

# Quarkonium production: where do we stand and where to go ?

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French-Ukrainian Workshop

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# Part I

## Quarkonium production mechanisms

# Approaches to Quarkonium Production

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  - 3 COLOUR OCTET MECHANISM (encapsulated in NRQCD): **higher Fock states** of the mesons taken into account;  $Q\bar{Q}$  can be produced in octet states with different quantum # as the meson; bleaching with semi-soft gluons ?

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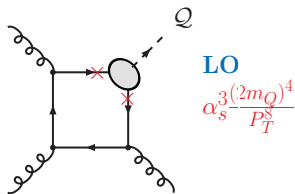
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## 3 COLOUR OCTET MECHANISM

- one non-perturbative parameter per Fock State
- expansion in  $v^2$ ; series can be truncated
- the phenomenology partly depends on this
- HQSS relates some non-perturbative parameters to each others and to a specific quarkonium polarisation

# Basic pQCD approach: the Colour Singlet Model (CSM)

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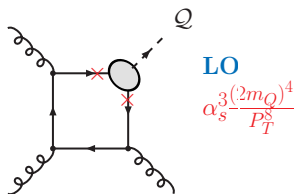


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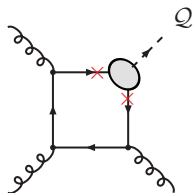
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$$\text{LO} \\ \alpha_s^3 \frac{(2m_Q)^4}{P_T^8}$$

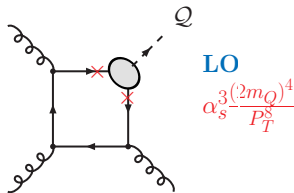
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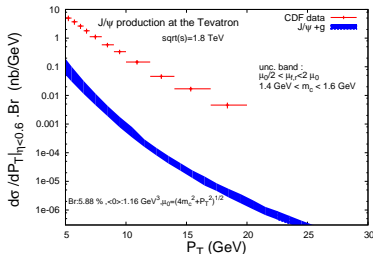
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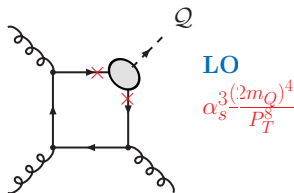
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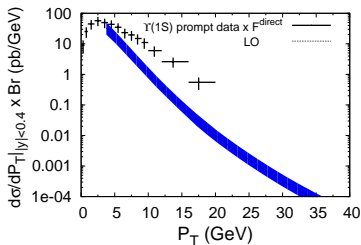
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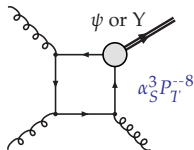
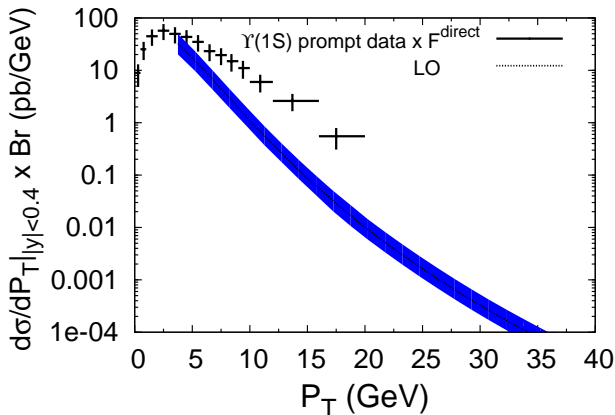


CDF, PRL 88:161802,2002

# QCD corrections to the CSM for $\Upsilon$ at colliders

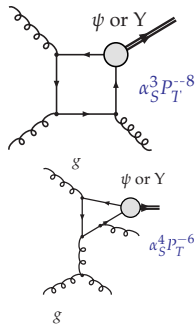
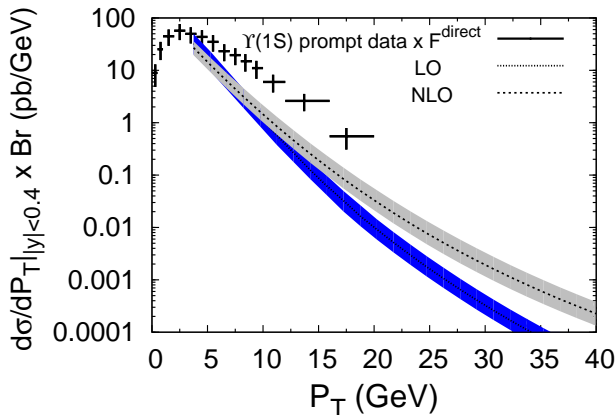
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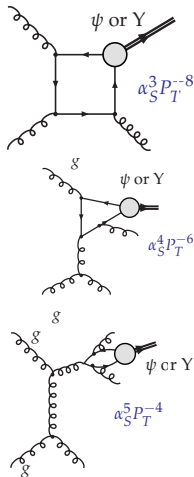
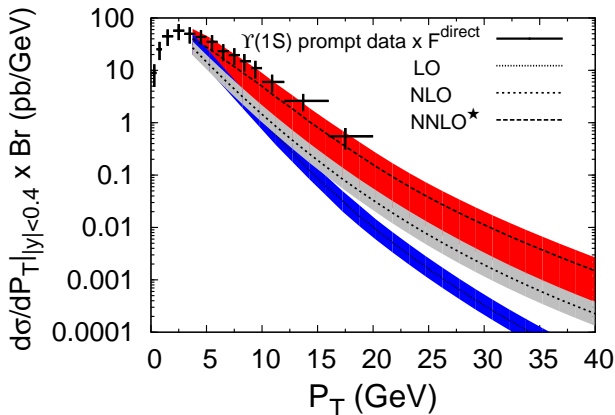
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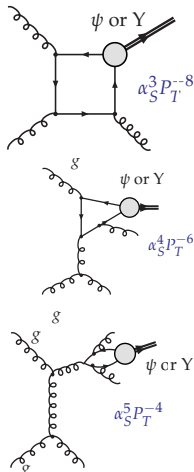
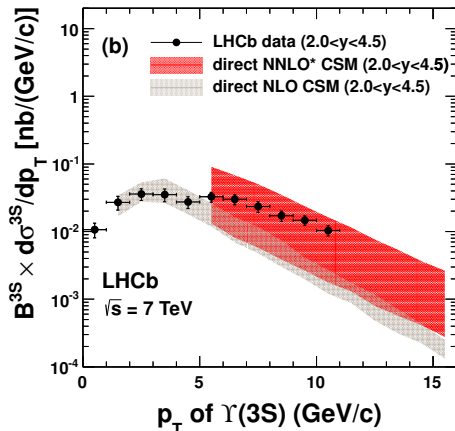
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Attention: the NNLO\* is not a complete NNLO  
 See a recent study by H.S. Shao JHEP 1901 (2019) 112

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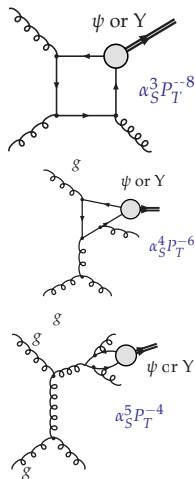
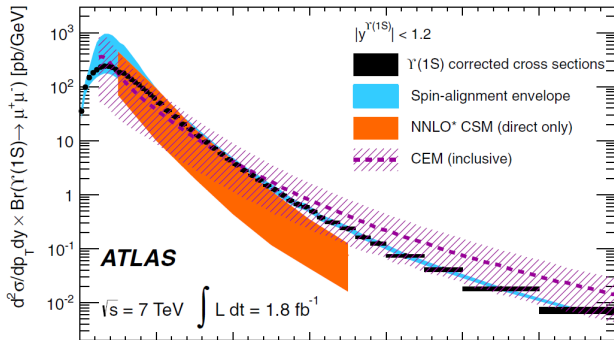


$\Upsilon(3S)$ : 60 % direct;  $\Upsilon(2S)$ : 60-70 % direct;  $\Upsilon(1S)$ : 50-70 % direct



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CSM theory curve extrapolated to prompt:  $\times 2$

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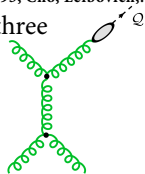
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- ✓ Gluon fragmentation then LO in  $\alpha_S$ : larger rates
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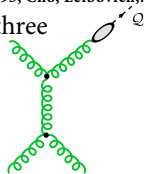
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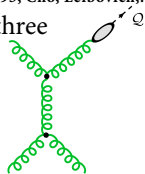
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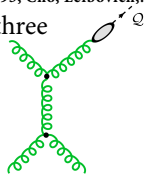
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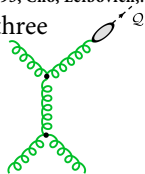
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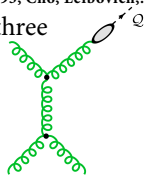
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✗ Cannot describe both the high- $P_T$  and  $P_T$ -integrated hadroproduction yields

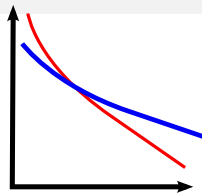




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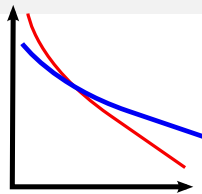
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$\psi$  data: a little less hard than the blue curve

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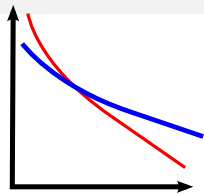
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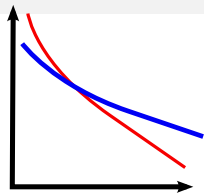
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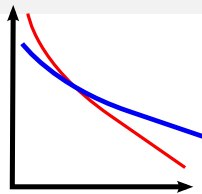
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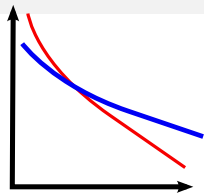
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# QCD corrections to the CEM $P_T$ dependence

JPL, H.S. Shao JHEP 1610 (2016) 153



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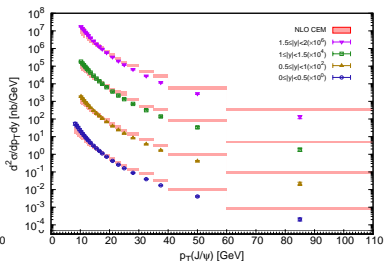
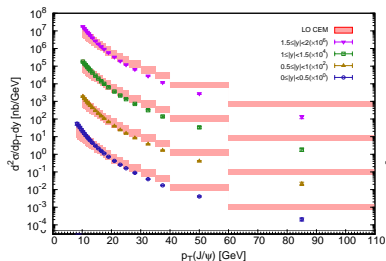
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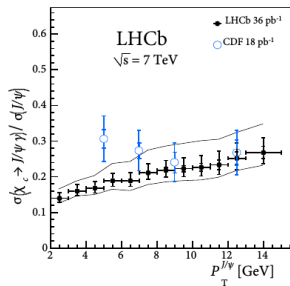
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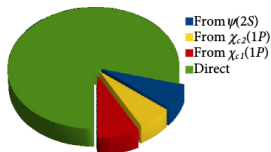


# Feed downs from the excited states

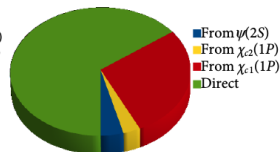
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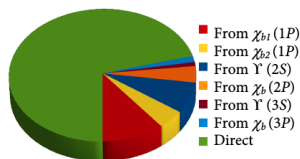
(b) Low  $P_T$   $J/\psi$



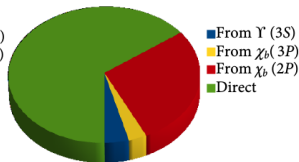
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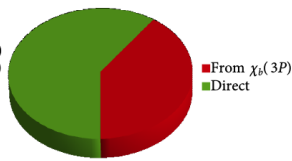
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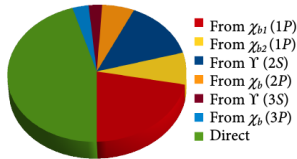
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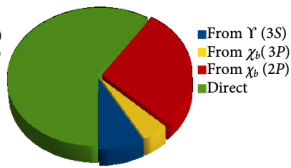
(b) Low  $P_T$   $\Upsilon(2S)$



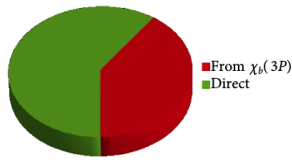
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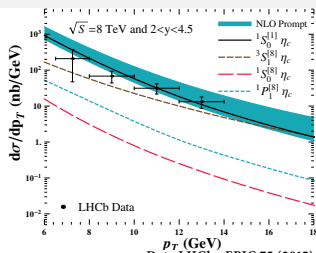
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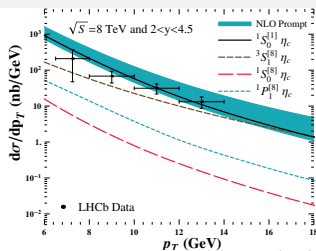
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# The last piece in the puzzle: the $\eta_c$



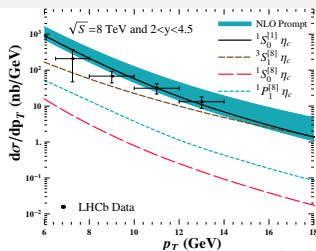
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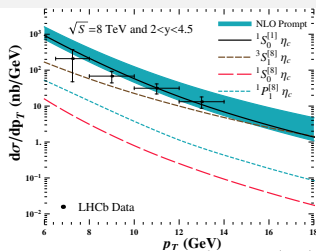
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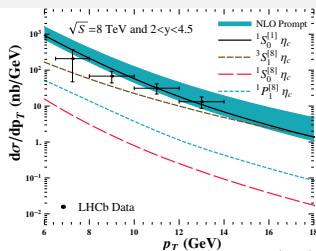


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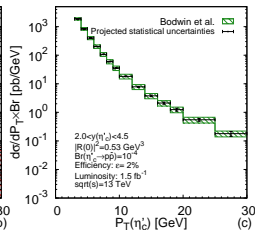
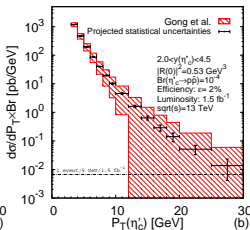
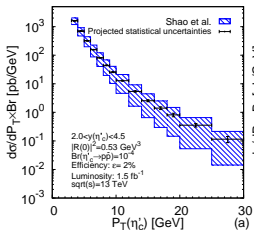
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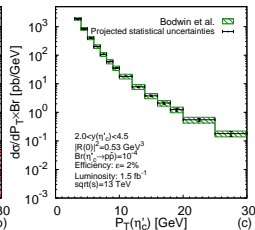
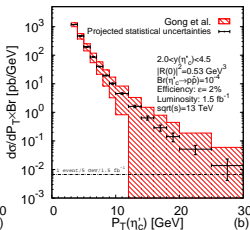
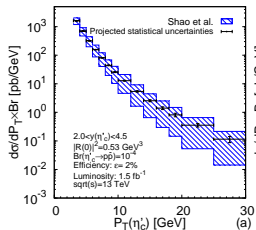
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→ Belle-II data on the inclusive  $\psi(2S)$  production will also be crucial

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See JPL. arXiv:1903.09185 [hep-ph] (Phys. Rept. 2020, In Press)

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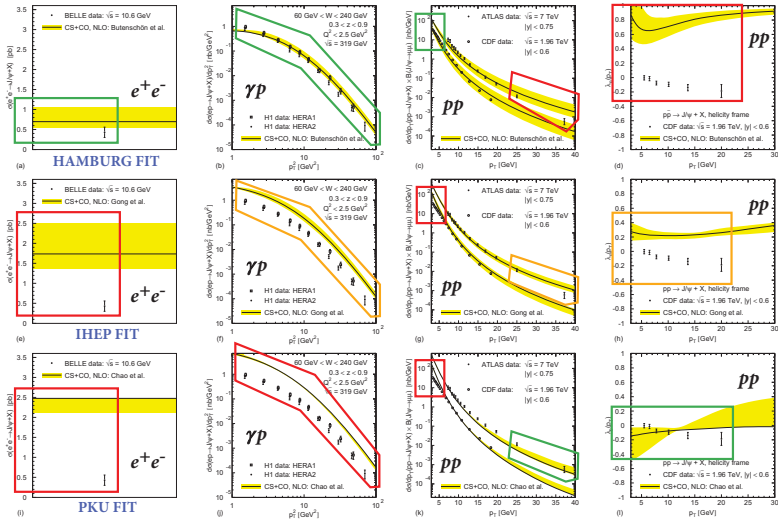
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- However, as we will now see, **these offer new ways to study DPS**

# Universality of NLO NRQCD fits ?

Plot from M. Butenschön (ICHEP 2012); Discussion in JPL, arXiv:1903.09185



Further caveats:  $\eta_c$  data !



## Part III

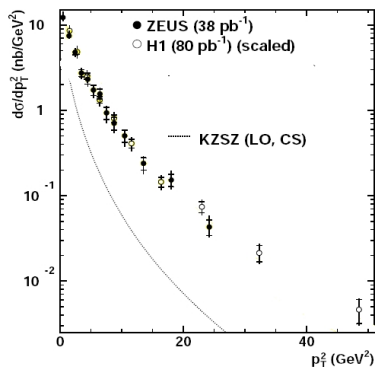
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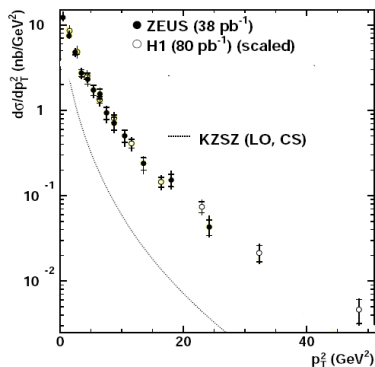


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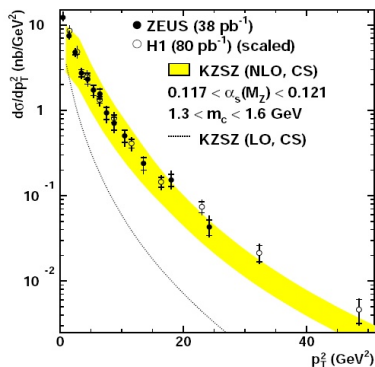


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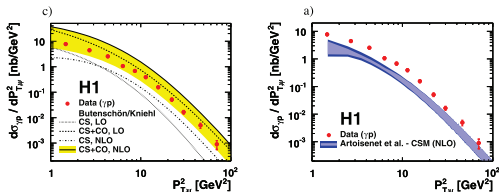
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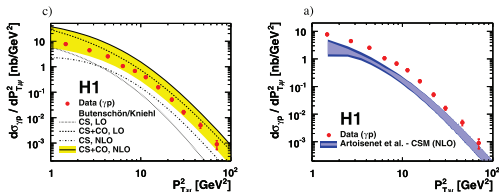
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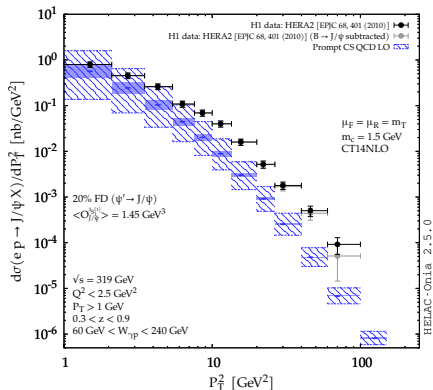
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→ Let us revisit this in view of the EIC prospects

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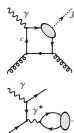
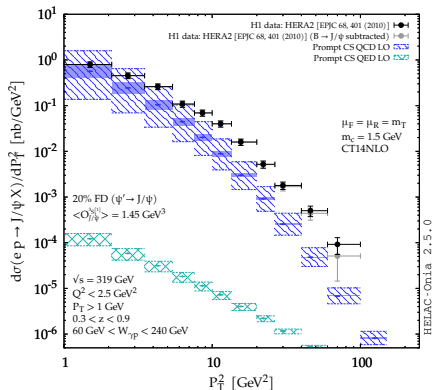
C.Flore, JPL, H.S. Shao, Y. Yedelkina, 2009.08264



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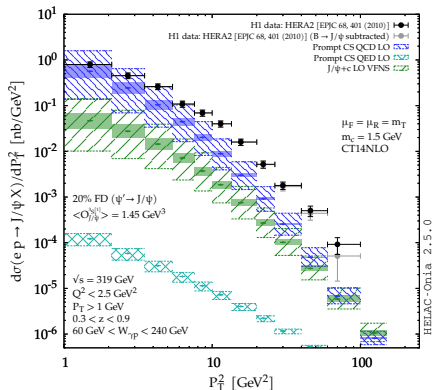
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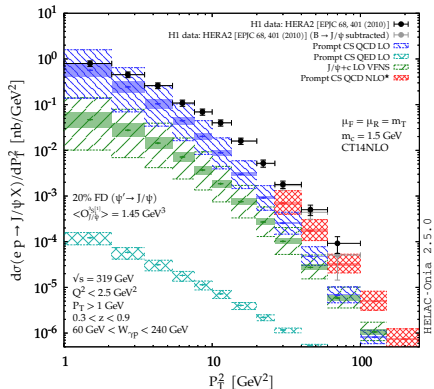


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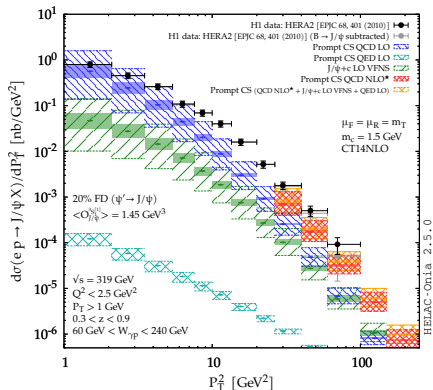


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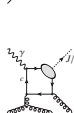
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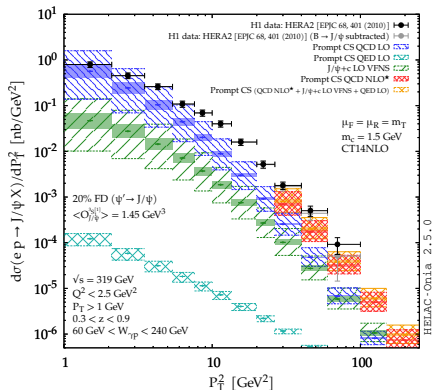


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[also NEW !]

- LO QCD does a good job at low  $P_T$
- LO QED much harder but small normalisation
- $J/\psi$ +charm: starts to matter at high  $P_T$
- NLO<sup>(\*)</sup> close the data, the overall sum nearly agrees with them
- Agreement when the expected  $B \rightarrow J/\psi$  feed down (always overlooked) is subtracted

[will matter at EIC]

[will also matter at EIC]

→ will restrict to CSM for EIC predictions

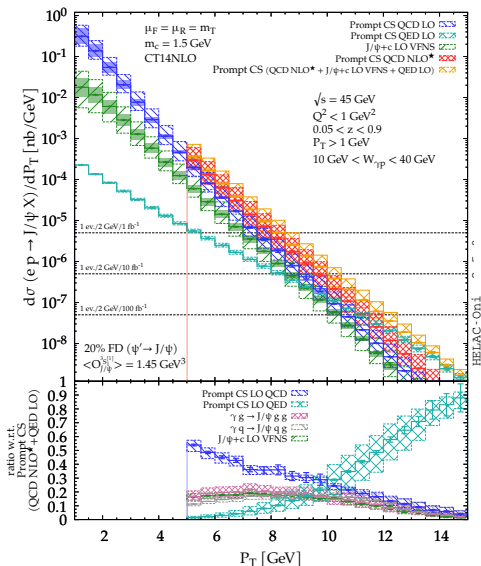
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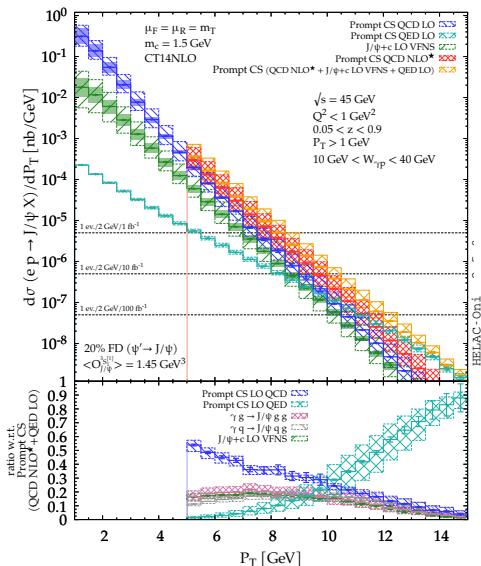
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- At  $\sqrt{s_{ep}} = 45 \text{ GeV}$ , one enters the **valence region**
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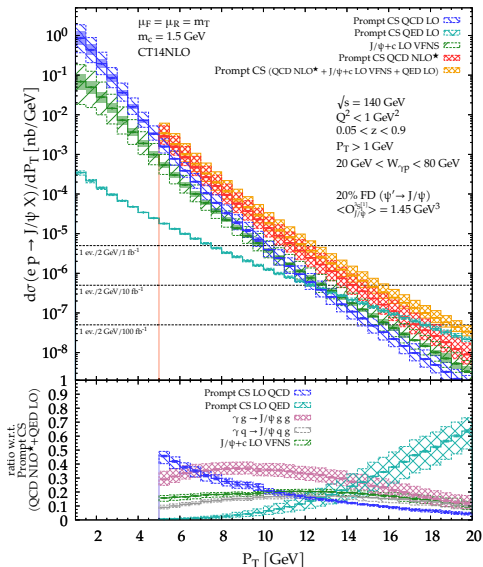
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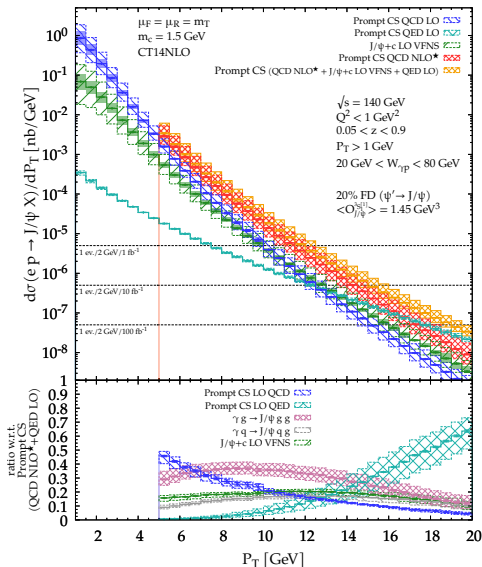
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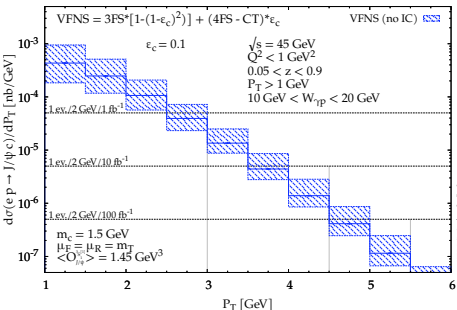
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- photon-gluon fusion remains dominant
- $J/\psi + 2$  hard partons dominant for  $P_T \sim 10 - 15 \text{ GeV}$
- Could lead to  $J/\psi + 2$  jets with moderate  $P_T$
- A priori the leading  $\text{jet}_1$  recoils on the  $J/\psi + \text{jet}_2$  pair
- $d\sigma$  should scale with  $M_{J/\psi + \text{jet}_2}^- M_{J/\psi}$

# $J/\psi$ +charm associated production at the EIC

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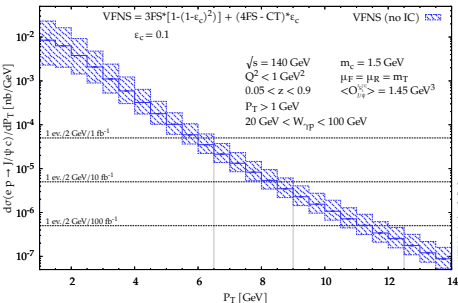


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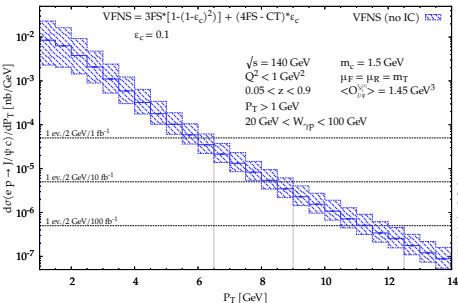


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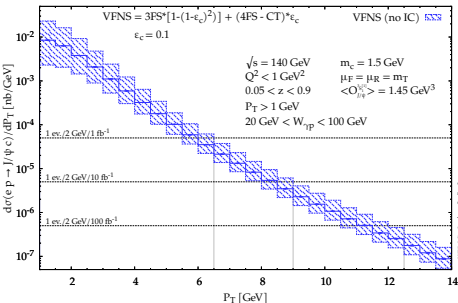
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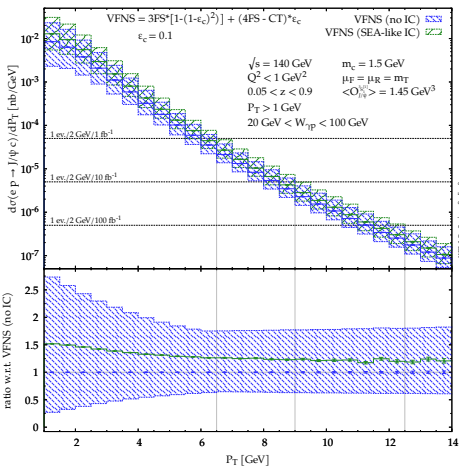
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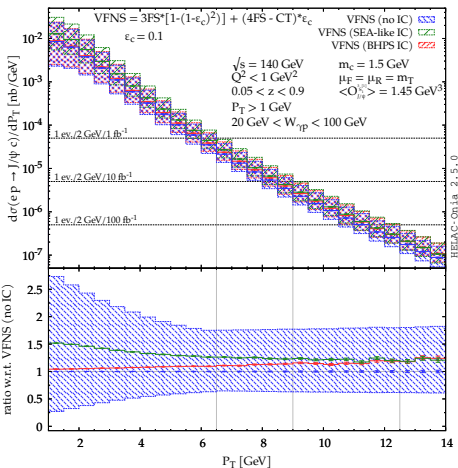
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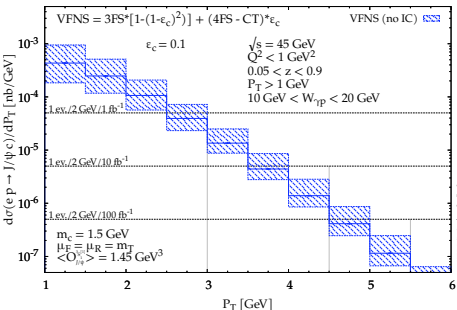
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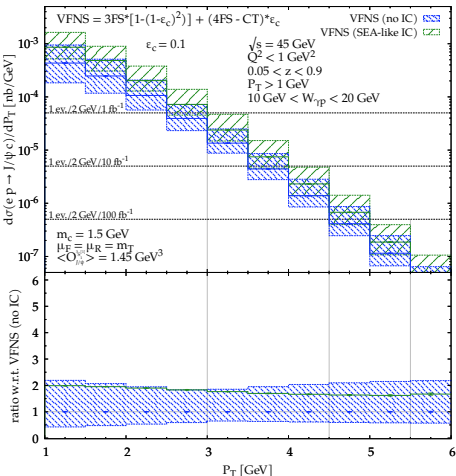
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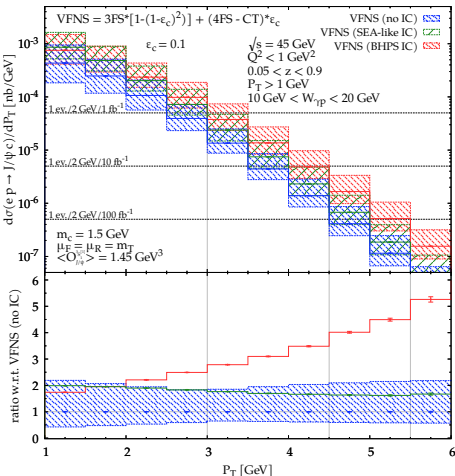
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- At  $\sqrt{s_{ep}} = 140 \text{ GeV}$ ,  $P_T$  range up to 10-12 GeV
- Could be observed via charm jet
- Rates could be enhanced by **colour transfers** when  $M_{J/\psi+c} \rightarrow M_{J/\psi} + m_c$

• 4FS  $\gamma c \rightarrow J/\psi c$  could be enhanced by **intrinsic charm**

• Small effect at  $\sqrt{s_{ep}} = 140 \text{ GeV}$

[We used IC  $c(x)$  encoded in CT14NNLO]

• Measurable effect at  $\sqrt{s_{ep}} = 45 \text{ GeV}$ : **BHPS valence-like peak visible!**

# Part IV

## Associated-quarkonium production

# Going further with associated-quarkonium production



# Going further with associated-quarkonium production

See section 3 of JPL, arXiv:1903.09185 [hep-ph] (Phys. Rept. 2020, In Press)

Observables	Experiments	CSM	CEM	NRQCD	Interest
$J/\psi+J/\psi$	LHCb, CMS, ATLAS, D0 (+NA3)	NLO, NNLO*	NLO	LO	Prod. Mechanism (CS dominant) + DPS + gluon TMD
$J/\psi+D$	LHCb	LO	LO ?	LO	Prod. Mechanism (c to $J/\psi$ fragmentation) + DPS
$J/\psi+Y$	D0	(N)LO	NLO	LO	Prod. Mechanism (CO dominant) + DPS
$J/\psi+\text{hadron}$	STAR	LO	--	LO	B feed-down; Singlet vs Octet radiation
$J/\psi+Z$	ATLAS	NLO	NLO	Partial NLO	Prod. Mechanism + DPS
$J/\psi+W$	ATLAS	LO	NLO	NLO (?)	Prod. Mechanism (CO dominant) + DPS
$J/\psi$ vs mult.	ALICE, CMS (+UA1)	--	--	--	Initial vs Final state effects ?
$J/\psi$ in jet.	LHCb, CMS	LO	--	LO	Prod. Mechanism (?)
$J/\psi(Y) + \text{jet}$	--	--	--	--	Prod. Mechanism (QCD corrections)
Isolated $J/\psi(Y)$	--	--	--	--	Prod. Mechanism (CS dominant ?)
$J/\psi+b$	--	--	--	LO	Prod. Mechanism (CO dominant) + DPS
$Y+D$	LHCb	LO	LO ?	LO	DPS
$Y+\gamma$	--	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CO LDME mix) + gluon TMD/PDF
$Y$ vs mult.	CMS	--	--	--	
$Y+Z$	--	NLO	LO ?	LO	Prod. Mechanism + DPS
$Y+Y$	CMS	NLO ?	NLO	LO ?	Prod. Mechanism (CS dominant ?) + DPS + gluon TMD

# Part V

## Quarkonium-pair production

# On the importance of QCD corrections to $J/\psi + J/\psi$ production

JPL, H.-S. Shao PRL 111, 122001 (2013); PLB 751 (2015) 479; CMS JHEP 1409 (2014) 094; ATLAS EPJC (2017) 77:76

- At Born (LO) order, the  $P_T^{\psi\psi}$  spectrum is  $\delta(P_T^{\psi\psi})$ :  $2 \rightarrow 2$  topologies

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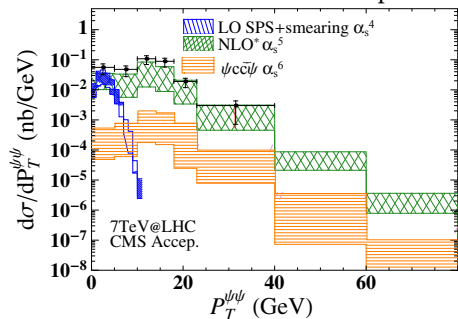
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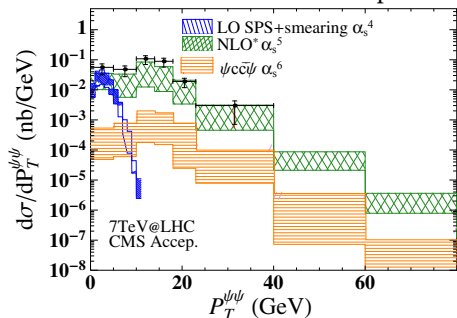
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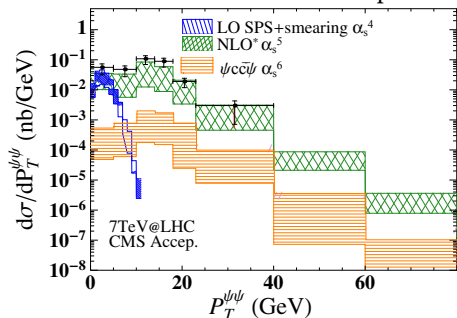


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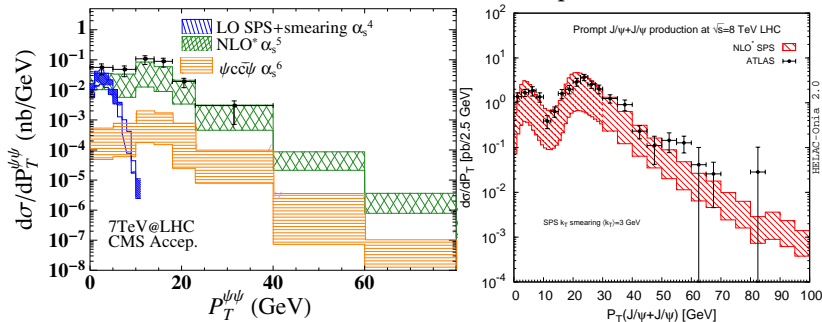


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- Confirmation at larger  $P_T^{\psi\psi}$  with ATLAS data!



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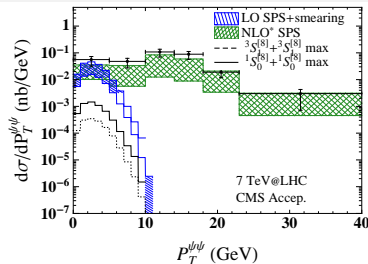
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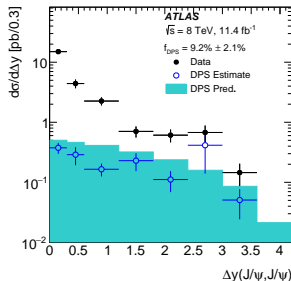
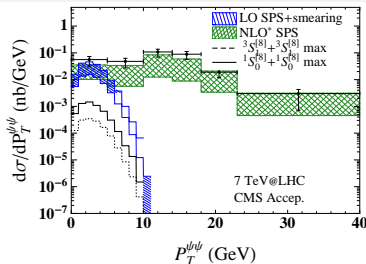
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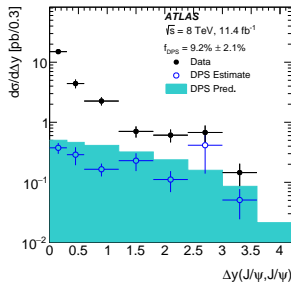
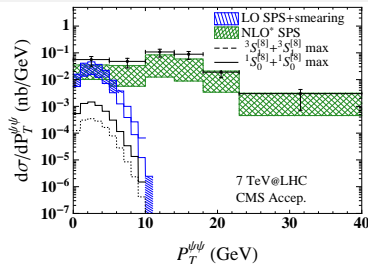
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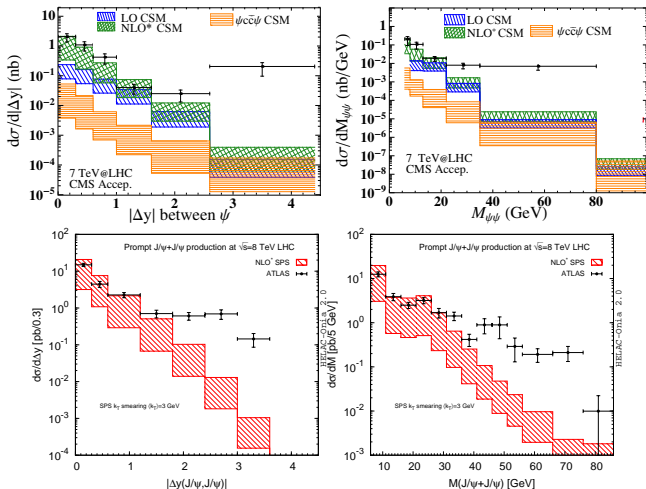
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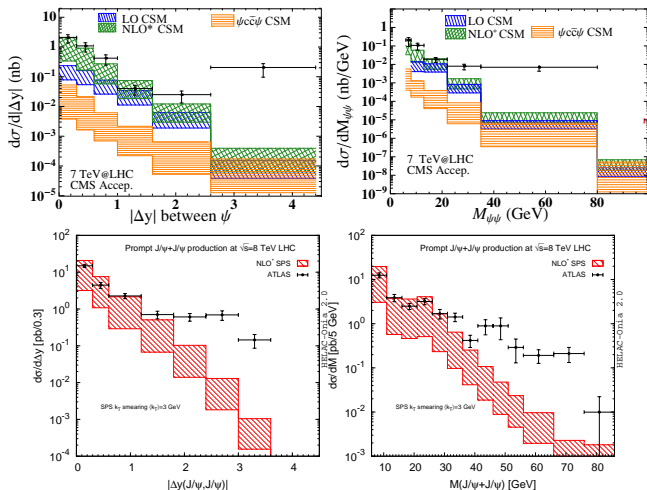
- DPS in LHCb data [kinematical distributions a priori under-control: independent scatterings]



# A puzzle at large $\Delta y$ (or $M_{\psi\psi}$ ) ?



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The most natural solution for this excess is the independent production of two  $J/\psi$

→ **double parton scattering**



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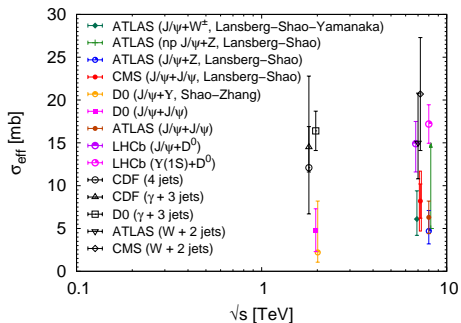
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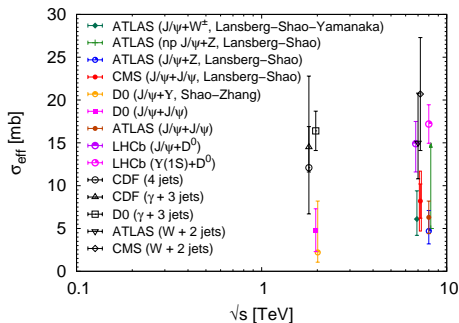
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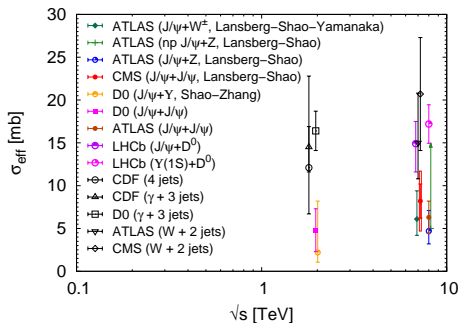


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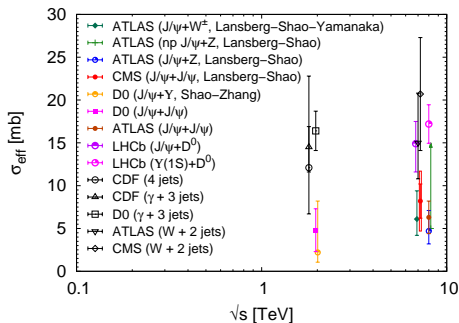
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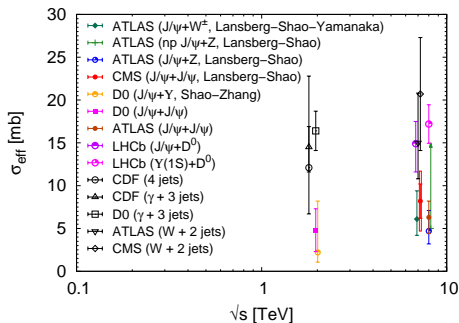
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- Looking at the **feed-down pattern** likely necessary to check the SPS/DPS ratio

# Harvesting quarkonium data: 5 extractions using theory

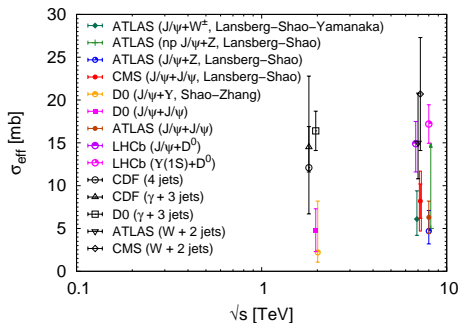


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D0 PRL 116 (2016) 082002 + H.S. Shao - Y. J. Zhang PRL 117 (2016) 062001



# Harvesting quarkonium data: 5 extractions using theory



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D0 PRL 116 (2016) 082002 + H.S. Shao - Y. J. Zhang PRL 117 (2016) 062001

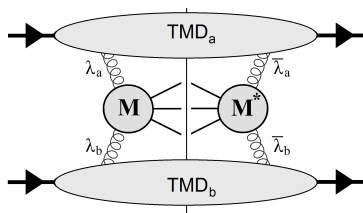
- Except for both LHCb extractions, all the quarkonium-based extraction point at very small  $\sigma_{\text{eff}}$  values: dependence on the flavour, the rapidity or the scale(s) ?

## Part VI

# Quarkonium-pair production at the LHC and gluon TMDs

# $gg$ fusion in arbitrary unpolarised process [colourless final state]

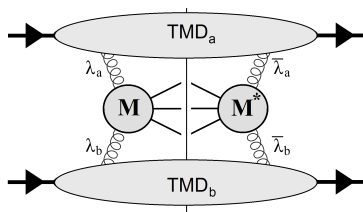
$$d\sigma^{gg} \propto$$



# $gg$ fusion in arbitrary unpolarised process [colourless final state]

$$d\sigma^{gg} \propto \underbrace{F_1}_{\substack{\text{helicity non-flip,} \\ \text{azimuthally independent}}} \left( \sum_{\lambda_a, \lambda_b} \hat{\mathcal{M}}_{\lambda_a, \lambda_b} \hat{\mathcal{M}}_{\lambda_a, \lambda_b}^* \right) C[f_1^g f_1^g]$$

$\Rightarrow$  helicity non-flip, azimuthally independent



# gg fusion in arbitrary unpolarised process [colourless final state]

$$d\sigma^{gg} \propto$$

 $F_1$ 

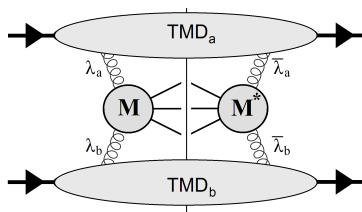
$$\left( \sum_{\lambda_a, \lambda_b} \hat{\mathcal{M}}_{\lambda_a, \lambda_b} \hat{\mathcal{M}}_{\lambda_a, \lambda_b}^* \right) \mathcal{C}[f_1^g f_1^g]$$

$\Rightarrow$  helicity non-flip, **azimuthally independent**

 $F_2$ 

$$+ \left( \sum_{\lambda} \hat{\mathcal{M}}_{\lambda, \lambda} \hat{\mathcal{M}}_{-\lambda, -\lambda}^* \right) \mathcal{C}[w_2 \times h_1^{\perp g} h_1^{\perp g}]$$

$\Rightarrow$  double helicity flip, **azimuthally independent**



# gg fusion in arbitrary unpolarised process [colourless final state]

$$d\sigma^{gg} \propto$$

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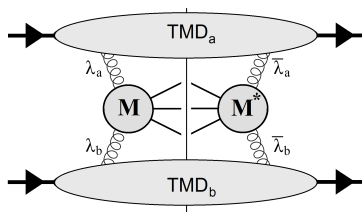
$\Rightarrow$  double helicity flip, **azimuthally independent**

 $F_3$ 

$$+ \left( \sum_{\lambda_a, \lambda_b} \hat{\mathcal{M}}_{\lambda_a, \lambda_b} \hat{\mathcal{M}}_{-\lambda_a, \lambda_b}^* \right) \mathcal{C}[w_3 \times f_1^g h_1^{\perp g}] +$$

$\{a \leftrightarrow b\}$

$\Rightarrow$  single helicity flip,  **$\cos(2\phi)$ -modulation**



# gg fusion in arbitrary unpolarised process [colourless final state]

$$d\sigma^{gg} \propto$$

 $F_1$ 

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$$+ \left( \sum_{\lambda} \hat{\mathcal{M}}_{\lambda, \lambda} \hat{\mathcal{M}}_{-\lambda, -\lambda}^* \right) \mathcal{C}[w_2 \times h_1^{1g} h_1^{1g}]$$

$\Rightarrow$  double helicity flip, **azimuthally independent**

 $F_3$ 

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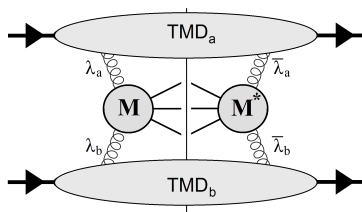
$\{a \leftrightarrow b\}$

$\Rightarrow$  single helicity flip,  **$\cos(2\phi)$ -modulation**

 $F_4$ 

$$+ \left( \sum_{\lambda} \hat{\mathcal{M}}_{\lambda, -\lambda} \hat{\mathcal{M}}_{-\lambda, \lambda}^* \right) \mathcal{C}[w_4 \times h_1^{1g} h_1^{1g}]$$

$\Rightarrow$  double helicity flip,  **$\cos(4\phi)$ -modulation**



# TMD modelling : $f_1^g$ and the relevance of the LHCb data

JPL, C. Pisano, F. Scarpa, M. Schlegel, PLB 784(2018)217



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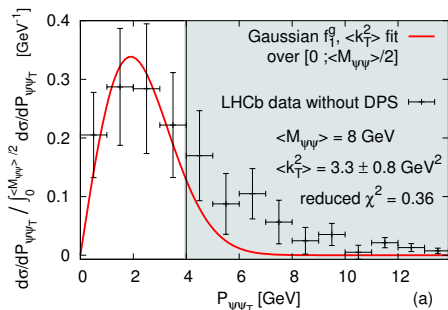
JPL, C. Pisano, F. Scarpa, M. Schlegel, PLB 784(2018)217

- $f_1^g$  modelled as a Gaussian in  $\vec{k}_T$  :  $f_1^g(x, \vec{k}_T^2) = \frac{g(x)}{\pi \langle k_T^2 \rangle} \exp\left(\frac{-\vec{k}_T^2}{\langle k_T^2 \rangle}\right)$   
where  $g(x)$  is the usual collinear PDF
- **First experimental determination** [with a pure colorless final state] of  $\langle k_T^2 \rangle$   
by fitting  $\mathcal{C}[f_1^g f_1^g]$  over the normalised LHCb  $d\sigma/dP_{\psi\psi_T}$  spectrum at 13 TeV  
from which we have subtracted the DPS yield determined by LHCb

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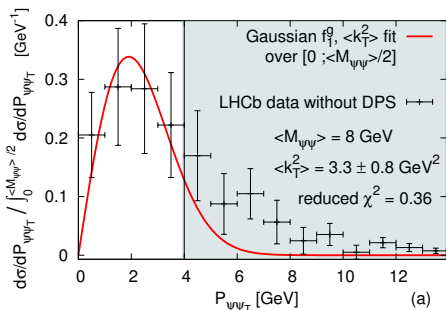
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- Integration over  $\phi \Rightarrow \cos(n\phi)$ -terms cancel out
- $F_2 \ll F_1 \Rightarrow$  only  $\mathcal{C}[f_1^g f_1^g]$  contributes to the cross-section
- No evolution so far:  $\langle k_T^2 \rangle \sim 3 \text{ GeV}^2$   
accounts both for non-perturbative and perturbative broadenings at a scale close to  $M_{\psi\psi} \sim 8 \text{ GeV}$
- Disentangling such (non-)perturbative effects requires **data at different scales**

# Switching on TMD evolution

F. Scarpa, D. Boer, M.G. Echevarria, JPL, C. Pisano, M. Schlegel, EPJC (2020) 80:87

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F. Scarpa, D. Boer, M.G. Echevarria, JPL, C. Pisano, M. Schlegel, EPJC (2020) 80:87

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$$\langle k_T^2 \rangle \sim 3 \text{ GeV}^2$$

# Switching on TMD evolution

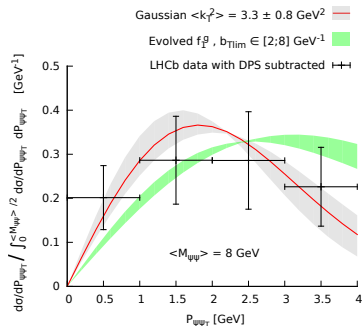
F. Scarpa, D. Boer, M.G. Echevarria, JPL, C. Pisano, M. Schlegel, EPJC (2020) 80:87

- With a fit we obtained  
 $\langle k_T^2 \rangle \sim 3 \text{ GeV}^2$
- Let us compare such a value with what a proper NLL evolution up to the scale  $M_{\psi\psi} \sim 8 \text{ GeV}$  would give

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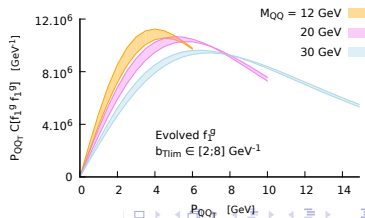
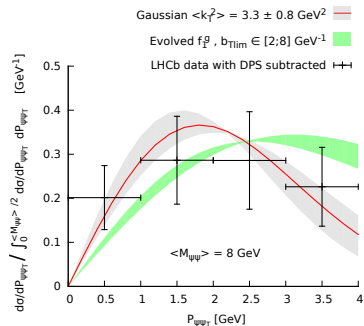
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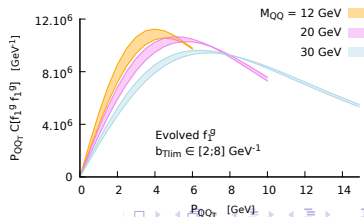
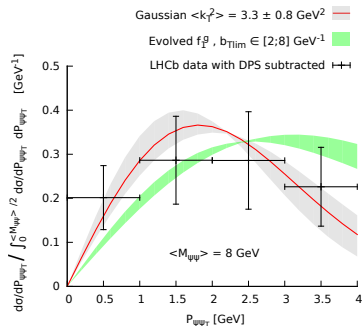




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- Evolution effects are measurable
- So far, no  $x$  dependence information



# LO predictions for quarkonia → NLOAccess [in2p3.fr/nloaccess]

## NLOAccess

Virtual Access: Automated perturbative NLO calculations for heavy ions and quarkonia (NLOAccess)

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### GENERAL DESCRIPTION

#### Objectives:

NLOAccess will give access to automated tools generating scientific codes allowing anyone to evaluate observables -such as production rates or kinematical properties - of scatterings involving hadrons. The automation and the versatility of these tools are such that these scatterings need not to be pre-coded. In other terms, it is possible that a random user may request for the first time the generation of a code to compute characteristics of a reaction which nobody thought of before. NLOAccess will allow the user to test the code and then to download to run it on its own computer. It essentially gives access to a dynamical library

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### Welcome to HELAC-Onia Web!

HELAC-Onia is an automatic matrix element generator for the calculation of the heavy quarkonium helicity amplitudes in the framework of NRQCD factorization. The program is able to calculate helicity amplitudes of multi P-wave quarkonium states production at hadron colliders and electron-positron colliders by including new P-wave off-shell currents. Besides the high efficiencies in computation of multi-leg processes within the Standard Model, HELAC-Onia is also sufficiently numerical stable in dealing with P-wave quarkonia and P-wave color-octet intermediate states.

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