

# Summary of Generative Modelling Workshop

Learning to Discover, Paris 2022  
Johnny Raine, University of Geneva



Three long talks, two shorter talks, two breakout sessions, one happy hour



# Topics

1. Detector simulation
2. Four-vector simulation
3. Molecules
4. PDE Solving

# Detector Simulation

## Generative Modelling for Detector Simulation

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## Fast Calorimeter Simulation Challenge 2022

calochallenge.github.io/homepage



Michele Faucci Giannelli, Gregor Kasieczka,  
Claudius Krause, Ben Nachman, Dalila Salamani,  
David Shih, and Anna Zaborowska

Learning to Discover, Workshop on Generative Models,  
April 26th 2022



## Meta-learning for fast simulation of multiple calorimeter responses

Dalila Salamani, Anna Zaborowska & Witold Pokorski  
CERN, EF-SFT

This work benefited from support by the CERN Strategic R&D Programme on Technologies for Future Experiments (CERN-OPEN-2018-000)

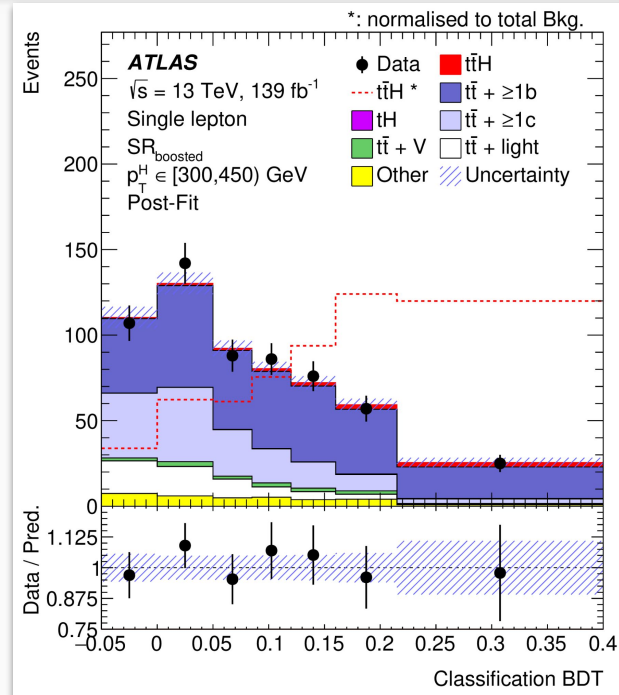


*Learning to discover, Workshop on Generative Models 26/04/2022*

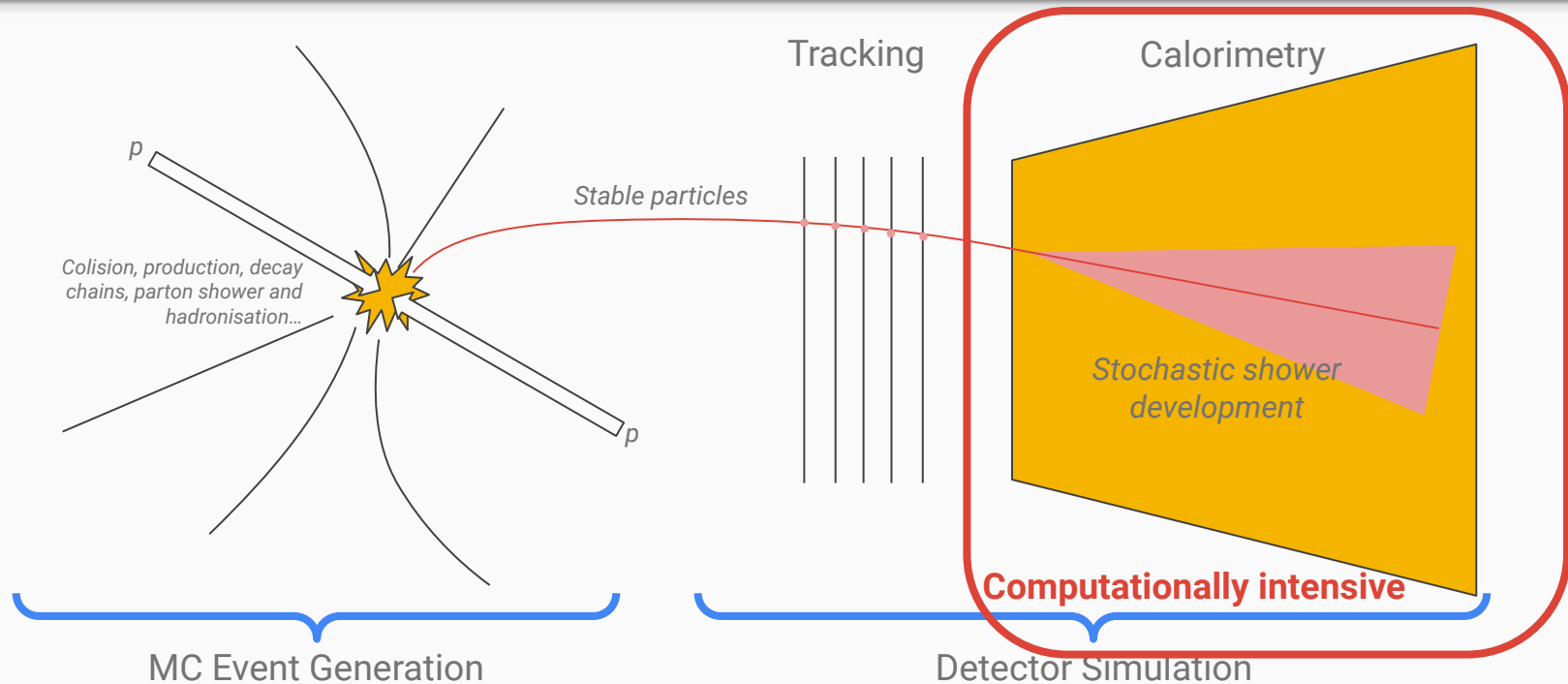
# Introduction

Key part of a physics analyses is to have a reference

- Does data fit Hypothesis 1 or Hypothesis 2?
  - Amount of signal on top of background
  - Deviation away from expectation
- Need accurate simulation of underlying processes->recorded data in most settings

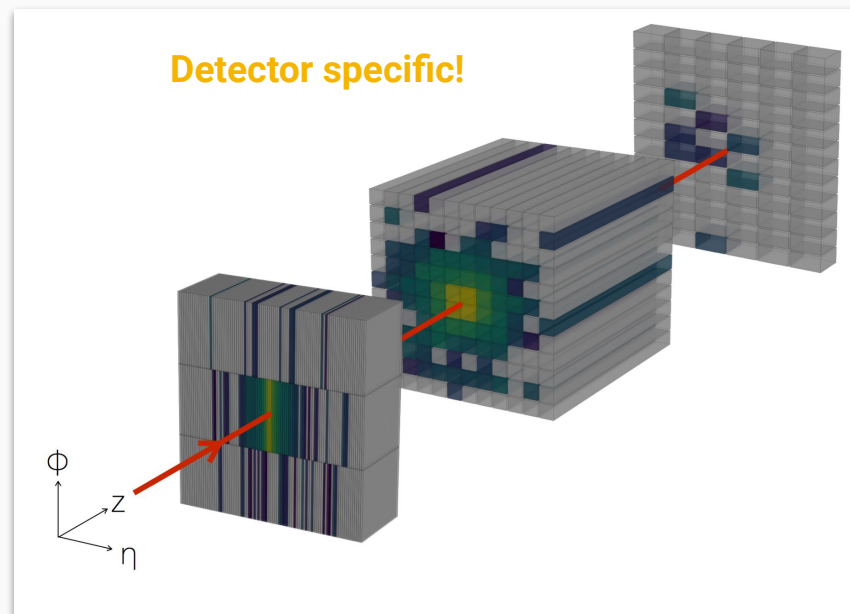


# What happens in a particle collision



# Calorimeter Output

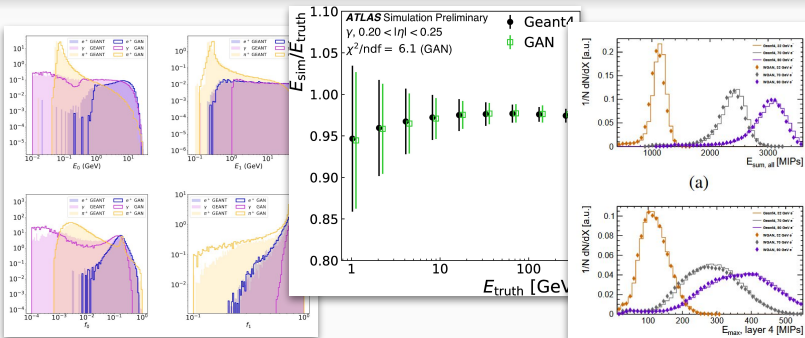
- Individual particle traverses detector
- Energy deposited in many cells from secondary particles in shower
- Can build an “image” but
  - **High dynamic range** of “pixels”
  - Often very **sparse**
  - **Stochastic** - same incoming particle results in different shower
- Assess performance with complex distributions over many events



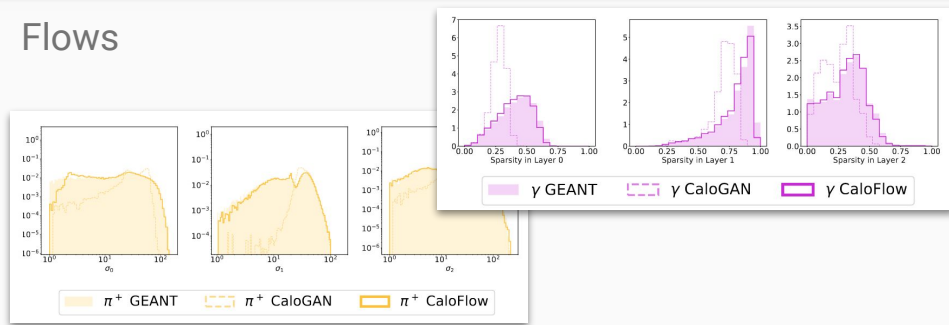
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# Wide range of models

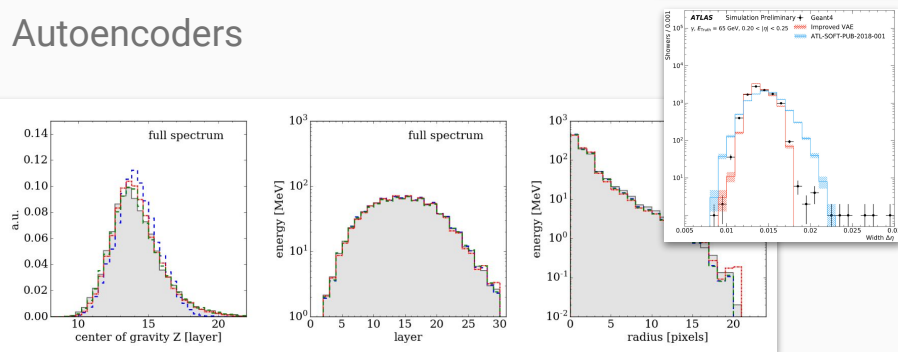
## GANs



## Flows



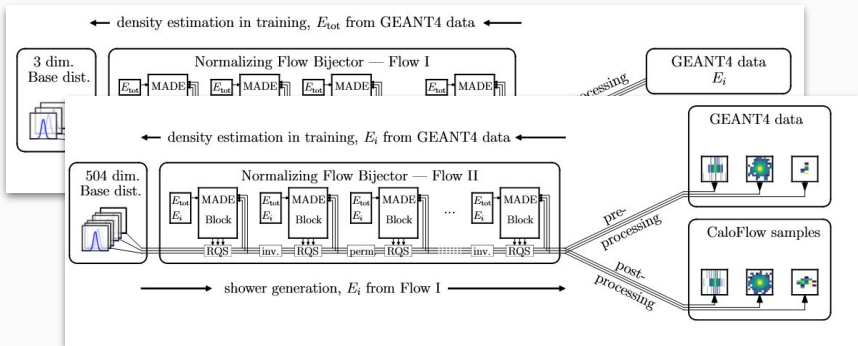
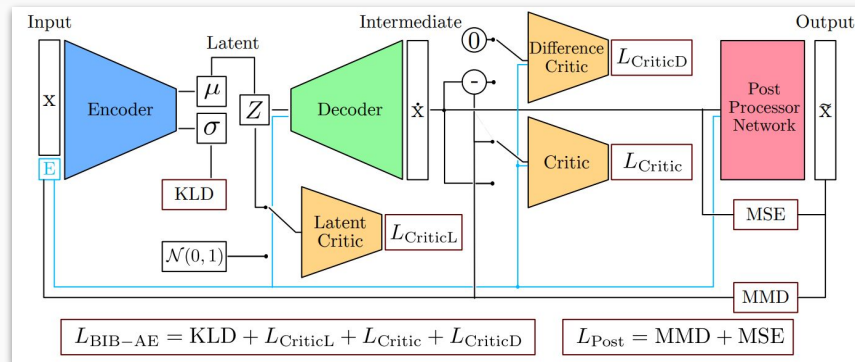
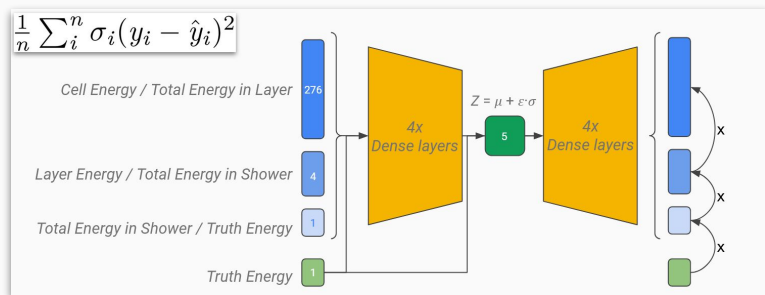
## Autoencoders



Performance measured over lots of distributions

- Impossible to judge individual showers

# Wide range of models of varying complexity



But lots of common themes

- Focus on better modelling of total energy
  - Additional critic/constrainer networks
  - Auxilliary term in loss
- Widths and sparsity of data is a challenge!

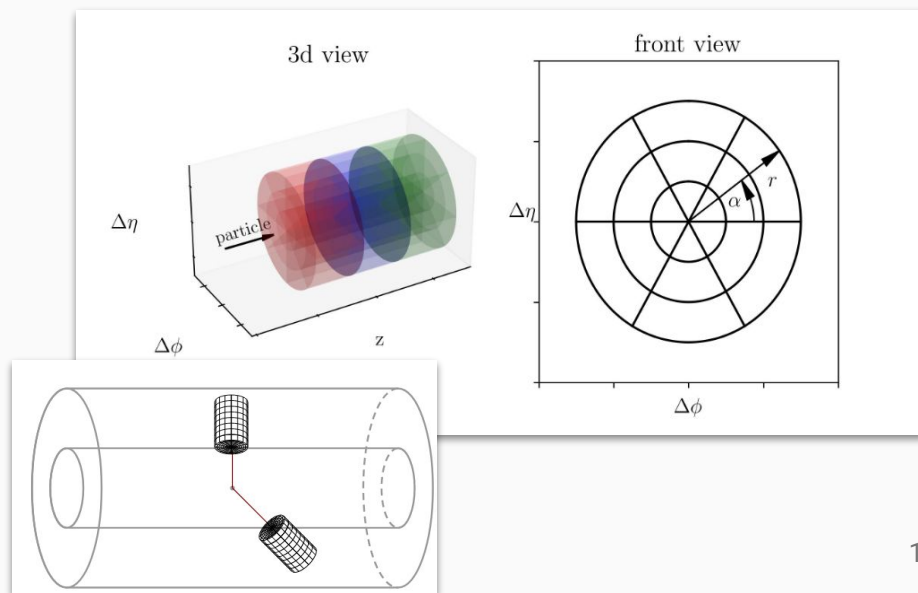
# Calorimeter Challenge

Lots of models but not easy to compare - different detectors, different datasets

- Challenge: 3 datasets for benchmarking
- Same format, different granularity
- Increasing complexity through granularity
  - Dim.  $O(500)$ ,  $O(6000)$ ,  $O(40k)$

Dataset 1: ATLAS open data, detector, layers

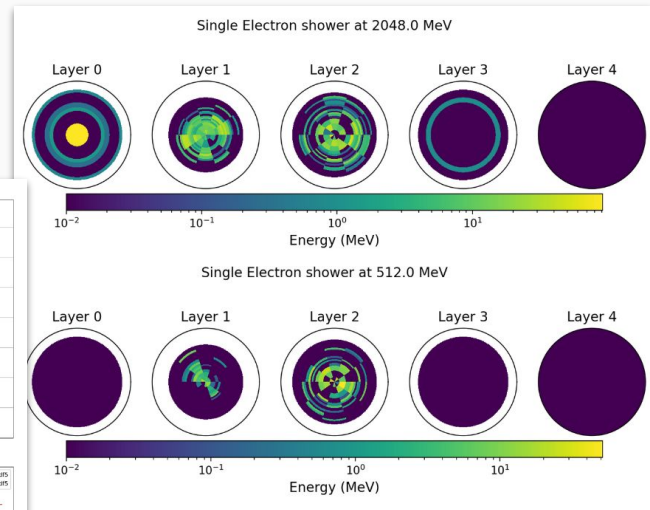
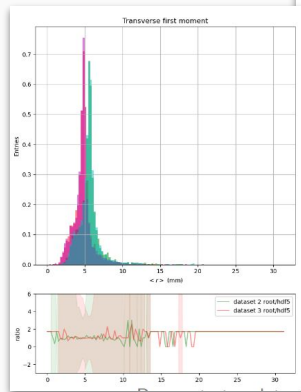
Dataset 2+3: Simplistic geometry, but 45 layers



# Calorimeter Challenge

Lots of models but not easy to compare - different detectors, different datasets

- Provide **common** code for evaluating **metrics**, plots
- Inference framework for fair **timing comparison**
- Three granularities, additional slices of detector available



# Input data challenges

Sparsity of deposits and reproducing high dynamic range still a tough ask!

Getting tails of distributions hard

- But often key descriptors for underlying physics

Need to accurately learn the PDF of showers including the stochasticity

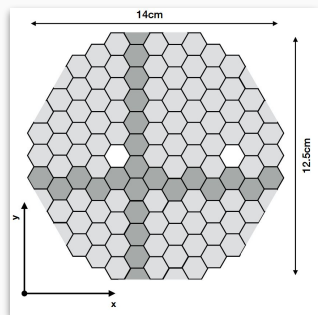
- How to enhance focus on reconstruction of tails but keep this property
- Only a handful of conditional parameters - particle four vector

Detectors not designed to be easy to simulate!

# Data format

Not restricted to using readout or detector

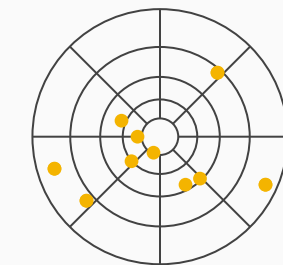
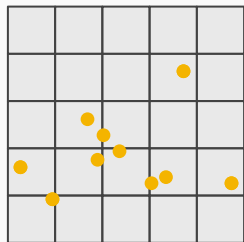
- Use more natural representation?



Work with detector cells

Learn in needed domain, granularity

Doesn't generalise with  
consistent geometry  
Geometry often nontrivial



Map hits to polar grid

Shower evolution cone shaped

To remove edge effects need fine,  
sparse, binning

Showers produce

- Variable number of energy deposits
- Correlated spatial ordering but no natural ordering

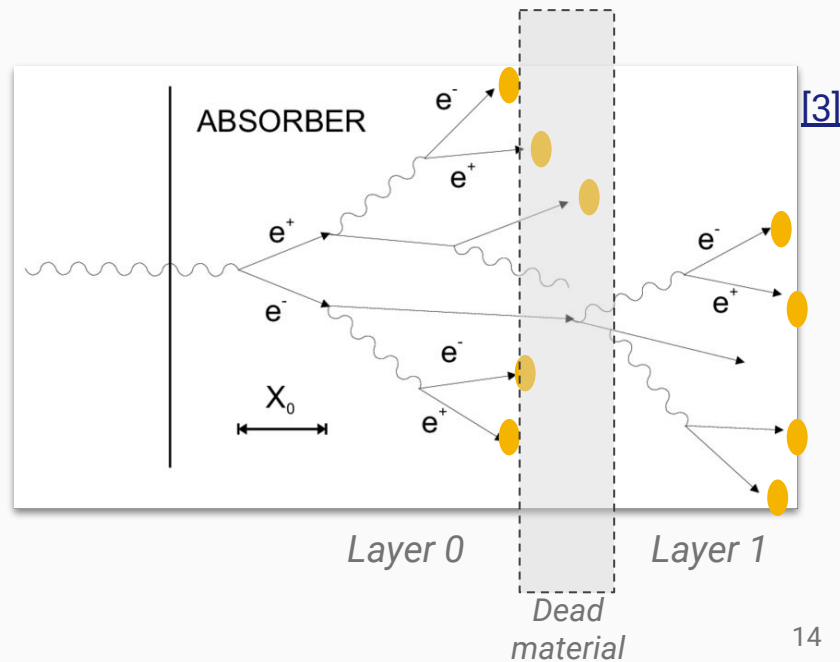


Point cloud

Direct translation of input data  
**Use graph networks!**  
Preserve natural symmetries

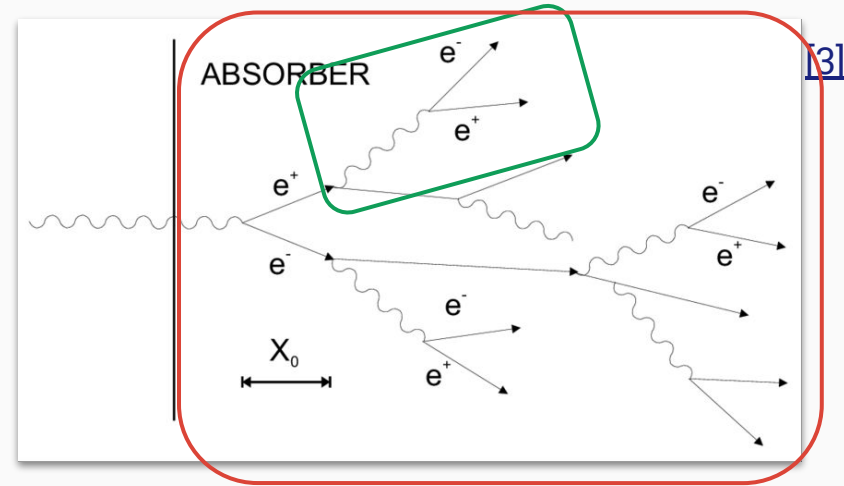
# Brainstorming discussion - Data

- Are we hiding information from the networks?
  - Don't utilise shower development
  - Only look at energy in active material
- How to use low level information
  - Inspiration from molecules?
  - Project into higher/lower dim space?



# Brainstorming discussion - Data

- Why not exploit underlying physics development in model design
- Characteristic of shower depends on particle and energy
  - Not what happened before
  - Could somehow exploit in development of shower?



# Brainstorming - Getting into production

- What do we need to generate - can focus too much on one thing!
  - Different particles, regions, physics of interest mandate differences
  - Avoid being fooled you're doing well looking just at one distribution
- Scalability
  - Can we handle higher dimensions, validation
  - Can overshoot needed granularity - more margin for error
- Aim instead to fix faster simulation, don't replace
  - **Multi-fidelity simulation**
- How to **transfer** to more **regions/particles/detectors**

# Meta-Learning

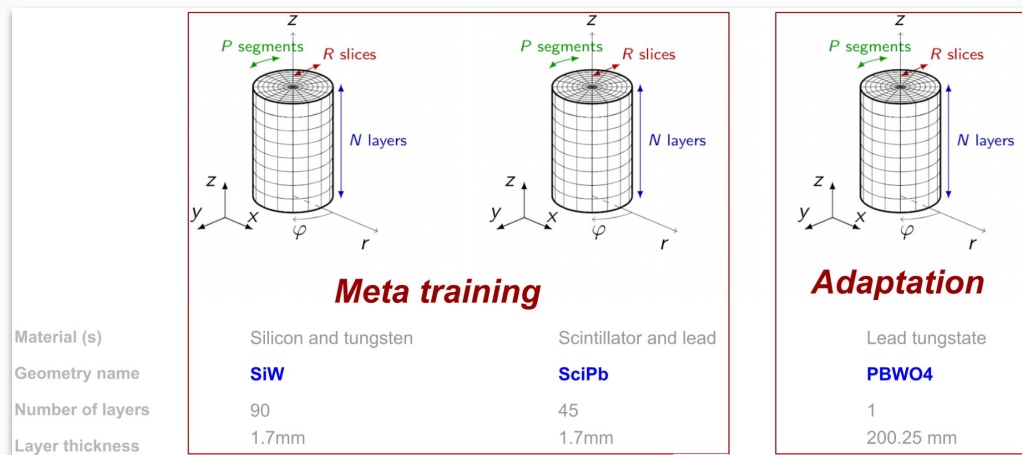
How easily can we adapt for different detector materials?

Autoencoder model, fixed input/output description

- **Generalised description of a shower**

Train on one composition, apply to another

- Provide initial general solution
- Can it save training time with adaptation?

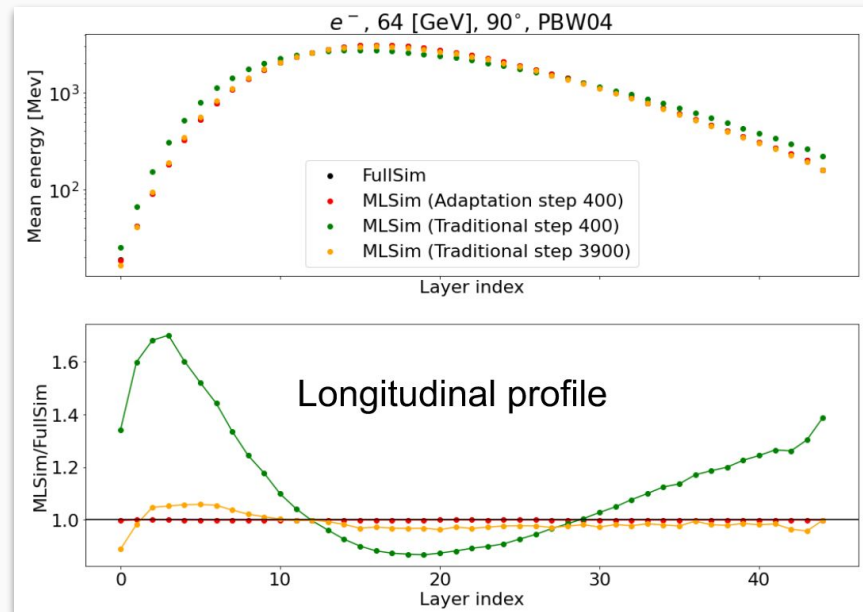


# Meta-Learning

Compare

- **Transfer learning** w/ 400 epochs
- **400 epochs** from scratch
- **3900 epochs** from scratch

In generalised shower representation  
much faster convergence  
(order seconds!)



# Four-vector Simulation

## 4-Momentum Generation

Sascha Diefenbacher, University of Hamburg

Learning To Discover, Paris 2022



Universität Hamburg

DER FORSCHUNG | DER LEHRE | DER BILDUNG

CLUSTER OF EXCELLENCE

QUANTUM UNIVERSE

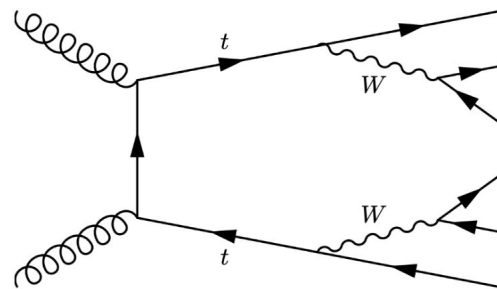
# Four vector simulation

- Look to replace MC generation of underlying physics processes
- Output four momenta of particles
- Studied with
  - GANs
  - Flows

- Particle number and type fixed
- Ordered list of floats

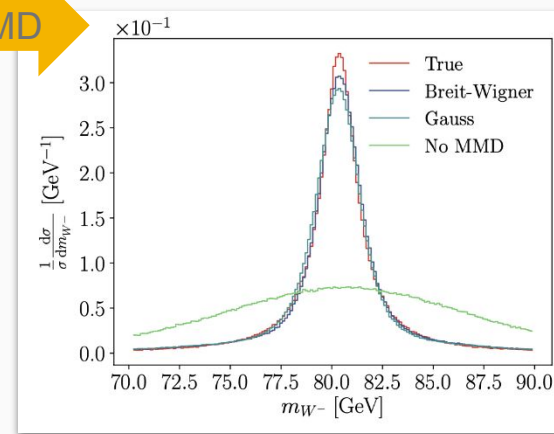
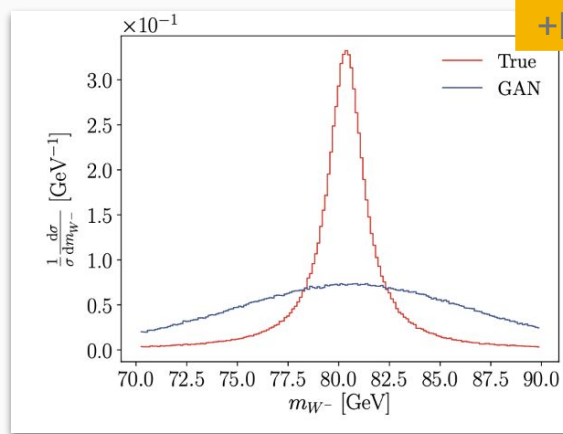
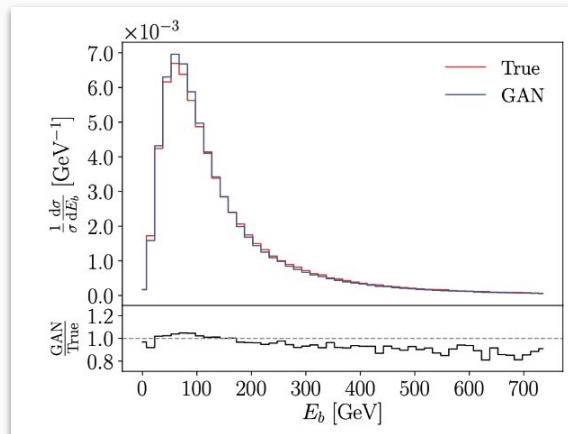
$$\begin{bmatrix} p_{1,particle1} \\ p_{2,particle1} \\ p_{3,particle1} \\ \vdots \\ p_{3,particle6} \end{bmatrix}$$

$$pp \rightarrow t\bar{t} \rightarrow (bW^-) (\bar{b}W^+) \rightarrow (bq_1\vec{q}'_1) (\bar{b}q_2\vec{q}'_2)$$



# GANs

Using GANs gets direct targets well modelled but building correlated distributions too wide! Add MMD term

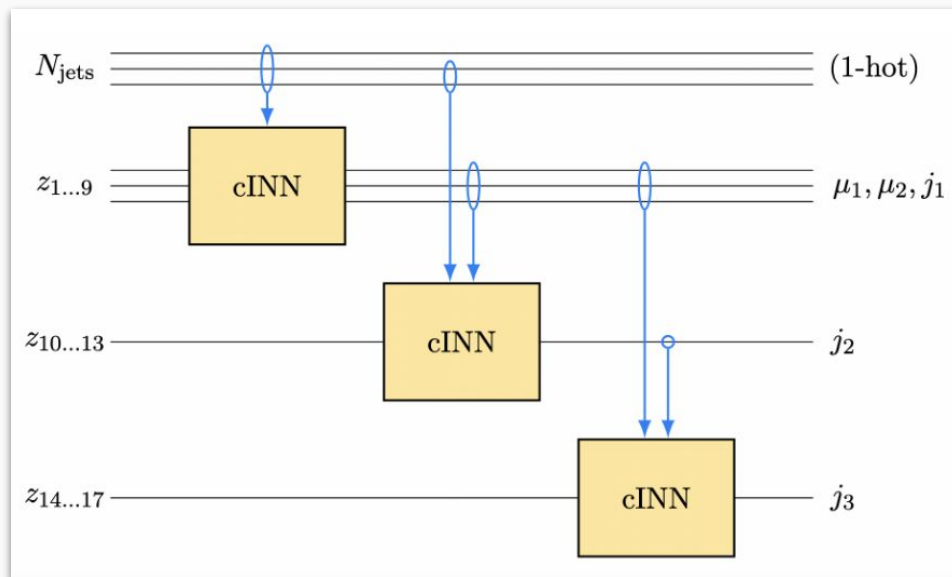


# Flows

Well suited to low dimensionality, good at learning density dist. (read correlations!)

Flows have fixed dimensionality

- Want to Generate processes with variable multiplicities
- Be clever with architecture

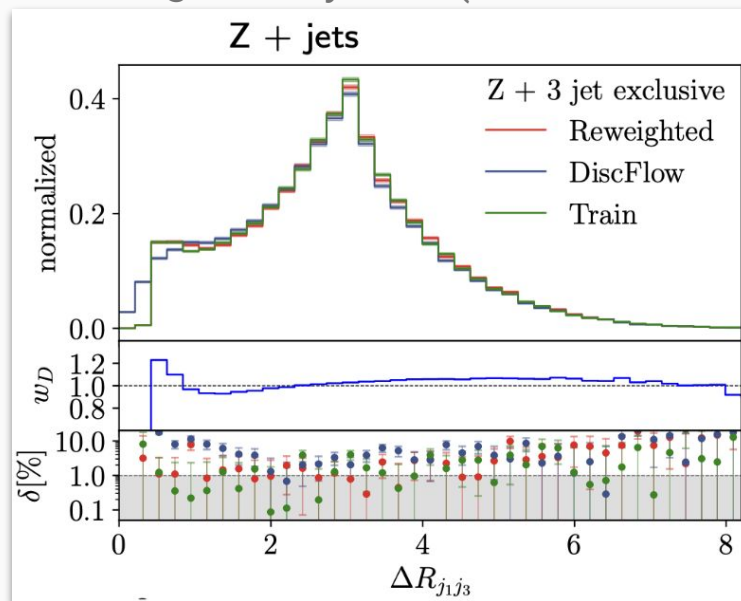


# Flows

Well suited to low dimensionality, good at learning density dist. (read correlations!)

- Much better performance than GANs, but some residuals
- Correct with ML reweighting

Using Bayesian NNs doesn't capture mismodelling with an uncertainty!



# Brainstorming

Many similarities across detector simulation and event generation

- Focus on wide range of distributions constructed from outputs
- Need to be smart with architecture design and losses!

How much do we need to replace, where can we speed up current implementations with ML

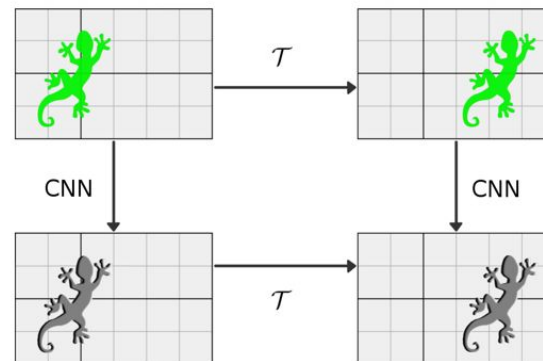
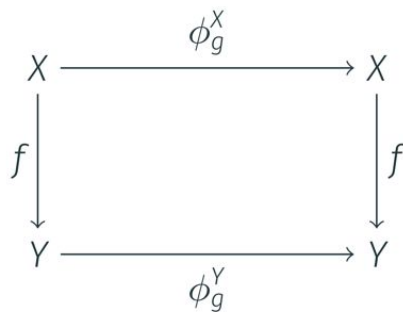
- Getting **final closure with reweighting** seen already with Flows, PDEs
- Speed up and **replace slow components** e.g. Vegas integration
- **MCMC with generative modelling** shown to be powerful

# Molecule Generation



# Equivariances in Networks

let  $f: X \rightarrow Y$  be a function and  $\phi^X$  and  $\phi^Y$  be transformations on  $X$  and  $Y$   
 then  $f$  is said to be *equivariant* iff  $f \circ \phi_g^X = \phi_g^Y \circ f$



# Equivariances in Networks

Updating nodes and rotating are equivariant operations  
Need to make sure updates in GNN are equivariant

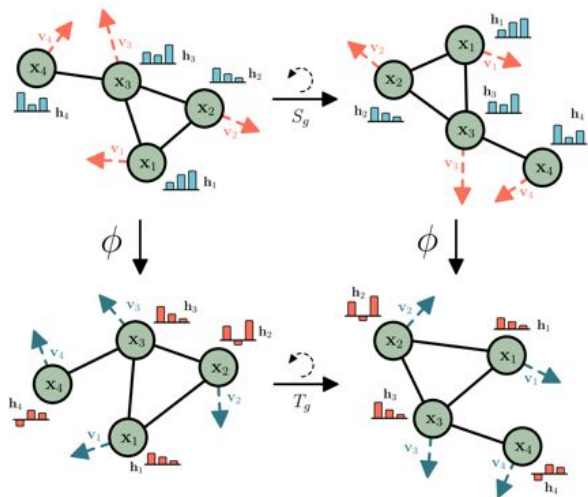


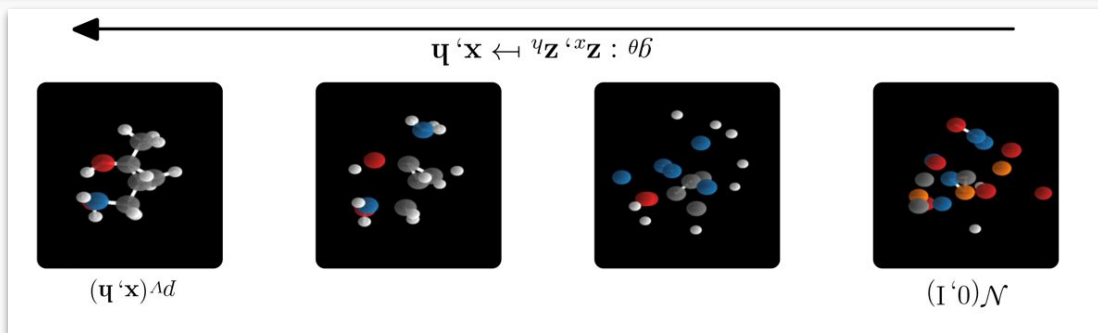
Figure 1. Example of rotation equivariance on a graph with a graph neural network  $\phi$

$$\mathbf{m}_{ij} = \phi_e(\mathbf{h}_i^l, \mathbf{h}_j^l, d_{ij}^2, a_{ij}), \mathbf{h}_i^{l+1} = \phi_h(\mathbf{h}_i^l, \sum_{j \neq i} \tilde{e}_{ij} \mathbf{m}_{ij}),$$

$$\mathbf{x}_i^{l+1} = \mathbf{x}_i^l + \sum_{j \neq i} \frac{\mathbf{x}_i^l - \mathbf{x}_j^l}{d_{ij} + 1} \phi_x(\mathbf{h}_i^l, \mathbf{h}_j^l, d_{ij}^2, a_{ij}), \quad (12)$$

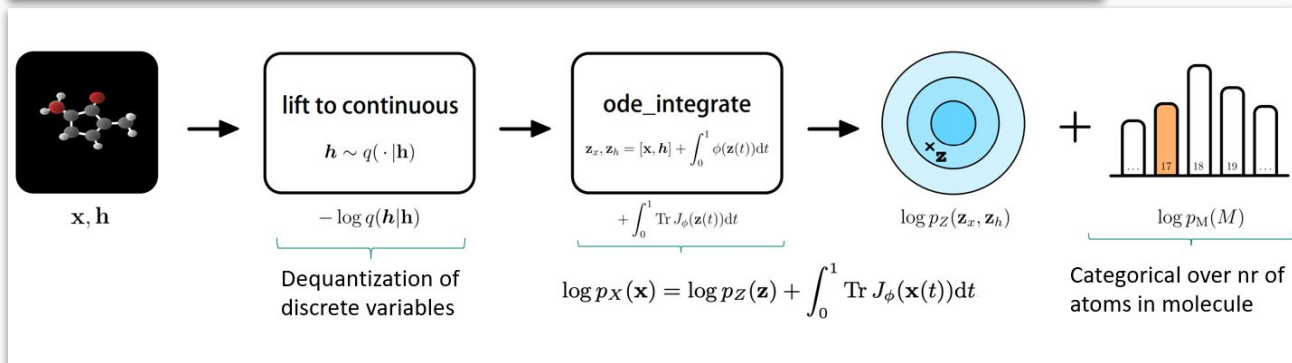
GNNs can be used as blocks in many network architectures

# Molecule generation with equivariant flows



Apply normalising flows to molecule generation

Transformation parametrised with equivariant operations



# Molecule generation with equivariant flows

Encoder (noiser)

$$q(\mathbf{z}_t | \mathbf{z}_s) = \mathcal{N}(\mathbf{z}_t | \alpha_t \mathbf{z}_s, \sigma_t^2 \mathbf{I})$$

$$\mathbf{z}_t = \alpha_t \mathbf{x} + \sigma_t \epsilon$$

Objective

$$\log p(\mathbf{x}) \geq \mathcal{L}_0 + \mathcal{L}_{\text{base}} + \sum_{t=1}^T \mathcal{L}_t$$

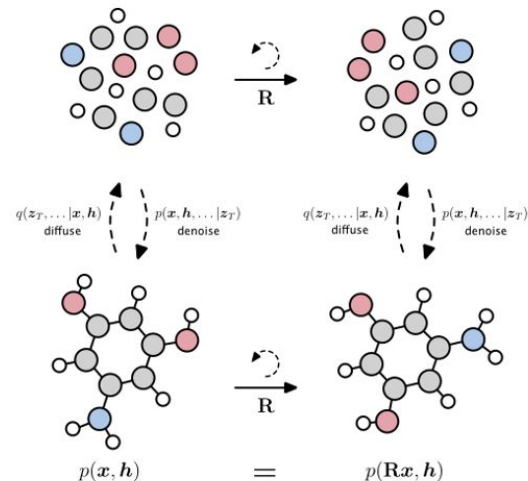
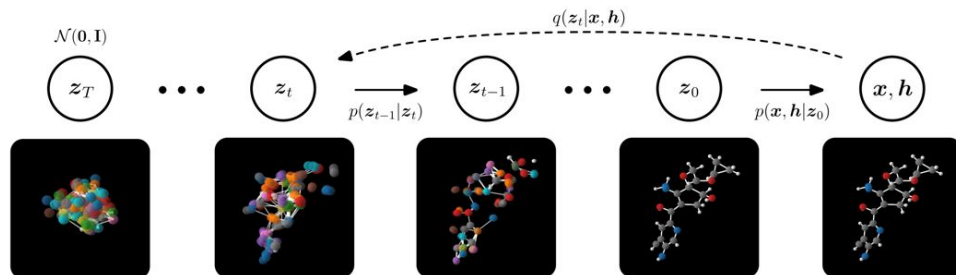
$$\mathcal{L}_t = -\text{KL}(q(\mathbf{z}_s | \mathbf{x}, \mathbf{z}_t) \| p(\mathbf{z}_s | \mathbf{z}_t))$$

Decoder (denoiser)

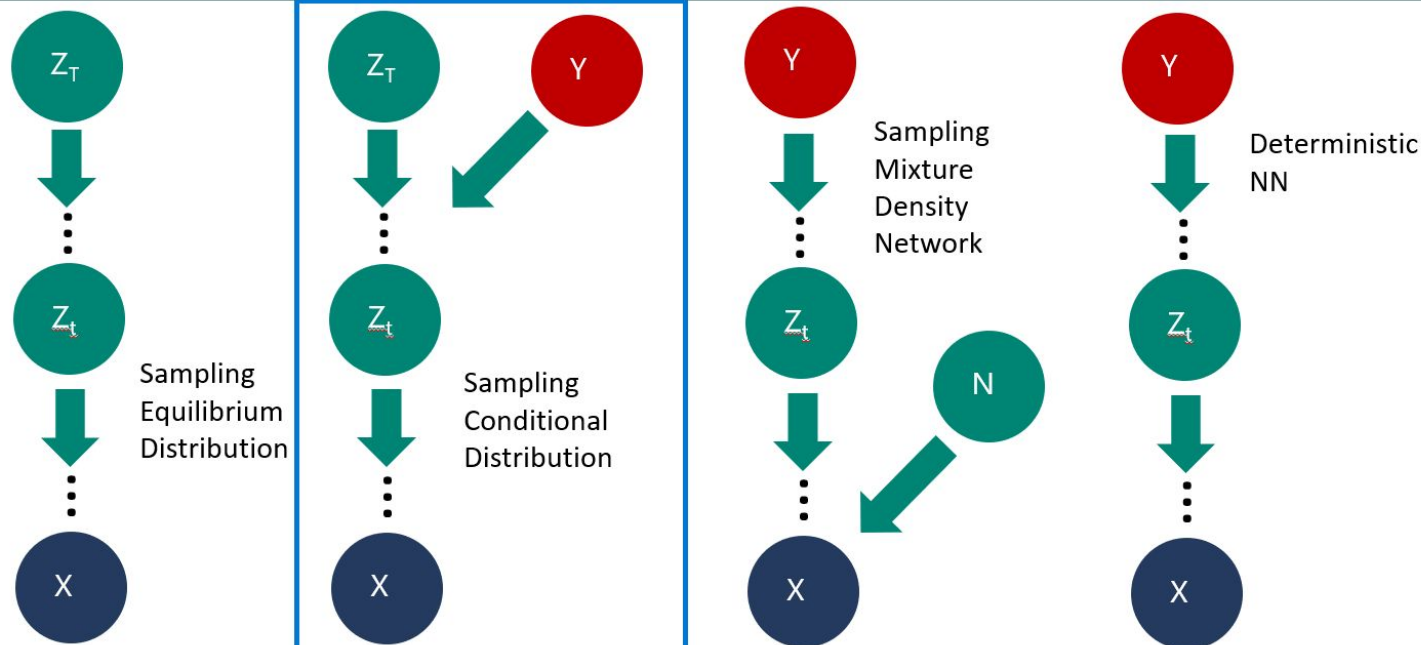
$$p(\mathbf{z}_s | \mathbf{z}_t) = \mathcal{N}(\mathbf{z}_s | \boldsymbol{\mu}_{t \rightarrow s}(\hat{\mathbf{x}}, \mathbf{z}_t), \sigma_{t \rightarrow s}^2 \mathbf{I})$$

$$\hat{\mathbf{x}} = \phi(\mathbf{z}_t, t) \xrightarrow{\text{EGNN Model}} \hat{\epsilon} = \phi(\mathbf{z}_t, t)$$

$$q(\mathbf{z}_s | \mathbf{x}, \mathbf{z}_t) = \mathcal{N}(\mathbf{z}_s | \boldsymbol{\mu}_{t \rightarrow s}(\mathbf{x}, \mathbf{z}_t), \sigma_{t \rightarrow s}^2 \mathbf{I})$$



## Conditional Generation is Hard (but = holy grail)



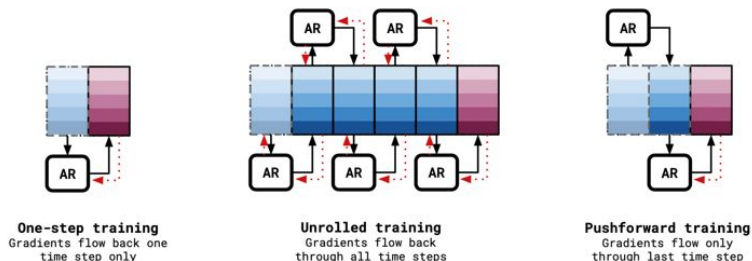
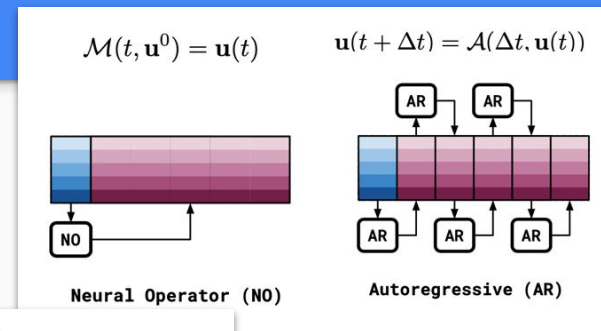
# PDEs

Describe evolution of systems

Great talk from Max Welling

$$L_{\text{stability}} = \mathbb{E}_k \mathbb{E}_{\mathbf{u}^{k+1} | \mathbf{u}^k, \mathbf{u}^k \sim p_k} [\mathbb{E}_{\epsilon | \mathbf{u}^k} [\mathcal{L}(\mathcal{A}(\mathbf{u}^k + \epsilon), \mathbf{u}^{k+1})]]$$

$$\text{with } (\mathbf{u}^k + \epsilon) = \mathcal{A}(\mathbf{u}^{k-1})$$

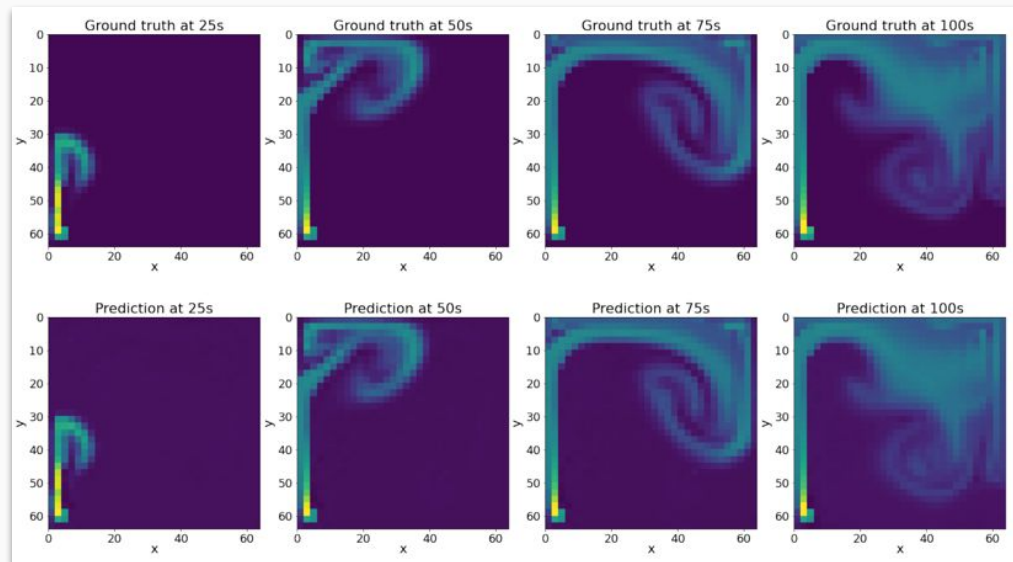


- We train to predict the right answer from a noisy input.
- Noise is given by numerical integration errors.
- Temporal bundling: predict many timesteps in together.

# PDEs

Great predictions for time evolution of systems

- Smoke with 2D Navier Stokes
- Shock waves with Burgers equation
- Modelling waves with KdV equation



# Summary

# Summary

Great workshop with lots of discussion - big focus on detector simulation

- Very active area in HEP with generative modelling
- By no means a solved problem, but moving to deployment

Success in wide range of physical sciences and applications

Room for lots more synergy and inspiration between models across physics domains, leveraging symmetries and invariances

# Backup

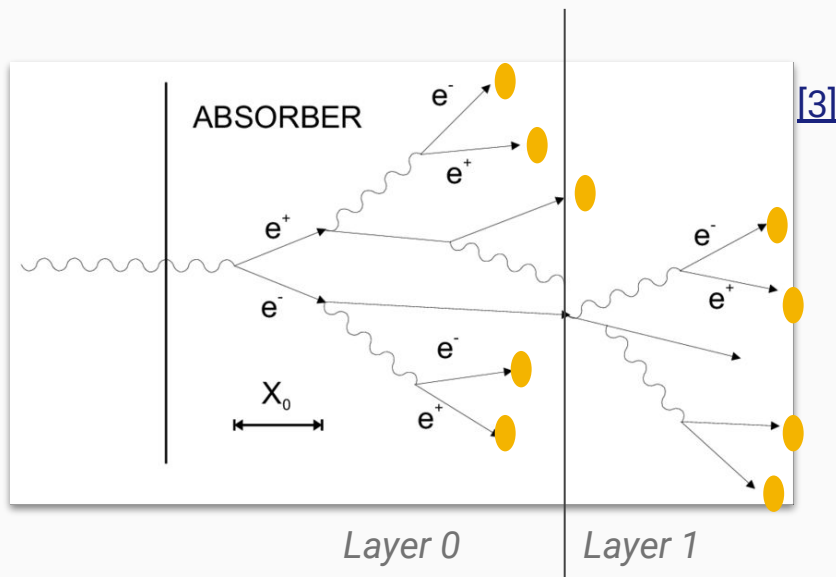
# Point Clouds

But! - Don't record history of shower development

- Each point (E, x) is end of a branch!
- Multiplicity can be incredibly high
- Points aren't directly connected
- Density of points between layers correlated but cannot easily build a physical graph
- Typically no time information, just layer depth

And for sampling calorimeters dead material

- Low sampling fraction - lots of missed hits!



*Current point cloud models aren't designed to learn underlying structure - they focus on learning surfaces or connected structure!  
Difficult to use standard benchmarks!*