

# NEW OBSERVABLES IN QUARKONIUM PRODUCTION AT PROTON COLLIDERS

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# Part I

## Introduction

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  - 3 COLOUR OCTET MECHANISM (encapsulated in NRQCD): **higher Fock states** of the mesons taken into account;  $Q\bar{Q}$  can be produced in octet states with different quantum # as the meson; bleaching with semi-soft gluons ?

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## 3 COLOUR OCTET MECHANISM

- one non-perturbative parameter per Fock State
- expansion in  $v^2$ ; series can be truncated
- the phenomenology partly depends on this
- HQSS relates some non-perturbative parameters to each others and to a specific quarkonium polarisation

## Part II

# Impact of the QCD corrections to the these models

# QCD corrections to the CSM for $\Upsilon$ at colliders

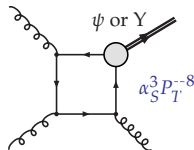
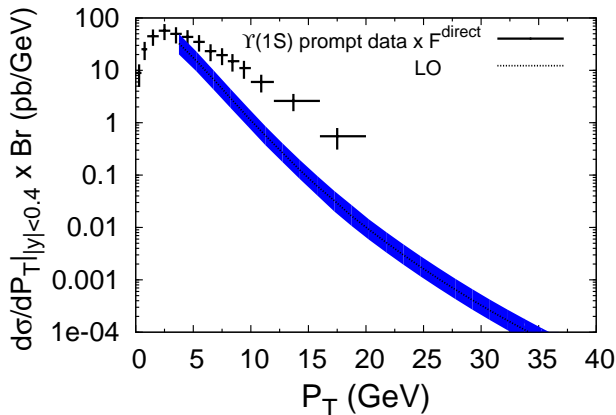


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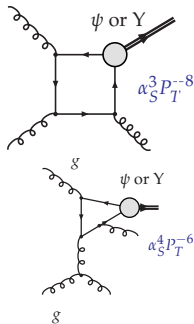
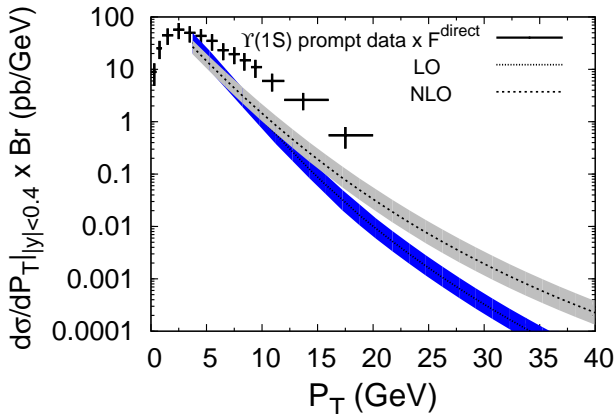


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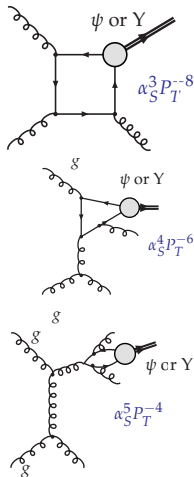
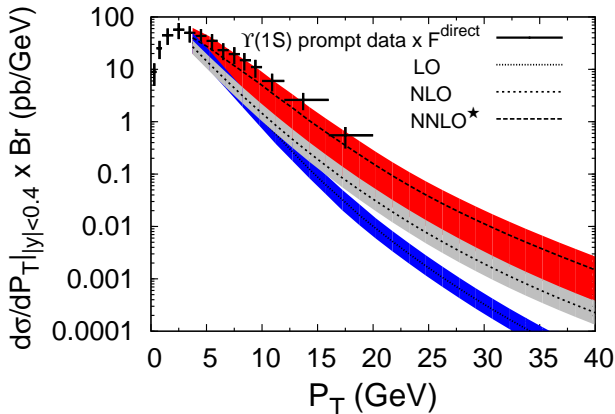
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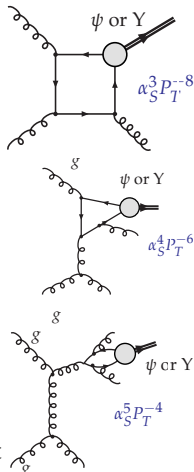
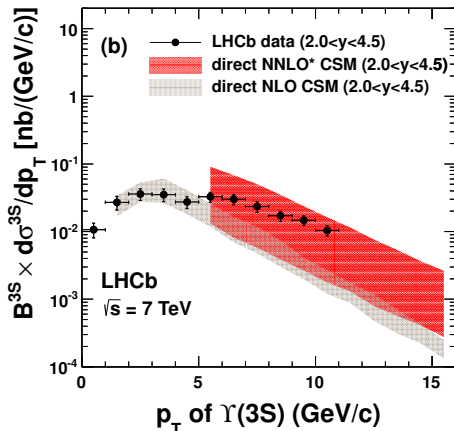
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Attention: the NNLO\* is not a complete NNLO  
 See a recent study by H.S. Shao [arXiv:1809.02369 \[hep-ph\]](https://arxiv.org/abs/1809.02369)

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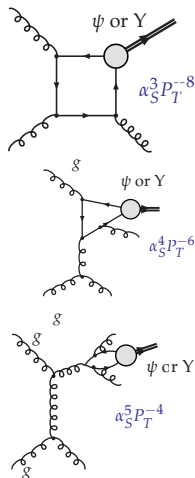
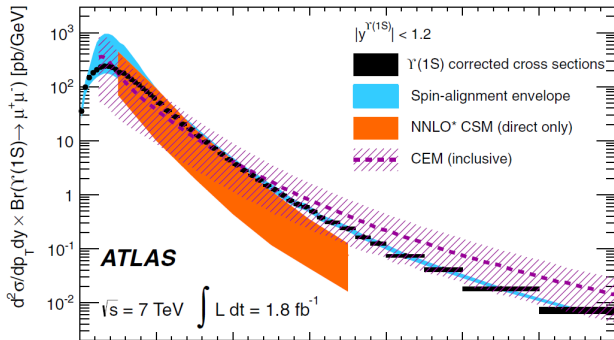
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$\Upsilon(3S)$ : 60-70 % direct;  $\Upsilon(2S)$ : 60-70 % direct;  $\Upsilon(1S)$ : 50-70 % direct

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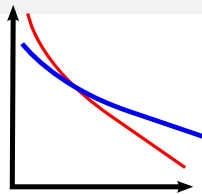


CSM theory curve extrapolated to prompt:  $\times 2$

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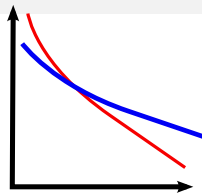
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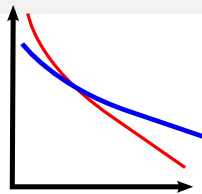


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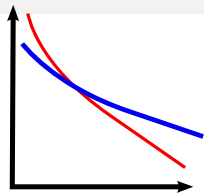
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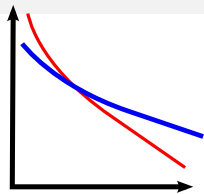
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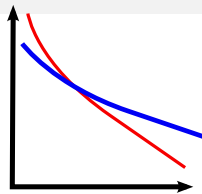
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- Polarisation:  ${}^1S_0^{[8]}$  : unpolarised;  ${}^3S_1^{[8]}$  &  ${}^3P_J^{[8]}$  : transverse



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JPL, H.S. Shao JHEP 1610 (2016) 153

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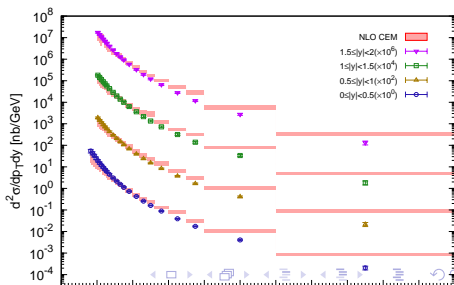
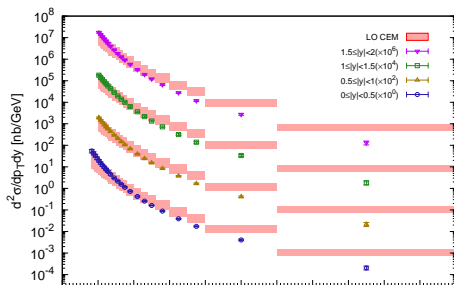
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- This motivates the study of new observables

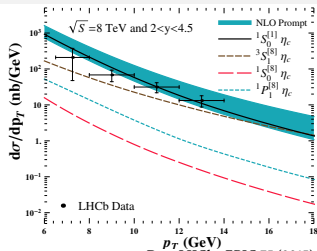
which can be more discriminant for specific effects [e.g. associated production]

## Part III

# New observables in quarkonium production

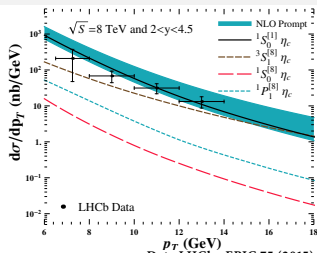
## III.1 PSEUDOSCALAR QUARKONIA

# From exotic to essential



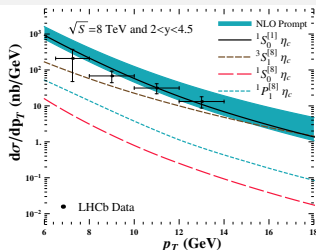
Data LHCb : EPJC 75 (2015) 311 (plot from H. Hanet *et al.* PRL 114 (2015) 092005)

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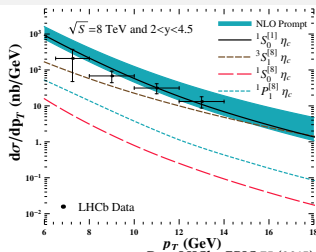
- $\eta_c$  x-section measured by LHCb **very well described by the CS** contribution (Solid Black Curve)
- Any **CO** contribution would create a **surplus**
- Even *neglecting* the *dominant* CS, this induces **constraints on  $J/\psi$  LDMEs** via HQSS :

$$\langle J/\psi ({}^1S_0^{[8]}) \rangle = \langle \eta_c ({}^3S_1^{[8]}) \rangle < 1.46 \times 10^{-2} \text{ GeV}^3$$

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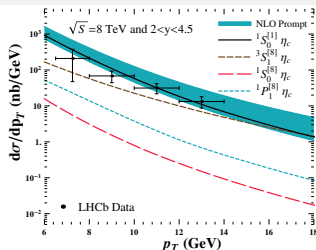
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Data LHCb: EPJC 75 (2015) 311 (plot from H. Hanet *et al.* PRL 114 (2015) 092005)

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- **Nobody foresaw the impact of measuring  $\eta_c$  yields:** 3 PRL published **right after** the LCHb data came out (Hamburg) M. Butenschoen *et al.* PRL 114 (2015) 092004; (PKU) H. Han *et al.* 114 (2015) 092005; (IHEP) H.F. Zhang *et al.* 114 (2015) 092006

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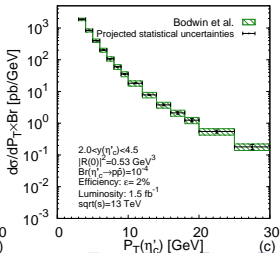
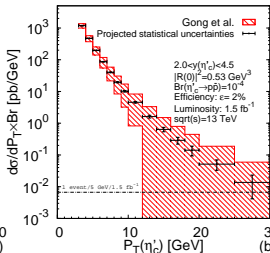
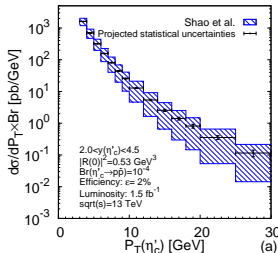
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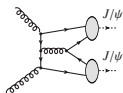


## III.2 QUARKONIUM PAIRS

# On the importance of $\alpha_s^5$ contributions to $J/\psi + J/\psi$ & $J/\psi + \eta_c$

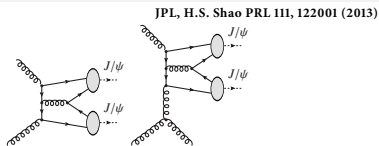
JPL, H.S. Shao PRL 111, 122001 (2013)

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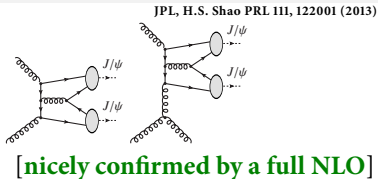
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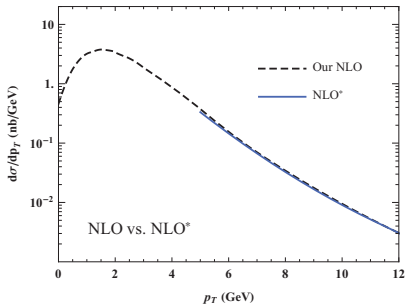


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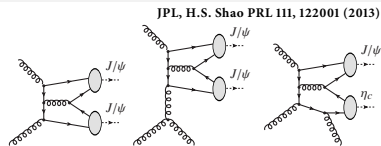


L.P. Sun *et al.* arXiv:1404.4042 [hep-ph]



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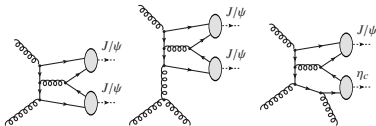
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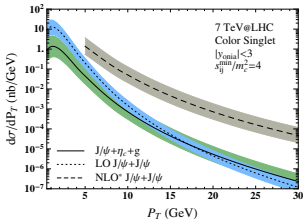
JPL, H.S. Shao PRL 111, 122001 (2013)



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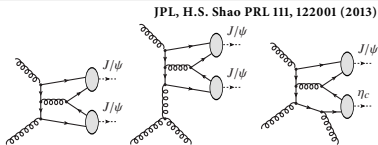
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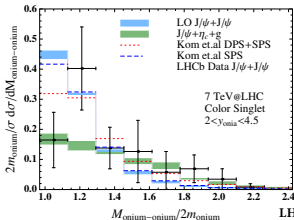
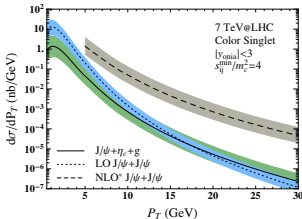
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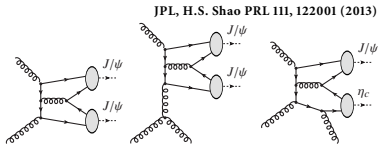


LHCb PLB 707 (2012) 52

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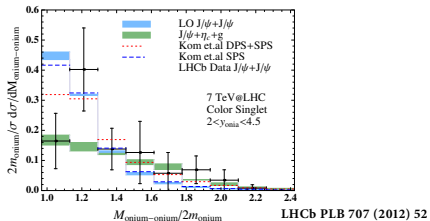
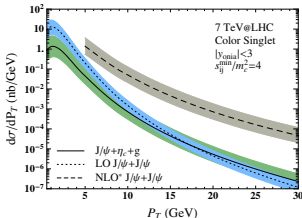
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JPL, H.-S. Shao PRL 111, 122001 (2013); PLB 751 (2015) 479

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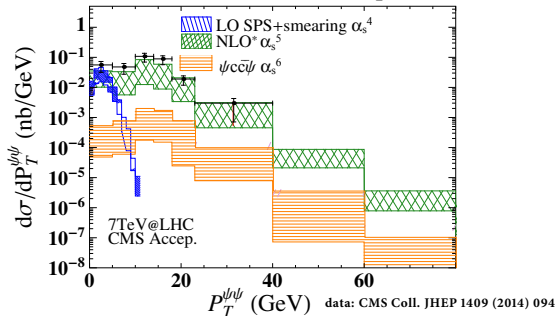
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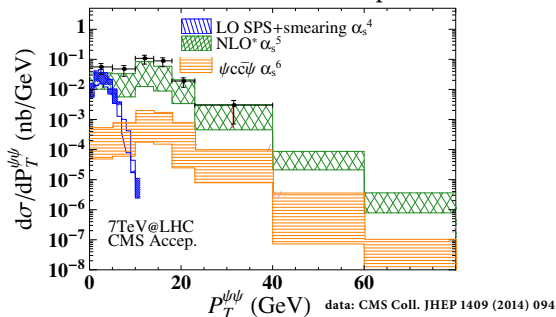
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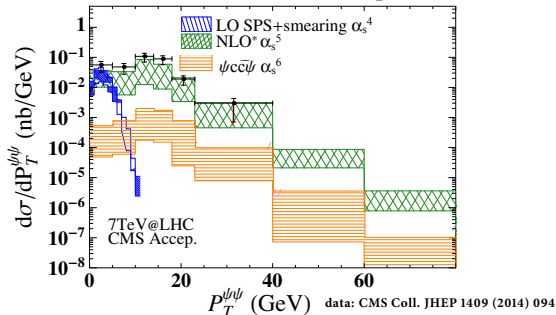


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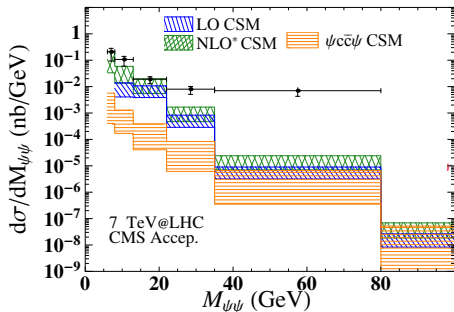
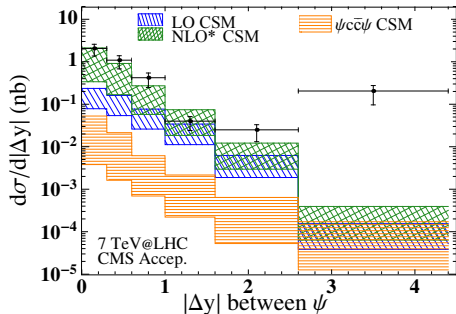
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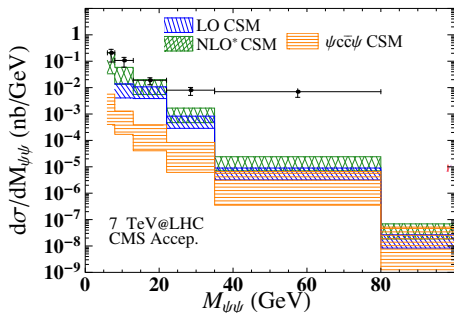
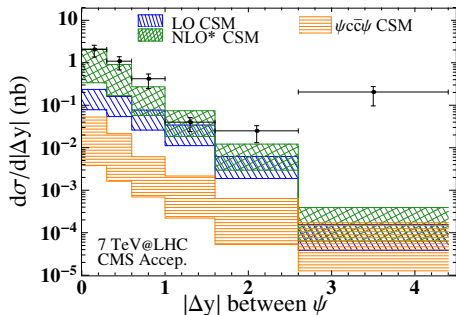
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# The so-called CMS puzzle



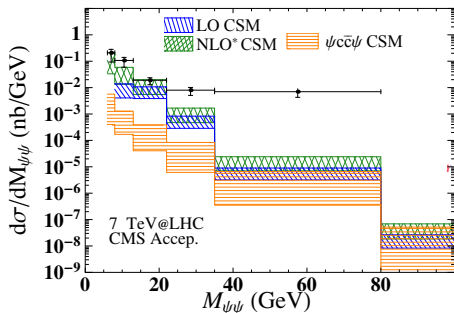
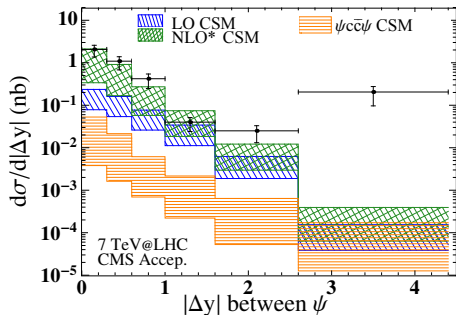


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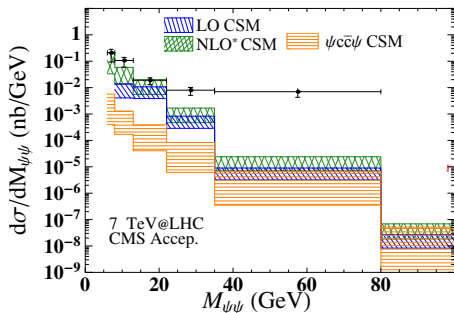
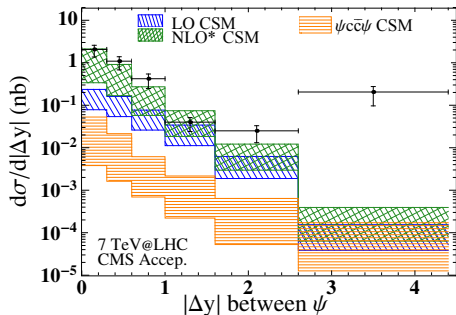
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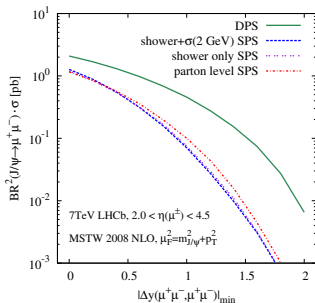
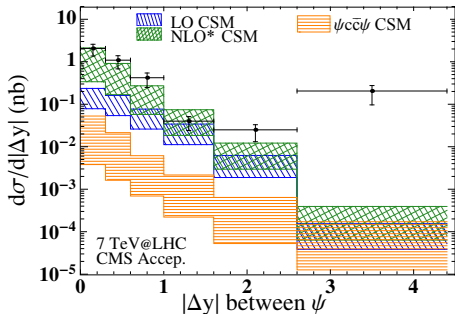
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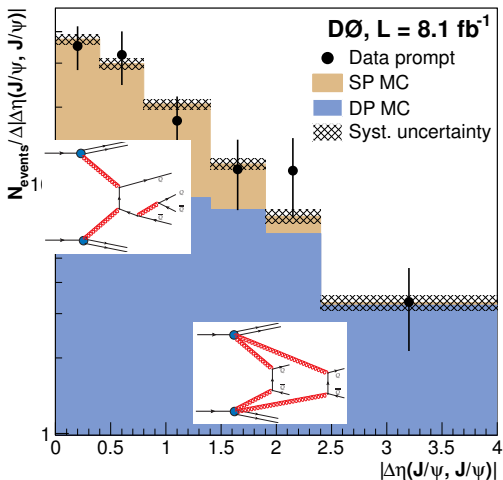


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C.H. Kom, A. Kulesza, W.J. Stirling PRL 107 (2011) 082002

# On the importance of double parton scatterings at large $\Delta\eta$

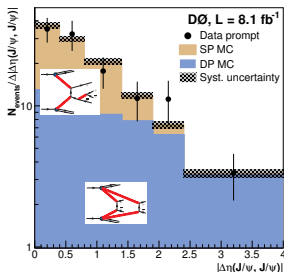
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D0 Coll. PRD 90 (2014) 111101

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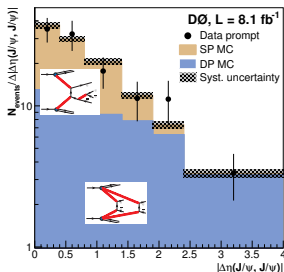


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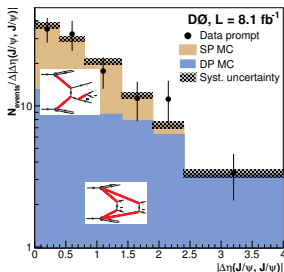


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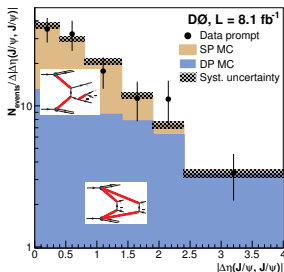
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# On the importance of double parton scatterings at large $\Delta y$ I

In fact, the argument of C.H. Kom, A. Kulesza, and W.J. Stirling was used by D0 to separate out DPS from SPS contributions



D0 Coll. PRD 90 (2014) 111101

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- A question arises: using  $\sigma^{\text{DPS}} = \frac{1}{2} \frac{\sigma_{\psi} \sigma_{\psi}}{\sigma_{\text{eff}}}$  and  $\sigma_{\text{eff}} = 4.8 \pm 2.5 \text{ mb}$ , can one account for the large  $\Delta y$  CMS data ?

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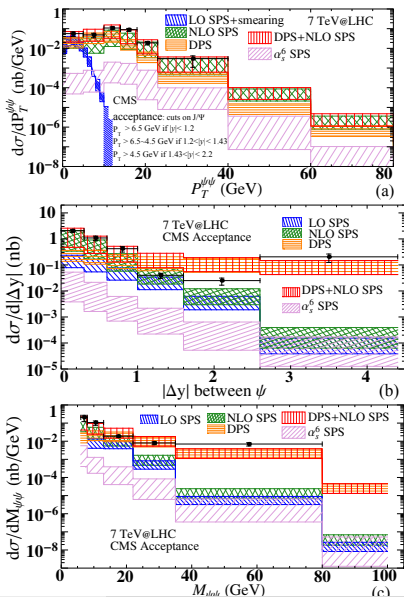
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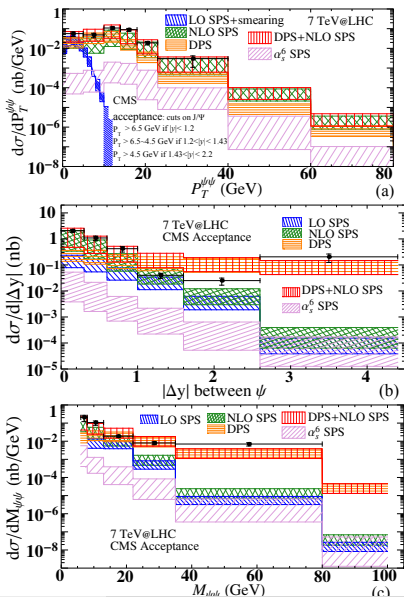
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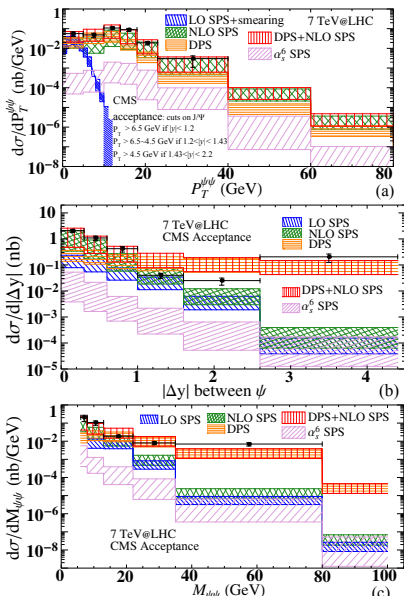
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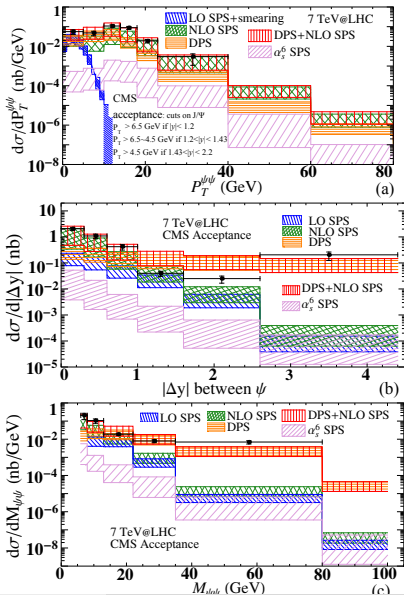
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# Comparison with ATLAS data

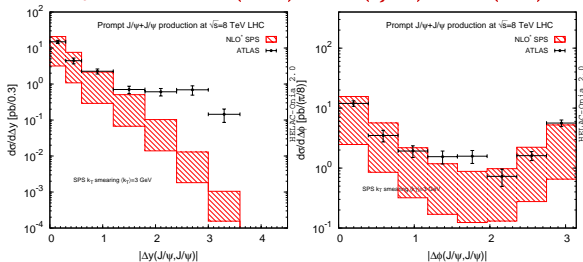
ATLAS Eur. Phys. J. C (2017) 77:76

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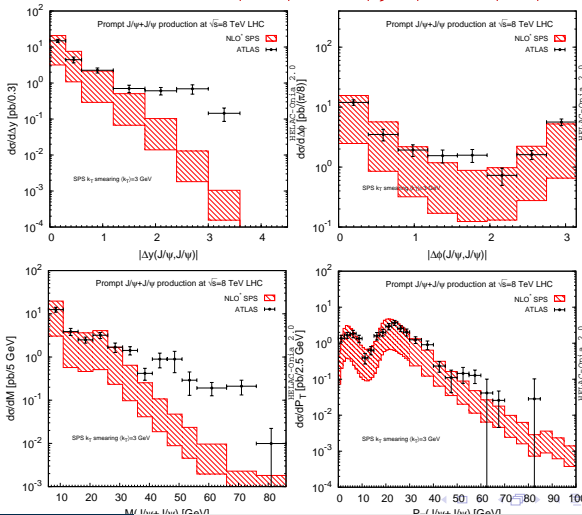
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JPL, H.-S. Shao PLB 751 (2015) 479

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- $J/\psi + \eta_c$  can also tell something about DPS and about  $\sigma_{\text{eff}}$

## III.3 QUARKONIUM AND VECTOR BOSONS

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JPL, H.S. Shao, JHEP 1610 (2016) 153

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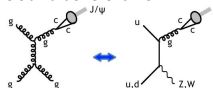
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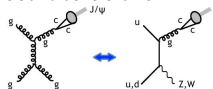
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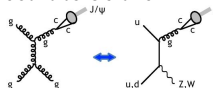
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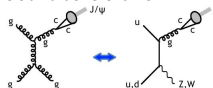
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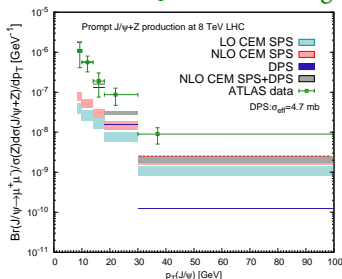
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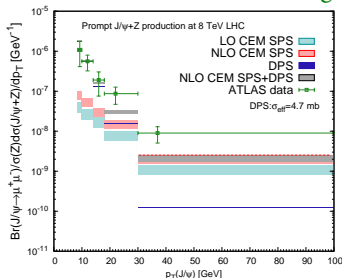
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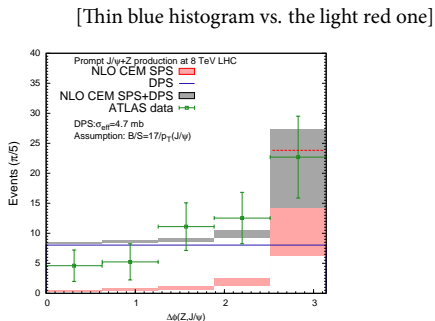
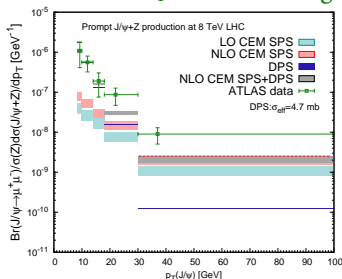


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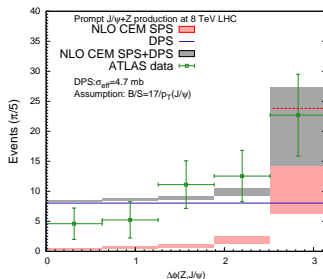
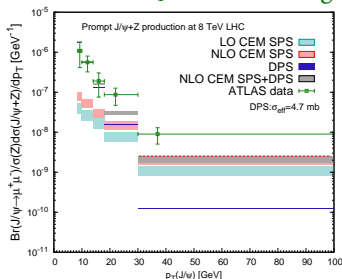
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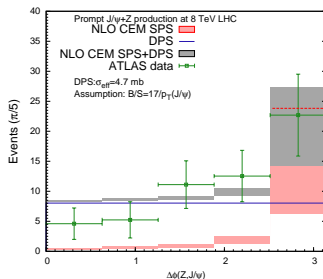
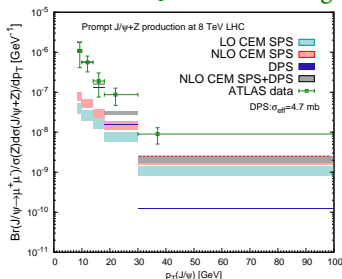
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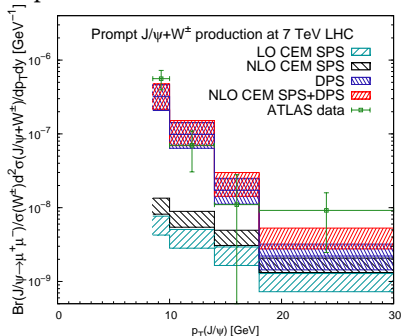
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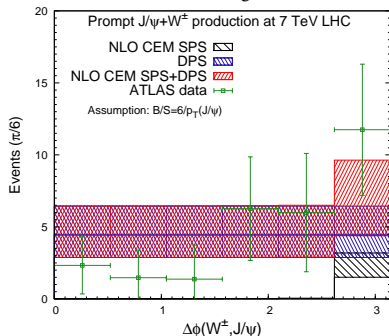
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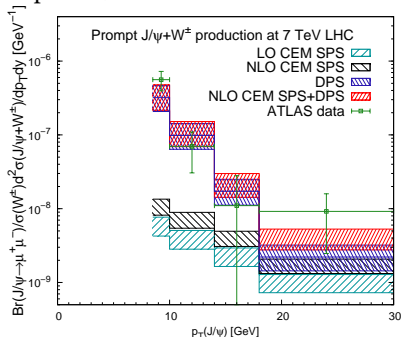
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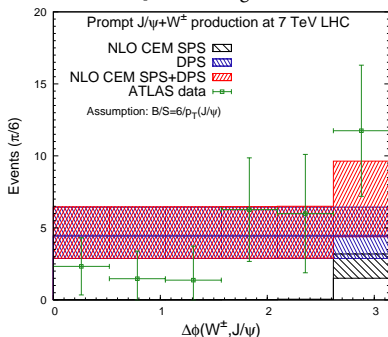
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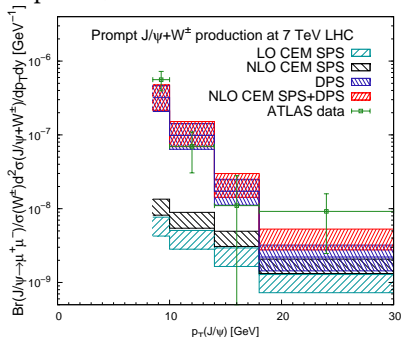
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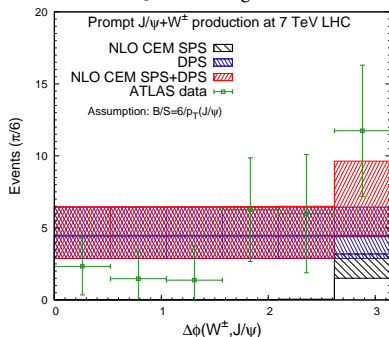
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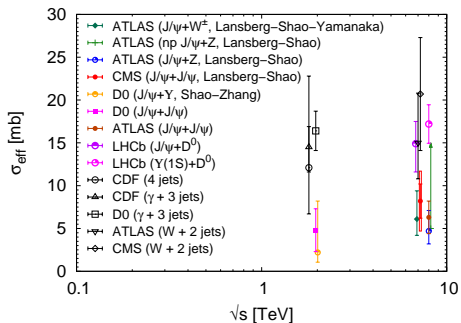


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## III.4 ALTOGETHER

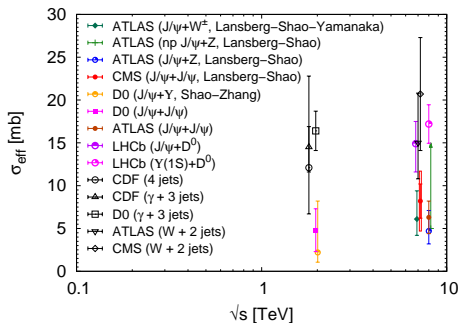
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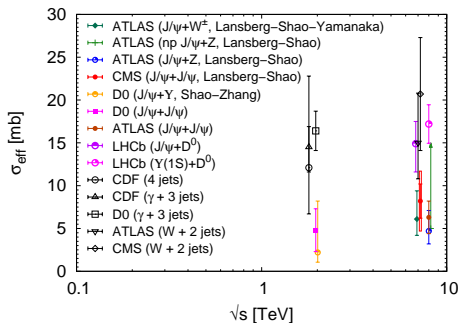


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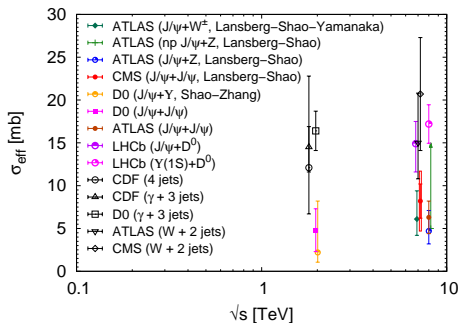
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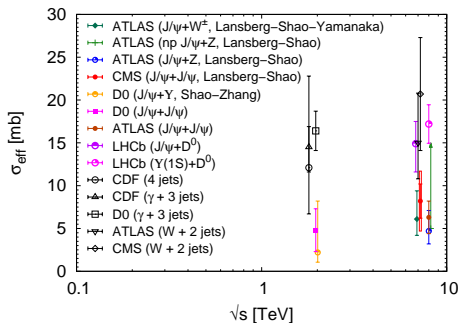
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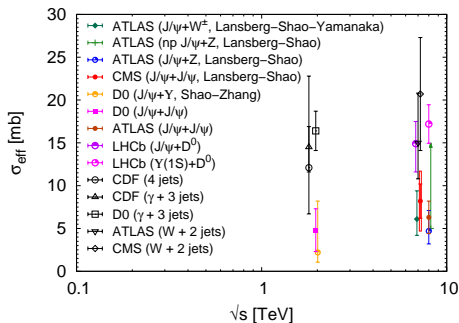
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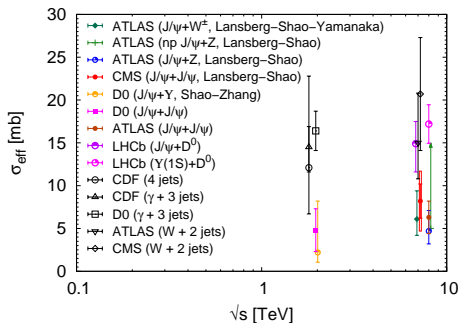
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CMS JHEP05(2017)013

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- D0  $J/\psi + Y$  data clearly points at a very large DPS

CMS JHEP05(2017)013

D0 PRL 116 (2016) 082002 + H.S. Shao - Y. J. Zhang PRL 117 (2016) 062001

# Part IV

## Conclusion

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- They also start to tell us new information on the gluon Transverse Momentum Distribution distributions

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Observables	Experiments	CSM	CEM	NRQCD	Interest
$J/\psi+J/\psi$	LHCb, CMS, ATLAS, D0 (+NA3)	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CS dominant) + DPS + gluon TMD
$J/\psi+D$	LHCb	LO	LO ?	LO	Prod. Mechanism (c to J/psi fragmentation) + DPS
$J/\psi+\Upsilon$	D0	(N)LO	LO ?	LO	Prod. Mechanism (CO dominant) + DPS
$J/\psi+\text{hadron}$	STAR	LO	--	LO	B feed-down; Singlet vs Octet radiation
$J/\psi+Z$	ATLAS	NLO	NLO	Partial NLO	Prod. Mechanism + DPS
$J/\psi+W$	ATLAS	LO	NLO	NLO (?)	Prod. Mechanism (CO dominant) + DPS
$J/\psi$ vs mult.	ALICE, CMS (+UA1)	--	--	--	
$J/\psi+b$	-- (LHCb, D0, CMS ?)	--	--	LO	Prod. Mechanism (CO dominant) + DPS
$\Upsilon+D$	LHCb	LO	LO ?	LO	DPS
$\Upsilon+\gamma$	--	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CO LDME mix) + gluon TMD/PDF
$\Upsilon$ vs mult.	CMS	--	--	--	
$\Upsilon+Z$	--	NLO	LO ?	LO	Prod. Mechanism + DPS
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## NLOAccess

Virtual Access: Automated perturbative NLO calculations for heavy ions and quarkonia (NLOAccess)

[General description](#) [Participants](#) [Tasks](#) [Links and resources](#)

### GENERAL DESCRIPTION

#### Objectives:

NLOAccess will give access to automated tools generating scientific codes allowing anyone to evaluate observables -such as production rates or kinematical properties - of scatterings involving hadrons. The automation and the versatility of these tools are such that these scatterings need not to be pre-coded. In other terms, it is possible that a random user may request for the first time the generation of a code to compute characteristics of a reaction which nobody thought of before. NLOAccess will allow the user to test the code and then to download to run it on its own computer. It essentially gives access to a dynamical library.

[Show more](#)

This project has been included in the STRONG2020 submission for EU funding.

🔍 To search type and hit enter



## Automated perturbative NLO calculation with HELAC-Onia Web

### Welcome to HELAC-Onia Web!

HELAC-Onia is an automatic matrix element generator for the calculation of the heavy quarkonium helicity amplitudes in the framework of NRQCD factorization. The program is able to calculate helicity amplitudes of multi P-wave quarkonium states production at hadron colliders and electron-positron colliders by including new P-wave off-shell currents. Besides the high efficiencies in computation of multi-leg processes within the Standard Model, HELAC-Onia is also sufficiently numerical stable in dealing with P-wave quarkonia and P-wave color-octet intermediate states.

Already registered to the portal? Please login.

Do you not have an account? Make a registration request.

Part V

Backup

# Comparison with the new LHCb data at 13 TeV

LHCb JHEP06(2017)047

$\sigma(\psi\psi)$ nb	no $P_T$ cut	$P_T > 1$ GeV	$P_T > 3$ GeV
NLO* CS	$15.4 \pm 2.2^{+51}_{-12}$	$14.8 \pm 1.7^{+53}_{-12}$	$6.8 \pm 0.6^{+22}_{-5}$
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DPS [ $\sigma_{\text{eff}} = 14.5 \pm 1.7^{+1.7}_{-2.3}$ mb]	$8.1 \pm 0.9^{+1.6}_{-1.3}$	$7.5 \pm 0.8^{+1.5}_{-1.2}$	$4.9 \pm 0.5^{+1.0}_{-0.8}$
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- **Agreement** between CSM NLO and data
- **Large scale uncertainty** for the NLO\*, greatly **reduced at NLO**
- **REMINDER:** it is not an option to "switch off"/ignore the NLO CS contribution [parameter free]

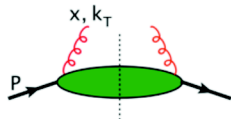
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- **REMINDER:** it is not an option to "switch off"/ignore the NLO CS contribution [parameter free]
- Yet, **room for DPS**; however tension if  $\sigma_{\text{eff}} \simeq 7$  mb
- **Tension between LHCb and other di- $J/\psi$  extractions** [rapidity effect ?]

# Gluon TMDs in unpolarised protons

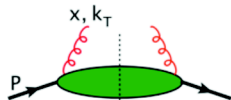




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- Gauge-invariant definition:

$$\Phi_g^{\mu\nu}(x, \mathbf{k}_T, \zeta, \mu) \equiv \int \frac{d(\xi \cdot P) d^2 \xi_T}{(xP \cdot n)^2 (2\pi)^3} e^{i(xP + k_T) \cdot \xi} \langle P | F^{n\nu}(0) \mathcal{U}_{[0, \xi]} F^{n\mu}(\xi) \mathcal{U}'_{[\xi, 0]} | P \rangle \Big|_{\xi \cdot P' = 0}$$

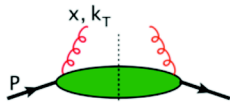


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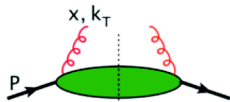
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- Parametrisation:

$$\Phi_g^{\mu\nu}(x, \mathbf{k}_T, \zeta, \mu) = -\frac{1}{2x} \left\{ g_T^{\mu\nu} f_1^g(x, k_T, \mu) - \left( \frac{k_T^\mu k_T^\nu}{M_p^2} + g_T^{\mu\nu} \frac{\mathbf{k}_T^2}{2M_p^2} \right) h_1^{\perp g}(x, k_T, \mu) \right\} + \text{suppr.}$$

P. J. Mulders, J. Rodrigues, PRD 63 (2001) 094021; D. Boer *et al.* JHEP 1610 (2016) 013

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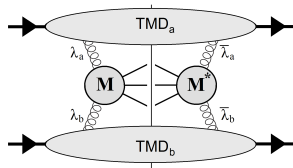
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- $f_1^g$ : TMD distribution of **unpolarised** gluons
- $h_1^{\perp g}$ : TMD distribution of **linearly polarised** gluons

[Helicity-flip distribution]

# $gg$ fusion in arbitrary unpolarised process [colourless final state]

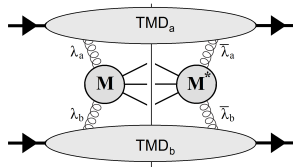
$$d\sigma^{gg} \propto$$



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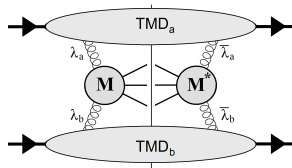
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$\Rightarrow$  helicity non-flip, **azimuthally independent**

 $F_2$ 

$$+ \left( \sum_{\lambda} \hat{\mathcal{M}}_{\lambda, \lambda} \hat{\mathcal{M}}_{-\lambda, -\lambda}^* \right) \mathcal{C}[w_0 \times h_1^{\perp g} h_1^{\perp g}]$$

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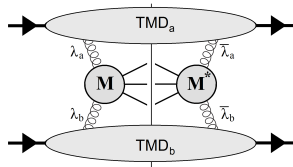
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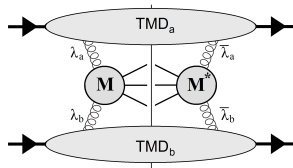
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$\Rightarrow$  double helicity flip,  **$\cos(4\phi)$ -modulation**





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None are measured so far ...

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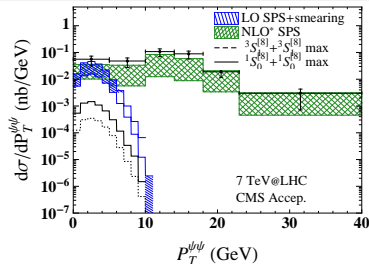
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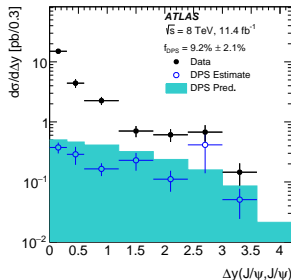
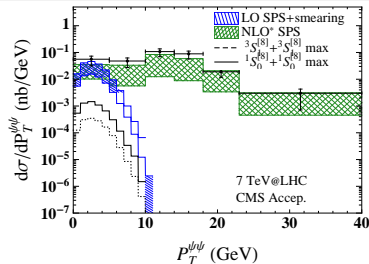
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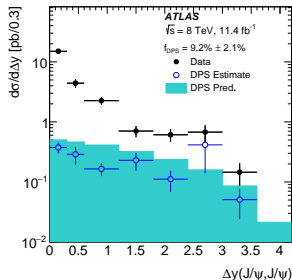
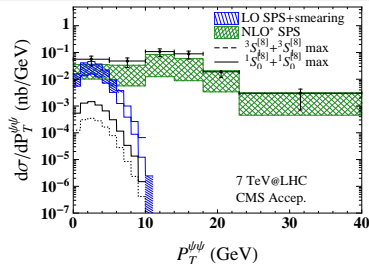
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- DPS in LHCb data [kinematical distributions well controlled : independent scatterings]



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JPL, C. Pisano, F. Scarpa, M. Schlegel, arXiv:1710.01684

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$$F_4 = F_1 \text{ at large } M_{QQ}$$

$\Rightarrow$  di- $J/\psi$  (or di- $\Upsilon$ ) **maximise** the observability of **cos 4 $\phi$**  modulations  
in a kinematical region where **data are already taken !**

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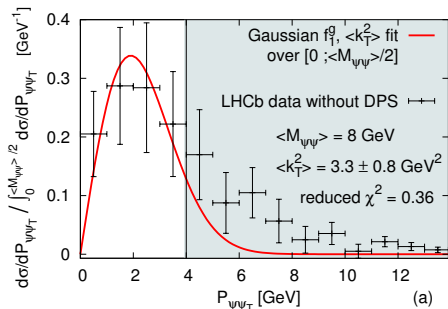
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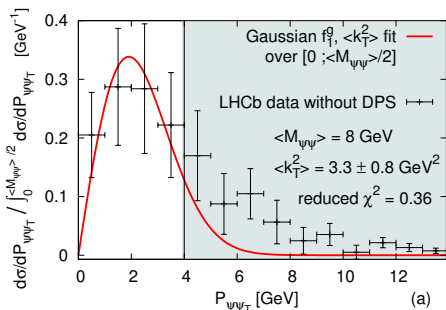




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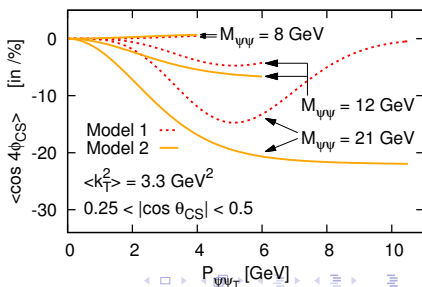
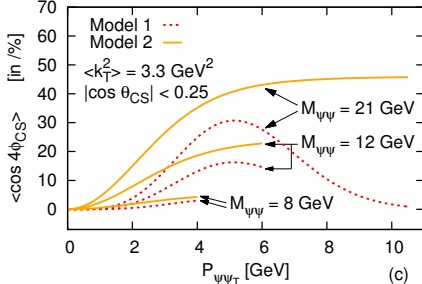
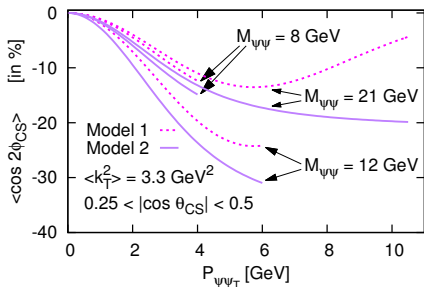
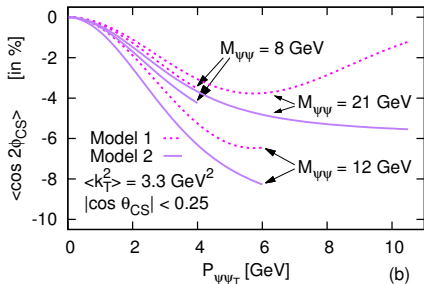
- Integration over  $\phi \Rightarrow \cos(n\phi)$ -terms cancel out
- $F_2 \ll F_1 \Rightarrow$  only  $\mathcal{C}[f_1^g f_1^g]$  contributes to the cross-section
- No evolution so far:  $\langle k_T^2 \rangle \sim 3 \text{ GeV}^2$   
accounts both for non-perturbative and perturbative broadenings at a scale close to  $M_{\psi\psi} \sim 8 \text{ GeV}$
- Disentangling such (non-)perturbative effects requires **data at different scales**

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- In the QGP, do quarkonia behave more like colorful gluons  
or colorless photons ?

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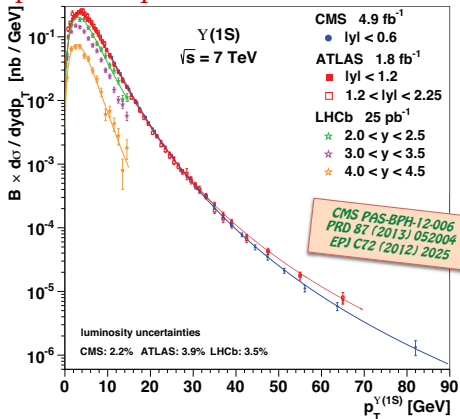
- If color is bleaching at short distances (Color Singlet Model), low- $P_T$  quarkonia can be used to extract the distribution of **linearly polarised gluon in unpolarised protons**,  $h_1^{\perp g}(x, k_T, \mu)$  D. Boer, C. Pisano. PRD 86 (2012) 094007
- Different **nuclear suppression** depending on how the pair hadronizes J.W. Qiu, J. P. Vary, X.F. Zhang, PRL 88 (2002) 232301
- **Saturation effects** depend on the colour state of the propagating pair D. Kharzeev, *et al.* PRL 102 (2009) 152301; F. Dominguez, *et al.* PLB 710 (2012) 182; Y.Q. Ma, *et al.* PRD 92 (2015) 071901
- Most of the proton-nucleus and nucleus-nucleus collision data lie at  $P_T \lesssim m_Q$
- In the QGP, do quarkonia behave more like colorful gluons  
or colorless photons ?
- If regeneration is at work, how does it happen ? statistically ? according to the charm-quark distribution in the charmonium (wave-function) ?
- etc ...

Why is it important to know how low- $P_T$  quarkonia are produced

Also because, some very high  $P_T$  quarkonia which we study can be **as rare as a few millionth of the produced quarkonia**

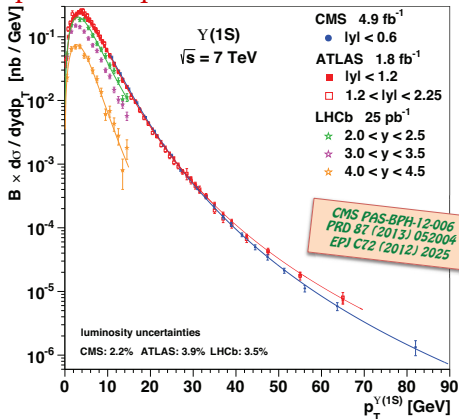
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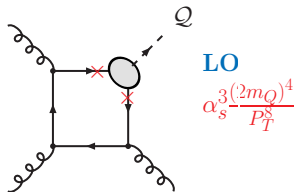


Most probably the production of a  $\Upsilon$  with  $P_T = 90 \text{ GeV}$ , even also  $20 \text{ GeV}$ , has very few things to do with the bulk of  $\Upsilon$

# Basic pQCD approach: the Colour Singlet Model (CSM)

C.-H. Chang, NPB172, 425 (1980); R. Baier & R. Rückl Z. Phys. C 19, 251(1983);

⇒ Perturbative creation of 2 quarks  $Q$  and  $\bar{Q}$  BUT

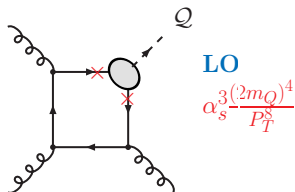


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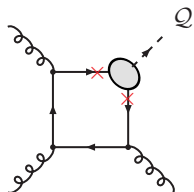
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⇒ Non-perturbative binding of quarks



LO

$$\alpha_s^3 \frac{(2m_Q)^4}{P_T^8}$$

→ Schrödinger wave function

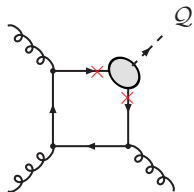


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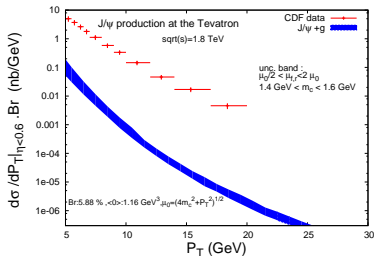
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$$\text{LO} \propto_s^3 \frac{(2m_Q)^4}{P_T^8}$$

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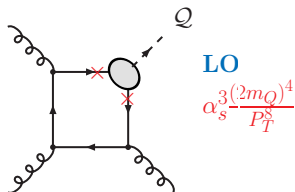
CDF, PRL 79:572 & 578,1997

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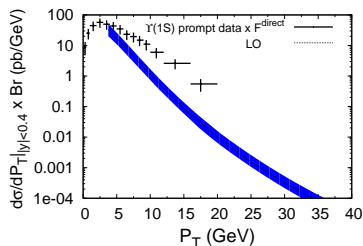
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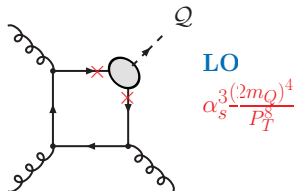
CDF, PRL 88:161802,2002

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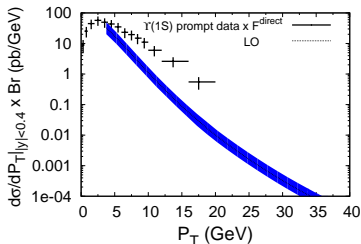
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⇒ Non-perturbative binding of quarks

→ Schrödinger wave function



⇒ Large QCD corrections from new topologies reduce the gap with data at mid and large  $P_T$

# The LO CSM accounts for the $P_T$ -integrated yield

S. J. Brodsky and JPL, PRD 81 051502 (R), 2010; JPL, PoS(ICHEP 2010), 206 (2010); NPA 910-911 (2013) 470

→ The yield vs.  $\sqrt{s}, y$

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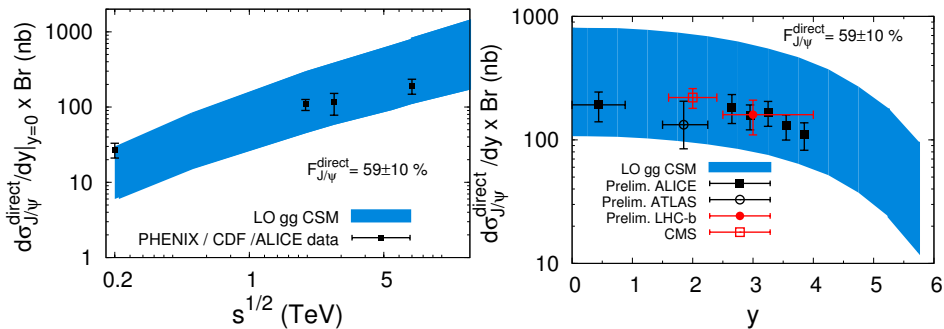
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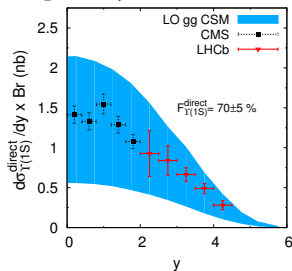


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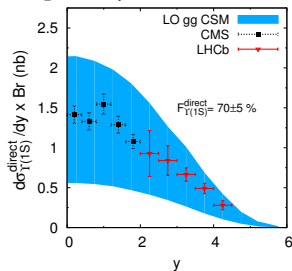
CMS PRD 83 (2011) 112004; LHCb EPJC 72 (2012) 2025

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CMS PRD 83 (2011) 112004; LHCb EPJC 72 (2012) 2025

- Unfortunately, very large th. uncertainties: masses, scales ( $\mu_R, \mu_F$ ), gluon PDFs at low  $x$  and  $Q^2, \dots$

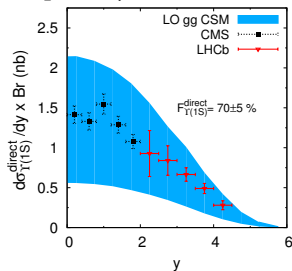


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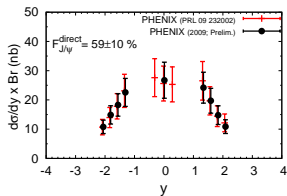
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- Unfortunately, very large th. uncertainties: masses, scales ( $\mu_R, \mu_F$ ), gluon PDFs at low  $x$  and  $Q^2, \dots$
- Earlier claims that CSM contribution to  $d\sigma/dy$  was small were based on the **incorrect assumption that  $\chi_c$  feed-down was dominant**

## NLO CSM at RHIC

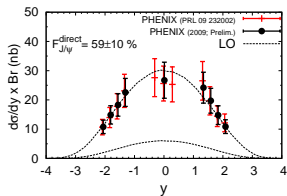
 $\rightarrow J/\psi$ 

S. J. Brodsky and JPL, PRD 81 051502 (R), 2010.



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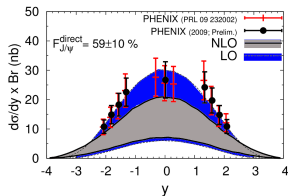
S. J. Brodsky and JPL, PRD 81 051502 (R), 2010.

 $\rightarrow J/\psi$ LO:  $gg \rightarrow J/\psi g$  (see slide 5, **nothing new !**)

# NLO CSM at RHIC

→  $J/\psi$

S. J. Brodsky and JPL, PRD 81 051502 (R), 2010.



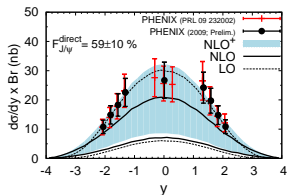
**NLO:**  $gg \rightarrow J/\psi gg, gq \rightarrow J/\psi gq, \dots$

using the matrix elements from J.Campbell, F. Maltoni, F. Tramontano, PRL 98:252002,2007

## NLO CSM at RHIC

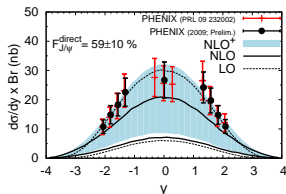
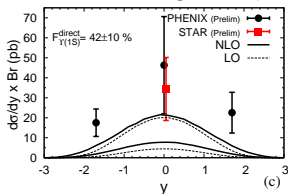
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NLO<sup>+</sup>: possible **new contribution** at LO  $cg \rightarrow J/\psi c$

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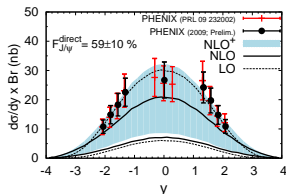
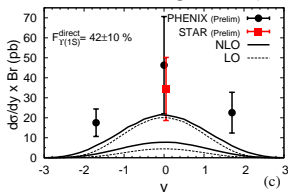
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 $\rightarrow J/\psi$ NLO<sup>+</sup>: possible **new contribution** at LO  $cg \rightarrow J/\psi c$  $\rightarrow \Upsilon^*$ 

\* Sorry: I should update these plots (updated data and fraction is about 60%)

## NLO CSM at RHIC

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 $\rightarrow J/\psi$ NLO<sup>+</sup>: possible **new contribution** at LO  $cg \rightarrow J/\psi c$  $\rightarrow \Upsilon^*$ 

A priori, good convergence NLO w.r.t. LO

[I will come back to that later]

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## Analysis of charmonium production at fixed-target experiments in the NRQCD approach

F. Maltoni<sup>a</sup>, J. Spengler<sup>b</sup>, M. Bargiotti<sup>c</sup>, A. Bertin<sup>c</sup>, M. Bruschi<sup>c</sup>, S. De Castro<sup>c</sup>, L. Fabbri<sup>c</sup>,  
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- At  $\alpha_S^2$ , one only has CO contributions  
:  
2 → 1 processes :  $q + \bar{q} \rightarrow Q\bar{Q}[{}^3S_1^{[8]}]$  and  $g + g \rightarrow Q\bar{Q}[{}^1S_0^{[8]}, {}^3P_{J=0,1,2}^{[8]}]$



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- At  $\alpha_S^3$ , one has in addition real emissions (including **one CS process**)

$$g + g \rightarrow Q\bar{Q}[^1S_0^{[8]}, ^3S_1^{[8]}, ^3P_{J=0,2}^{[8]}] + g, \quad g + q(\bar{q}) \rightarrow Q\bar{Q}[^1S_8^{[0]}, ^3S_1^{[8]}, ^3P_{J=0,2}^{[8]}] + q(\bar{q})$$

$$q + \bar{q} \rightarrow Q\bar{Q}[^1S_0^{[8]}, ^3S_1^{[8]}, ^3P_{J=0,1,2}^{[8]}] + g \text{ and } \mathbf{g + g \rightarrow Q\bar{Q}[^3S_1^{[1]}] + g}$$



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- Done with **NRQCD LDMEs fitted at LO on  $P_T$  spectra from CDF ( $\simeq 2$  TeV)**

Table 1

Reference NRQCD matrix elements for charmonium production. The color-singlet matrix elements are taken from the potential model calculation of [14, 15]. The color-octet matrix elements have been extracted from the CDF data [16] in Ref. [17]

$H$	$\langle \mathcal{O}_8^H \rangle$	$\langle \mathcal{O}_8^H[{}^3S_1] \rangle$	$\langle \mathcal{O}_8^H[{}^1S_0^{(8)}] \rangle = \langle \mathcal{O}_8[{}^3P_0^{(8)}] \rangle / m_c^2$
$J/\psi$	1.16 GeV <sup>3</sup>	$1.19 \times 10^{-2}$ GeV <sup>3</sup>	$1.0 \times 10^{-2}$ GeV <sup>3</sup>
$\psi(2S)$	0.76 GeV <sup>3</sup>	$0.50 \times 10^{-2}$ GeV <sup>3</sup>	$0.42 \times 10^{-2}$ GeV <sup>3</sup>
$\chi_{c0}$	0.11 GeV	$0.31 \times 10^{-2}$ GeV <sup>3</sup>	–

# NLO NRQCD up to RHIC II

## Abstract

We present an analysis of the existing data on charmonium hadro-production based on non-relativistic QCD (NRQCD) calculations at the next-to-leading order (NLO). All the data on  $J/\psi$  and  $\psi(2S)$  production in fixed-target experiments and on  $pp$  collisions at low energy are included. We find that *the amount of color-octet contribution needed to describe the data is about 1/10 of that found at the Tevatron.*

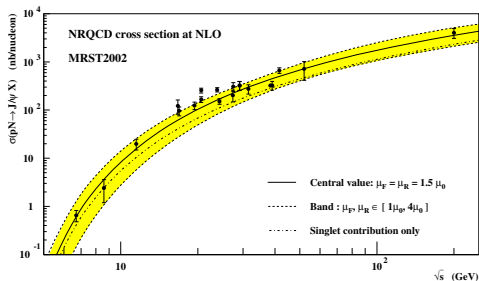
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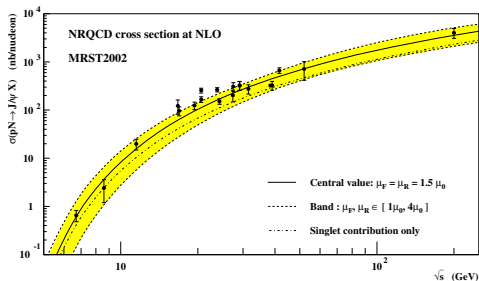


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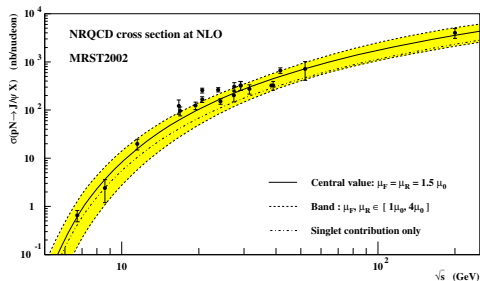
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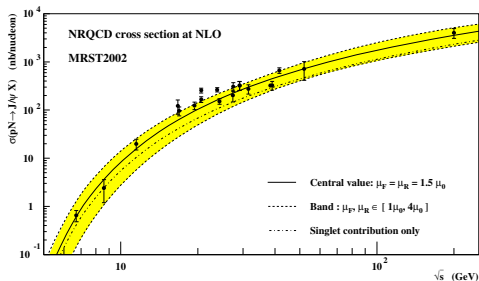


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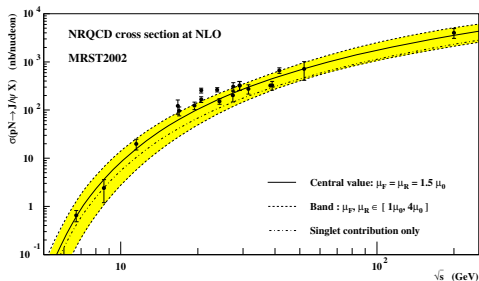
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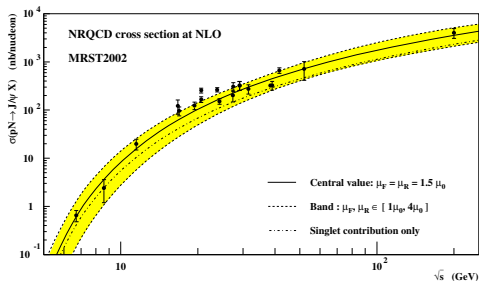
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[Y. Feng, JPL, J.X. Wang, EPJC (2015)75:313]

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- **constant** feed-down (FD) fractions

- $F_{J/\psi}^{\text{direct}} = 60 \pm 10\%$

- $F_{\Upsilon(1S)}^{\text{direct}} = 66 \pm 10\%$

- $F_{\Upsilon(1S+2S+3S)}^{\text{direct}} = 60 \pm 10\%$

- Uncertainty on  $F^{\text{direct}}$  combined in quadrature with that of data

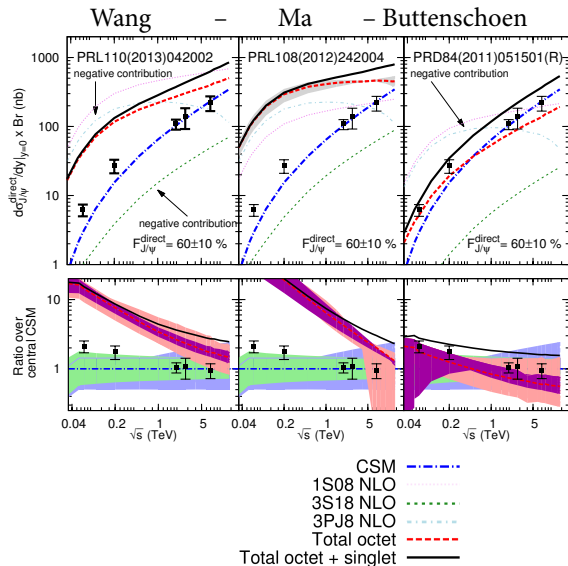
*Arguable but accounts for a possible energy dependence of the FD fraction*

# What we did II

We used LDMEs **fitted at NLO/one loop on the  $P_T$  spectra**

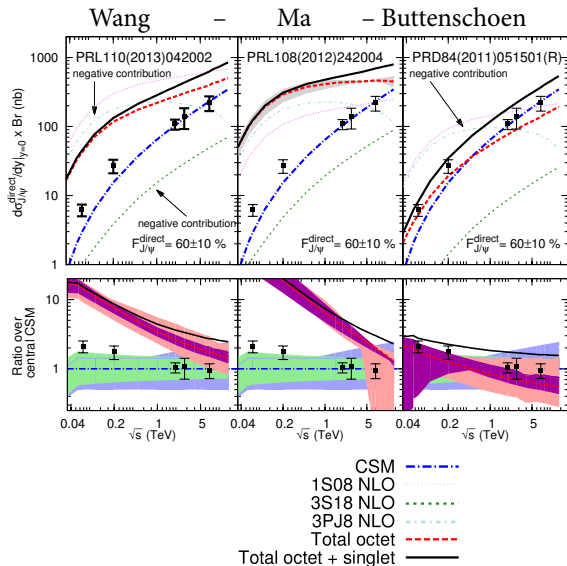
	Ref.	$\langle \mathcal{O}_{J/\psi}({}^3P_0^{[8]}) \rangle$ (in $\text{GeV}^5$ )	$\langle \mathcal{O}_{J/\psi}({}^1S_0^{[8]}) \rangle$ (in $\text{GeV}^3$ )	$\langle \mathcal{O}_{J/\psi}({}^3S_1^{[8]}) \rangle$ (in $\text{GeV}^3$ )
• $J/\psi$	Y.-Q. Ma, <i>et al.</i> PRL 106 (2011) 042002.	$-2.0 \times 10^{-3}$	$7.8 \times 10^{-2}$	0
		$2.1 \times 10^{-2}$	$3.5 \times 10^{-2}$	$5.8 \times 10^{-3}$
		$4.1 \times 10^{-2}$	0	$1.1 \times 10^{-2}$
	B. Gong, <i>et al.</i> PRL 110 (2013) 042002	$-2.2 \times 10^{-2}$	$9.7 \times 10^{-2}$	$-4.6 \times 10^{-3}$
M. Butenschoen, B. Kniehl. PRD (2011) 051501	$-9.1 \times 10^{-2}$	$3.0 \times 10^{-2}$	$1.7 \times 10^{-3}$	
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• $\psi'$	B. Gong, <i>et al.</i> PRL 110 (2013) 042002	$9.5 \times 10^{-3}$	$-1.2 \times 10^{-4}$	$3.4 \times 10^{-3}$
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• $Y(1S)$	B. Gong, <i>et al.</i> PRL 112 (2014) 3, 032001.	$-10.36 \times 10^{-2}$	$11.15 \times 10^{-2}$	$-4.1 \times 10^{-2}$

[We have also added the fit of G.T. Bodwin, *et al.*, PRL 113, 022001 (2014) even though it is based on a fragmentation function approach]

Results for the  $J/\psi$ 

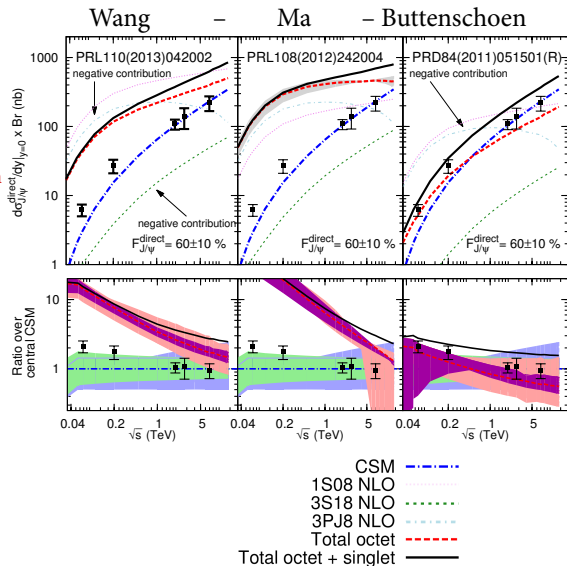
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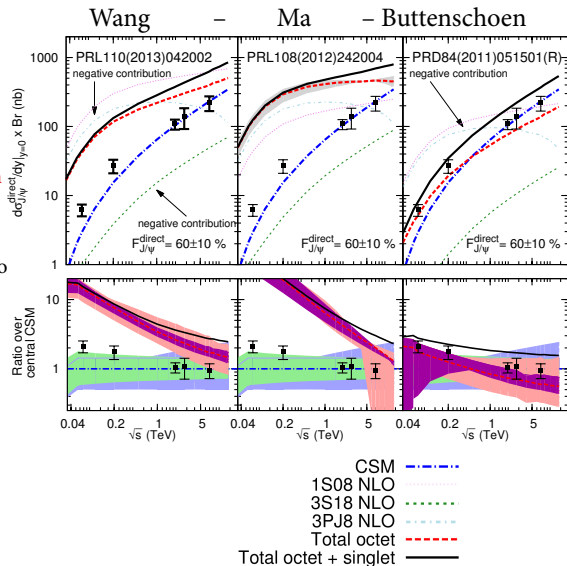
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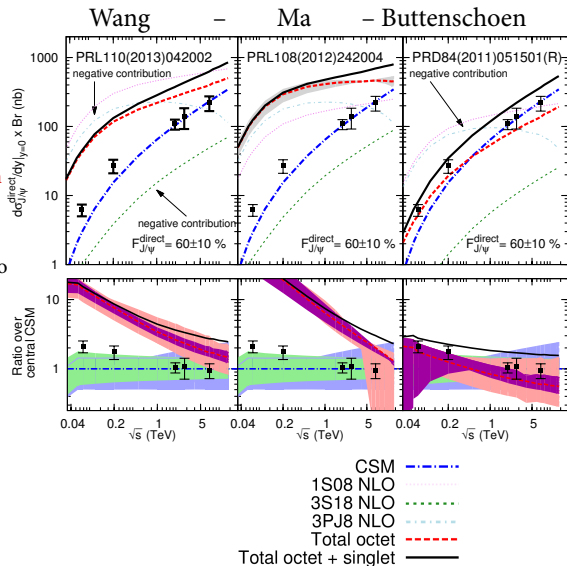
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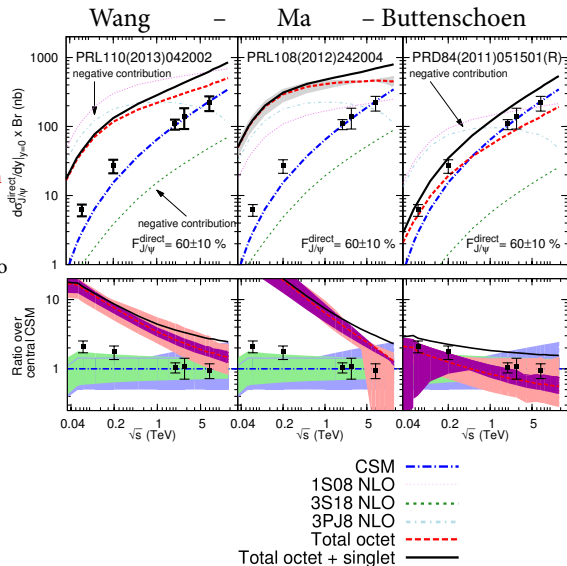
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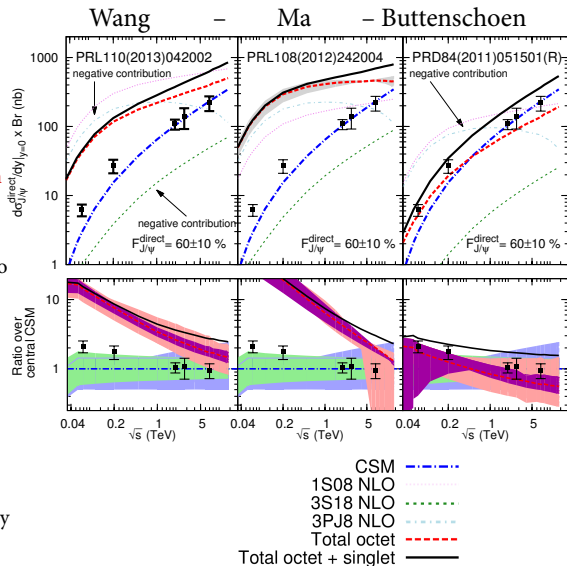
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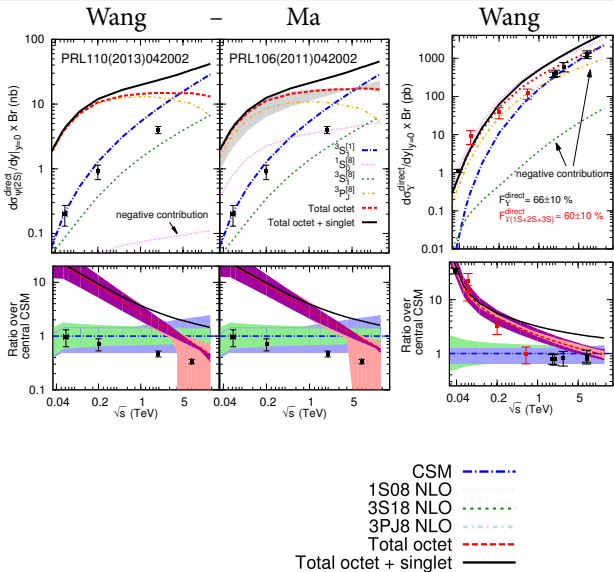




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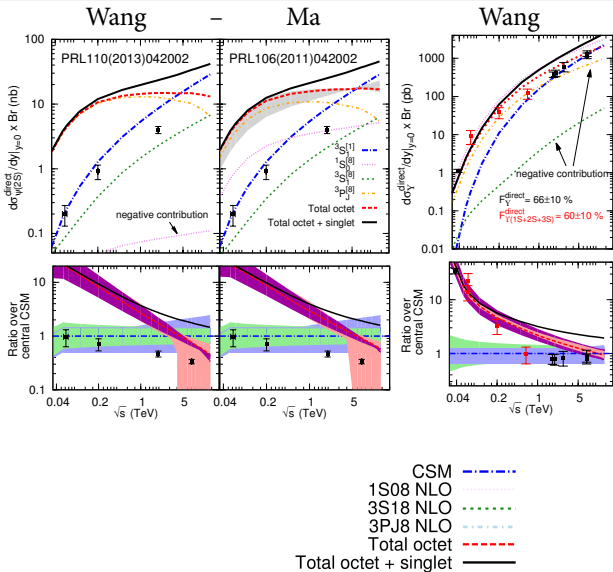
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- Not a surprise since **the CSM alone accounts well for the data**; adding any contribution creates a “surplus”



Results for the  $\psi'$  and  $\Upsilon$ 

Results for the  $\psi'$  and  $\Upsilon$ For  $\psi(2S)$ 

- Worse than for  $J/\psi$
- CSM even tends to overshoot at large  $\sqrt{s}$  – yet in agreement within uncertainties (lower panel)
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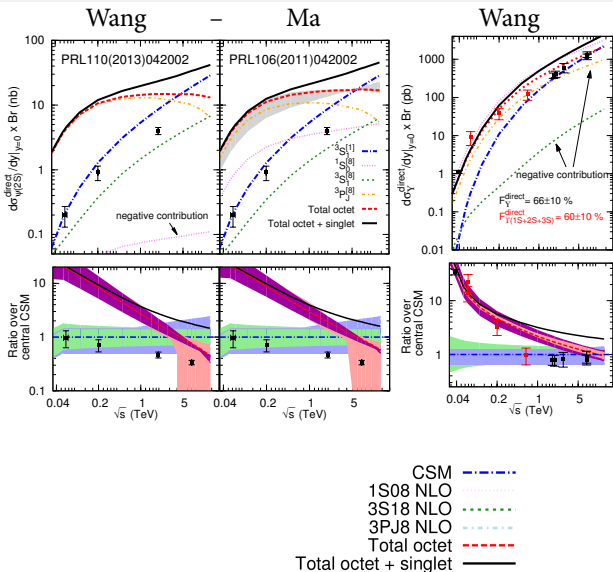


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For  $Y(1S)$ 

- Reasonable trend for  $Y$
- CSM is doing a perfect job in the TeV range – note that the RHIC points moved down
- On the other hand, CO needed at low  $\sqrt{s}$ ? High  $x$  gluon pdf underestimated?



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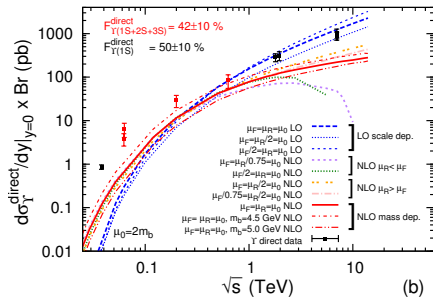
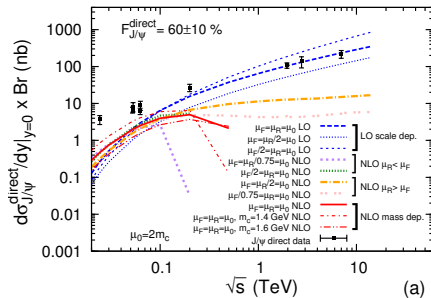
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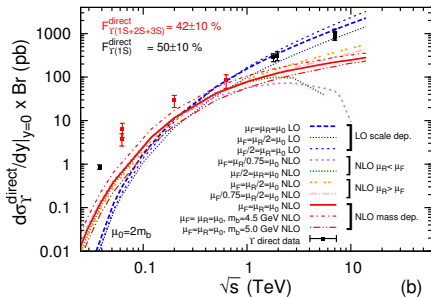
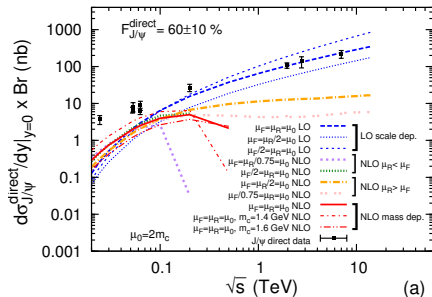
A. Petrelli, M. Cacciari, M. Greco, F. Maltoni and M. L. Mangano, Nucl. Phys. B 514 (1998) 245

We checked these with FDC

# CSM at one loop: Results

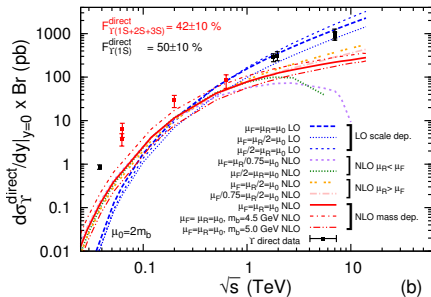
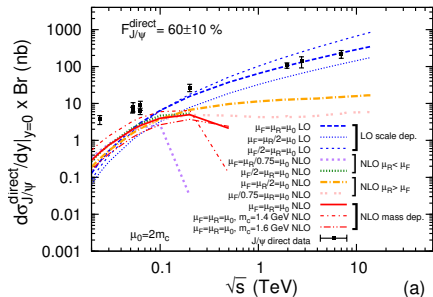


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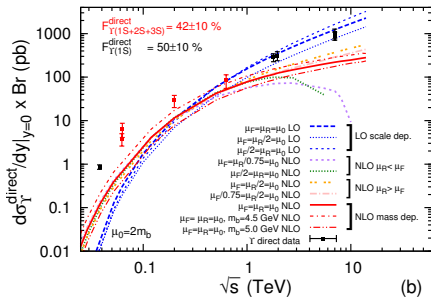
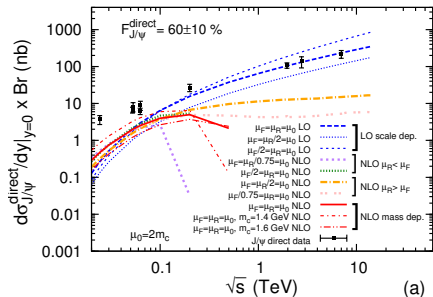
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Is it due to ISR, FSR ? Is NRQCD simply not holding at low  $P_T$  ?

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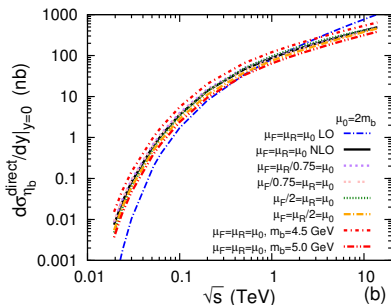
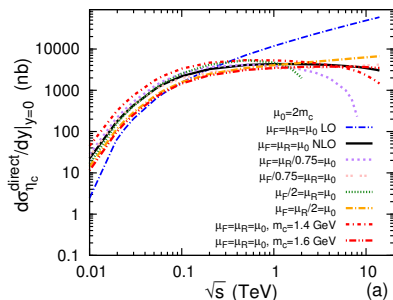


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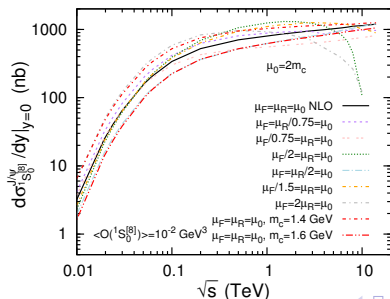
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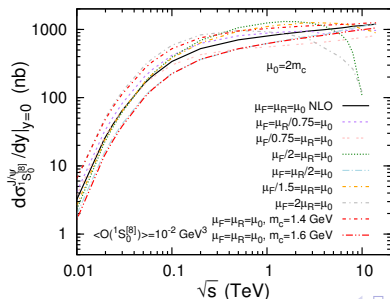
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- No sign of negative terms in the **TMD factorisation approach** up to one loop

M. Echevarria, T. Kasemets, JPL, C. Pisano A. Signori (in progress); J.P. Ma, J.X. Wang, S. Zhao, PRD 88 (2013) 014027



# A glimmer of hope: Low $P_T$ $\chi_{Q1}/\chi_{Q2}$

LHCb, JHEP 10(2013)115 & JHEP 1410 (2014) 88 ; CMS, EPJC, 72, 2257 (2012); ATLAS, JHEP 07(2014)154

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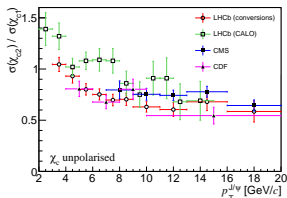
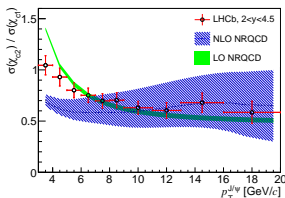
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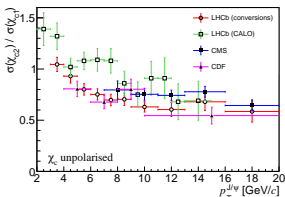
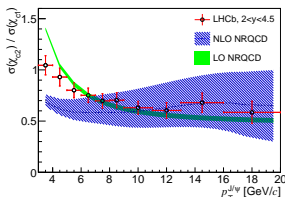
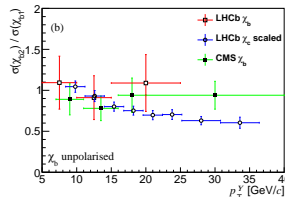
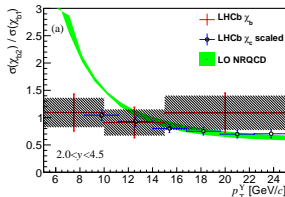
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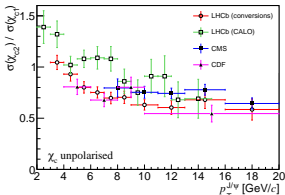
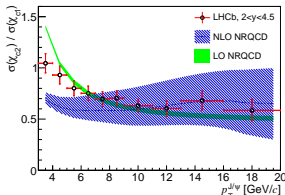


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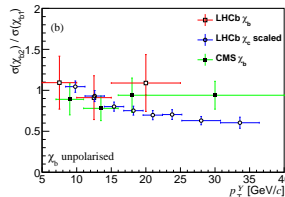
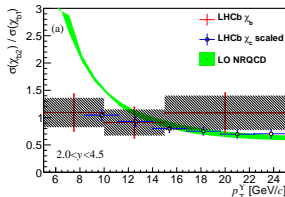
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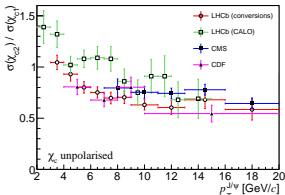
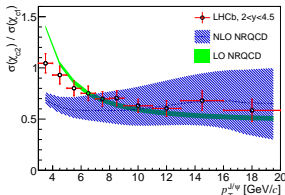
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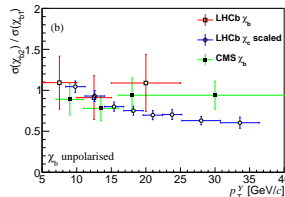
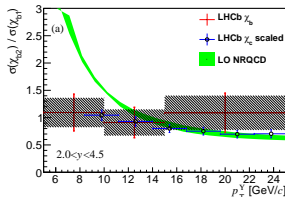
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- The nature (quantum #) of the produced final state seems still relevant !

# Basics of the Colour Evaporation Model

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- Based on Quark-Hadron duality argument, one writes

H. Fritzsch, PLB 67 (1977) 217; F. Halzen, PLB 69 (1977) 105

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- It can easily be check by MCFM at NLO for instance

<http://mcfm.fnal.gov/>

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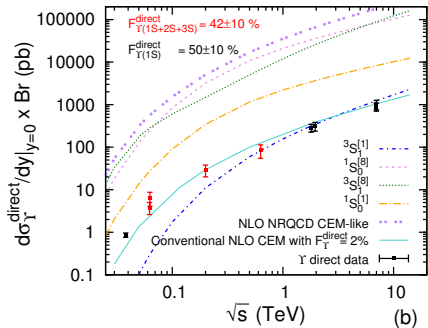
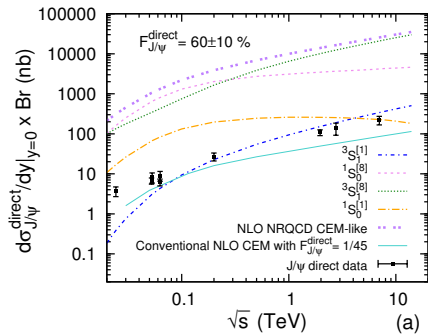
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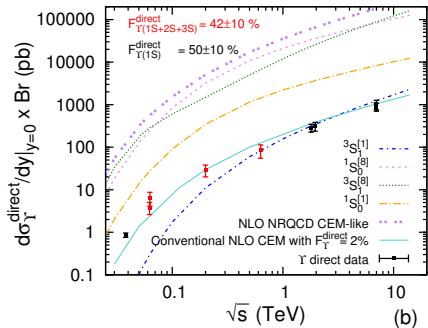
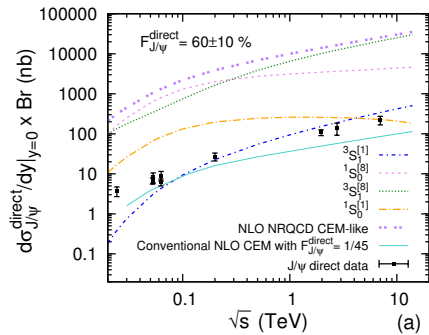
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- If, as it should be in NRQCD,  $\langle \mathcal{O}_{3S_1}(^3S_1^{[1]}) \rangle$  is the usual CS LDME, *i.e.*  $\frac{2N_C}{4\pi} (2J+1) |R(0)|^2$ , everything is fixed

## CEM results

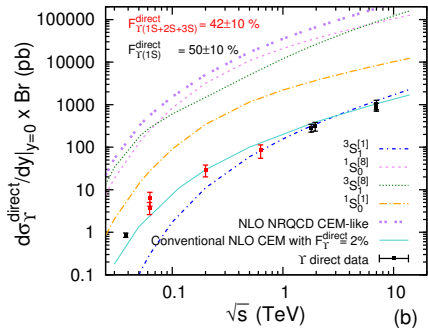
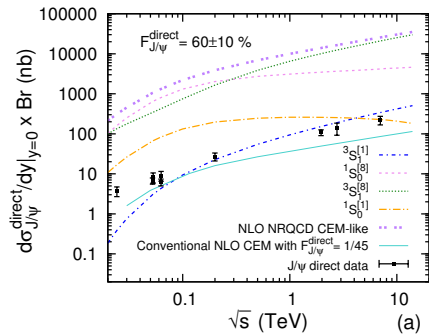


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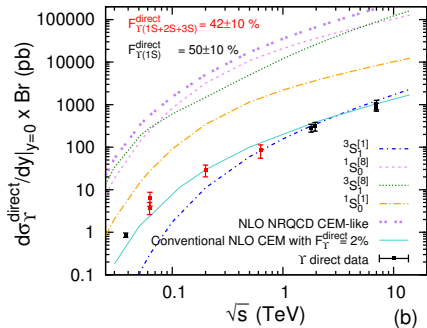
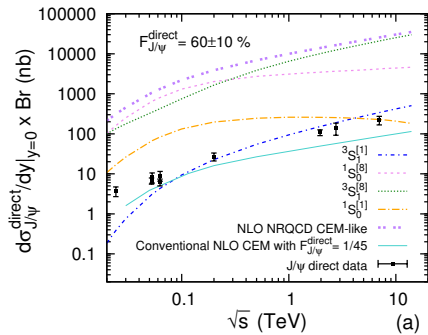
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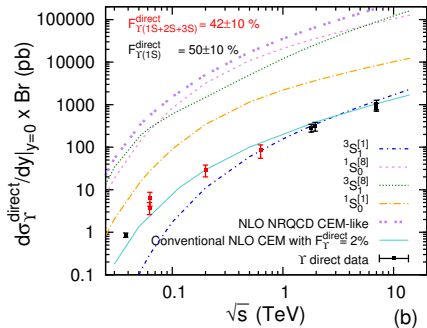
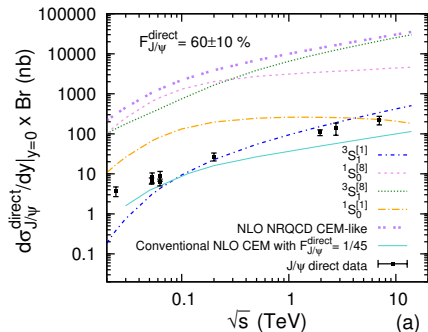
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  - Weird energy behaviour
- Conventional CEM does a pretty good job
  - No th. uncertainty shown
  - “Natural” value of  $F_{J/\psi}^{\text{direct}}$  is ok