

- Quantum gases
- Atoms and light in dense or complex media
- Quantum optics and quantum information
- Test of fundamental interactions and metrology

2 research teams

International collaborations

Metrology of simple systems and fundamental tests

H atom spectroscopy $\rightarrow R_\infty, r_p$
(F. Nez)

Heavy ions and exotic ions
(P. Indelicato)

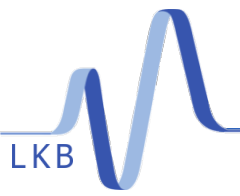
Atom interferometry $\rightarrow \alpha$
(S. Guellati, P. Cladé)

CREMA
(Muonic Atom spectroscopy)

Metrology of trapped ions

H_2^+ spectroscopy
(L. Hilico) $\rightarrow m_p / m_e$
HMI theory R_∞, r_p
(JPK)

GBAR
(Gravitational Behaviour of Anti-hydrogen at Rest)



I. Introduction

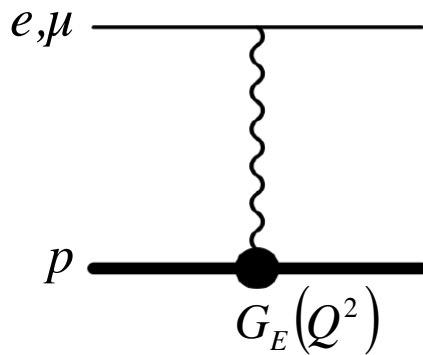
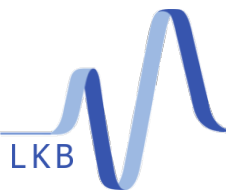
Atomic energy levels, and the proton radius

II. Current status of the “puzzle”

After recent measurements in hydrogen

III. New experiments

Focus on the hydrogen molecular ions



The proton radius is defined as

$$r_p^2 \equiv -6 \left. \frac{dG_E}{dQ^2} \right|_{Q^2=0}$$

G_E : Sachs electric form factor

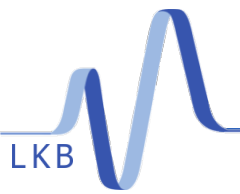
- Modification of the Coulomb potential w.r.t. a point-like proton:

$$\delta V(\mathbf{r}) = -4\pi\alpha \int \frac{d^3q}{(2\pi)^3} \frac{[G_E(\mathbf{q}^2) - 1] e^{-i\mathbf{q}\cdot\mathbf{r}}}{\mathbf{q}^2}$$

Leading order: $G_E(\mathbf{q}^2) - 1 \approx -\frac{\mathbf{q}^2 r_p^2}{6}$ In atomic physics: $r_p q \sim r_p / a_0 \sim 10^{-5}$



$$\delta V(\mathbf{r}) = \frac{2\pi\alpha}{3} r_p^2 \delta(\mathbf{r})$$



Shift of an atomic bound state: $\Delta E = \langle \psi | \delta V | \psi \rangle = \frac{2}{3} \pi \alpha |\psi(0)|^2 r_p^2$

Hydrogen-like atom, nl state:

$$\Delta E = \frac{2\alpha^4}{3n^3} m_r^3 r_p^2 \delta_{l0}$$

Orders of magnitude

Hydrogen atom, 1S state: $\Delta E / h \approx 1.2 \text{ MHz} \approx \mathbf{5 \cdot 10^{-10}}$ ν_{1S-2S}

Exp. accuracy $\approx 10 \text{ kHz} \Rightarrow \approx \mathbf{1\%}$ on r_p

Muonic hydrogen, 2S state: $\Delta E / h \approx 0.96 \text{ THz} \approx \mathbf{2\%}$ of ν_{2S-2P}

Exp. / theor. accuracy $\approx 0.5 \text{ GHz} \Rightarrow \approx \mathbf{5 \cdot 10^{-4}}$ on r_p

- Main dependences on fundamental constants

$$E_{n,l,j} = hcR_\infty \left[\underbrace{-\frac{1}{n^2} \frac{1}{1+1/\mu_{pe}}}_{\text{Schrödinger}} + \underbrace{\alpha^2 A(n,l,j)}_{\text{Relativistic and QED corr.}} + \underbrace{\frac{4}{3n^3} \left(\frac{r_p}{a_0}\right)^2 \delta_{l0}}_{\text{Finite nuclear size corr.}} + \dots \right]$$

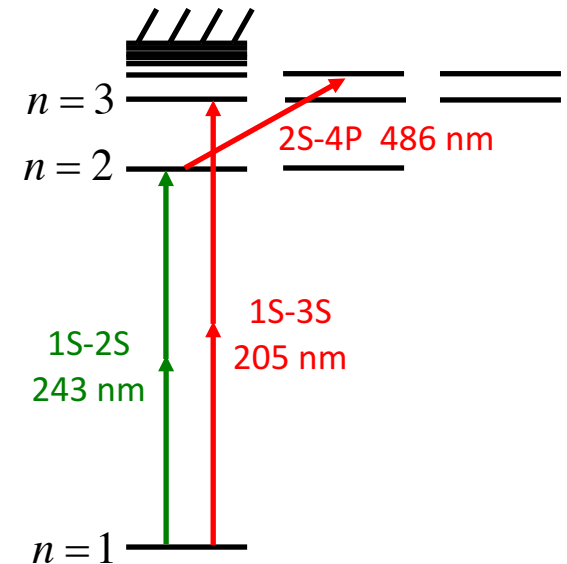
- $\mu_{pe} = m_p / m_e$ and α determined by other experiments

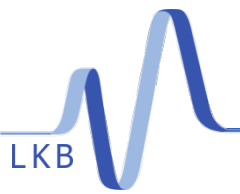
- 2 measurements required to determine R_∞ and r_p

➤ A **single** narrow transition: 1S-2S ($\Delta\nu = 1.3$ Hz) measured with high accuracy.

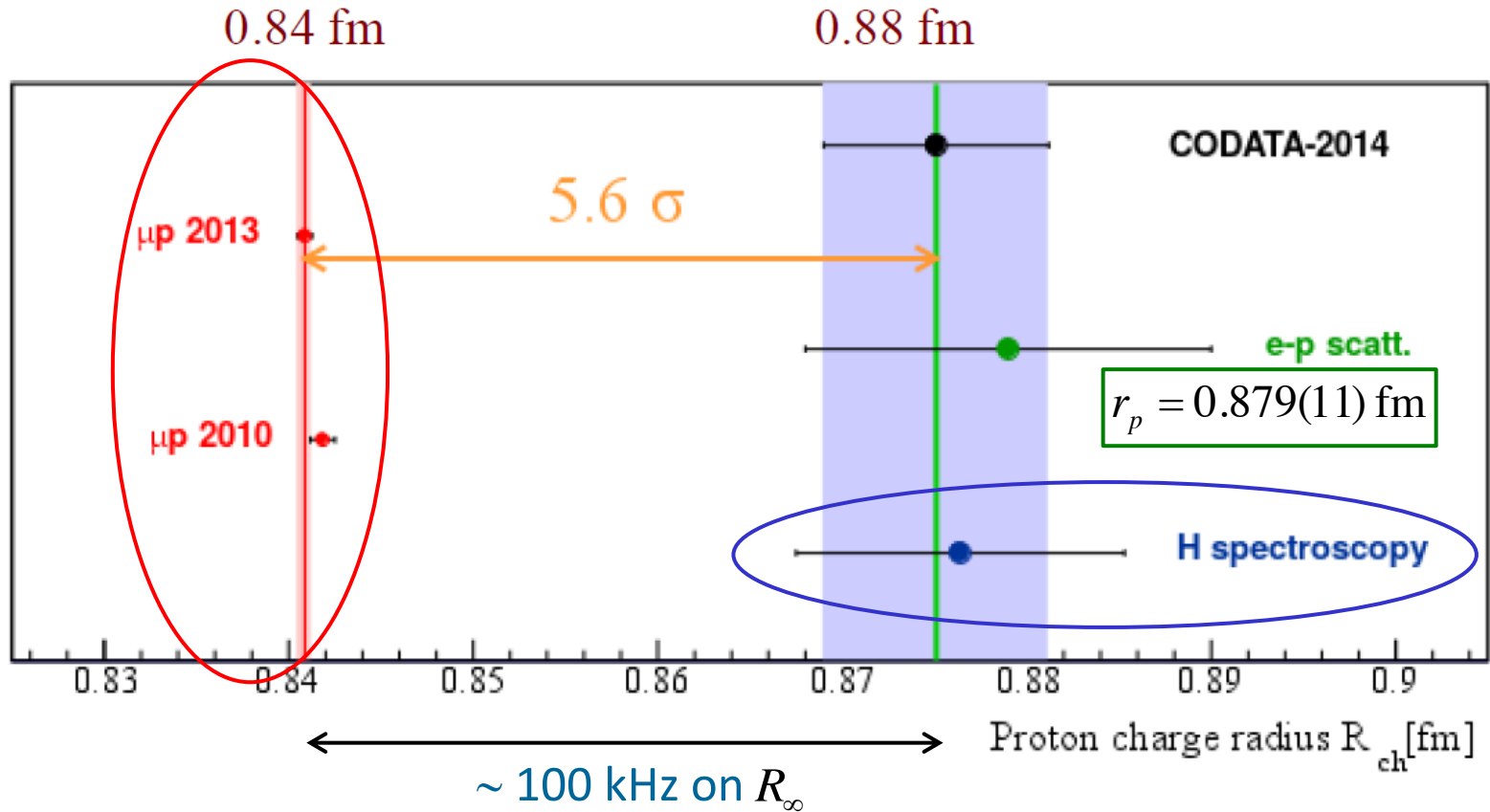
➤ Other transitions: natural width \sim MHz.

Each measurement, **combined with 1S-2S**, yields a **correlated pair** (R_∞, r_p) .





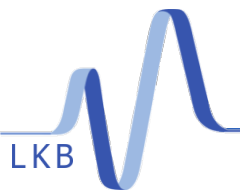
The proton-radius puzzle



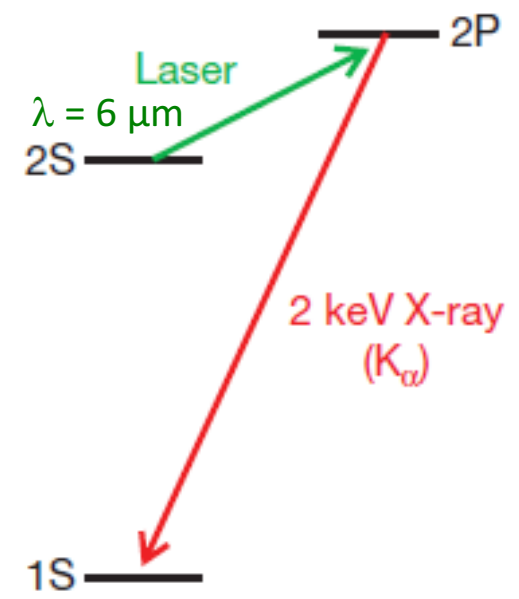
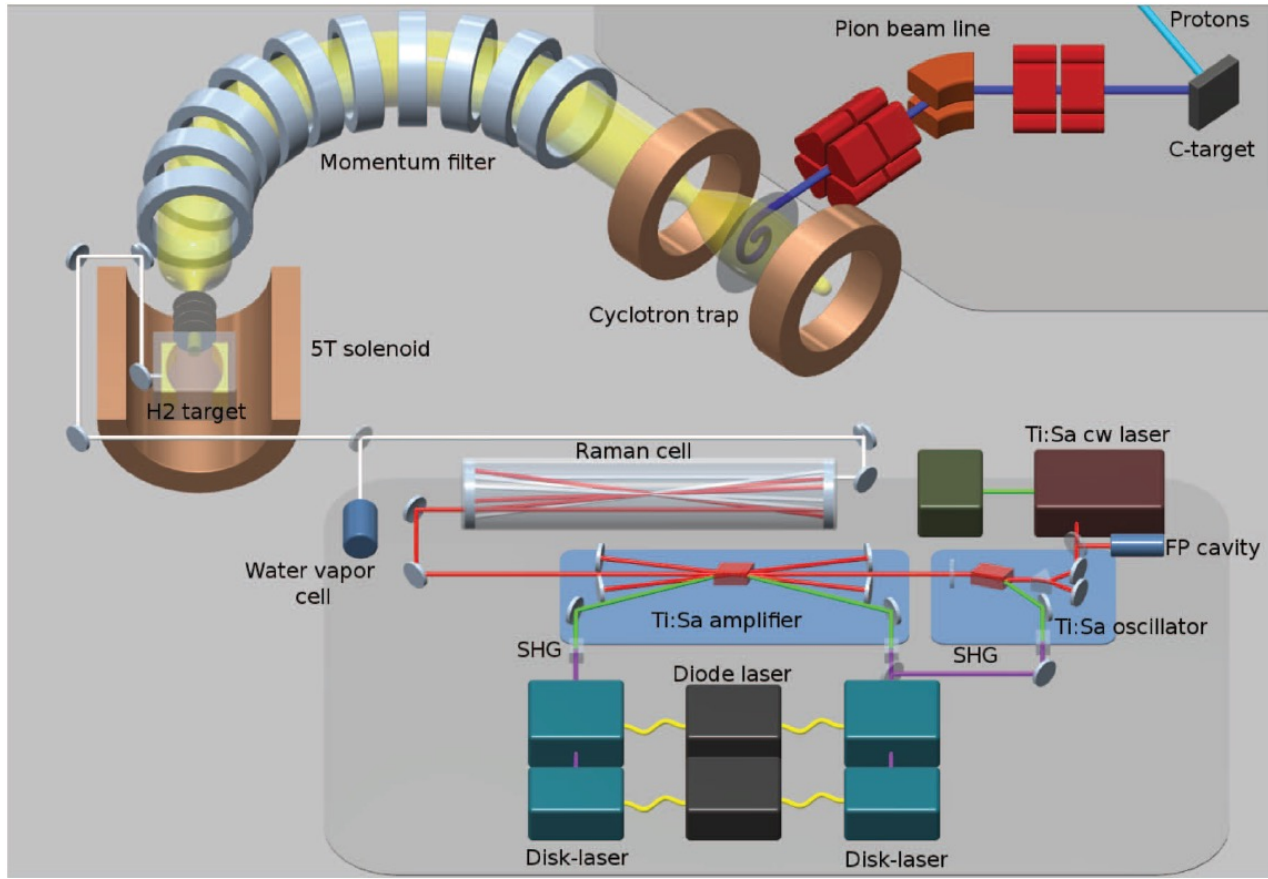
CODATA 2014: P.J. Mohr, D.B. Newell, and B.N. Taylor, Rev. Mod. Phys. **88**, 035009 (2016)

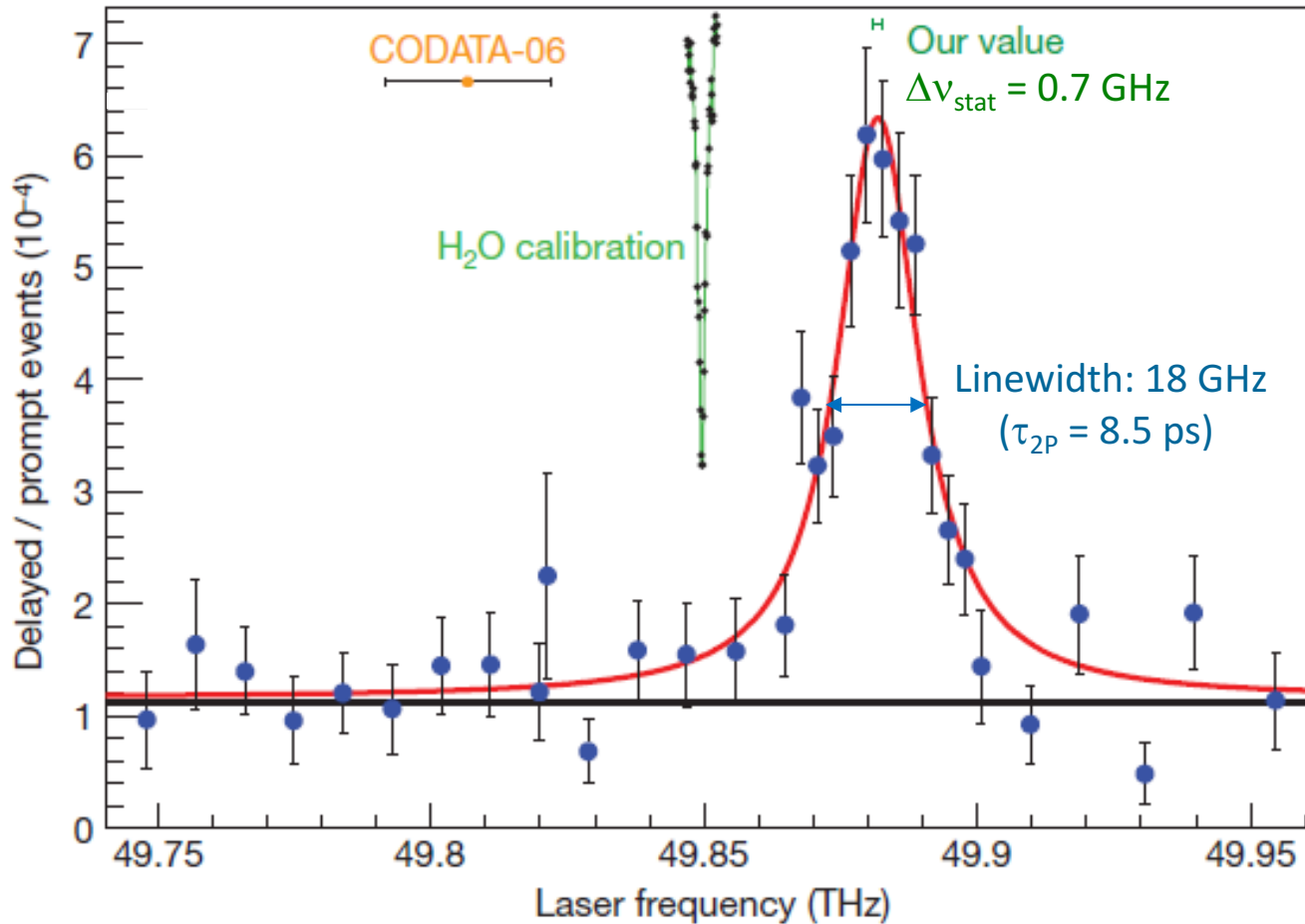
e-p scattering: J. Arrington and I. Sick., J. Phys. Chem. Ref. Data 44, 031204 (2015)

- 1) μp spectroscopy
- 2) H spectroscopy



Muonic hydrogen spectroscopy at PSI

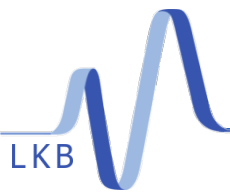




$$r_p = 0.84087(39) \text{ fm}$$

R. Pohl et al., Nature **466**, 213 (2010)

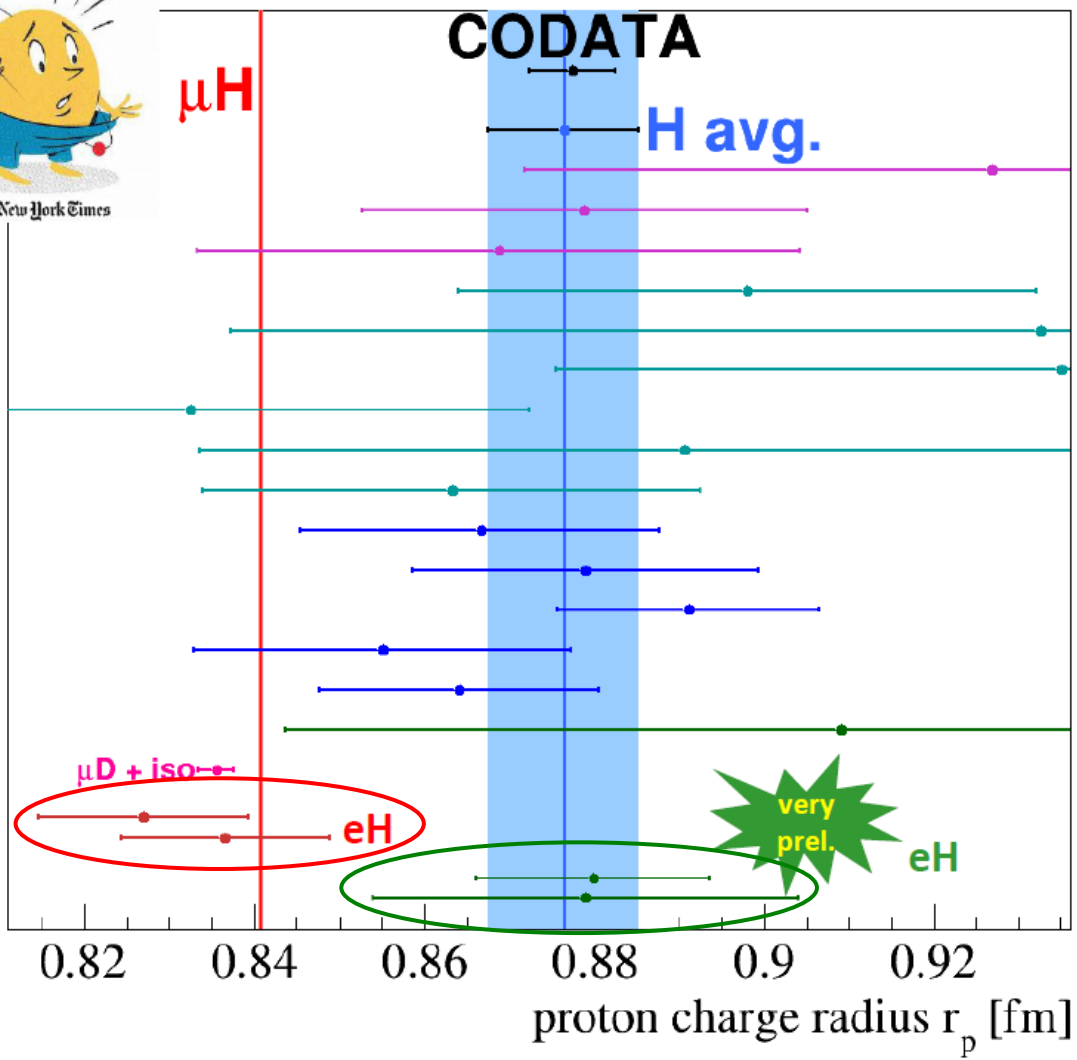
A. Antognini et al., Science **339**, 417 (2013)

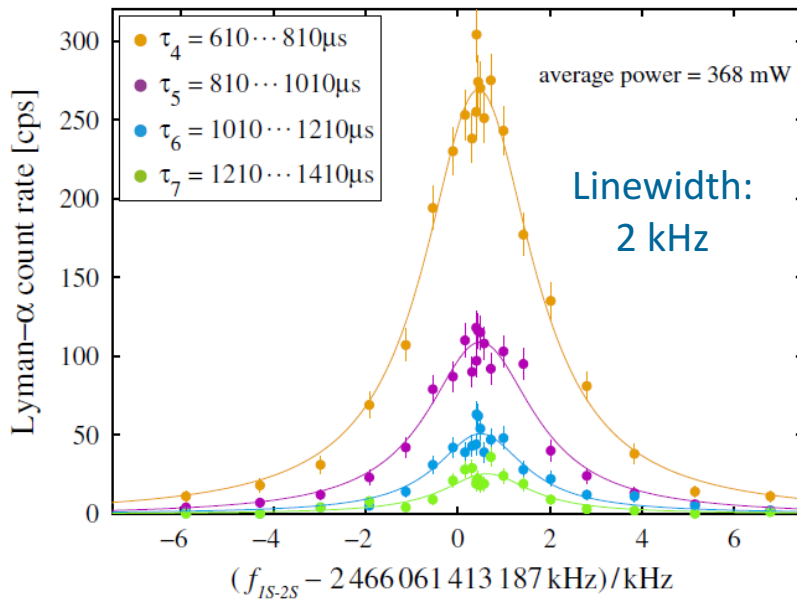
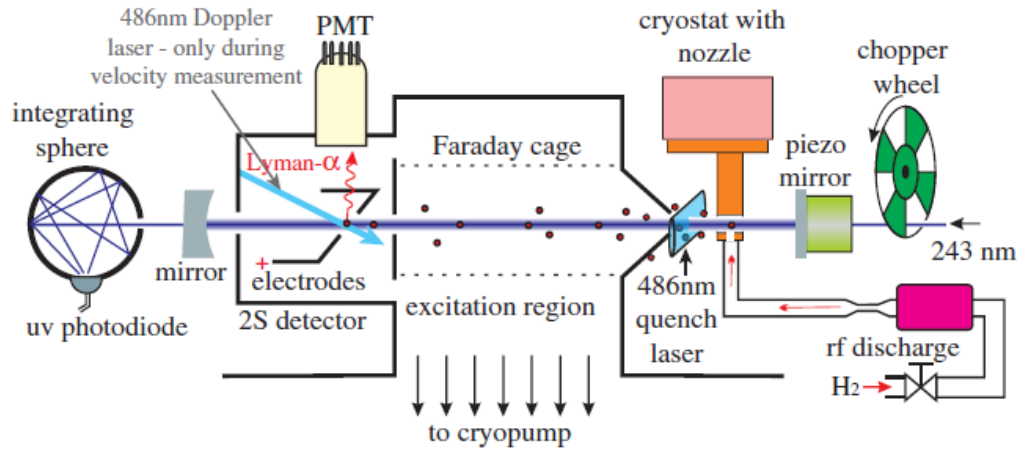


H atom spectroscopy



- 2S → 2P_{1/2}
- 2S → 2P_{1/2}
- 2S → 2P_{3/2}
- 1S → 2S + 2S → 4S_{1/2}
- 1S → 2S + 2S → 4D_{5/2}
- 1S → 2S + 2S → 4P_{1/2}
- 1S → 2S + 2S → 4P_{3/2}
- 1S → 2S + 2S → 6S_{1/2}
- 1S → 2S + 2S → 6D_{5/2}
- 1S → 2S + 2S → 8S_{1/2}
- 1S → 2S + 2S → 8D_{3/2}
- 1S → 2S + 2S → 8D_{5/2}
- 1S → 2S + 2S → 12D_{3/2}
- 1S → 2S + 2S → 12D_{5/2}
- 1S → 2S + 1S → 3S_{1/2}
- NEW** 1S → 2S + 2S → 4P_{1/2}
- NEW** 1S → 2S + 2S → 4P_{3/2}
- NEW** 1S → 2S + 1S → 3S_{3/2}



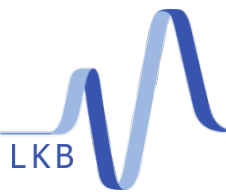


$$f_{1S-2S} = 2\,466\,061\,413\,187\,035\ (10)\ \text{Hz}$$

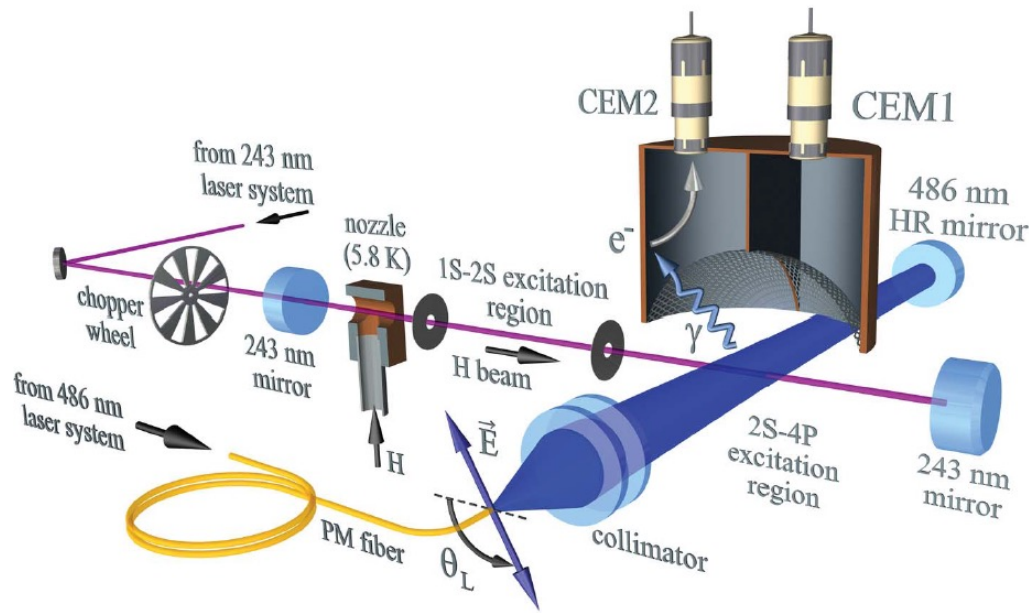
C.G. Parthey et al., PRL **107**, 203001 (2011)

$$f_{1S-2S} = 2\,466\,061\,413\,187\,018\ (11)\ \text{Hz}$$

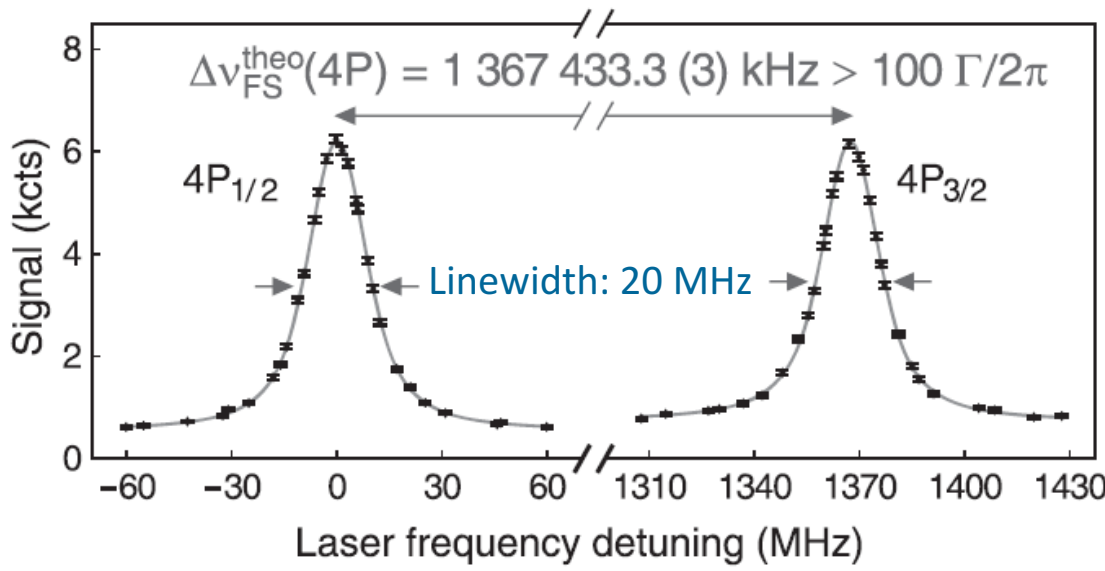
A. Matveev et al., PRL **110**, 230801 (2013)



- Determine the center of a line to a small fraction (10^{-3} - 10^{-4}) of its width
- High statistics
- Precise understanding of lineshape and systematic effects:
 - 1st or 2nd-order Doppler effect: velocity distribution in atomic beam
 - AC Stark shift (especially for two-photon transitions)
 - Pressure (collision) shift
 - Quantum interference effect
 - ...

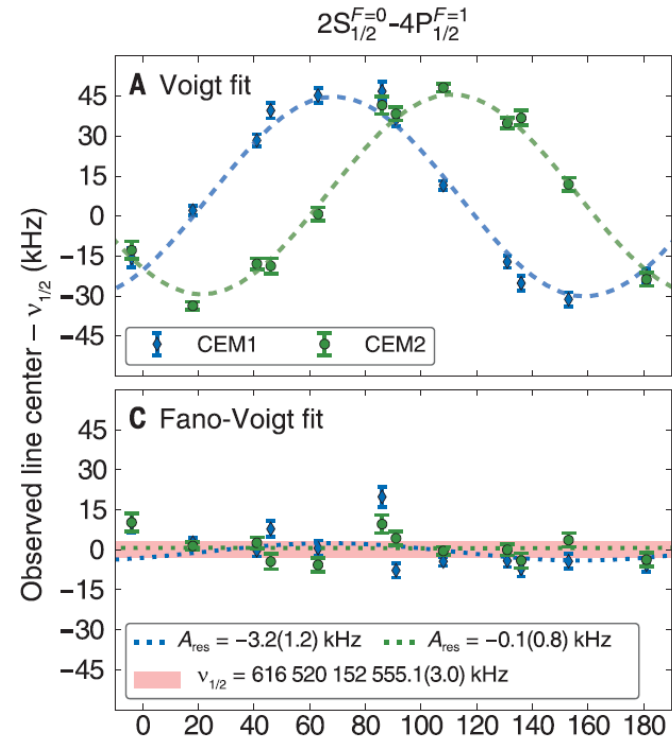
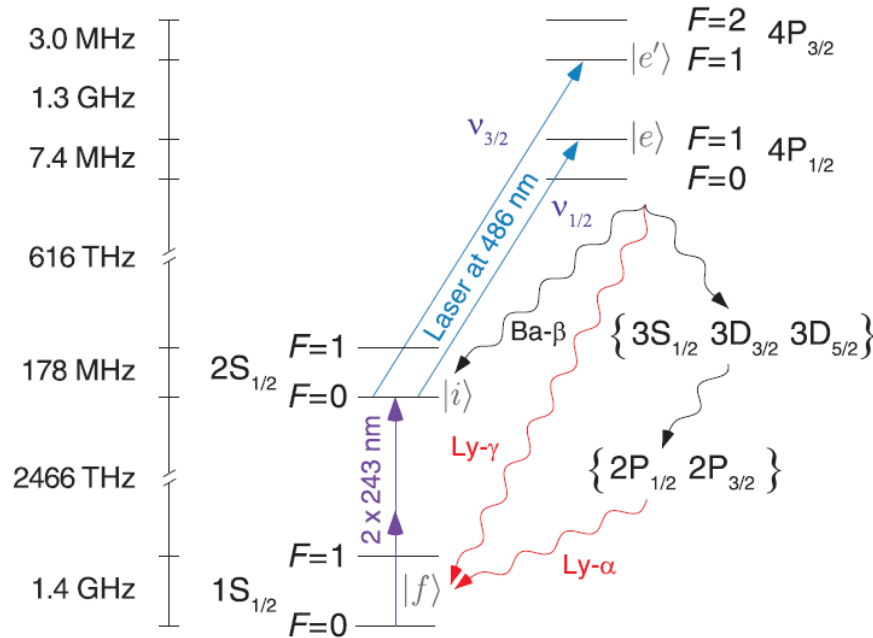


- Cold (5.8 K) H(2S) atoms
- Single hyperfine level populated: $2S_{1/2} F=0$



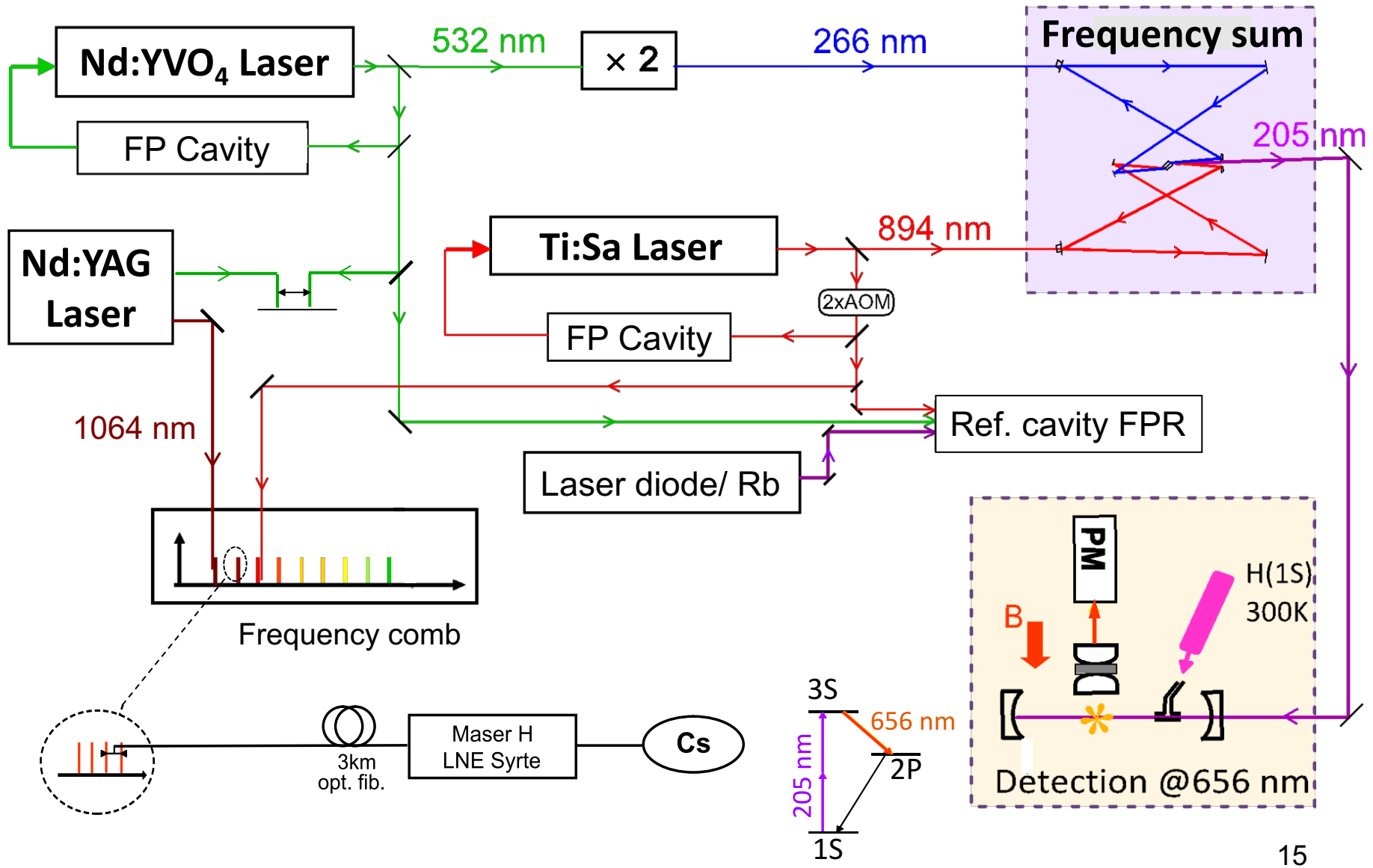
- Natural linewidth: 12.9 MHz
- + Doppler broadening, power broadening

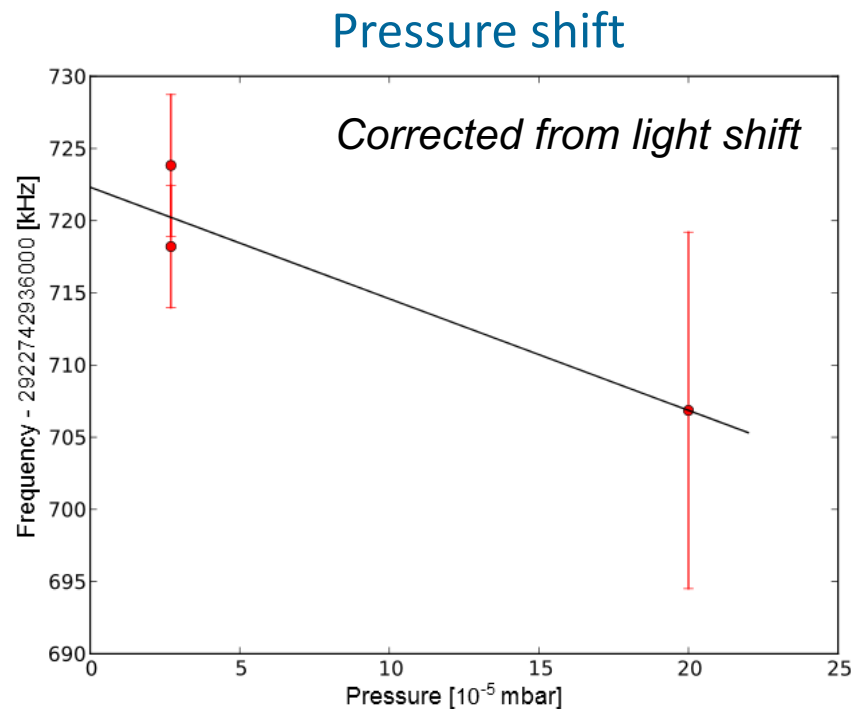
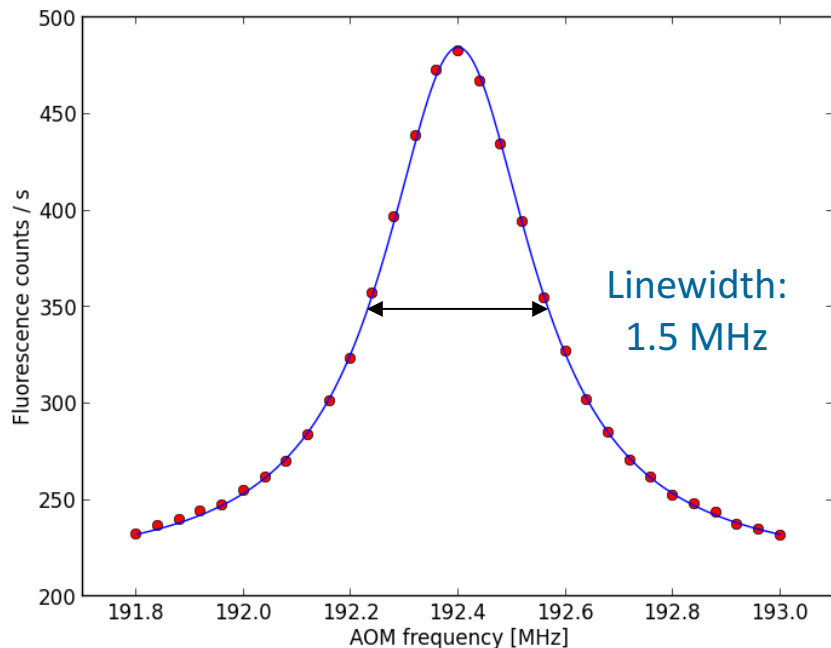
Quantum interference effect



$$f_{2S-4P} = 616\,520\,931\,626.8(2.3) \text{ kHz} \quad \Delta f \sim 10^{-4} \Gamma !$$

Main source of uncertainty: 1st-order Doppler shift





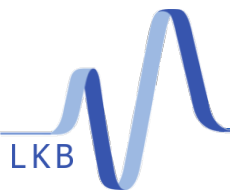
$$f_{1S-3S} = 2\,922\,743\,278\,xxx.x (2.4) \text{ kHz}$$

S. Galtier et al., J. Phys. Chem. Ref. Data **44**, 031201 (2015)

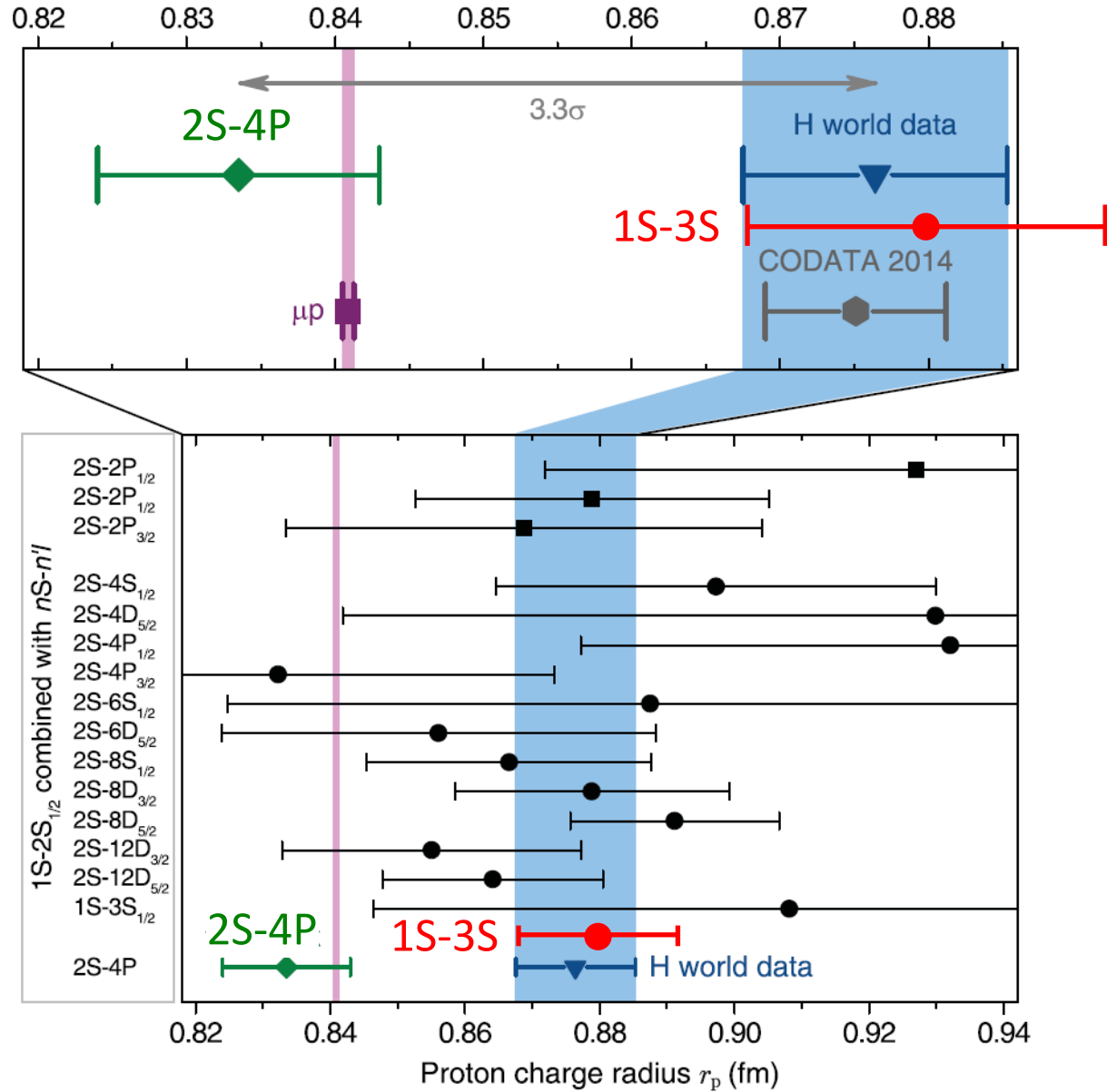
QI effect: H. Fleurbaey, F. Biraben, L. Julien, JPK, F. Nez, PRA **95**, 052503 (2017)

H. Fleurbaey et al., *in preparation*

➤ Next step : cold (77K) H beam



Overview



“To summarize, the possibilities are:

1. The **electronic hydrogen experiments** are almost, but not quite, as accurate as stated.
2. The **QED calculations in μp** are almost, but not quite, as accurate as stated.
3. The two-photon exchange term that depends on **proton polarizability** has not been correctly evaluated.
4. The electron and the muon really do have different interactions with the proton so there is **physics beyond the Standard Model**.

None of these possibilities seem very likely, but all must be pursued.”

R. Pohl et al., Annu. Rev. Nucl. Part. Sci. **63**, 175 (2013)

C.E. Carlson, Progr. Part. Nucl. Phys. **82**, 59 (2015)

*“Beyer et al. do not claim to have solved the proton-size puzzle. After all, it is only one measurement, and the data analysis was very complicated. Moreover, one would need to understand why other measurements in hydrogen are so far off or, possibly, exhibit a systematic shift in the same direction. There is presently no explanation for that. Also, the proton size deduced from electron-proton scattering disagrees. **Thus, more measurements are what is needed.**”*

W. Vassen, Science (Perspective) **358**, 39 (2017)

➤ Hydrogen-like systems

electronic

2S-2P in **H** (YU Toronto) $\Rightarrow r_p$

1S-2S in **He⁺** (VU Amsterdam + MPQ Garching) $\Rightarrow R_\infty, r_\alpha$

Rydberg states in High-Z ions (NIST Gaithersburg) $\Rightarrow R_\infty$

muonic

2S-2P in **μ He⁺** (PSI) $\Rightarrow r_\alpha$

leptonic

1S-2S in **Positronium** e^+e^- (ETH Zürich + UC London) $\Rightarrow R_\infty$

1S-2S in **Muonium** μ^+e^- (PSI + ETH Zürich) $\Rightarrow \mu$ -specific forces ?

➤ One-electron molecules $\Rightarrow R_\infty, r_p, m_p / m_e (+r_d, m_d / m_e)$
H₂⁺ / HD⁺ (VU Amsterdam + Düsseldorf + LKB Paris)

➤ Two-electron atoms

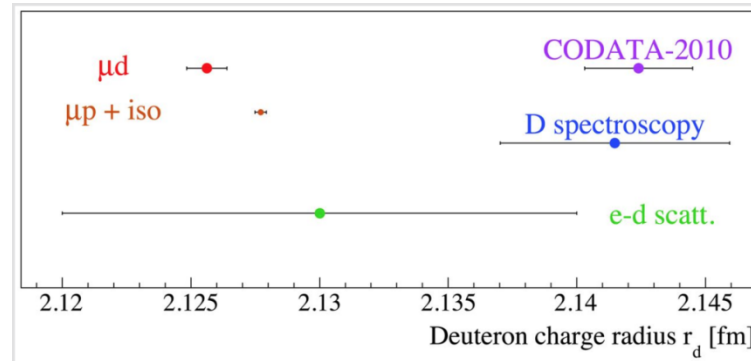
He (VU Amsterdam + Hefei) $\propto r_\alpha$

➤ Two-electron molecules $\Rightarrow R_\infty, r_p, m_p / m_e (+r_d, m_d / m_e)$
H₂ / HD (VU Amsterdam + ETH Zürich)

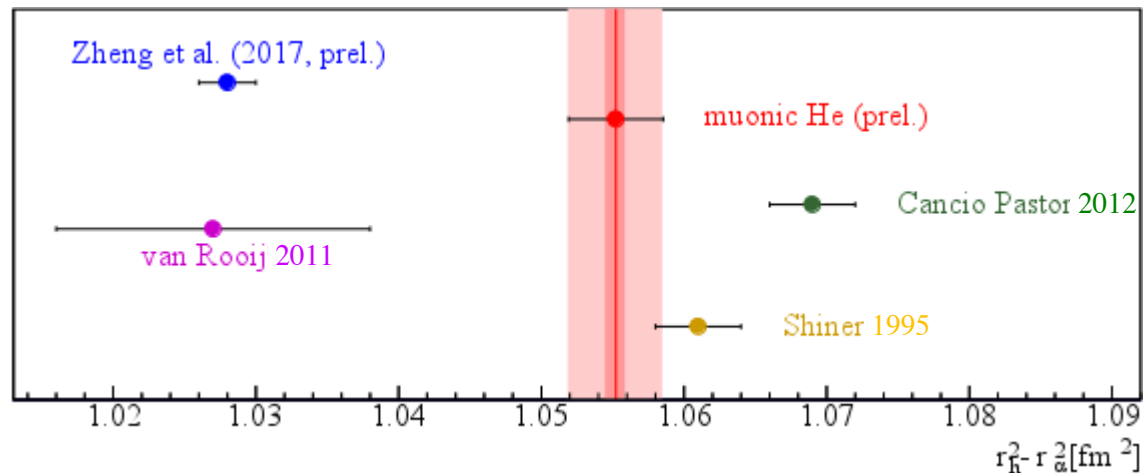
➤ Muonic Li, Be ... (JGU Mainz + PSI)

D / μ D
 discrepancy

Deuteron radius



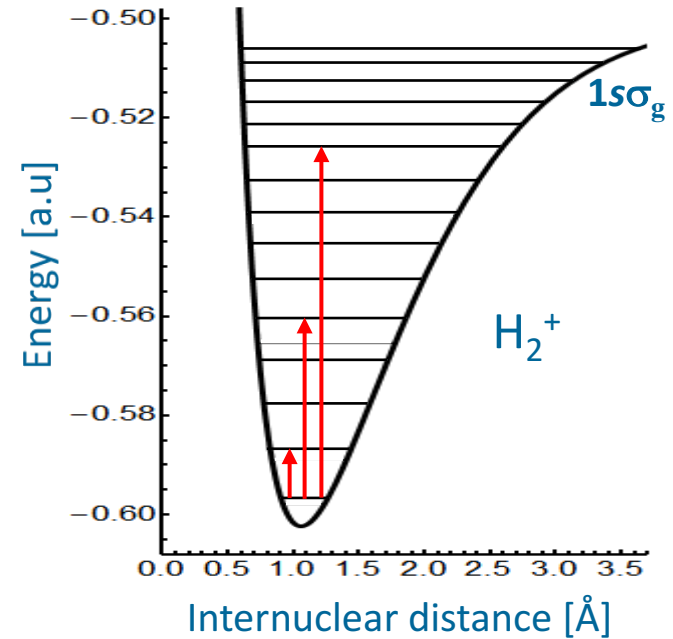
$^3\text{He}/^4\text{He}$ isotope shift (preliminary)



Another $>5\sigma$ discrepancy ?

Dependence of **ro-vibrational transition frequencies** on fundamental constants :

$$\nu = cR_\infty \left[\varepsilon_{nr} \mu_n + \alpha^2 F_{QED}(\alpha) + \sum_n A_n^{fs} (r_n/a_0)^2 \right]$$



1. Strong dependence on μ_n : $\varepsilon_{nr} \propto 1/\sqrt{m_r}$

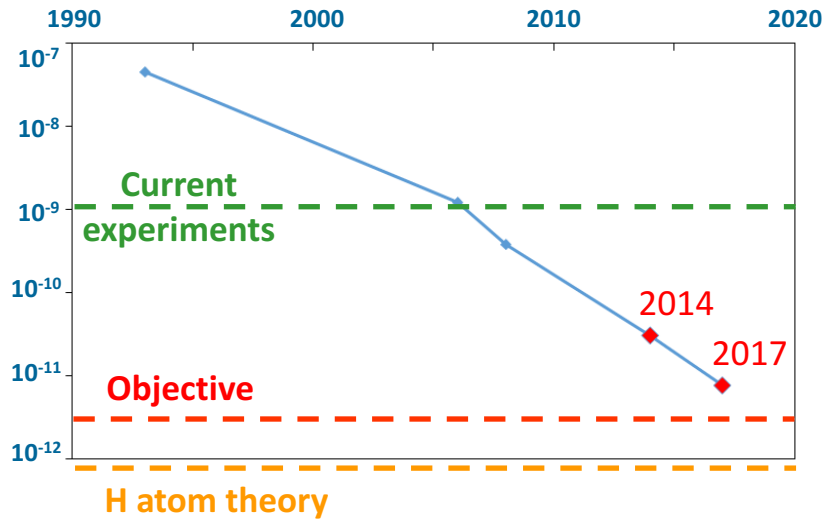
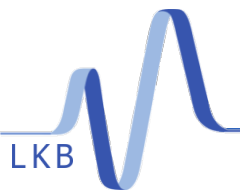
⇒ Determination of μ_{pe} and μ_{dp} by laser spectroscopy of H_2^+/HD^+

W.H. Wing, G.A. Ruff, W.E. Lamb Jr., J.J. Spezeski, PRL **36**, 1488 (1976)

2. *All* ro-vibrational transitions in $1s\sigma_g$ electronic state are *very narrow*

⇒ Measuring **several transitions** in H_2^+/HD^+ could provide a reliable determination of R_∞ , r_p , r_d , cross-checking H/D results and shedding light on the proton-radius puzzle.

J.Ph. Karr, L. Hilico, J.C.J. Koelemeij, V.I. Korobov, PRA **94**, 050501(R) (2016)



$H_2^+ (v = 0, L=0) \rightarrow (v'=1, L'=0)$ interval in kHz

ν_{nr}	65 687 511 047.0
ν_{α^2}	1091 040.5
ν_{α^3}	-276 545.1
ν_{α^4}	-1952.0(1)
ν_{α^5}	121.8(1)
ν_{α^6}	-2.3(5)
ν_{tot}	65 688 323 710.1(5)(29)(11)

Theoretical uncertainty
 $7.6 \cdot 10^{-12}$

Uncert. on μ_{pe}

Discrepancies on R_∞ and r_p

V.I. Korobov, L. Hilico, J.-Ph. Karr, PRL **118**, 233001 (2017)

- Further improvement by a factor of 2-3 would allow **discriminating** between conflicting measurements of R_∞, r_p, r_d from a well-chosen set of ro-vibrational transitions.

One-photon ro-vibrational transitions in HD⁺

- Sympathetic cooling by laser-cooled Be⁺ (T~10 mK)
- Detection by selective dissociation of the excited state (REMPD)
- Measurement of HD⁺ ion number by motional excitation

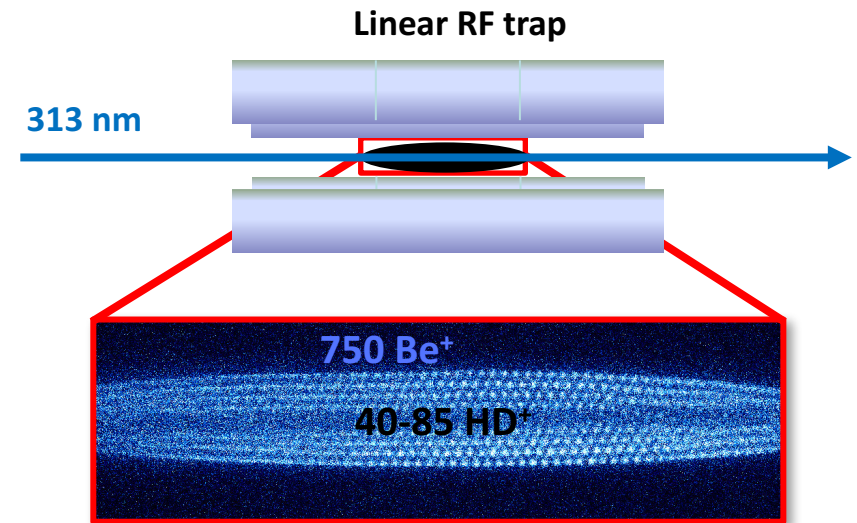
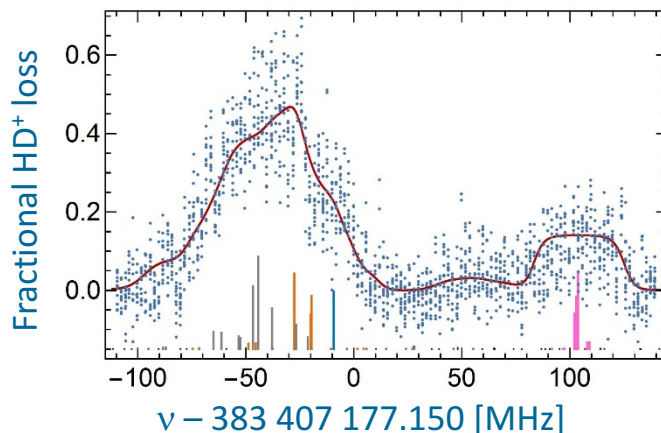


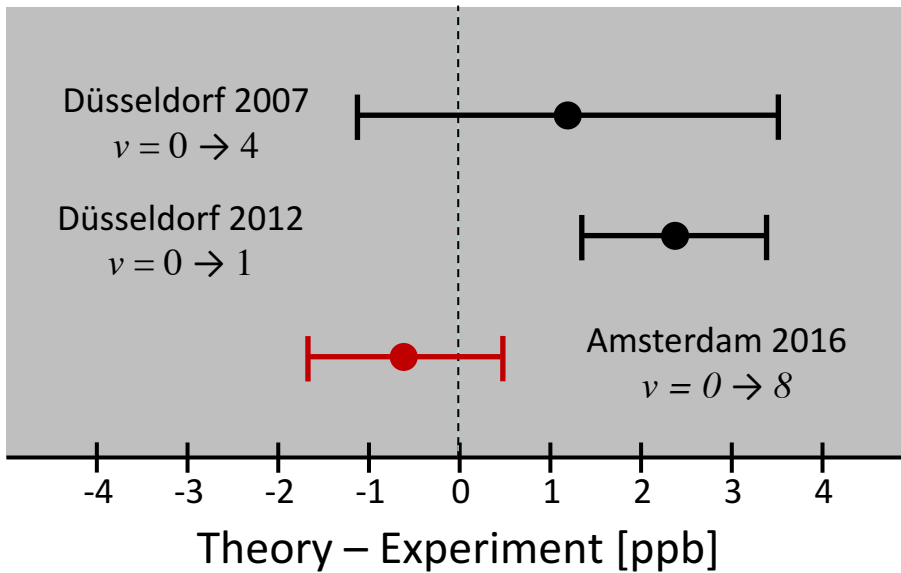
Image: J.C.J. Koelemeij (VU Amsterdam)

HD⁺ $\nu = 0 \rightarrow 8$ transition



Main limitation: Doppler broadening

J.Biesheuvel, J.-Ph. Karr, L. Hilico, K.S.E. Eikema, W. Ubachs, J.C.J. Koelemeij, *Nature Comm.* **7**, 10385 (2016)

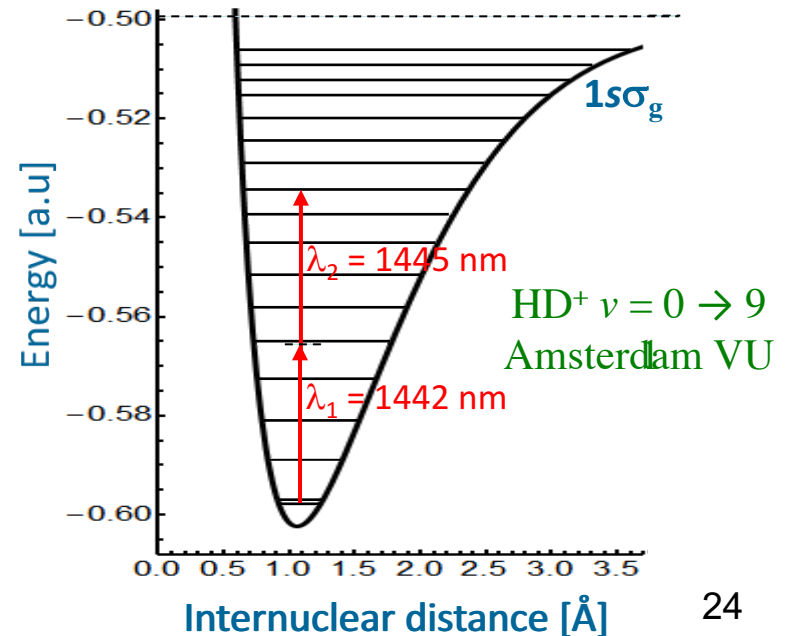


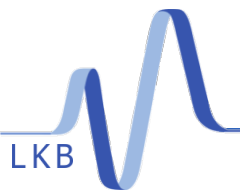
⇒ Determination of μ_{pe}
with 2.5 ppb accuracy

S. Patra, J.-Ph. Karr, L. Hilico,
M. Germann, V.I. Korobov, J.C.J. Koelemeij,
arXiv:1710.11537, to appear in J. Phys. B

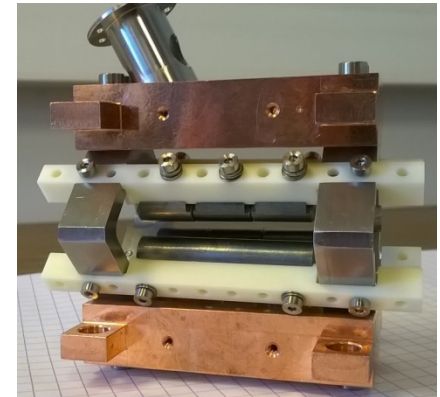
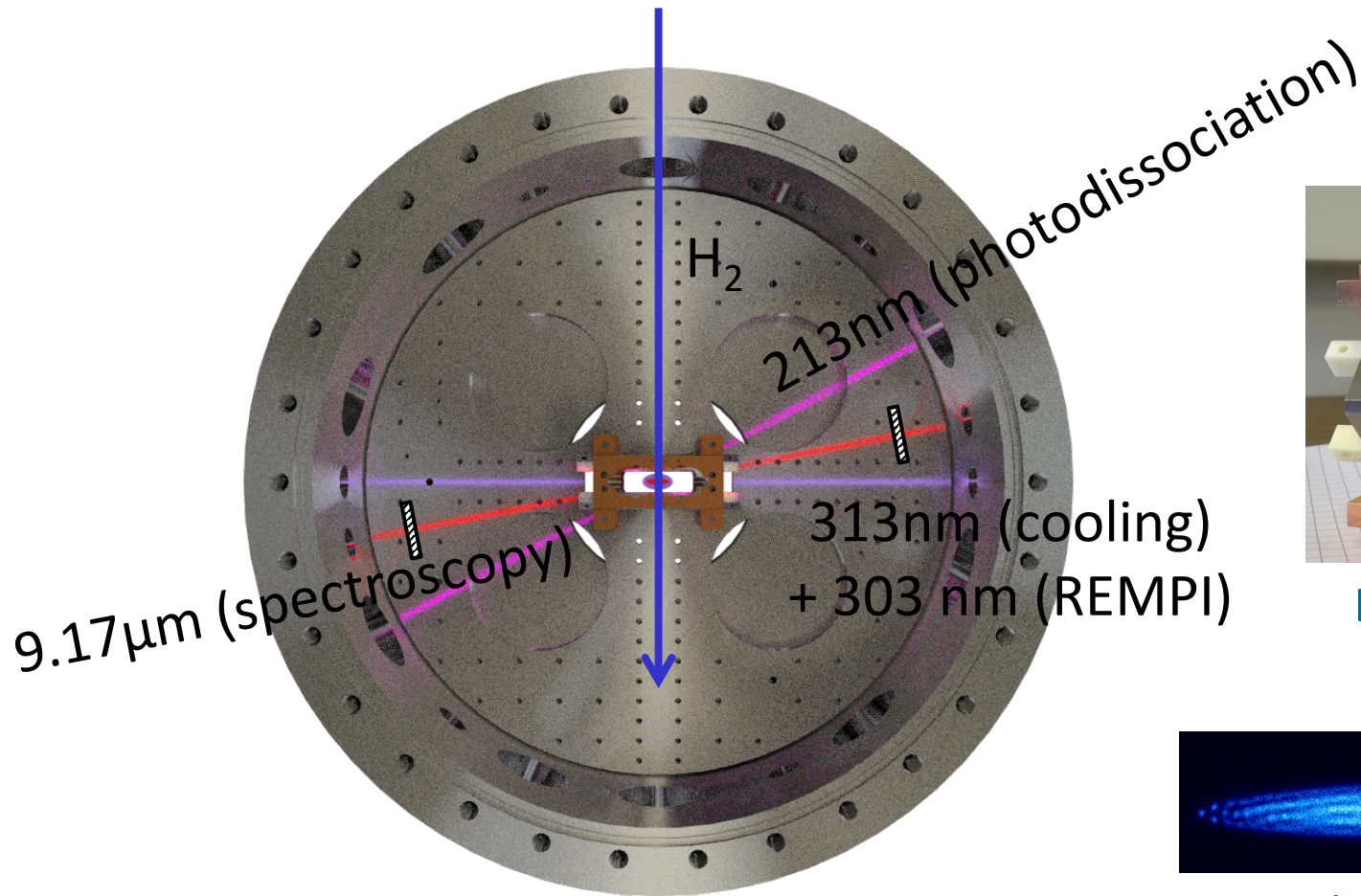
Next step:

**Doppler-free two-photon
transitions**
Goal accuracy : 10^{-12}

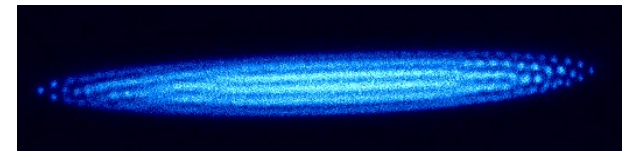




H₂⁺ two-photon spectroscopy setup

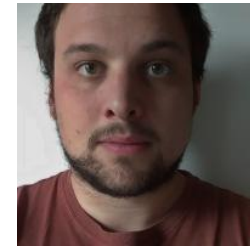
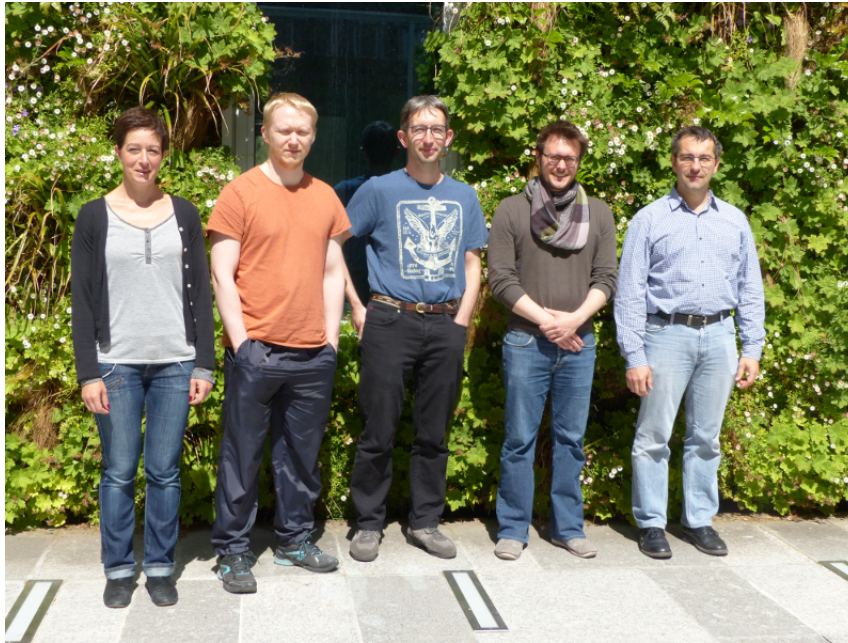


Linear ion trap



Crystal of laser-cooled Be⁺

Albane Douillet Nicolas Sillitoe (PhD) Johannes Heinrich (PhD) Laurent Hilico



Thomas Louvradoux (PhD)



Vladimir Korobov
(JINR, Dubna, Russia)

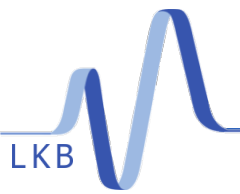
Amsterdam VU



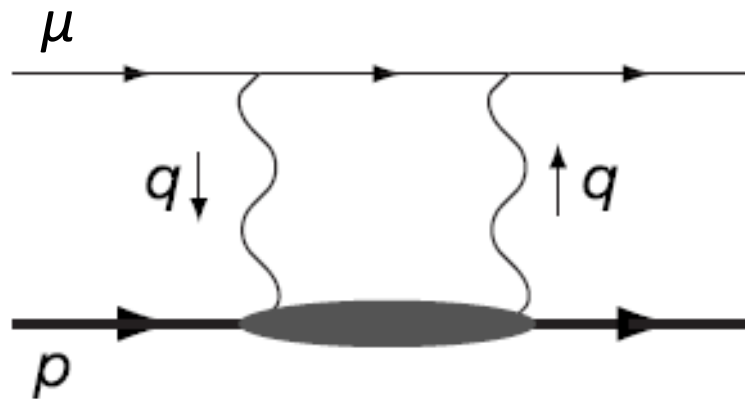
Jeroen Koelemeij

Sayan Patra
Matthias Germann
Juriaan Biesheuvel
Frank Cozijn
Kjeld Eikema
Wim Ubachs

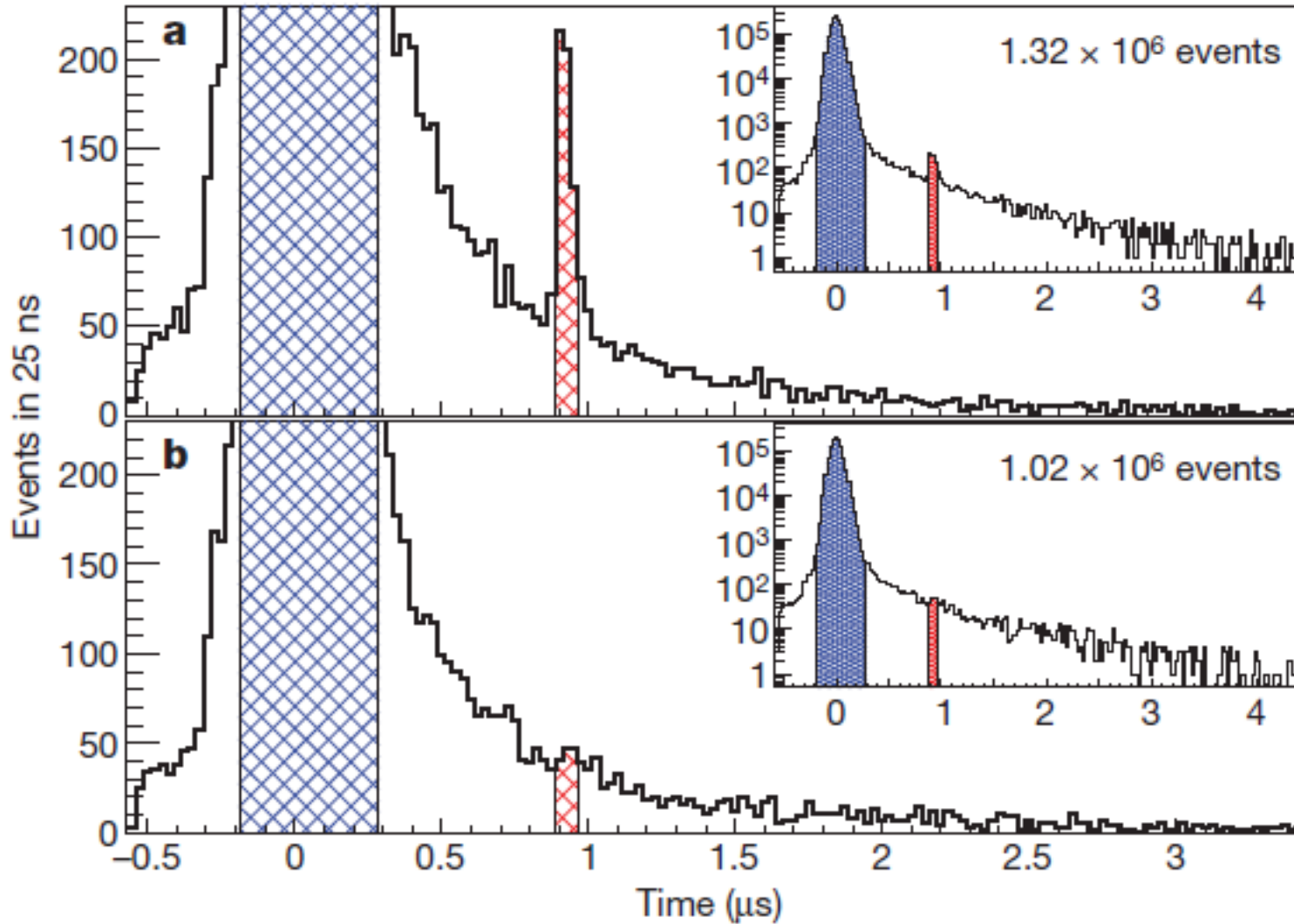


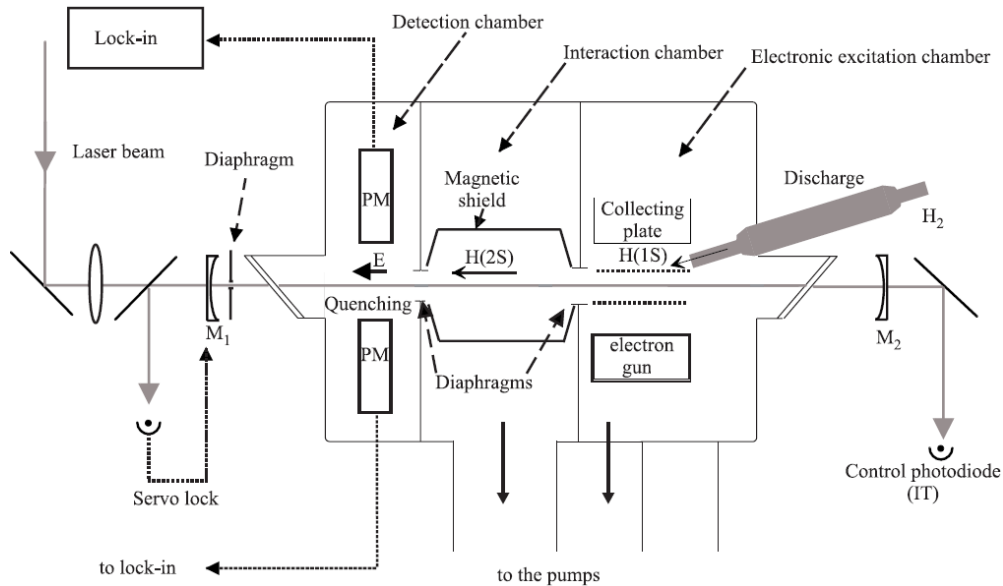


In addition to the leading term, higher-order QED corrections involving the proton structure have to be considered.

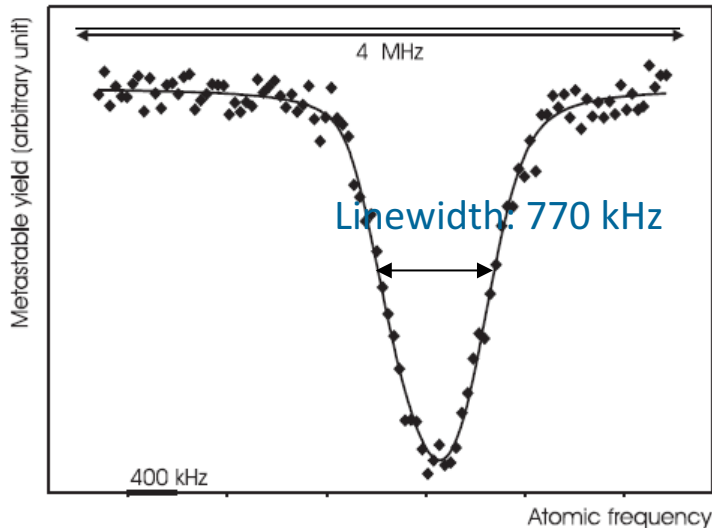


- Two-photon exchange :
- elastic
 - inelastic : **proton polarizability**
 - subtraction of QED correction to proton radius





Example: $2S_{1/2}-8S_{1/2}$



$$f(2S_{1/2}-8S_{1/2}) = 770\,649\,350\,012.0(8.6) \text{ kHz} \\ (+ 4 \text{ other transitions})$$

Main source of uncertainty: AC Stark shift

B. De Beauvoir et al., PRL **78**, 440 (1997) and EPJD **12**, 61 (2000)
 C. Schow et al., PRL **82**, 4960 (1999).