

Supersymmetry and indirect constraints

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Searches for New Physics

- direct detection of new physics particles
- nature of Dark Matter
- indirect evidence for new physics

Indirect constraints

- search for new physics effects
- guideline for other searches
- check consistencies with direct observations

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Where to look for?

SUSY models can be divided into two categories:

- R-parity conserving models
- R-parity violating models

R-parity conserving models can also be divided according to how SUSY breaks:

- mSUGRA $\{m_0, m_{1/2}, A_0, \tan \beta, \text{sign}(\mu)\}$
- NUHM $\{\text{mSUGRA parameters} + M_A \text{ and } \mu\}$
- AMSB $\{m_0, m_{3/2}, \tan \beta, \text{sign}(\mu)\}$
- GMSB $\{\Lambda, M_{\text{mess}}, N_5, c_{\text{grav}}, \tan \beta, \text{sign}(\mu)\}$

In these models, SUSY effects always appear in loops

→ difficult to detect unless the SM process is absent or loop-mediated.

→ Good places to look for: $B - \bar{B}$ mixing, $b \rightarrow s\gamma$, ...

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SUSY Constraints

Observable	Constraint measure
$BR(B_s \rightarrow \mu\mu)$	0 ± 0
ΔM_{B_s}	0 ± 0
$\sin^2 \theta_{\text{eff}}$	0.007 ± 0
$BR(B \rightarrow \tau\nu)$	0.011 ± 0
M_W	0.051 ± 0.001
$BR(b \rightarrow s\gamma)$	0.188 ± 0.003
$\Delta_{0-}(b \rightarrow s\gamma)$	0.208 ± 0.006
$(g-2)_\mu$	0.390 ± 0.012
$\Omega_{DM} h^2$	0.443 ± 0.006
m_h	0.453 ± 0.053

Molding power of individual observables
for a specific MSSM scenario with $\mu > 0$

Allanach, Dolan and Weber, arXiv:0806.1184

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A public C-program for calculating different observables in supersymmetry

- Automatic calculation in mSUGRA, NUHM, AMSB and GMSB scenarios
- Compatible with the SUSY Les Houches Accord Format (SLHA2)
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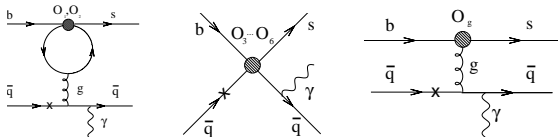
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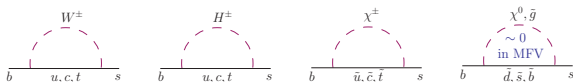
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1. Isospin asymmetry of $B \rightarrow K^* \gamma$ at NLO

Contributing loops:



$$\Delta_{0-} \equiv \frac{\Gamma(\bar{B}^0 \rightarrow \bar{K}^{*0} \gamma) - \Gamma(B^- \rightarrow K^{*-} \gamma)}{\Gamma(\bar{B}^0 \rightarrow \bar{K}^{*0} \gamma) + \Gamma(B^- \rightarrow K^{*-} \gamma)}$$

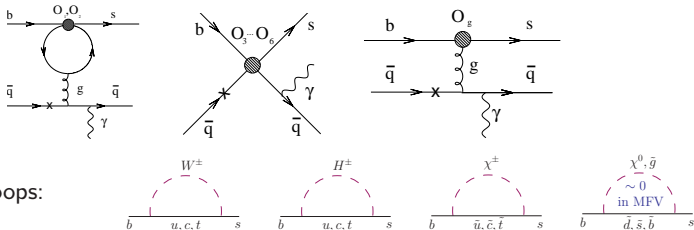
$$\Delta_{0-} = \text{Re}(b_d - b_u), \quad b_q = \frac{12\pi^2 f_B Q_q}{m_b T_1^{B \rightarrow K^*} a_7^c} \left(\frac{f_{K^*}^\perp}{m_b} K_1 + \frac{f_{K^*} m_{K^*}}{6\lambda_B m_B} K_2 \right)$$

$$a_7^c = C_7 + \frac{\alpha_s(\mu) C_F}{4\pi} \left(C_1(\mu) G_1(s_p) + C_8(\mu) G_8 \right) + \frac{\alpha_s(\mu_h) C_F}{4\pi} \left(C_1(\mu_h) H_1(s_p) + C_8(\mu_h) H_8 \right)$$

In the Standard Model: $\Delta_{0-} \simeq 8\%$

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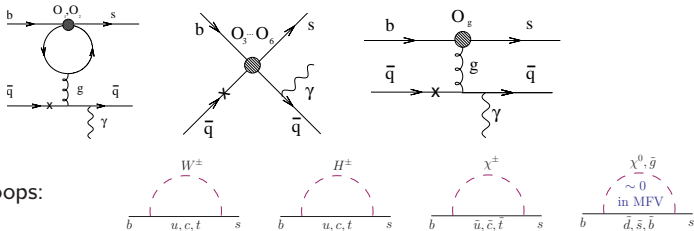
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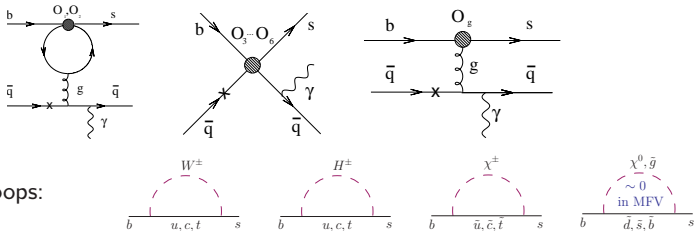
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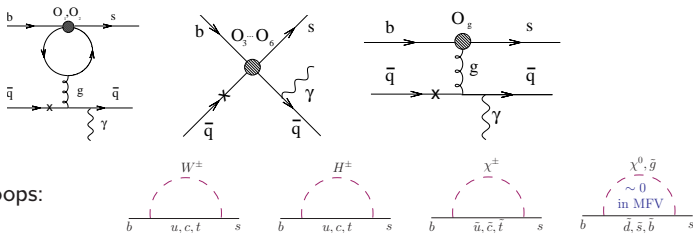
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2. Inclusive branching ratio of $B \rightarrow X_s \gamma$ at NNLO

$$\mathcal{B}(\bar{B} \rightarrow X_s \gamma)_{E_\gamma > E_0} = \mathcal{B}(\bar{B} \rightarrow X_c e \bar{\nu})_{\text{exp}} \left| \frac{V_{ts}^* V_{tb}}{V_{cb}} \right|^2 \frac{6\alpha_{\text{em}}}{\pi C} [P(E_0) + N(E_0)]$$

$$\text{with } C = \left| \frac{V_{ub}}{V_{cb}} \right|^2 \frac{\Gamma[\bar{B} \rightarrow X_c e \bar{\nu}]}{\Gamma[\bar{B} \rightarrow X_u e \bar{\nu}]}$$

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SM prediction: $\mathcal{B}[\bar{B} \rightarrow X_s \gamma] = (3.15 \pm 0.23) \times 10^{-4}$

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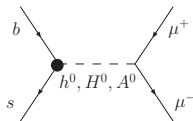
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3. Branching ratio of $B_s \rightarrow \mu^+ \mu^-$

$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = \frac{G_F^2 \alpha^2}{64 \pi^3} f_{B_s}^2 \tau_{B_s} M_{B_s}^3 |V_{tb} V_{ts}^*|^2 \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}} \\ \times \left\{ \left(1 - \frac{4m_\mu^2}{M_{B_s}^2}\right) M_{B_s}^2 |C_S|^2 + \left|C_P M_{B_s} - 2 C_A \frac{m_\mu}{M_{B_s}}\right|^2 \right\}$$



Upper limit: $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 5.8 \times 10^{-8}$ at 95% C.L.

SM predicted value: $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{SM} \sim 3 \times 10^{-9}$

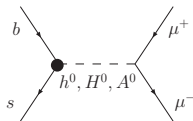
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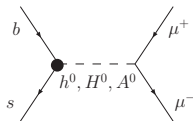
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$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = \frac{G_F^2 \alpha^2}{64\pi^3} f_{B_s}^2 \tau_{B_s} M_{B_s}^3 |V_{tb} V_{ts}^*|^2 \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}} \\ \times \left\{ \left(1 - \frac{4m_\mu^2}{M_{B_s}^2}\right) M_{B_s}^2 |C_S|^2 + \left|C_P M_{B_s} - 2 C_A \frac{m_\mu}{M_{B_s}}\right|^2 \right\}$$



Upper limit: $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 5.8 \times 10^{-8}$ at 95% C.L.

SM predicted value: $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{SM} \sim 3 \times 10^{-9}$

Interesting in the high $\tan \beta$ regime, where the SUSY contributions can lead to an $O(100)$ enhancement over the SM:

$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{MSSM} \sim \frac{m_b^2 m_\mu^2 \tan^6 \beta}{M_A^4}$$

SuperIso v2.3: implemented observables

4. Branching ratio of $B \rightarrow \tau \nu$

Tree level process, mediated by W^+ and H^+ , higher order corrections from sparticles



$$\mathcal{B}(B \rightarrow \tau \nu) = \frac{G_F^2 |V_{ub}|^2}{8\pi} m_\tau^2 f_B^2 m_B \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 \left|1 - \left(\frac{m_B^2}{m_{H^+}^2}\right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta}\right|^2$$

$$\epsilon_0 = -\frac{2\alpha_s}{3\pi} \frac{\mu}{m_{\tilde{g}}} H_2 \left(\frac{m_Q^2}{m_{\tilde{g}}^2}, \frac{m_D^2}{m_{\tilde{g}}^2}\right), \quad H_2(x, y) = \frac{x \ln x}{(1-x)(x-y)} + \frac{y \ln y}{(1-y)(y-x)}$$



Large uncertainty from V_{ub}

Also implemented in SuperIso:

$$R_{\tau \nu \tau}^{\text{MSSM}} = \frac{\text{BR}(B_u \rightarrow \tau \nu_\tau)_{\text{MSSM}}}{\text{BR}(B_u \rightarrow \tau \nu_\tau)_{\text{SM}}} = \left[1 - \left(\frac{m_B^2}{m_{H^+}^2}\right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta}\right]^2$$

SuperIso v2.3: implemented observables

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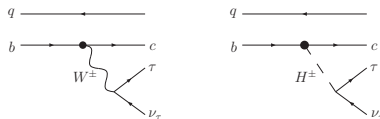
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SuperIso v2.3: implemented observables

5. Branching ratio of $B \rightarrow D\tau\nu$

Another tree level process:



$$\frac{d\Gamma(B \rightarrow D\ell\bar{\nu})}{dw} = \frac{G_F^2 |V_{cb}|^2 m_B^5}{192\pi^3} \rho_V(w) \left[1 - \frac{m_\ell^2}{m_B^2} \left| 1 - \frac{t(w)}{(m_b - m_c)} \frac{m_b}{m_{H^\pm}^2} \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right|^2 \rho_S(w) \right]$$

$w = v_B \cdot v_D$ ρ_V and ρ_S : vector and scalar Dalitz density contributions

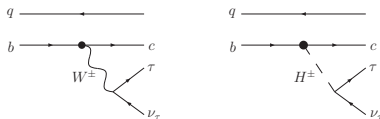
- Depends on V_{cb} , which is known to better precision than V_{ub}
- Larger branching fraction than $B \rightarrow \tau\nu$
- Experimentally challenging due to the presence of neutrinos in the final state

Implemented in SuperIso: $\mathcal{B}(B^- \rightarrow D^0 \tau^- \nu)$ and $\frac{\mathcal{B}(B^- \rightarrow D^0 \tau^- \nu)}{\mathcal{B}(B^- \rightarrow D^0 e^- \nu)}$

SuperIso v2.3: implemented observables

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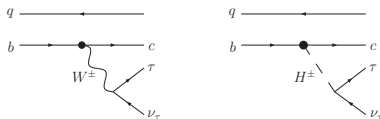
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Superlso v2.3: implemented observables

6. Branching ratio of $K \rightarrow \mu\nu$

Tree level process similar to $B \rightarrow \tau\nu$

Two observables are implemented in Superlso:

$$\frac{\Gamma(K \rightarrow \mu\nu)}{\Gamma(\pi \rightarrow \mu\nu)} = \left| \frac{V_{us}}{V_{ud}} \right|^2 \frac{f_K^2 m_K}{f_\pi^2 m_\pi} \left(\frac{1 - m_\ell^2/m_K^2}{1 - m_\ell^2/m_\pi^2} \right)^2 \\ \times \left(1 - \frac{m_{K^+}^2}{M_{H^+}^2} \left(1 - \frac{m_d}{m_s} \right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right)^2 (1 + \delta_{\text{em}})$$

$$R_{\ell 23} = \left| \frac{V_{us}(K_{\ell 2})}{V_{us}(K_{\ell 3})} \times \frac{V_{us}(0^+ \rightarrow 0^+)}{V_{ud}(\pi_{\ell 2})} \right| = \left| 1 - \frac{m_{K^+}^2}{M_{H^+}^2} \left(1 - \frac{m_d}{m_s} \right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right|$$

Large uncertainty from f_K/f_π

SuperIso v2.3: implemented observables

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Large uncertainty from f_K/f_π

SuperIso v2.3: implemented observables

7. Anomalous magnetic moment of muon $a_\mu = (g - 2)/2$

Latest measurement on e^+e^- data: $a_\mu^{\text{exp}} = (11\,659\,208.0 \pm 6.3) \times 10^{-10}$

Bennett *et al.*, Phys. Rev. D73 (2006)

SM prediction: $a_\mu^{\text{SM}} = (11\,659\,178.5 \pm 6.1) \times 10^{-10}$

MSSM contributions:

$$\delta a_\mu^{\text{SUSY}} = \delta a_\mu^{\chi^0} + \delta a_\mu^{\chi^\pm} + \delta a_{\mu, 2\text{loop}}^{\text{SUSY}}$$

Deviation from the SM:

$$\delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (29.5 \pm 8.8) \times 10^{-10}$$

SuperIso v2.3: implemented observables

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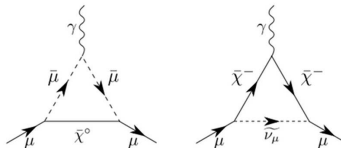
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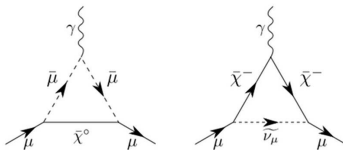
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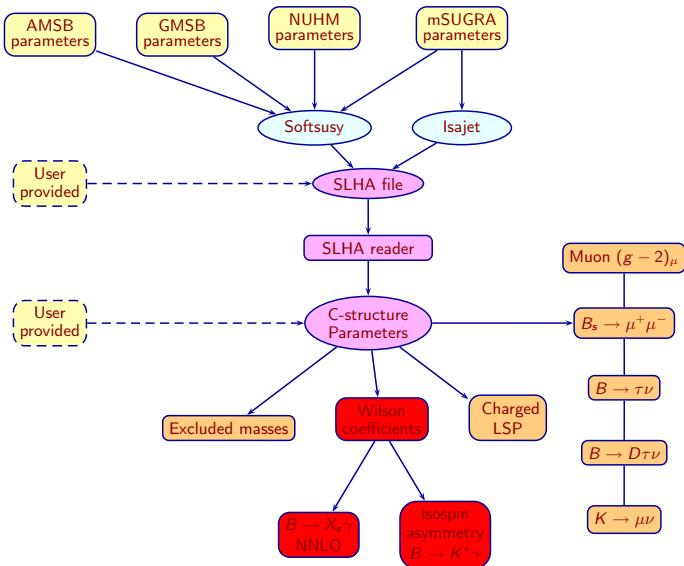
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SuperIso v2.3



SuperIso v2.3

Can be downloaded from:

<http://www3.tsl.uu.se/~nazila/superiso/>

Manual:

F. Mahmoudi, arXiv:0710.2067, Comput. Phys. Commun. 178, 745 (2008)

F. Mahmoudi, arXiv:0808.3144 [hep-ph]

For more information:

F. Mahmoudi, JHEP 0712, 026 (2007)

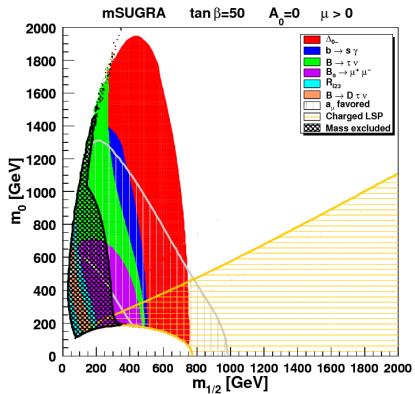
M. Ahmady & F. Mahmoudi, Phys. Rev. D75 (2007)

A. Arbey & F. Mahmoudi, Phys. Lett. B (2008)

D. Eriksson, F. Mahmoudi, O. Stål, JHEP 0811, 035 (2008)

Combined constraints in the MSSM

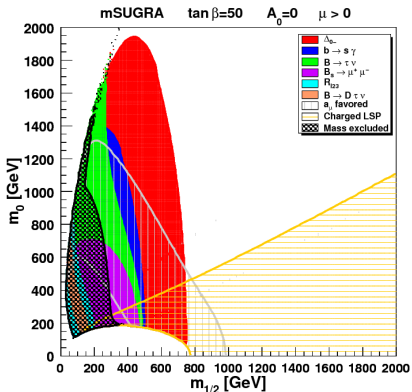
mSUGRA



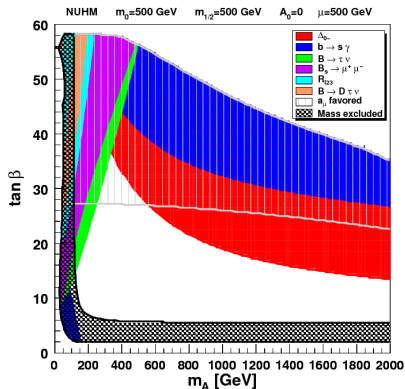
F. Mahmoudi, arXiv:0808.3144

Combined constraints in the MSSM

mSUGRA



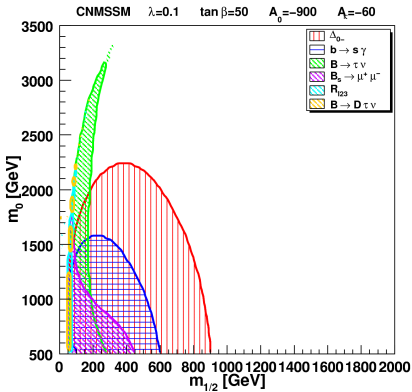
NUHM



F. Mahmoudi, arXiv:0808.3144

Combined constraints in the NMSSM

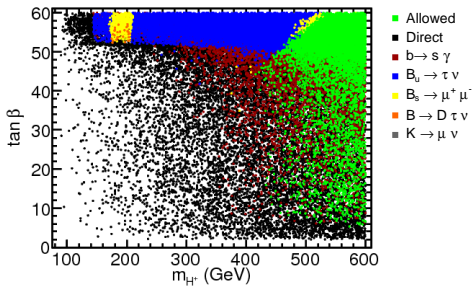
CNMSSM



F. Mahmoudi, preliminary results

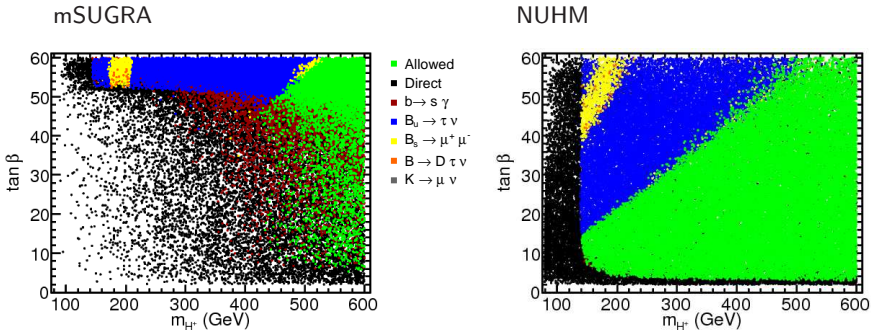
Application to the charged Higgs

mSUGRA



D. Eriksson, F. Mahmoudi, O. Stål, arXiv:0808.3551

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D. Eriksson, F. Mahmoudi, O. Stål, arXiv:0808.3551

Conclusion

- Indirect constraints and in particular flavor physics are essential to restrict new physics parameters
- That will become even more interesting when combined with LHC data
- This kind of analysis should be generalized to more new physics scenarios

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- Extension to NMSSM
- Implementation of the relic density calculation (with A. Arbey)
- Extension to NMFV
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