



# DETERMINING THE POLARISATION OF $\Lambda_c$ FROM THE DALITZ ANALYSIS OF THE $\Lambda_c \rightarrow P K \pi$ DECAY

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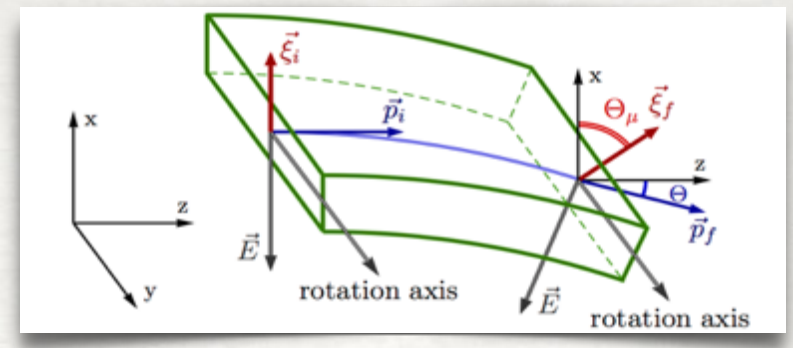
in collaboration with A. Korchin and V. Kovalchuk



my side from 2018 FU meeting...  
(see also talk by A. Fomin)

A. Fomin et al  
Eur.Phys.J.C 80 (2020)

# Towards $\mu_{\Lambda_c}$ measurement



- The magnetic moment can be determined by measuring the  $\Lambda_c$  polarisation passing through the bent crystal.
- Thus,  $\Lambda_c$  polarisation has to be measured.
- The angular distribution of the  $\Lambda_c$  decay carries information of polarisation however, it can not be separated so-called asymmetry parameter  $\alpha$ .
- We need to measure this parameter at LHCb **in advance**.

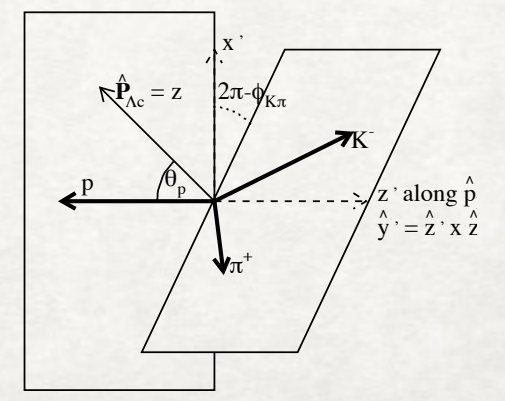
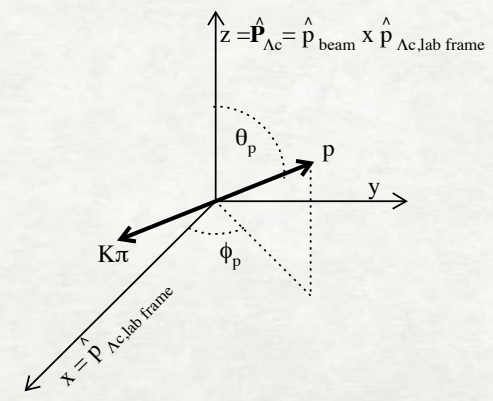
PHD PROJECT OF  
E. NIEL (IJCLAB)

$$\frac{1}{N} \frac{dN}{d \cos \vartheta_k} = \frac{1}{2} (1 + \alpha \xi_k \cos \vartheta_k) \Big|_{k=x,y,z}$$

↑ weak parameter     ↑ polarisation

INTERNSHIP PROJECT  
OF MAKSYM LIUL

- Theoretical computation of the  $\Lambda_c \rightarrow K \rho \pi$  decays





# What we understood in 2018...

- We studied the three body decays.
- $\Lambda_c \rightarrow \Lambda \pi \rightarrow p \pi \pi$  decay

$$\begin{aligned} \frac{dN}{d \cos \theta} &= 4m_\Lambda^2 N_1 N_2 (1 + \alpha_1 \alpha_2 \cos \theta - \xi (\alpha_1 - \alpha_2 \cos \theta)) \\ &= 4m_\Lambda^2 N_1 N_2 (1 - \xi \alpha_1 + \alpha_2 (\alpha_1 + \xi) \cos \theta) \end{aligned}$$

$$N_1 = (E_{\Lambda_c} + m_{\Lambda_c})|A|^2 + (E_{\Lambda_c} - m_{\Lambda_c})|B|^2$$

$$N_2 = (E_p + m_p)|a|^2 + (E_p - m_p)|b|^2$$

$$\alpha_1 = \frac{2\text{Re}(AB^*)|\vec{p}_{\Lambda_c}|}{N_1}$$

$$\alpha_2 = \frac{2\text{Re}(ab^*)|\vec{p}_p|}{N_2}$$

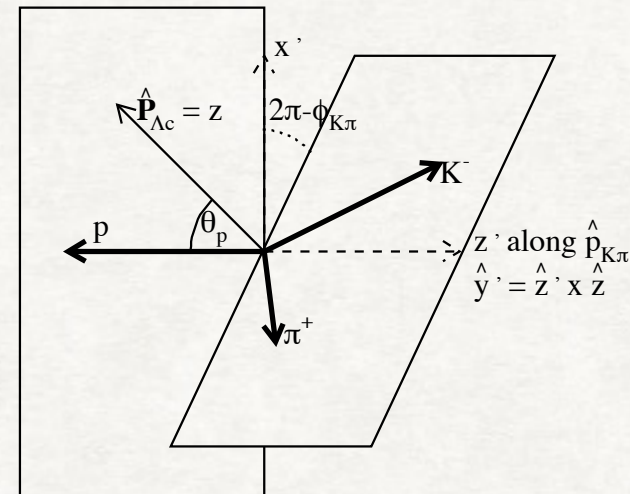
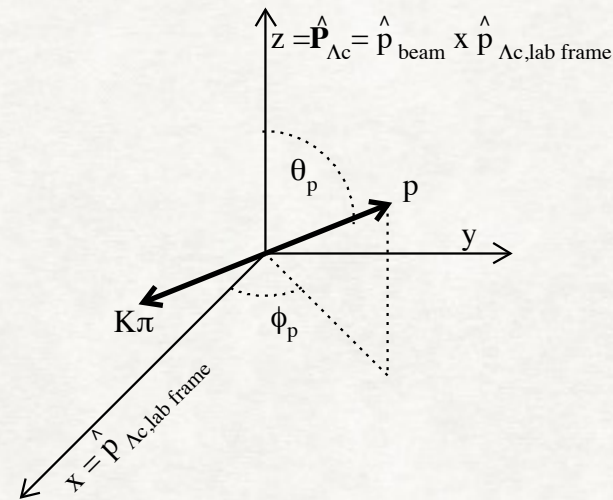
A, B: form factor for  $\Lambda_c \rightarrow \Lambda \pi$  decay  
 a, b: form factor for  $\Lambda \rightarrow p \pi$  decay

*parity violating*

- In this case where the first and the second decays are weak decays (both include parity violation), the angular dependence together with the information of  $\alpha_2 = 0.642 \pm 0.013$  allows to determine  $\xi$  and  $\alpha_1$  separately.
- Problem: the decay rate is very small.

# What we understood in 2018...

- $\Lambda_c \rightarrow (K^* p, \Delta^{++} K, \Lambda \pi) \rightarrow p K \pi$  decay
- This decay was studied by the Fermilab E791 experiment.
- We first followed their formalism (helicity amplitude method).





# What we understood in 2018...

- $\Lambda_c \rightarrow (K^* p, \Delta^{++} K, \Lambda \pi) \rightarrow p K \pi$  decay

The  $\Lambda_c \rightarrow K^*(\rightarrow K\pi)p$  decays

$$\frac{d\Gamma}{d\cos\theta d\cos\theta' d\phi} = a_0 + a_1 \cos 2\theta' + P_{\Lambda_c} \cos\theta (b_0 + b_1 \cos 2\theta') + P_{\Lambda_c} \sin\theta \sin 2\theta' (c_1 \cos(\phi - \phi') + c_2 \sin(\phi - \phi'))$$

$$a_0 = \frac{1}{8}(E_1^2 + 2E_2^2 + 2E_3^2 + E_4^2)$$

$$a_1 = -\frac{1}{8}(E_1^2 - 2E_2^2 - 2E_3^2 + E_4^2)$$

$$b_0 = \frac{1}{8}(E_1^2 - 2E_2^2 + 2E_3^2 - E_4^2)$$

$$b_1 = -\frac{1}{8}(E_1^2 + 2E_2^2 - 2E_3^2 - E_4^2)$$

$$c_1 = \frac{1}{2\sqrt{2}}(E_1 E_2 \cos(\phi_1 - \phi_2) - E_3 E_4 \cos(\phi_3 - \phi_4))$$

$$c_2 = \frac{1}{2\sqrt{2}}(E_1 E_2 \sin(\phi_1 - \phi_2) - E_3 E_4 \sin(\phi_3 - \phi_4))$$

E1, E4: form factor for S wave decay

E2, E3: form factor for P wave decay

*parity violating*

$P_{\Lambda_c}$ : polarisation (=  $\xi$ )

- We can not separately measure all the form factors and the polarisation in this case.

$$\{a_0, a_1, b_0, b_1, c_1, c_2\} \longrightarrow \{|E_1|, |E_2|, |E_3|, |E_4|, (\phi_1 - \phi_2), (\phi_3 - \phi_4), P_{\Lambda_c}\}$$

# What we understood in 2018...

- $\Lambda_c \rightarrow (K^* p, \Delta^{++} K, \Lambda \pi) \rightarrow p K \pi$  decay

The  $\Lambda_c \rightarrow \Delta^{++}(1232)(\rightarrow p\pi)K$  decays

$$\frac{d\Gamma}{d\cos\theta d\cos\theta' d\phi} = a_0 + a_1 \cos 2\theta' + P_{\Lambda_c} \cos\theta (b_0 + b_1 \cos 2\theta')$$

$$a_0 = \frac{5}{16}(F_1^2 + F_2^2)$$

$$a_1 = \frac{3}{16}(F_1^2 + F_2^2)$$

$$b_0 = \frac{5}{16}(F_1^2 - F_2^2)$$

$$b_1 = \frac{3}{16}(F_1^2 - F_2^2)$$

The  $\Lambda_c \rightarrow \Lambda(1520)(\rightarrow pK)\pi$  decays

$$\frac{d\Gamma}{d\cos\theta d\cos\theta' d\phi} = a_0 + a_1 \cos 2\theta' + P_{\Lambda_c} \cos\theta (b_0 + b_1 \cos 2\theta')$$

$$a_0 = \frac{5}{16}(H_1^2 + H_2^2)$$

$$a_1 = \frac{3}{16}(H_1^2 + H_2^2)$$

$$b_0 = \frac{5}{16}(H_1^2 - H_2^2)$$

$$b_1 = \frac{3}{16}(H_1^2 - H_2^2)$$

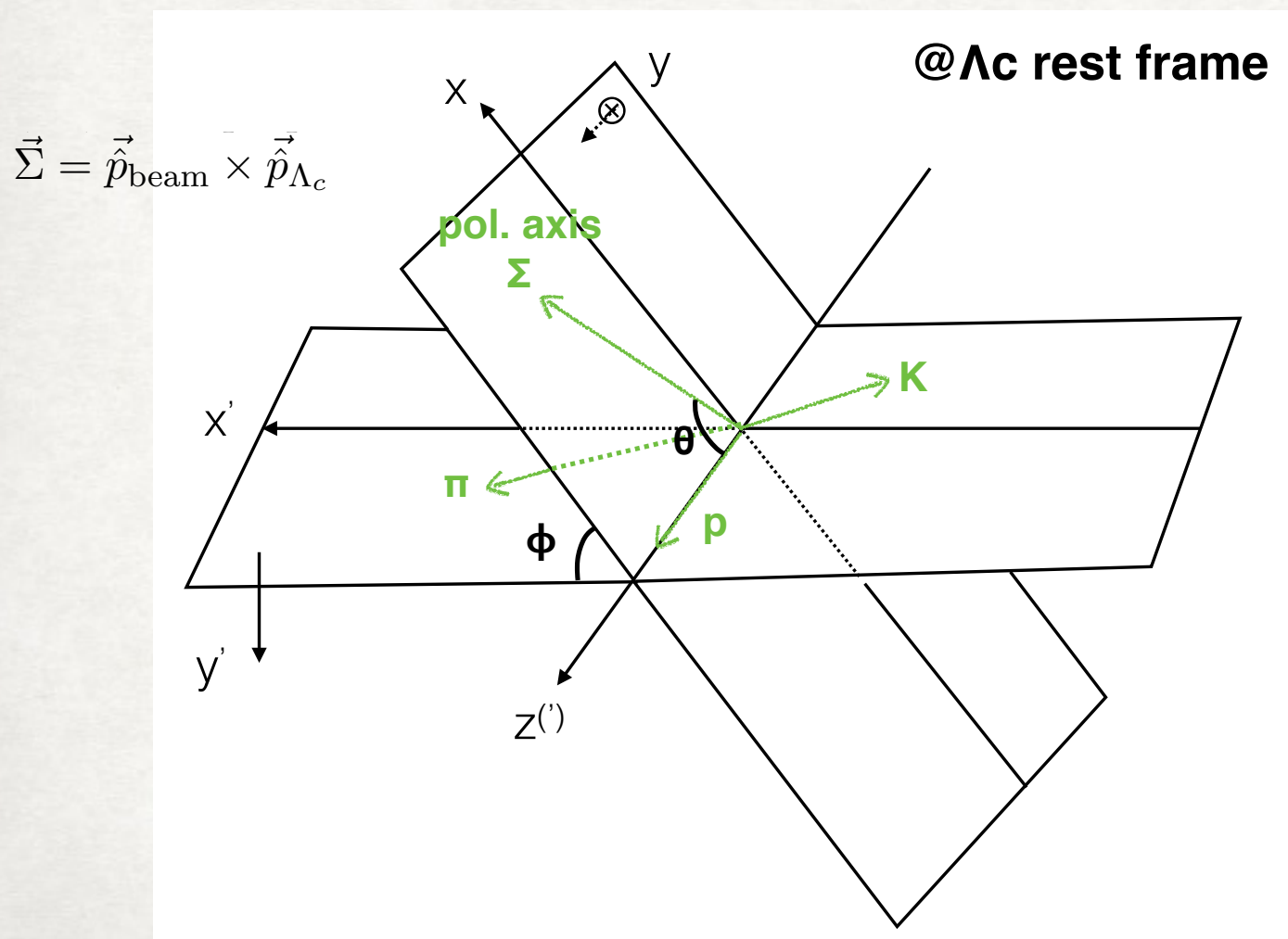
- The same conclusions: we can not separately measure all the form factors and the polarisation.
- The interference of these intermediate states allow the separation ???



# Computing the interference terms

E.K. A. Korchin, V. Kovalchuk in progress

- It seems complicated to compute the interference term in the helicity amplitude method where we use various rest frames ( $\rightarrow$  this problem is discussed and a solution is proposed in [arXiv:1910.04566](https://arxiv.org/abs/1910.04566)).
- We decided to use a single frame defined as



- We use  $\Lambda_c$  rest frame with
- $x'-y'-z'$ : the  $pK\pi$  decay plane
  - $x-z$ :  $p-\Sigma$  plane
  - $z''$ : proton direction

INTERNSHIP PROJECT  
OF ALEKSEY LUKIANCHUK

# Computing the interference terms

E.K. A. Korchin, V. Kovalchuk in progress

- We don't rely on the helicity amplitude method and compute it according to Feynman rules.

$$d\Gamma(\xi) = \frac{1}{(2\pi)^4} \frac{1}{32s^{3/2}} |\mathcal{M}|^2 dm_{12}^2 dm_{23}^2 d\theta$$

$$\mathcal{M} = \mathcal{M}_{\Lambda'} \mathcal{B}\mathcal{W}_{\Lambda'}(s_{12}) + \mathcal{M}_{\Delta^{++}} \mathcal{B}\mathcal{W}_{\Delta^{++}}(s_{13}) + \mathcal{M}_{K^*} \mathcal{B}\mathcal{W}_{K^*}(s_{23})$$

$$\begin{aligned} \mathcal{M}_{\Lambda'} &= \bar{u}(p) \lambda_p \mathcal{A}_{\Lambda'} u_{\Lambda_c}(Q) \\ \mathcal{M}_{\Delta^{++}} &= \bar{u}(p) \lambda_p \mathcal{A}_{\Delta^{++}} u_{\Lambda_c}(Q) \\ \mathcal{M}_{K^*} &= \bar{u}(p) \lambda_p \mathcal{A}_{K^*} u_{\Lambda_c}(Q) \end{aligned} \quad \mathcal{B}\mathcal{W}_R(s_R) = \frac{1}{s_R - m_R^2 + im_R \Gamma_R}$$

$$\begin{aligned} \mathcal{A}_{\Lambda'} &= G_{\Lambda'} \mathcal{B}\mathcal{W}_{\Lambda'}(s_{12}) \left\{ p_\mu \gamma_5 (q_1 + m_{\Lambda'}) R^{\mu\nu}(q_1) C_\nu^{\Lambda'} \right\} \\ \mathcal{A}_{\Delta^{++}} &= G_{\Delta^{++}} \mathcal{B}\mathcal{W}_{\Delta^{++}}(s_{13}) \left\{ p_\mu (q_2 + m_{\Delta^{++}}) R^{\mu\nu}(q_2) C_\nu^{\Delta^{++}} \right\} \\ \mathcal{A}_{K^*} &= G_{K^*} \mathcal{B}\mathcal{W}_{K^*}(s_{23}) \left\{ R^\mu(q_3) C_\mu^{K^*} \right\} \end{aligned}$$

$$\begin{aligned} C_\nu^{\Lambda'} &= Q_\nu (C \gamma_5 + D) \\ C_\nu^{\Delta^{++}} &= Q_\nu (A \gamma_5 + B) \\ C_\mu^{K^*} &= E_1 \gamma_\mu + E_2 Q_\mu + \gamma_5 (F_1 \gamma_\mu + F_2 Q_\mu) \end{aligned} \quad \text{parity violating}$$



# (interim) Results...

E.K. A. Korchin, V. Kovalchuk in progress

- Let us first see the individual resonance contributions. It turned out that the angular distribution fit in single expression:

$$d\Gamma(\xi) \propto [a_0 - b_0\xi \cos\theta - b_1\xi \sin\theta \cos\phi]$$

**$a_0, b_0, b_1$  are VERY complicated functions of the Dalitz variables**

## **example of $\Lambda c \rightarrow \Delta^{++} K \rightarrow p K \pi$**

$a_0, b_0, b_1$  are proportional to

$$\begin{aligned} a_0 &: |A|^2, |B|^2 \\ b_0 &: \xi \operatorname{Re}(AB^*) \\ b_1 &: \xi \operatorname{Re}(AB^*) \end{aligned}$$



Dalitz analysis gives information of

$$\begin{aligned} a_0 &\longrightarrow |A|, |B| \\ b_0 &\longrightarrow \xi |A| |B| \cos \delta_{AB} \\ \delta_{AB} &= \delta_A - \delta_B \end{aligned}$$

$a_0, b_{0,1}$  give information of  $|A|, |B|$  and  $\xi \cos \delta_{AB}$   
and can not provide  $\xi$  (unless  $\delta_{AB}=0$ )

# (interim) Results...

E.K. A. Korchin, V. Kovalchuk in progress

- Next we see the interference terms

**example of  $\Lambda c \rightarrow \Delta^{++} K \rightarrow p K \pi$   $\Lambda c \rightarrow \Lambda \pi \rightarrow p K \pi$  intermediate term**

$$d\Gamma(\xi) \propto [a_0 - b_0 \xi \cos \theta - b_1 \xi \sin \theta \cos \phi]$$

$$a_0 : |A|^2, |B|^2, |C|^2, |D|^2, \text{Re}(AD^*), \text{Re}(BC^*), \text{Im}(AD^*), \text{Im}(BC^*)$$

$$b_0 : \xi \text{Re}(AB^*), \xi \text{Im}(AB^*), \xi \text{Re}(CD^*), \xi \text{Im}(CD^*), \xi \text{Re}(AC^*), \xi \text{Im}(AC^*), \xi \text{Re}(BD^*), \xi \text{Im}(BD^*)$$

$$b_1 : \xi \text{Re}(AB^*), \xi \text{Im}(AB^*), \xi \text{Re}(CD^*), \xi \text{Im}(CD^*), \xi \text{Re}(AC^*), \xi \text{Im}(AC^*), \xi \text{Re}(BD^*), \xi \text{Im}(BD^*)$$

**imaginary part is now accessible!!!**

$$a_0 \longrightarrow |A|, |B|, |C|, |D|, |A||D| \cos \delta_{AD}, |A||D| \sin \delta_{AD}, |B||C| \cos \delta_{BC}, |B||C| \sin \delta_{BC}$$

$$b_0 \longrightarrow \xi |A||B| \cos \delta_{AB}, \xi |A||B| \sin \delta_{AB}, \xi |C||D| \cos \delta_{CD}, \xi |C||D| \sin \delta_{CD}, \\ \xi |A||C| \cos \delta_{AC}, \xi |A||C| \sin \delta_{AC}, \xi |B||D| \cos \delta_{BD}, \xi |B||D| \sin \delta_{BD}$$

**then, using the following relation, we can separate  $\xi$  !!!**

$$\frac{(\xi |A||B| \cos \delta_{AB})^2 + (\xi |A||B| \sin \delta_{AB})^2}{|A|^2 |B|^2} = \xi^2$$



# (interim) Results...

E.K. A. Korchin, V. Kovalchuk in progress

- Why are we accessible to the imaginary part???
- The A, B, C... function are actually multiplied by the Breit-Wigner of each resonance:

$$\begin{aligned} A &\longrightarrow A \mathcal{BW}_{\Delta^{++}}(s_{13}), & B &\longrightarrow B \mathcal{BW}_{\Delta^{++}}(s_{13}) \\ C &\longrightarrow C \mathcal{BW}_{\Lambda'}(s_{12}), & D &\longrightarrow D \mathcal{BW}_{\Lambda'}(s_{12}) \end{aligned}$$

- When we compute a single resonance, it simply factors out, e.g.

$$Re(AB^*) \longrightarrow Re(AB^*) |\mathcal{BW}_{\Delta^{++}}(s_{13})|^2$$

- When we have two resonances, these interfere and make it possible separate the real and imaginary parts

$$Re(AD^*) \longrightarrow Re(AD^*) Re(\mathcal{BW}_{\Delta^{++}}(s_{13}) \mathcal{BW}_{\Lambda'}^*(s_{12})) - Im(AD^*) Im(\mathcal{BW}_{\Delta^{++}}(s_{13}) \mathcal{BW}_{\Lambda'}^*(s_{12}))$$

# What's next ?

E.K. A. Korchin, V. Kovalchuk in progress

- We need to perform the sensitivity study “how precisely we can measure the polarisation  $\xi$  at LHCb/SMOG” (for now, with three resonances).
- By doing such study, one can clarify, e.g.
  - Is the Dalitz distributions different enough for the different resonances to distinguish A, B, C... parameters?
  - Is  $\phi$  distribution important in  $\xi$  determination?
- These are simultaneous fit of 8x2 form factors and 1 polarisation parameter.
- We developed a fit program called “Gampola” during internship of B. Knysh (now Belle II-IJCLab group ), which can do such a fit very fast.
- It will be great if a very motivated internship student could join to work on this exciting project!



# Conclusions

- The charm magnetic moment determination with bent-crystal requires a measurement of the  $\Lambda_c$  polarisation.
- It has been puzzling for us how to separately measure the asymmetry parameter and the polarisation.
- We introduced a new frame to compute the interference of the different intermediate states and have shown that indeed, the intermediate terms give extra information to determine full form factors and polarisation.
- We are now ready to perform the sensitivity study.
- The French-Ukraine collaboration have been very fruitful!
- Stay tuned!