

Multi-messenger astroparticle physics Introductory course

Outline of this lecture

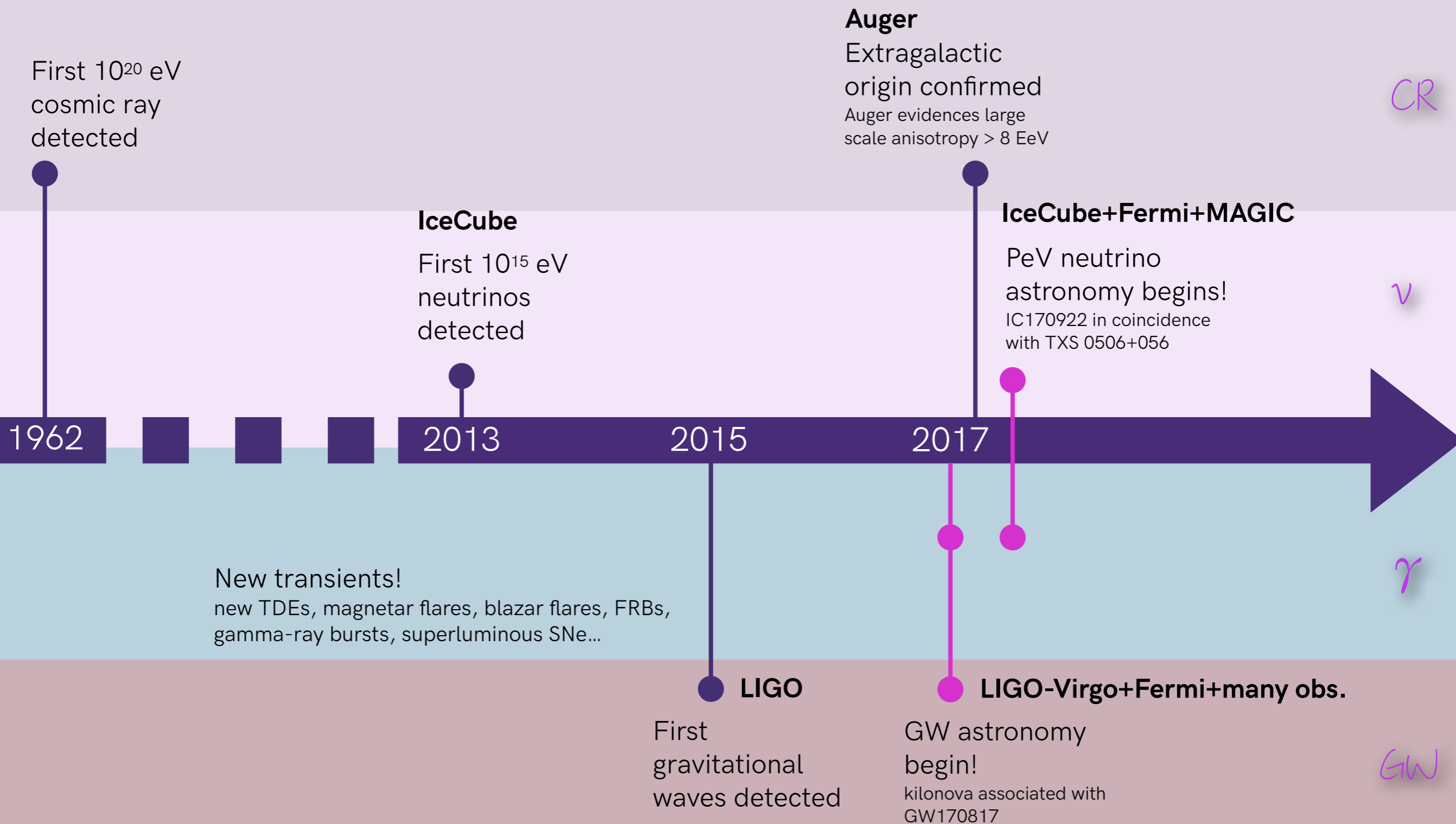
1. A multi-messenger picture is the natural way
2. Tools for multi-messenger astrophysics
 - Secondary production channels
 - Maximum energies & simple flux estimates
 - Cosmogenic neutrinos
 - Specificities of gamma rays
 - Panorama of simulation tools
3. Can we really do multi-messenger astrophysics?
 - GW-neutrino sources
 - Focus on neutrinos from transient sources
 - Opening the UHE neutrino window

1. A multi-messenger picture is the natural way



Introduction

Exciting times!



And we still don't know the origin of UHECRs

The complicated cosmic-ray journey

Source?

- particle injection?
- acceleration? shocks? reconnection?...

Outflow

- structure?
- B?
- size?

Cosmic backgrounds

interactions on CMB, UV/opt/IR photons

cosmogenic neutrino and gamma-ray production

Intergalactic magnetic fields

magnetic deflection
temporal & angular spread/shifts

Source population emissivity evolution

affects the diffuse astroparticle fluxes

Backgrounds

- radiative? baryonic?
- evolution, density?
- magnetic field: deflections?

associated neutrino and gamma-ray production

Observables

UHECR

- mass
- spectrum
- anisotropy

neutrinos

- flavors
- spectrum
- anisotropy
- time variabilities

multi-wavelength photons

- spectral features
- time variabilities
- angular spread
- source distribution

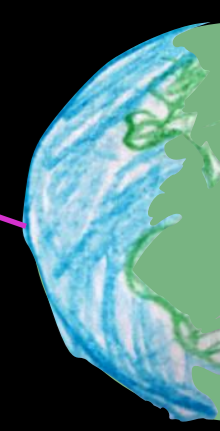
GW

- spectrum
- arrival directions
- time

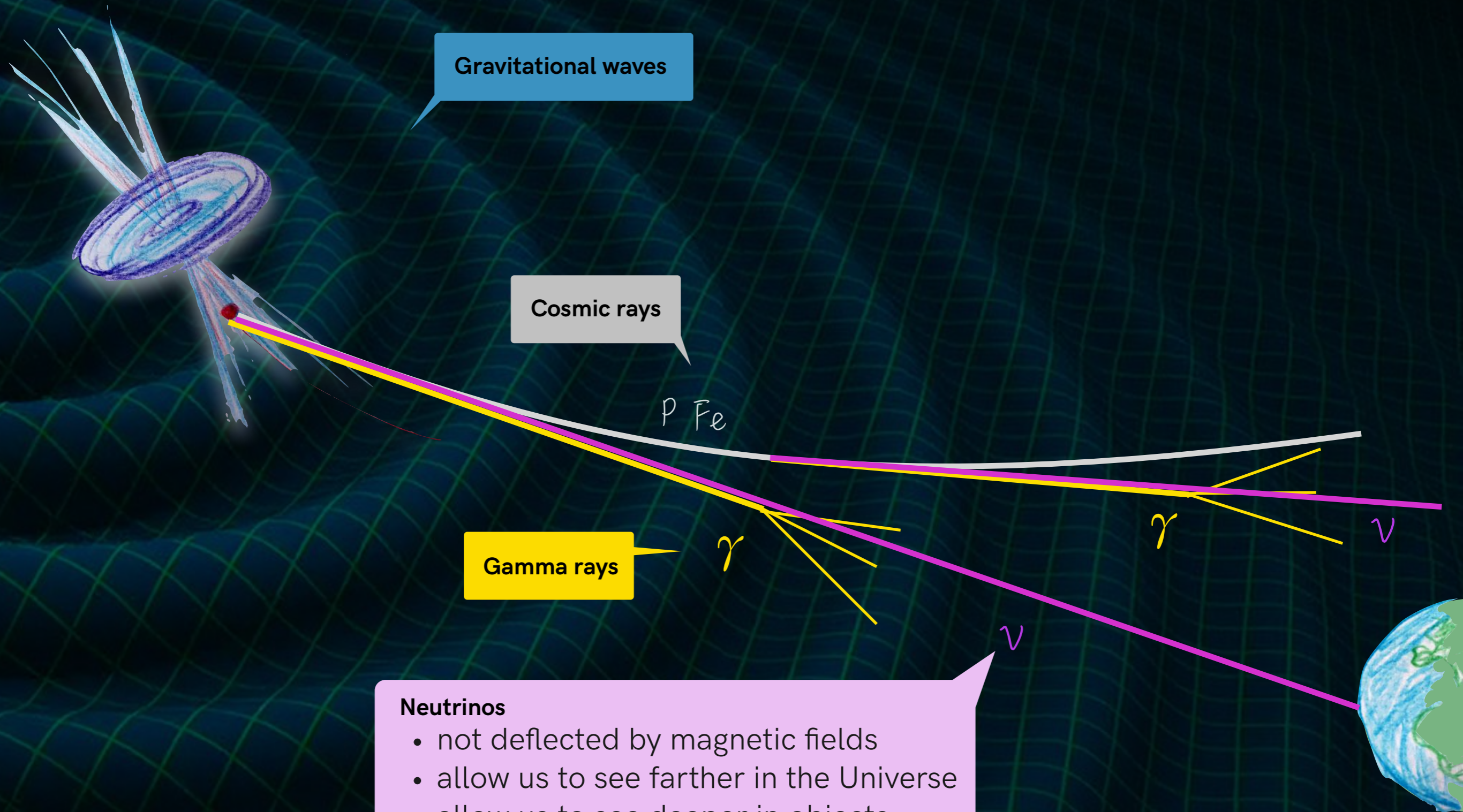
P Fe

γ ν

γ ν



Cosmic rays and friends



Gravitational waves

Cosmic rays

p Fe

Gamma rays

γ

γ

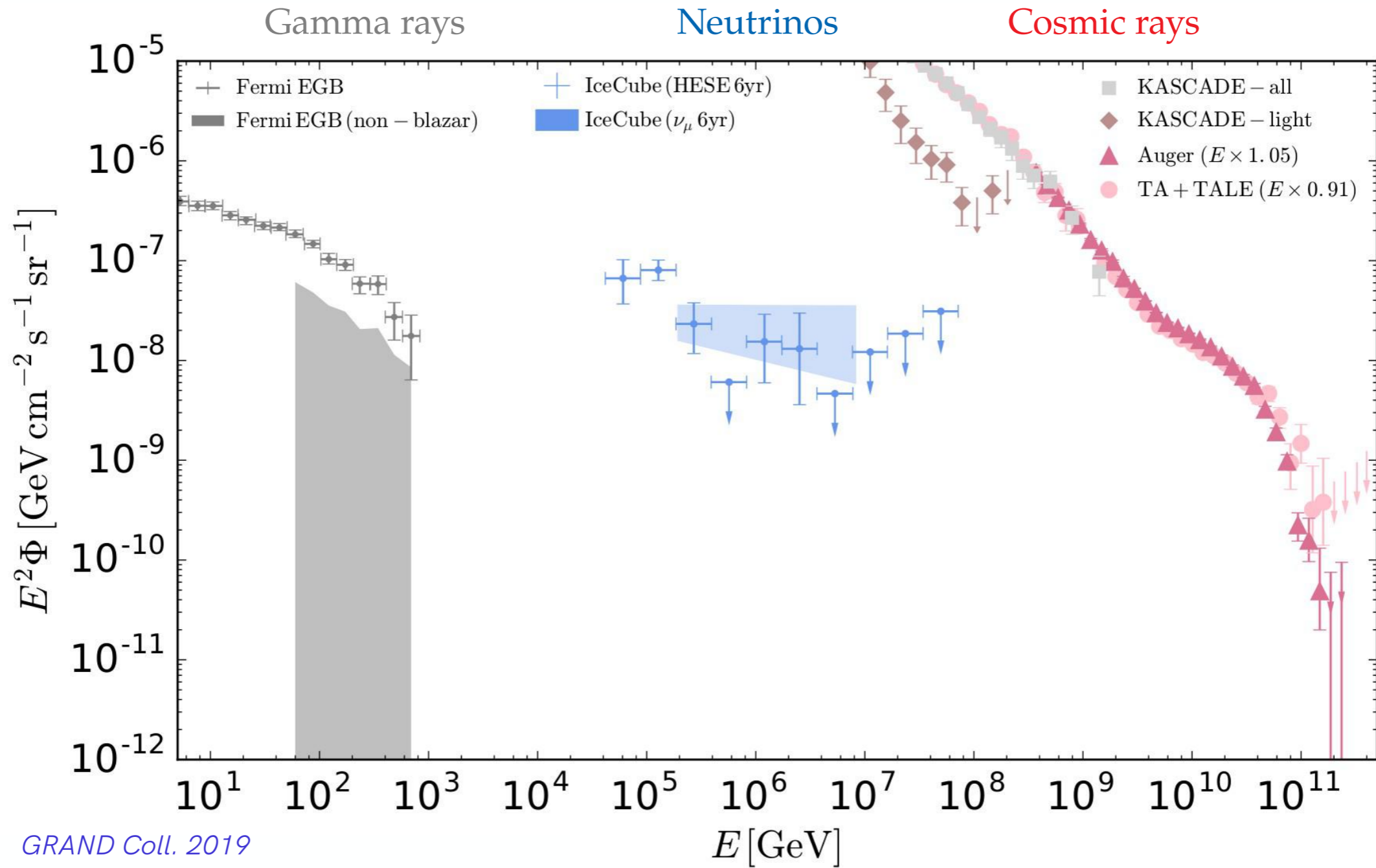
ν

ν

Neutrinos

- not deflected by magnetic fields
- allow us to see farther in the Universe
- allow us to see deeper in objects
- clear hadronic acceleration signature
- but: difficult to detect

A multi-messenger picture also *looks* like a natural way



A common multi-messenger source?

e.g., Fang & Murase 2017

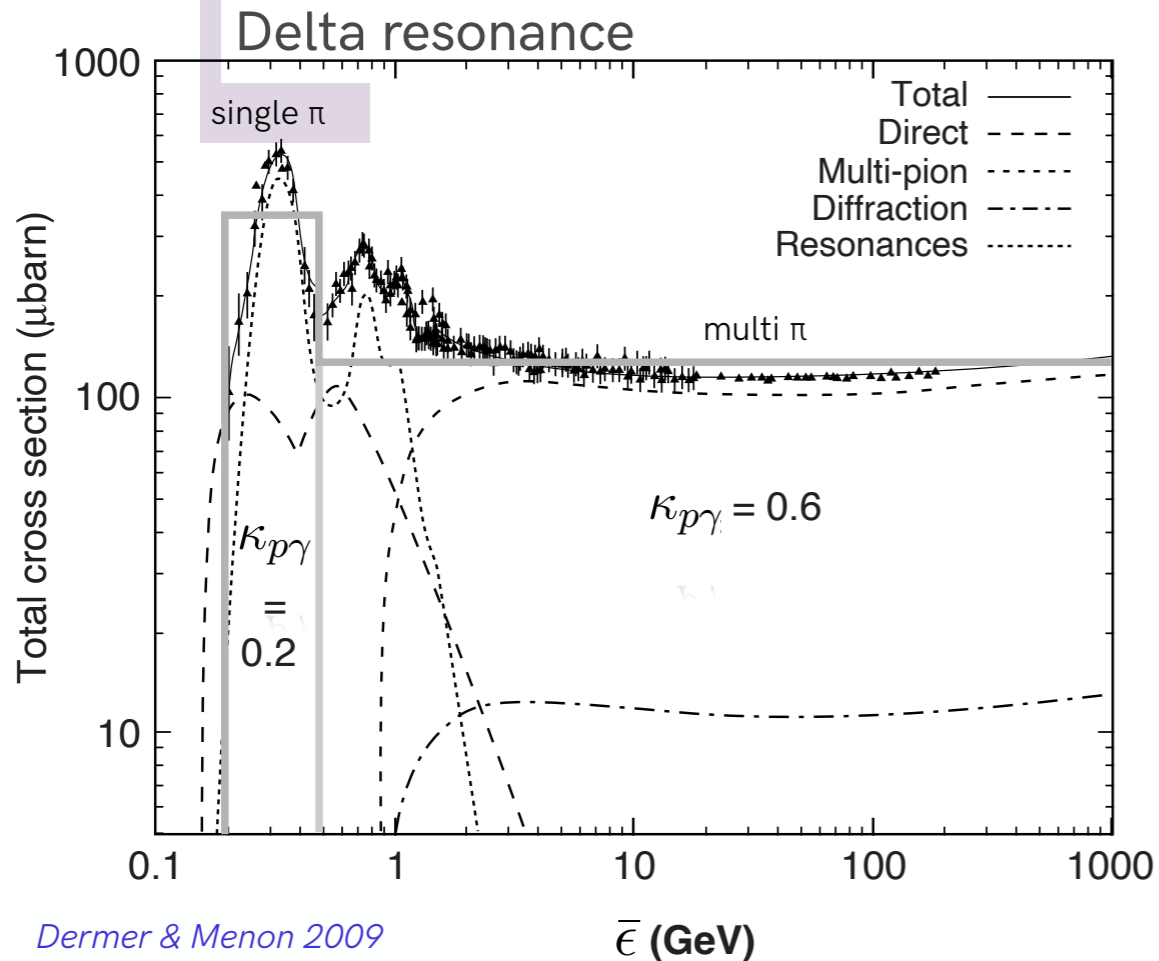
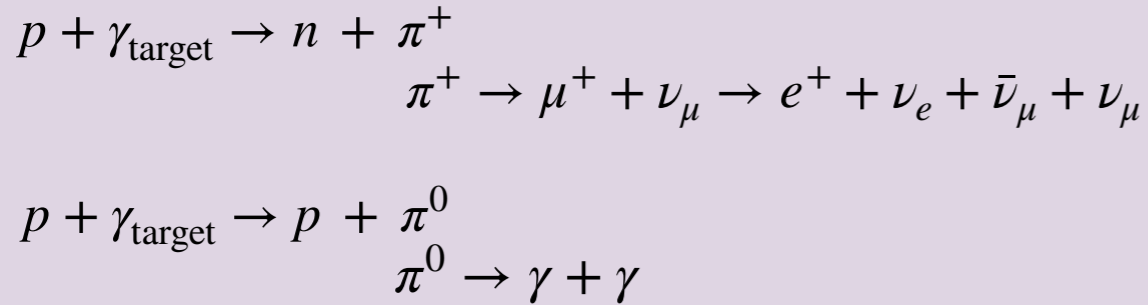
2. Tools for multi-messenger astrophysics

Secondary production channels

Photo-hadronic interactions

Table 9.1 Multiplicities ζ and Mean Fractional Energies χ of Secondaries Formed in Photomeson Production

Species	Single π		Multi- π	
	ζ^s	χ^s	ζ^m	χ^m
Neutrinos	$\zeta_v^s = 3/2$	$\chi_v^s = 0.05$	$\zeta_v^m = 6$	$\chi_v^m = 0.05$
Leptons	$\zeta_e^s = 1/2$	$\chi_e^s = 0.05$	$\zeta_e^m = 2$	$\chi_e^m = 0.05$
γ -rays	$\zeta_\gamma^s = 1$	$\chi_\gamma^s = 0.1$	$\zeta_\gamma^m = 2$	$\chi_\gamma^m = 0.1$
Neutrons	$\zeta_n^s = 1/2$	$\chi_n^s = 0.8$	$\zeta_n^m = 0.5$	$\chi_n^m = 0.4$
Protons	$\zeta_p^s = 1/2$	$\chi_p^s = 0.8$	$\zeta_p^m = 0.5$	$\chi_p^m = 0.4$
β -electrons	$\zeta_{\beta,e}^s = 1/2$	$\chi_{\beta,e}^s = 10^{-3}$	$\zeta_{\beta,e}^m = 1/2$	$\chi_{\beta,e}^m = 10^{-3}$
β -neutrinos	$\zeta_{\beta,\nu}^s = 1/2$	$\chi_{\beta,\nu}^s = 10^{-3}$	$\zeta_{\beta,\nu}^m = 1$	$\chi_{\beta,\nu}^m = 10^{-3}$



cross-section

$$\sigma_{p\gamma}(\bar{\epsilon}) = \begin{cases} 340 \mu\text{b}, & \bar{\epsilon}_{\text{th}} < \bar{\epsilon} < 500\text{MeV}, \\ 120 \mu\text{b}, & \bar{\epsilon} > 500\text{MeV}, \end{cases}$$

inelasticity

$$\kappa_{p\gamma}(\bar{\epsilon}) = \begin{cases} 0.2, & \bar{\epsilon}_{\text{th}} < \bar{\epsilon} < 500\text{MeV}, \\ 0.6, & \bar{\epsilon} > 500\text{MeV}, \end{cases}$$

Atoyan & Dermer, 2003

interaction timescale $t_{p\gamma}$

$$t_{p\gamma}^{-1}(\epsilon_p) = \frac{c}{2\gamma_p^2} \int_{\bar{\epsilon}_{\text{th}}}^{\infty} d\bar{\epsilon} \sigma_{p\gamma}(\bar{\epsilon}) \kappa_p(\bar{\epsilon}) \bar{\epsilon} \int_{\bar{\epsilon}/2\gamma_p}^{\infty} d\epsilon \epsilon^{-2} n_\epsilon$$

Photo-hadronic interaction timescale

barred quantities in proton rest frame

invariant energy of interaction =
photon energy in proton rest frame

$$\sqrt{s_{\text{int}}} = \bar{\epsilon} = \gamma_p \epsilon (1 + \beta_p \bar{\mu})$$

photon energy $\epsilon = h\nu/m_e c^2$
proton Lorentz factor $\gamma_p = E_p/m_p c^2 = (1 - \beta_p^2)^{-1/2}$
angle between proton and photon: θ $\mu = \cos \theta$

$$\begin{aligned} t_{p\gamma}^{-1} &= \frac{1}{\gamma_p} \left| \frac{d\gamma_p}{dt} \right| = \frac{1}{\gamma_p} \left| \frac{d\gamma_p}{d\bar{t}} \right| \left(\frac{d\bar{t}}{dt} \right) \\ &= \frac{1}{\gamma_p} \int_{\bar{\Omega}} \int_0^\infty n_{\text{ph}}(\bar{\epsilon}, \bar{\Omega}) c \sigma_{p\gamma}(\bar{\epsilon}) \kappa_{p\gamma}(\bar{\epsilon}) d\bar{\epsilon} d\bar{\Omega} \\ &= \frac{c}{\gamma_p} \int_0^\infty d\bar{\epsilon} \int_0^{2\pi} d\phi \int_{-1}^{+1} d\bar{\mu} n_{\text{ph}}(\bar{\epsilon}, \bar{\Omega}) \sigma_{p\gamma}(\bar{\epsilon}) \kappa_{p\gamma}(\bar{\epsilon}) \end{aligned}$$

$$d\bar{t} = \frac{1}{\gamma_p} dt$$

$$n_{\text{ph}}(\epsilon, \Omega) \equiv \frac{dN_{\text{ph}}}{d\epsilon d\Omega dV}$$

$$\sqrt{s_{\text{int}}} = \bar{\epsilon} = \gamma_p \epsilon (1 + \beta_p \bar{\mu}) \rightarrow \begin{cases} \bar{\mu} = \frac{1}{\beta_p} \left[\frac{\epsilon}{\gamma_p \bar{\epsilon}} - 1 \right] & \text{and} \quad d\bar{\mu} = \frac{1}{\beta_p \gamma_p} \frac{d\epsilon}{d\bar{\epsilon}} \\ n_{\text{ph}}(\bar{\epsilon}, \bar{\Omega}) = n_{\text{ph}}(\epsilon)/4\pi & \text{isotropic photon flux} \end{cases}$$

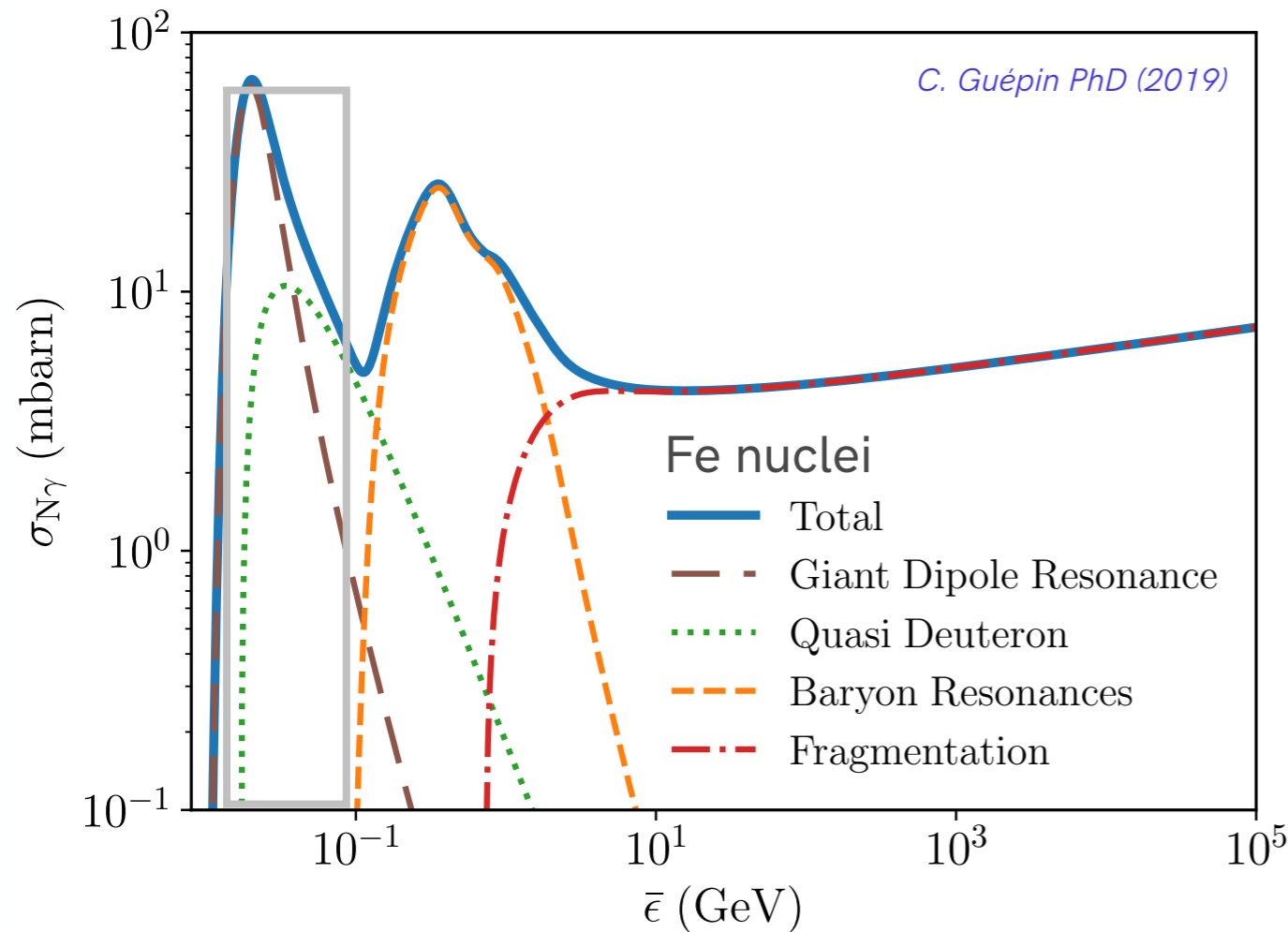
$$t_{p\gamma}^{-1} = \frac{c}{2\gamma_p^2 \beta_p} \int_0^\infty \frac{n_{\text{ph}}(\epsilon)}{\epsilon^2} \int_{\bar{\epsilon}_{\text{min}}}^{\bar{\epsilon}_{\text{max}}} \sigma_{p\gamma}(\bar{\epsilon}) \kappa_{p\gamma}(\bar{\epsilon}) d\bar{\epsilon}$$

$$\bar{\epsilon}_{\text{min}} = \frac{\epsilon}{\gamma_p(1 + \beta_p)} \sim \frac{\epsilon}{2\gamma_p} \rightarrow 0$$

$$\bar{\epsilon}_{\text{max}} = \frac{\epsilon}{\gamma_p(1 - \beta_p)} \sim 2\gamma_p \epsilon$$

Photo-disintegration $A + \gamma_{\text{target}}$

$$\text{nucleus energy } E_A = \gamma_A A m_p c^2$$



For all these processes:

E_A/A : energy per nucleon does not change

They don't all allow the direct production of pions, but they produce α particles
 \rightarrow pions (i.e. secondaries)

$\left. \begin{array}{l} \text{direct} \\ \pi \text{ production} \end{array} \right\}$
 $\left. \begin{array}{l} \text{production of nucleons} \\ \rightarrow \pi \text{ production} \end{array} \right\}$

"Delta" approximation:

$$\sigma_{\text{GDR}} \sim 1.45 \times 10^{-27} \text{ cm}^2 A$$

$$\bar{\epsilon}_{\text{GDR}} \sim 42.65 A^{-0.21} \text{ MeV}$$

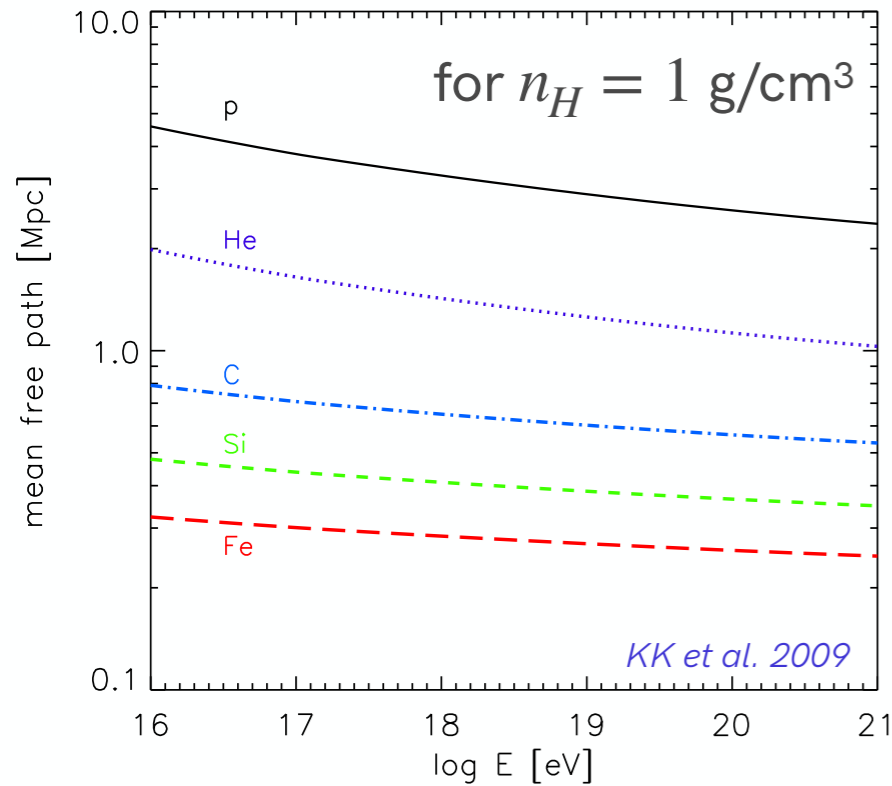
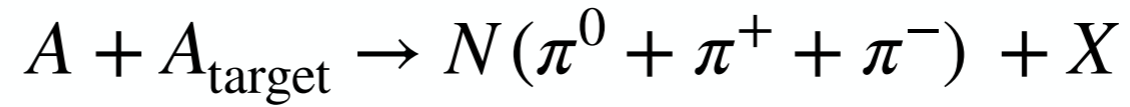
$$\Delta \bar{\epsilon} \sim 8 \text{ MeV}$$

Murase et al. PRD (2008)

For interaction channel i :

$$t_{A\gamma,i}^{-1} = \frac{c}{2\gamma_A^2} \int_0^\infty \frac{n_{\text{ph}}(\epsilon)}{\epsilon^2} \int_0^{2\gamma_A \bar{\epsilon}} \sigma_{A\gamma,i}(\bar{\epsilon}) d\bar{\epsilon}$$

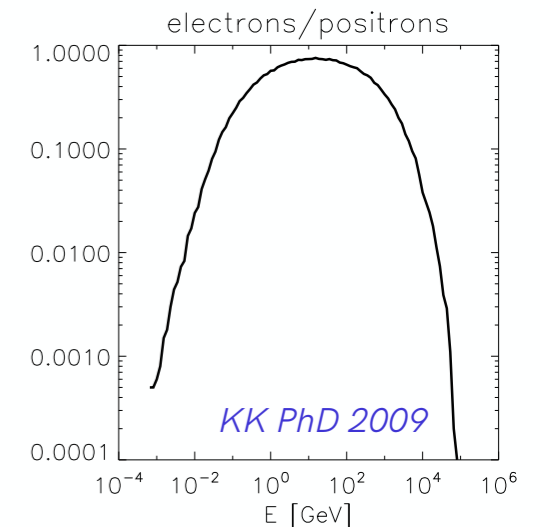
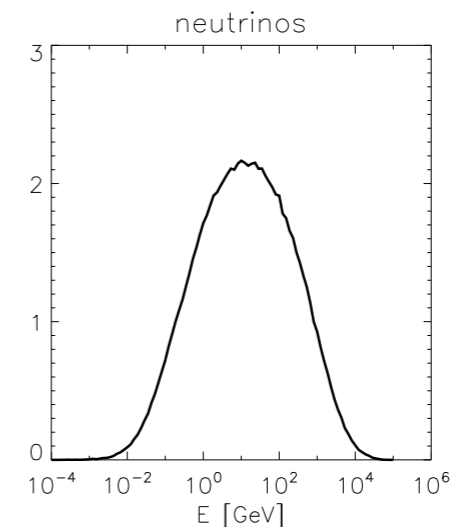
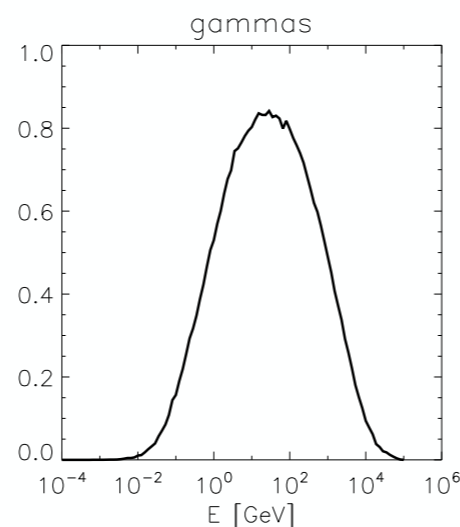
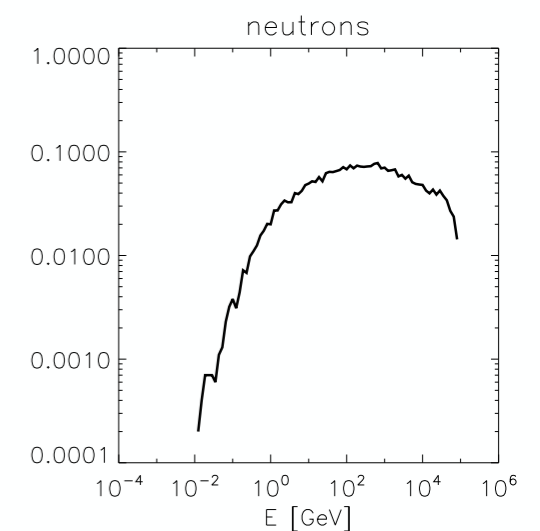
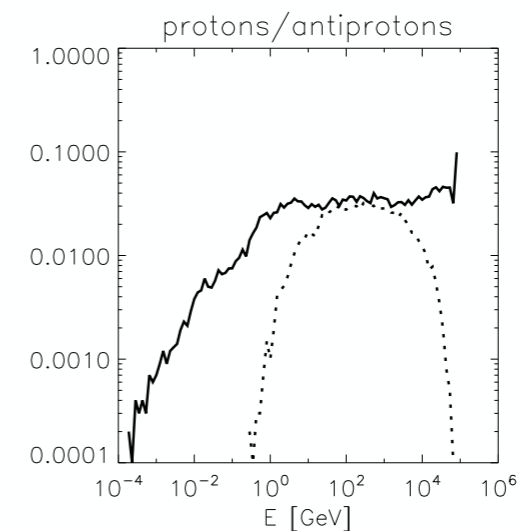
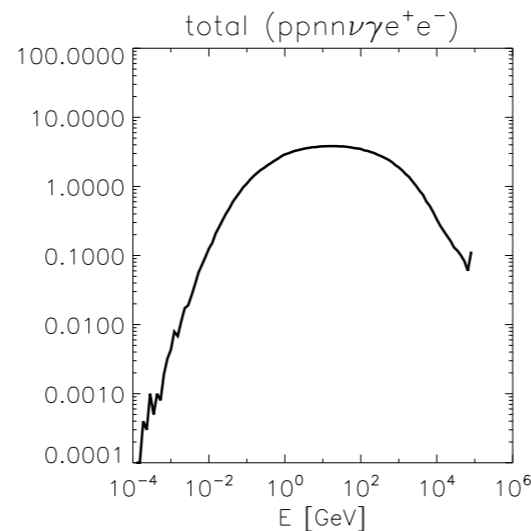
Hadronic interactions



spallation cross-section $A + p_{\text{target}}$:

$$\sigma_{\text{sp}}(E') \simeq [50.44 - 7.93 \log(E') + 0.61 \log^2(E')] A^{\beta_{\text{sp}}} \text{ mb}$$

$$t_{\text{sp}}^{-1} = n_A \sigma_{\text{sp}} c$$



Energy distribution of secondary particles produced by a pp interaction
Calculated with EPOS

2. Tools for multi-messenger astrophysics

**Maximum energies
& simple flux estimates**

Maximum cosmic ray energy at the source

*e.g., Guépin & KK (2017),
Guépin et al. (2018)
and many refs. therein*

For cosmic rays: $t'_{\text{acc}} \lesssim t'_{\text{dyn}}, t'_{\text{esc}}, t'_{\text{loss}}, t'_{\text{age}} \dots$

tip: write all these timescales in the comoving frame (primed quantities)

depends on
B strength
and structure

photo-hadronic/hadronic interactions

$$t'_{N\gamma}{}^{-1} = \frac{c}{2\gamma'^2} \int_0^\infty \frac{d\epsilon'}{\epsilon'^2} \frac{dn'_\gamma}{d\epsilon'}(\epsilon') \int_0^{2\gamma'\epsilon'} d\bar{\epsilon} \bar{\epsilon} \sigma_{N\gamma}(\bar{\epsilon})$$

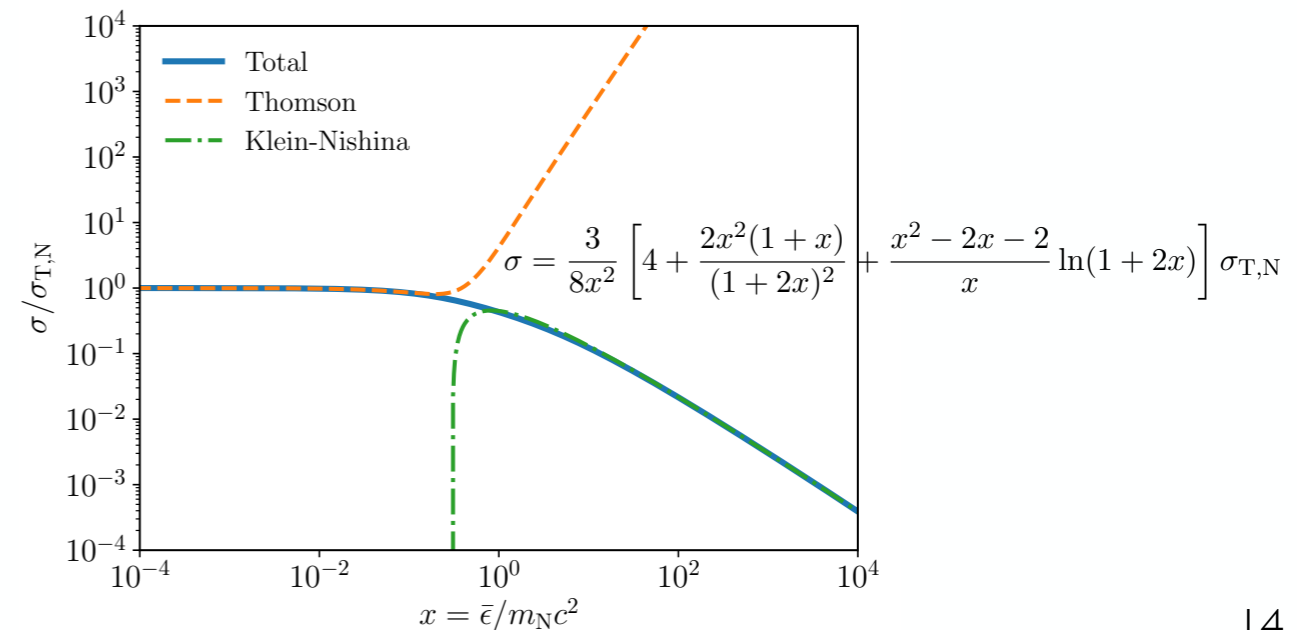
synchrotron radiation in B

$$t'_{\text{syn}} = \frac{3m_p c}{4\sigma_{T,p} U'_B} \frac{A^3}{Z^4} \frac{1}{\gamma'}$$

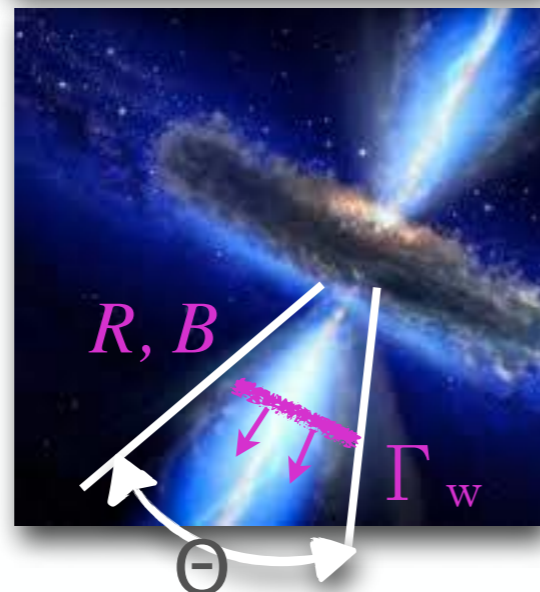
$$U'_B = B'^2 / 8\pi$$

magnetic energy density

inverse Compton



$$t_{\text{dyn}} \sim R / \beta_w \Gamma_w c$$



$t'_{\text{acc}} = \mathcal{A} t'_L$

depends on acc. mechanism and environment

Larmor time

$\mathcal{A} \gg 1$

$\mathcal{A} \sim 1$ at best

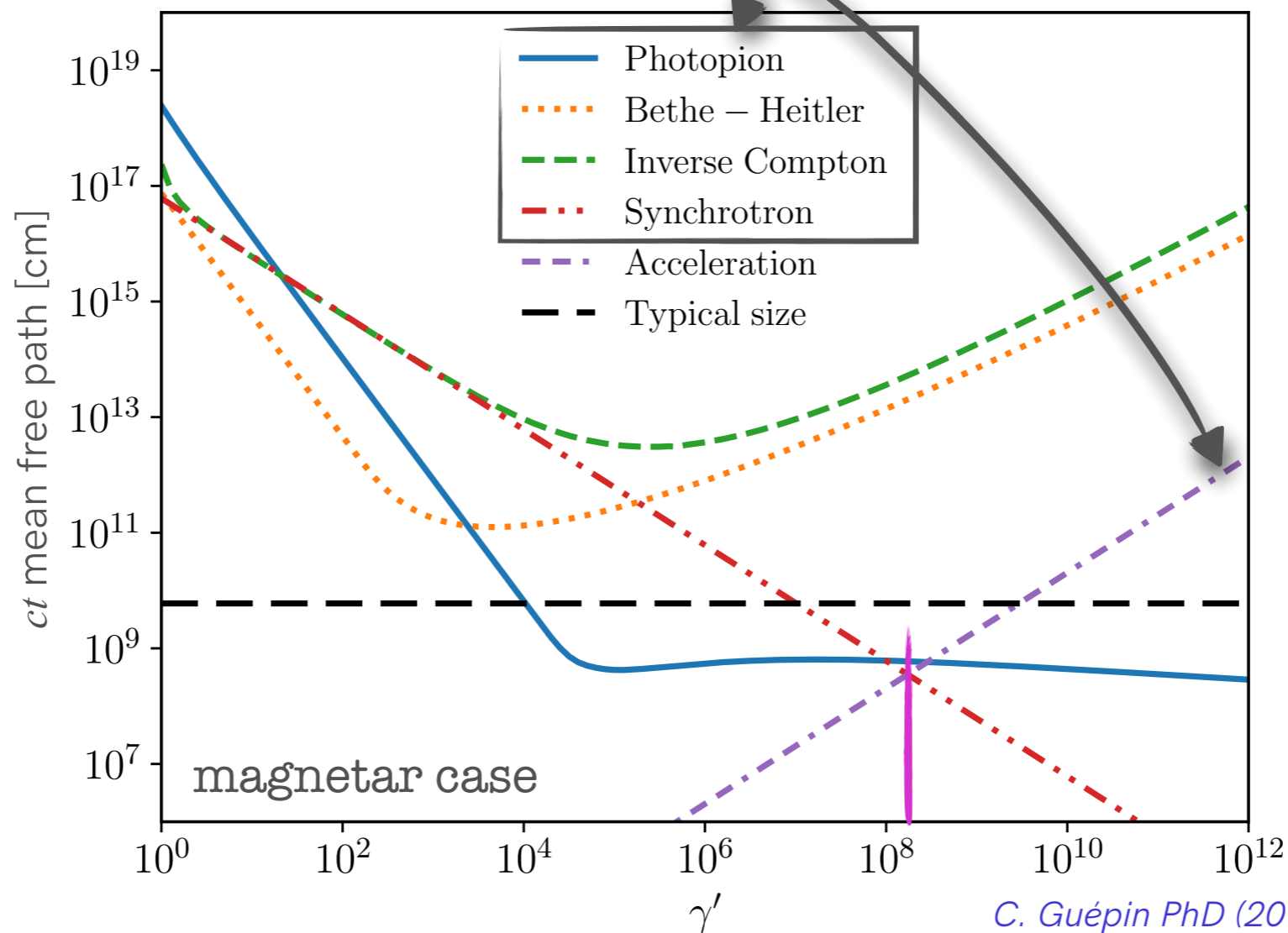
*e.g., Norman et al. 1995,
Waxman 1995,
Lytikov & Ouyed 2005,
Waxman 2005
Lemoine & Waxman 2009*

Maximum cosmic ray energy at the source

*e.g., Guépin & KK (2017),
Guépin et al. (2018)
and many refs. therein*

For cosmic rays: $t'_{\text{acc}} \lesssim t'_{\text{dyn}}, t'_{\text{esc}}, t'_{\text{loss}}, t'_{\text{age}} \dots$

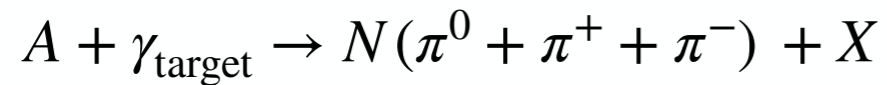
*tip: write all these timescales
in the comoving frame
(primed quantities)*



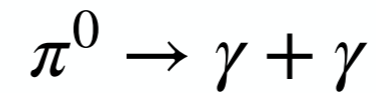
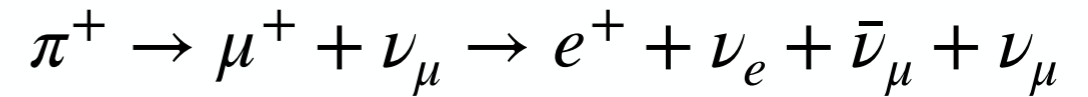
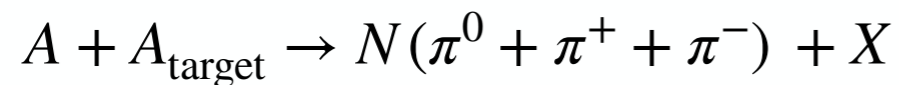
C. Guépin PhD (2019)

Secondary neutrino & gamma-ray energies

photo-hadronic interactions



hadronic interactions



$$E_\pi \sim \frac{1}{5} E_A / A$$

$$E_{\nu_\mu} \sim \frac{1}{4} E_\pi$$

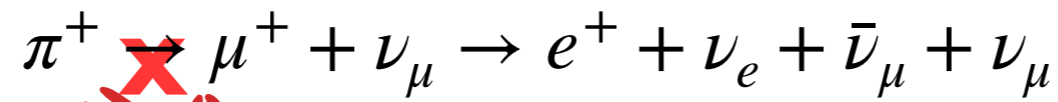
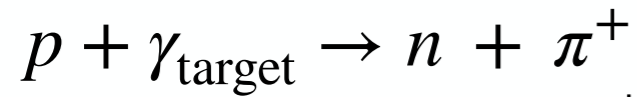
$$E_\gamma \sim \frac{1}{2} E_\pi$$

$$E_\nu \sim \frac{1}{5} \frac{1}{4} E_p \sim 0.05 \frac{E_A}{A}$$

$$E_\gamma \sim \frac{1}{5} \frac{1}{2} E_p \sim 0.1 \frac{E_A}{A}$$

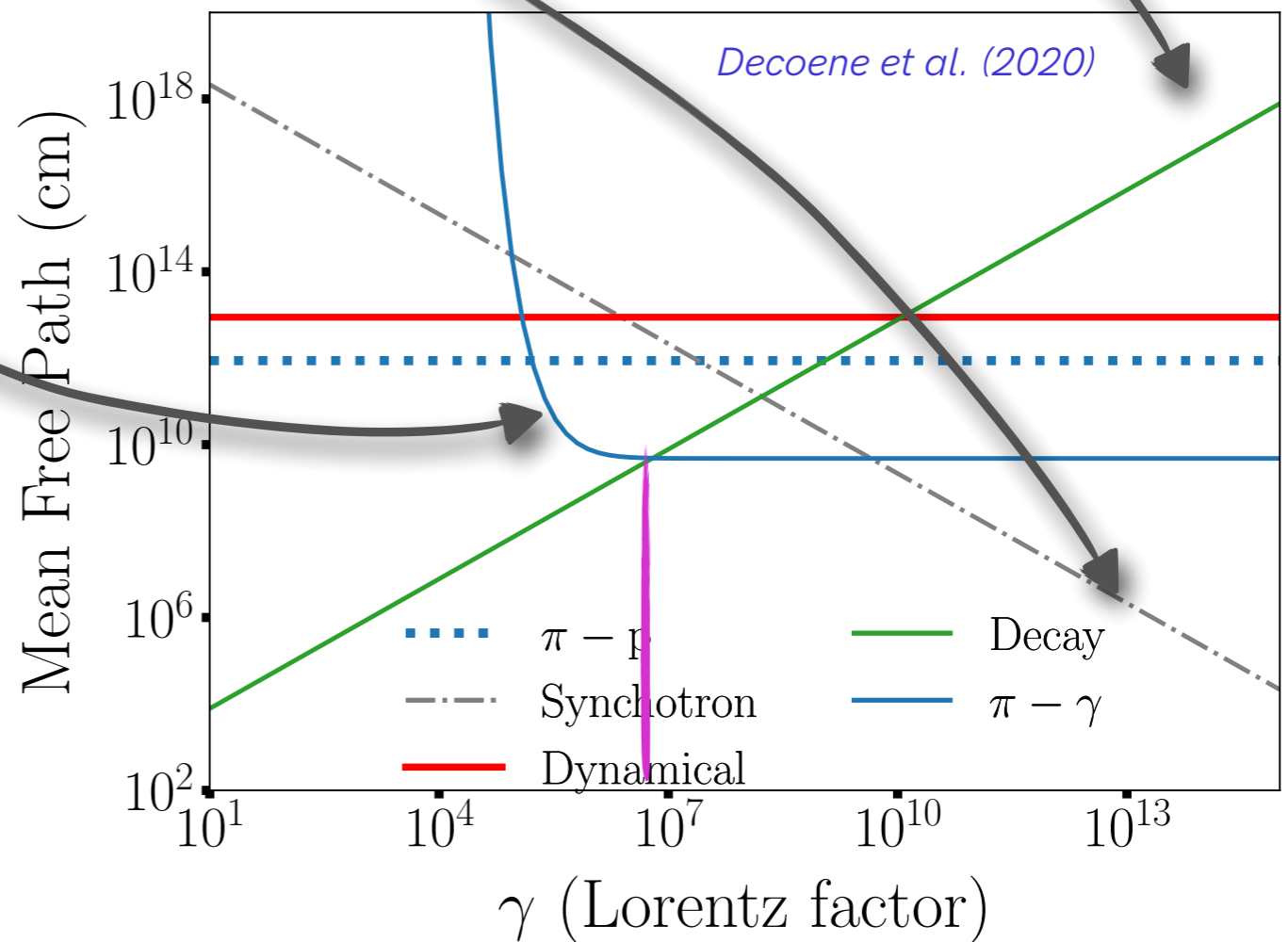
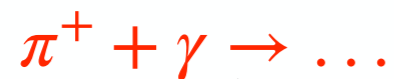
Neutrino energies at the source

pion & muon cooling in dense environments



cascades
no HE ν

synchrotron cooling
no HE ν



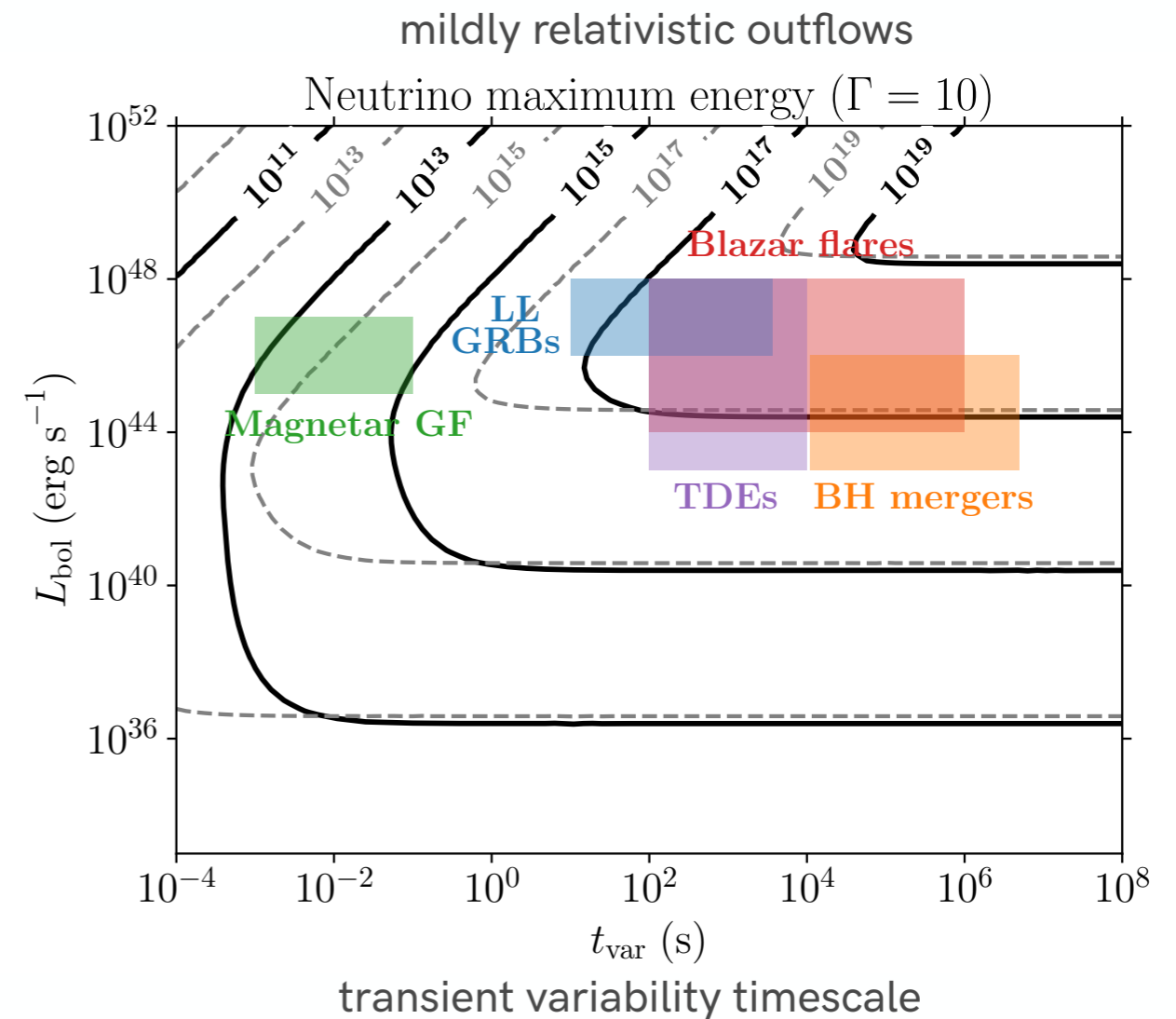
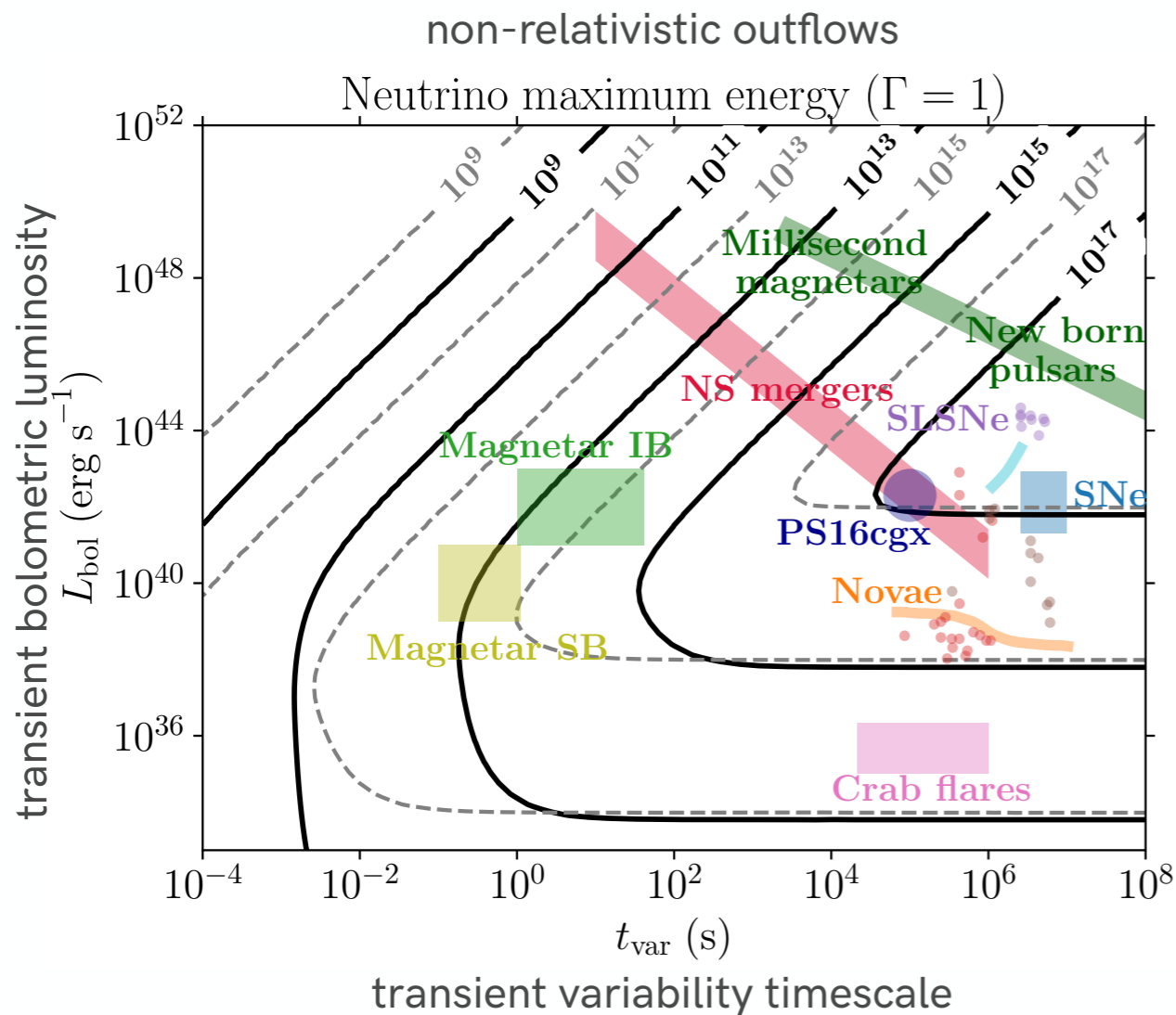
Example: pions in a kilonova ejecta

Maximum neutrino energy for transient sources

Guépin & KK (2017)
 Guépin, KK, Oikonomou, Nat. subm.

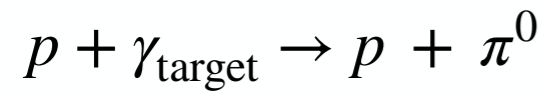
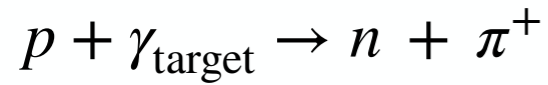
$E_\nu \sim 0.05E_p$ + taking into account possible pion and muon cooling

Bolometric luminosity L_{bol} related to magnetic field strength B (hence to $t_{\text{syn}}, t_{\text{acc}}, t_{\text{dyn}}$)



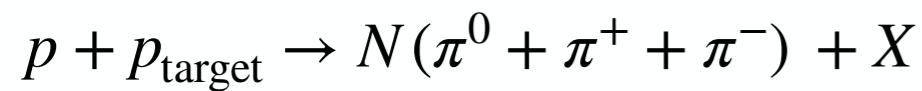
Simple estimates of secondary particle fluxes

photo-hadronic interactions

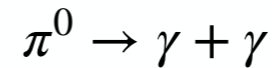
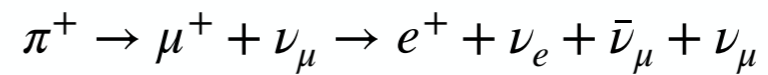


$$K_{\pi} = \frac{N_{\pi^{\pm}}}{N_{\pi^0}} \sim 1$$

hadronic interactions



$$K_{\pi} = \frac{N_{\pi^{\pm}}}{N_{\pi^0}} \sim 2$$



$$E_{\pi} \sim \frac{1}{5} E_p$$

$$E_{\nu_{\mu}} \sim \frac{1}{4} E_{\pi}$$

$$E_{\gamma} \sim \frac{1}{2} E_{\pi}$$

$f_{\text{mes}} ?$

$$p\gamma \left\{ \begin{array}{l} E_{\nu}^2 \Phi_{\nu} \sim 3 \frac{K_{\pi}}{1 + K_{\pi}} \frac{1}{4} E_{\pi}^2 \Phi_{\pi} \sim \frac{3}{8} f_{\text{mes}} E_p^2 \Phi_p \quad (3 \text{ flavors}) \\ E_{\gamma}^2 \Phi_{\gamma} \sim 2 \frac{1}{1 + K_{\pi}} \frac{1}{2} E_{\pi}^2 \Phi_{\pi} \sim \frac{1}{2} f_{\text{mes}} E_p^2 \Phi_p \end{array} \right.$$

$$E_{\nu}^2 \Phi_{\nu} \sim \frac{3}{4} E_{\gamma}^2 \Phi_{\gamma}$$

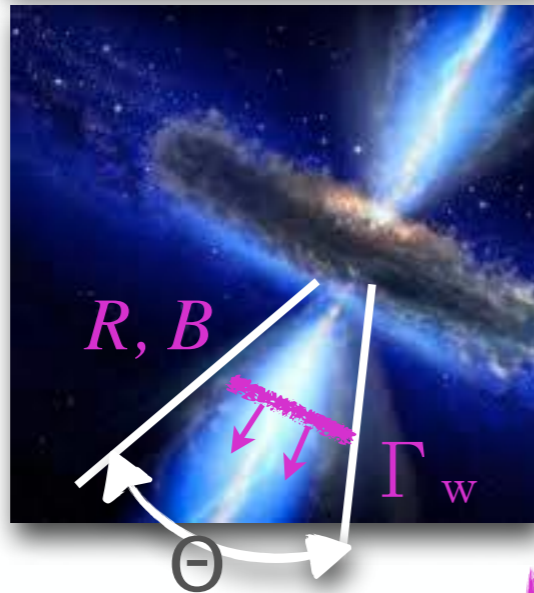
$$pp \left\{ \begin{array}{l} E_{\nu} \Phi_{\nu} \sim 3 \frac{2}{3} \frac{1}{4} E_{\pi}^2 \Phi_{\pi} \sim \frac{1}{2} f_{\text{mes}} E_p^2 \Phi_p \\ E_{\gamma}^2 \Phi_{\gamma} \sim 2 \frac{1}{3} \frac{1}{2} E_{\pi}^2 \Phi_{\pi} \sim \frac{1}{3} f_{\text{mes}} E_p^2 \Phi_p \end{array} \right.$$

$$E_{\nu}^2 \Phi_{\nu} \sim \frac{3}{2} E_{\gamma}^2 \Phi_{\gamma}$$

Meson production rates

tip: write all these timescales in the comoving frame (primed quantities)

$$t_{\text{dyn}} \sim R/\beta_w \Gamma_w c$$



examples:

synchrotron radiation in B

$$t'_{\text{syn}} = \frac{3m_p c}{4\sigma_{T,p} U'_B} \frac{A^3}{Z^4} \frac{1}{\gamma'}$$

$$U'_B = B'^2/8\pi$$

magnetic energy density

inverse Compton

$$t'_{\text{min}} = \min(t'_{\text{dyn}}, t'_{\text{acc}}, t'_{\text{loss}}, t'_{\text{diff}}, \dots)$$

$$f_{\text{mes}} = \frac{t'_{\text{min}}}{t'_{p\gamma,pp}}$$

$$\begin{cases} t'^{-1}_{N\gamma} = \frac{c}{2\gamma'^2} \int_0^\infty \frac{d\epsilon'}{\epsilon'^2} \frac{dn'_{\gamma}}{d\epsilon'}(\epsilon') \int_0^{2\gamma'\epsilon'} d\bar{\epsilon} \bar{\epsilon} \sigma_{N\gamma}(\bar{\epsilon}) \\ t'^{-1}_{pp} = n_p \sigma_{pp} c \end{cases}$$

modeling according to theory+observations

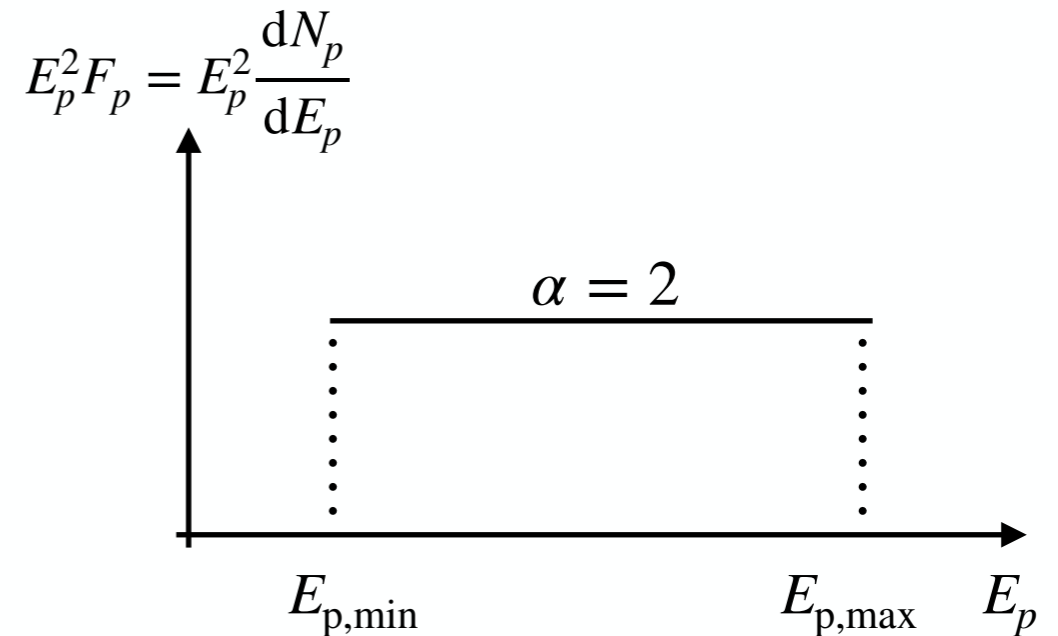
Secondary spectra at the source

Cosmic-ray spectrum:

Assuming some acceleration mechanism

$$E_p^2 F_p = \frac{1}{4\pi D_L^2} \frac{(2-\alpha)\eta_p L_{\text{bol}}}{E_{p,\text{max}}^{2-\alpha} - E_{p,\text{min}}^{2-\alpha}} E_p^{2-\alpha} \quad 1 \lesssim \alpha \lesssim 3$$

source distance
fraction of source bolometric luminosity



Photon spectrum: Broken power-law

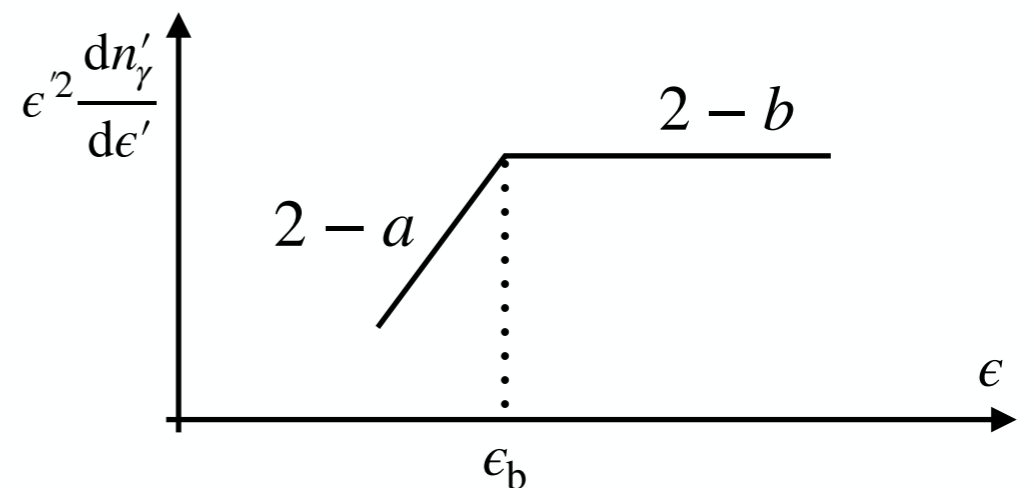
observed break energy

$$L_\gamma(\epsilon) = \epsilon^2 \frac{d\dot{N}_\gamma}{d\epsilon} = \begin{cases} L_b (\epsilon/\epsilon_b)^{2-a} & \epsilon_{\text{min}} \leq \epsilon \leq \epsilon_b \\ L_b (\epsilon/\epsilon_b)^{2-b} & \epsilon_b < \epsilon < \epsilon_{\text{max}} \end{cases}$$

ex: Prompt GRB gamma-ray spectrum (Band function)

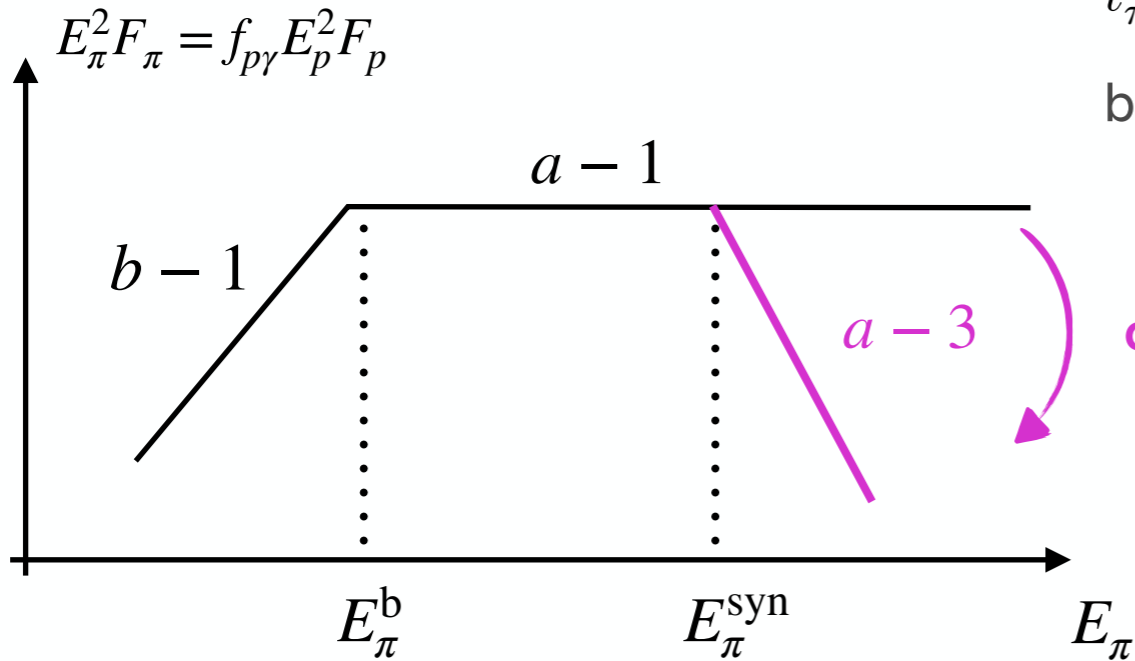
In the comoving frame (primed quantities):

$$\frac{dn'_\gamma}{d\epsilon'}(\epsilon') = \frac{L'_b}{4\pi R'^2 c \epsilon'^2} \times \begin{cases} (\epsilon'/\epsilon'_b)^{-a} & \epsilon' < \epsilon'_b \\ (\epsilon'/\epsilon'_b)^{-b} & \epsilon' > \epsilon'_b \end{cases}$$



Secondary spectra at the source

Meson spectrum



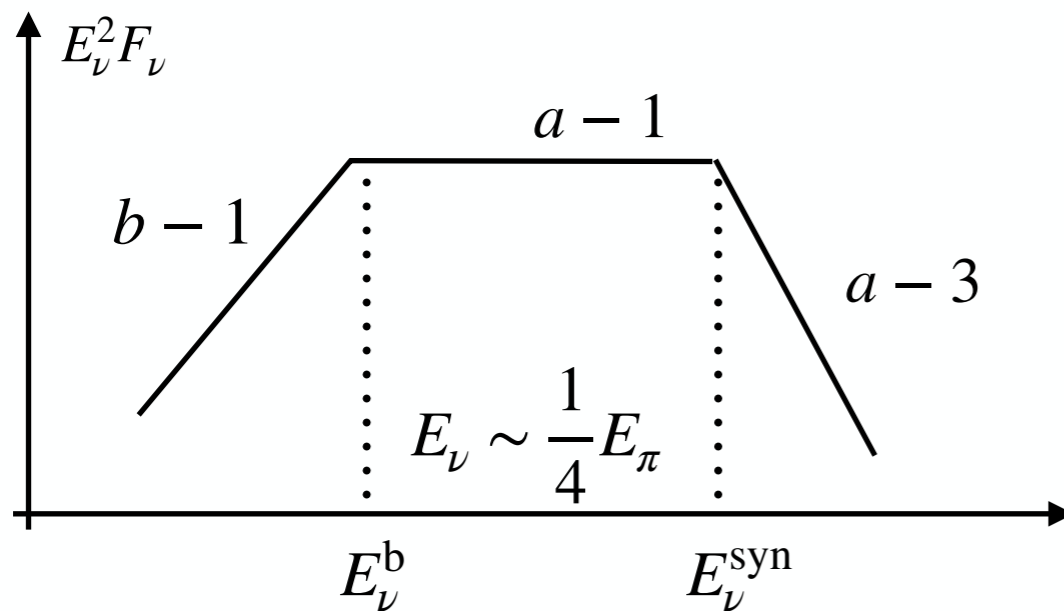
pion decay time:

$$t'_\pi(E_\pi) = \tau_\pi E_\pi (1+z) ((1+\beta)\Gamma m_\pi c^2)^{-1} \sim 0.9 \text{ s } E_{\pi,18} \Gamma_2^{-1}$$

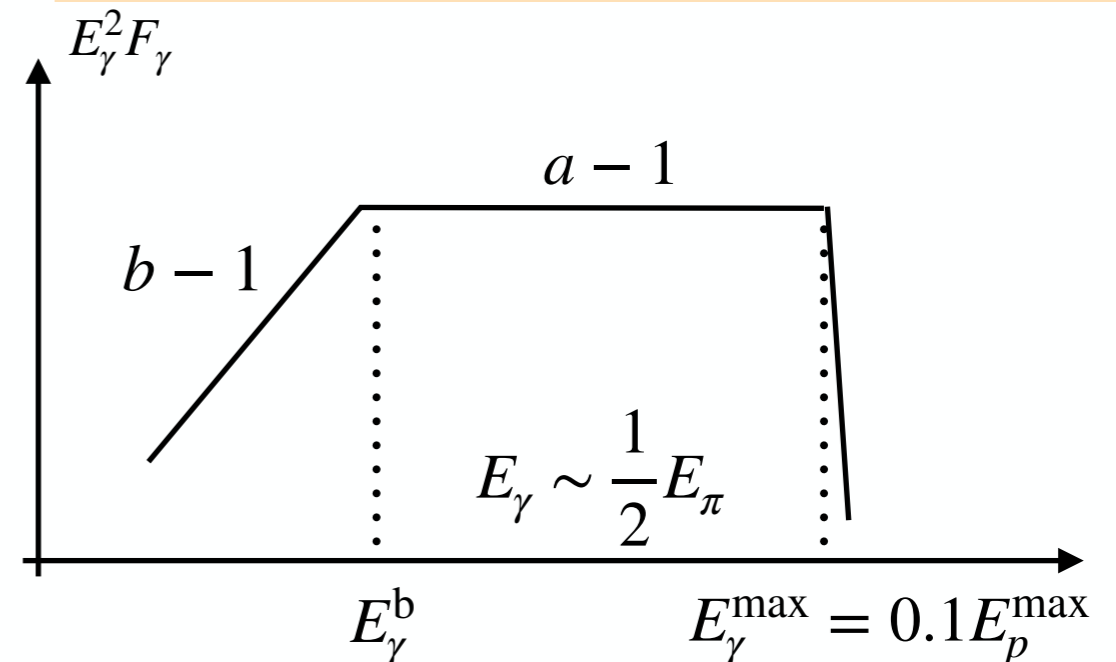
break energy: $E_\pi^b \sim 0.07 \text{ GeV}^2 \Gamma^2 / \epsilon_b$

cooling of charged mesons

Neutrino spectrum



Gamma-ray spectrum



Computing secondary fluxes at the source: key points

mechanisms:
 shock acceleration
 magnetic reconnection...

at various locations:
 inner/external/side jet
 wind
 accretion disk...

—> max. acceleration energy
 spectrum

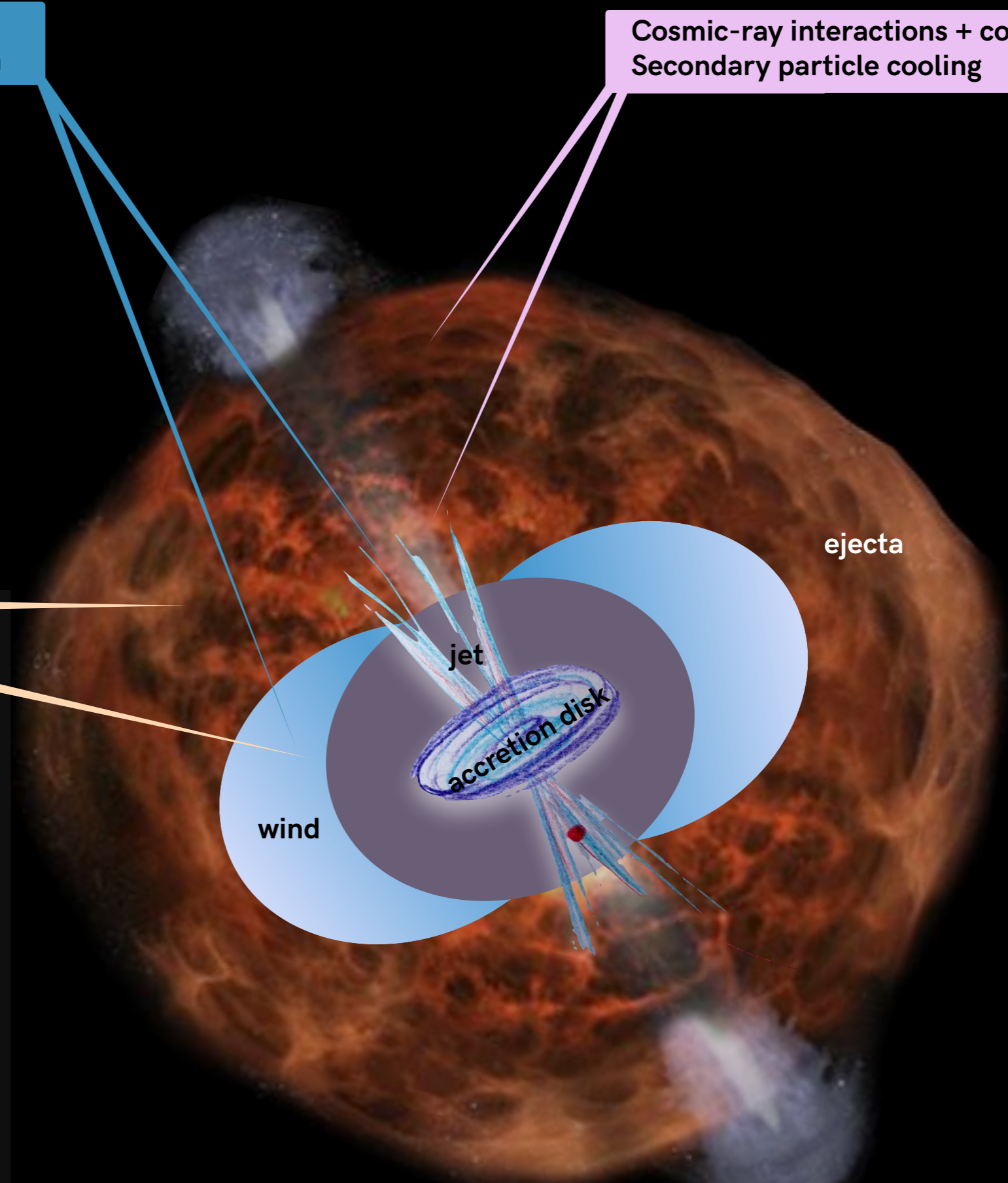
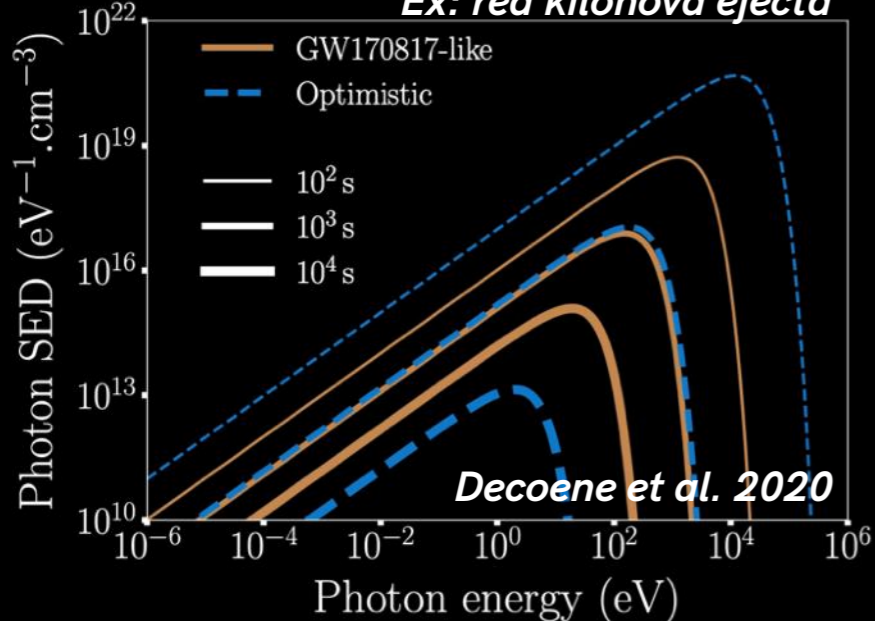
Cosmic-ray
 acceleration

Cosmic-ray interactions + cooling
 Secondary particle cooling

Radiative + hadronic
 backgrounds

density, spectra, time evolution
 in acceleration region and beyond

Ex: red kilonova ejecta



Integrating over source population

primed quantities in comoving frame

$$\Phi_\nu(E_\nu) = \frac{f_s}{4\pi} \int_0^{z_{\max}} \int_0^{t_\nu} \frac{dN_\nu[E_\nu(1+z)]}{dt' dE_\nu} \frac{1}{4\pi D^2} dt' \dot{\mathcal{R}}(z) 4\pi D^2 \frac{dD'}{dz} dz$$

normalization factor to fit UHECR spectrum if related

comoving distance

$$\dot{\mathcal{R}}(z) = g(z) \dot{\mathcal{R}}(0)$$

comoving source emissivity in $\text{Mpc}^{-3} \text{yr}^{-1}$

$g(z)$ = redshift evolution rate

for uniform evolution $g(z) = 1$

for star formation rate (SFR) evolution

$$g(z) = \begin{cases} (1+z)^{3.4}, & z < 1 \\ N_1(1+z)^{-0.3}, & 1 < z < 4 \\ N_1 N_4(1+z)^{-3.5}, & z > 4 \end{cases}$$

$N_\nu[E_\nu(1+z)]$
total number of neutrinos produced by 1 source

$$\Phi_\nu(E_\nu) = f_s \frac{c}{4\pi} \int_0^{z_{\max}} \dot{\mathcal{R}}(z) \frac{dN_\nu[E_\nu(1+z)]}{dE'} (1+z) \left(\frac{dt}{dz}\right) dz$$

$$E' = E_\nu(1+z)$$

comoving energy

$$dt/dz = 1 / \left(H_0(1+z) \sqrt{\Omega_M(1+z)^3 + \Omega_\Lambda} \right)$$

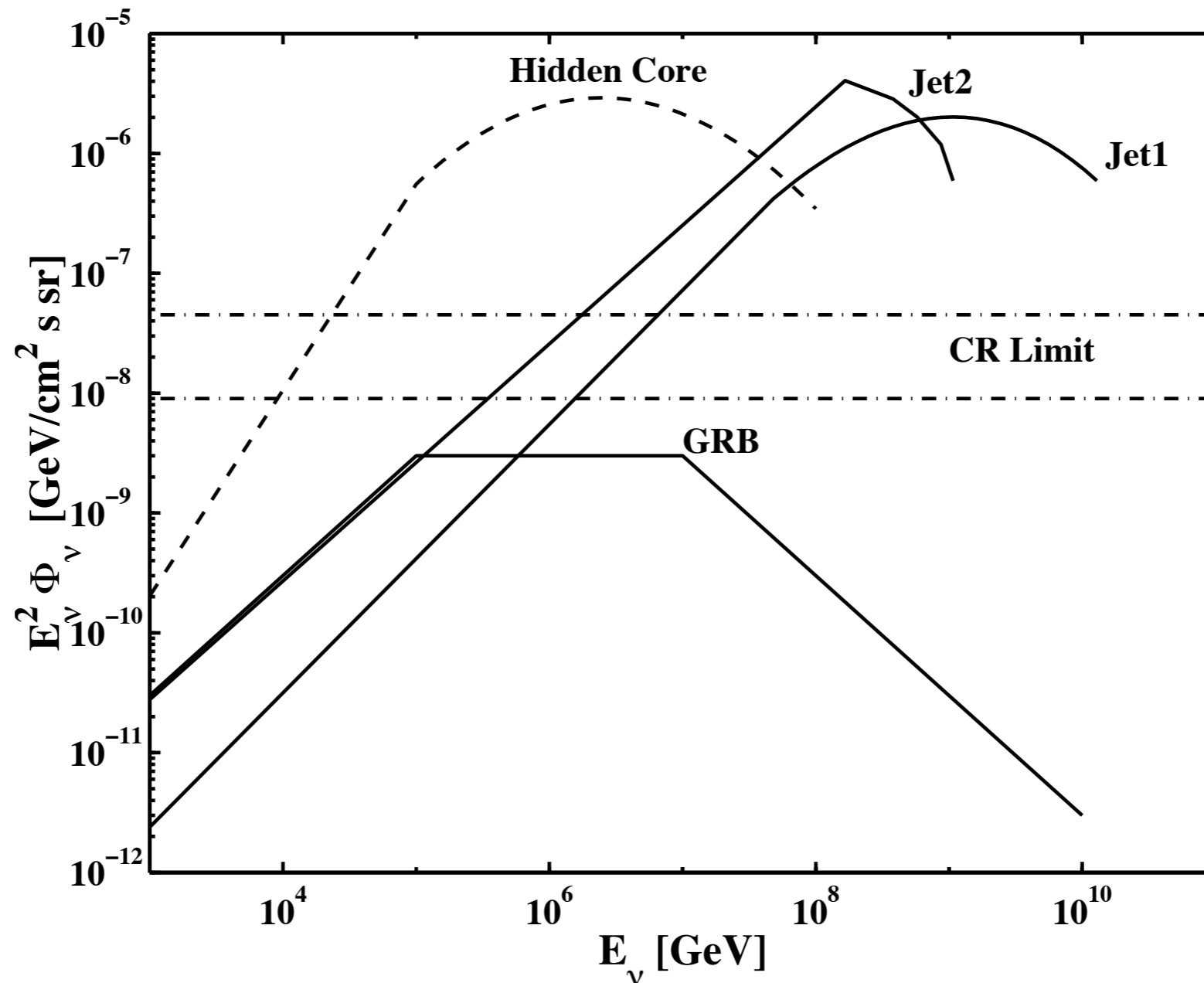
Waxman-Bahcall "limit"

Waxman & Bahcall, 1997

redshift energy loss
of neutrinos ~ 1

$$E_\nu^2 \Phi_\nu \sim \xi_z t_H \frac{c}{4\pi} \frac{3}{8} f_{\text{mes}} E_{\text{CR}}^2 \Phi_{\text{CR}}$$

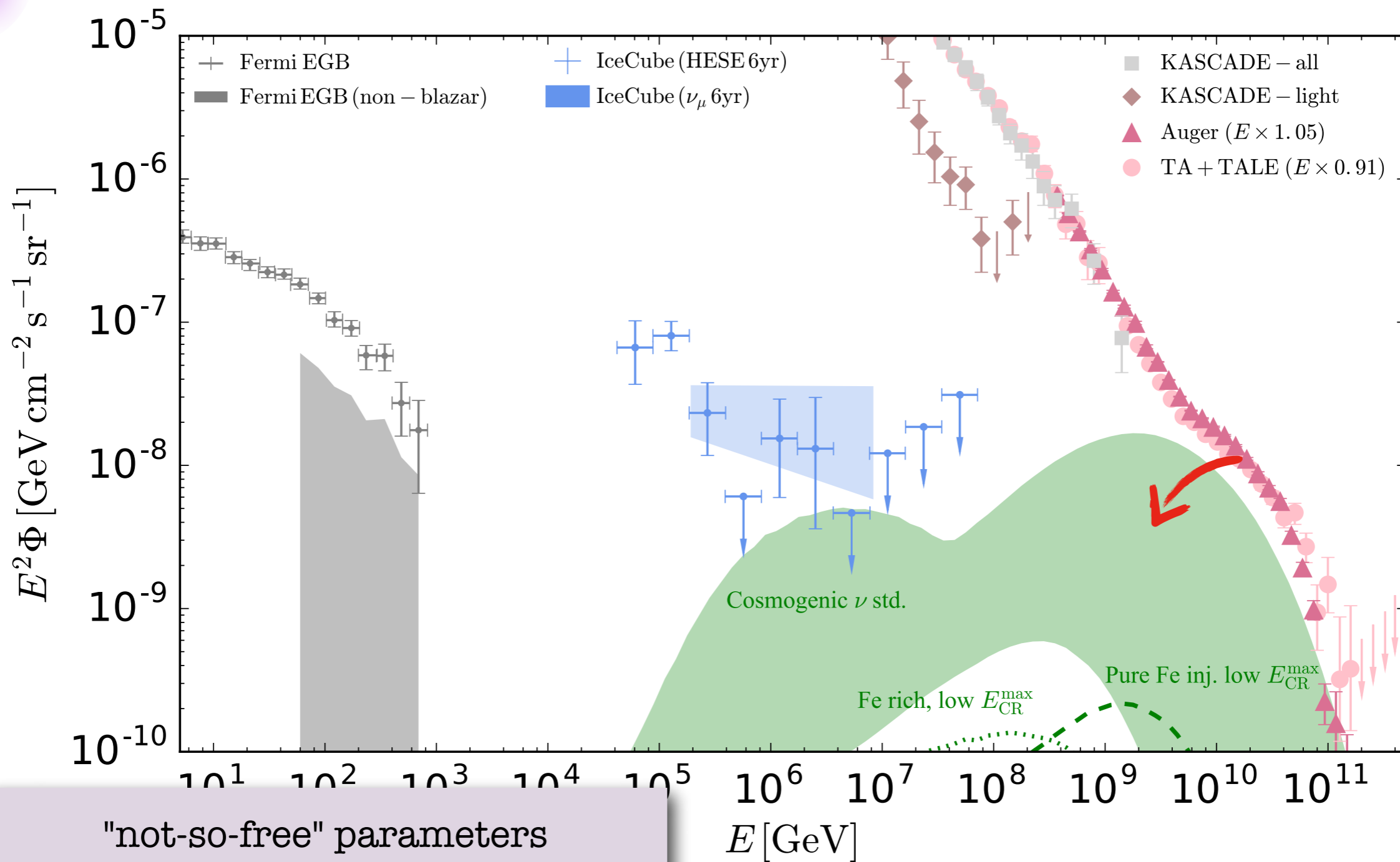
$$E_\nu^2 \Phi_\nu \sim 1.5 \times 10^{-8} \xi_z f_{\text{mes}} \text{ GeV cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \quad \Phi_{\nu_e} \approx \Phi_{\bar{\nu}_\mu} \approx \Phi_{\nu_\mu}$$



2. Tools for multi-messenger astrophysics

Cosmogenic neutrinos

The guaranteed cosmogenic neutrinos



K. Fang

"not-so-free" parameters

- A flux normalisation
- γ injection spectral index
- R_{max} (max. rigidity \sim max. p energy)
- composition
- source evolution history

cosmogenic neutrinos guaranteed
if sources of UHECRs
@cosmological distances

Cosmogenic neutrinos: production channels

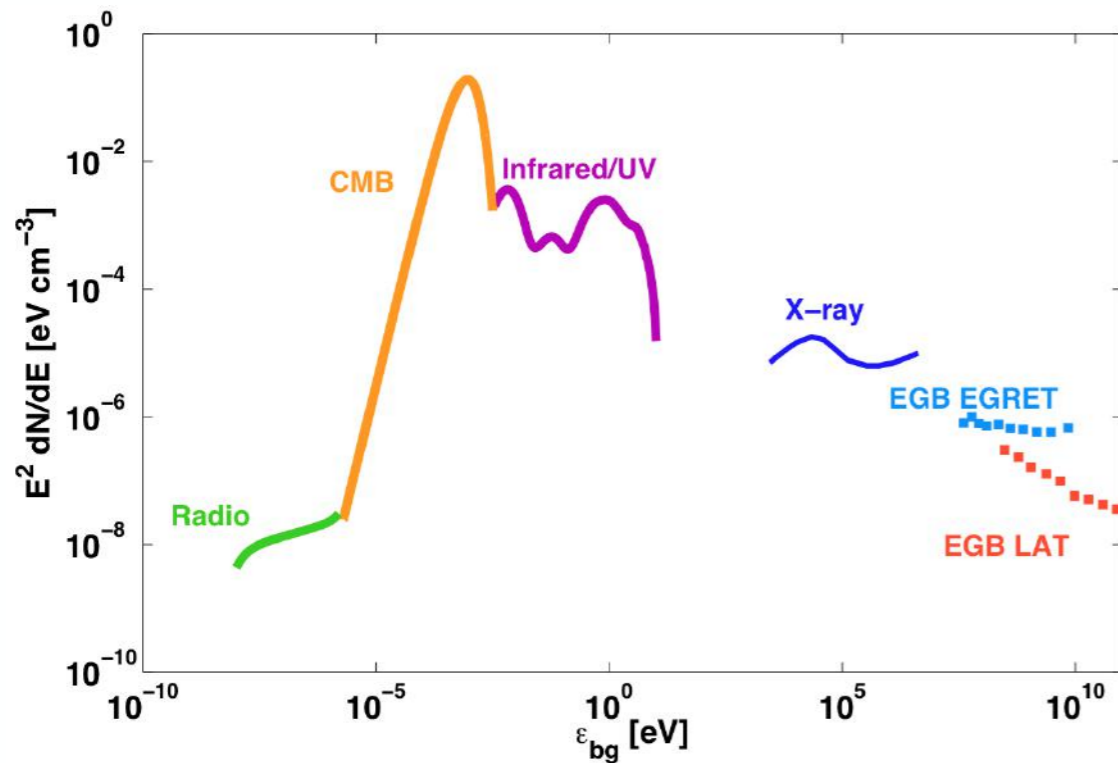
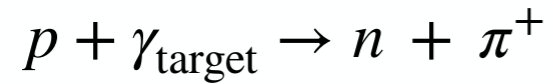
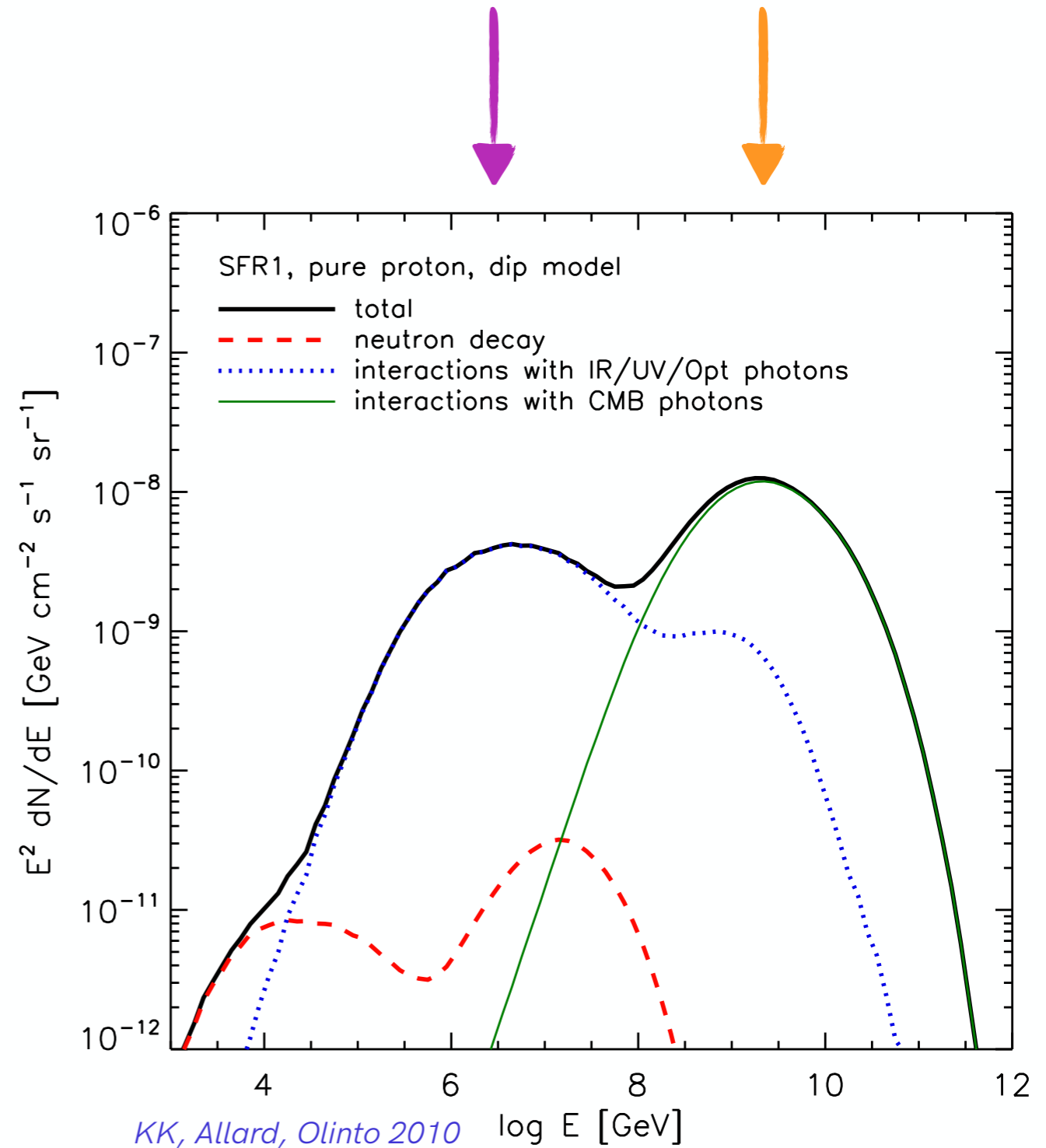


Figure 2.1. The spectrum of cosmic background radiations. The CMB is modelled as a blackbody spectrum at 2.725 K. The IR and UV backgrounds are from the work of Kneiske & Dole (2008). The extragalactic gamma-ray background datapoints (EGB) are from EGRET measurements (Sreekumar et al. 1998) and *Fermi*-LAT measurements (Abdo et al. 2010). For the X-ray and radio backgrounds the models presented in the works of Fabian & Barcons (1992), Clark et al. (1970) are shown respectively.

F. Oikonomou, PhD, 2014



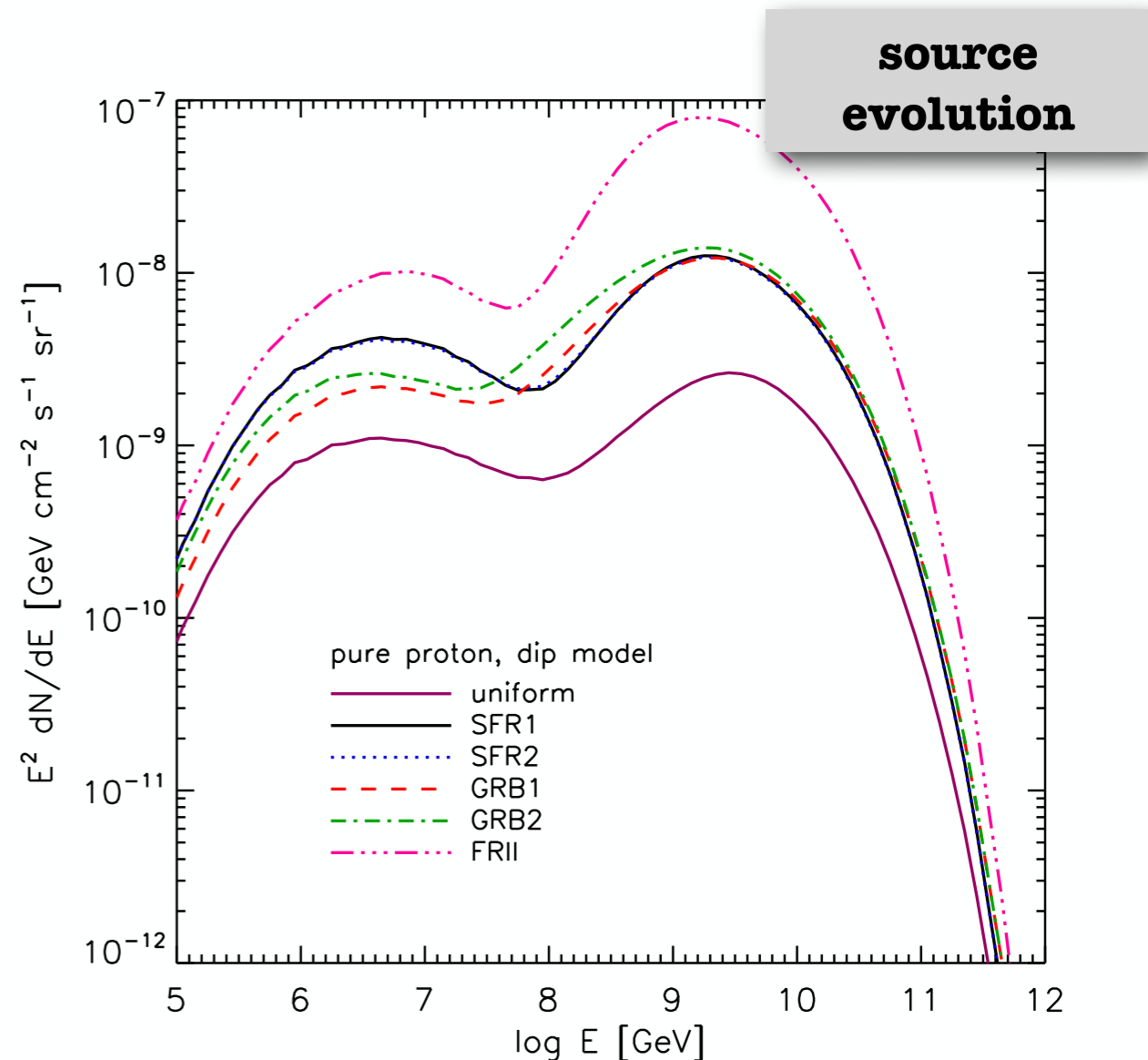
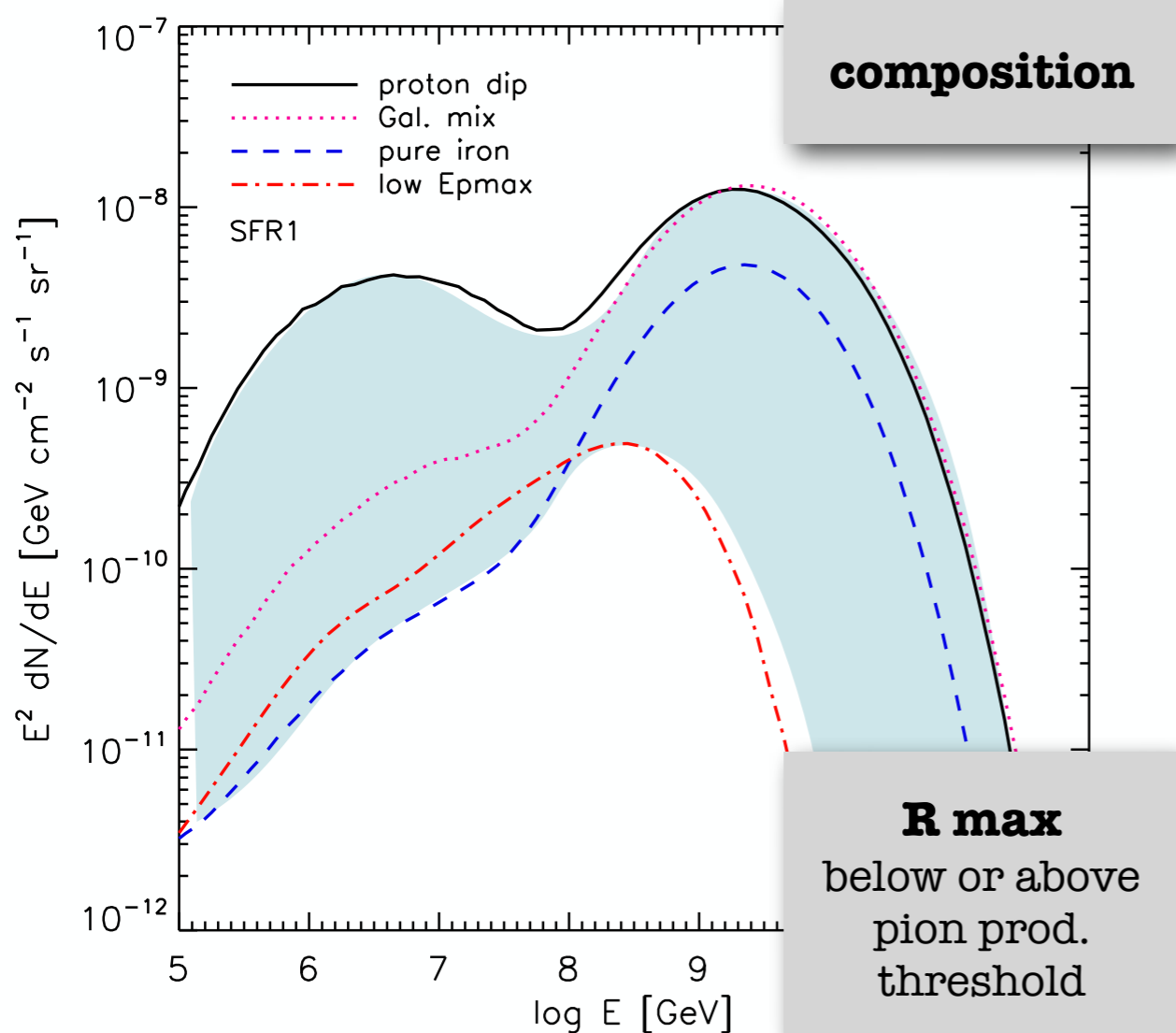
KK, Allard, Olinto 2010

"not-so-free" parameters

- A flux normalisation
- γ injection spectral index
- R_{\max} (max. rigidity \sim max. p energy)
- composition
- source evolution history

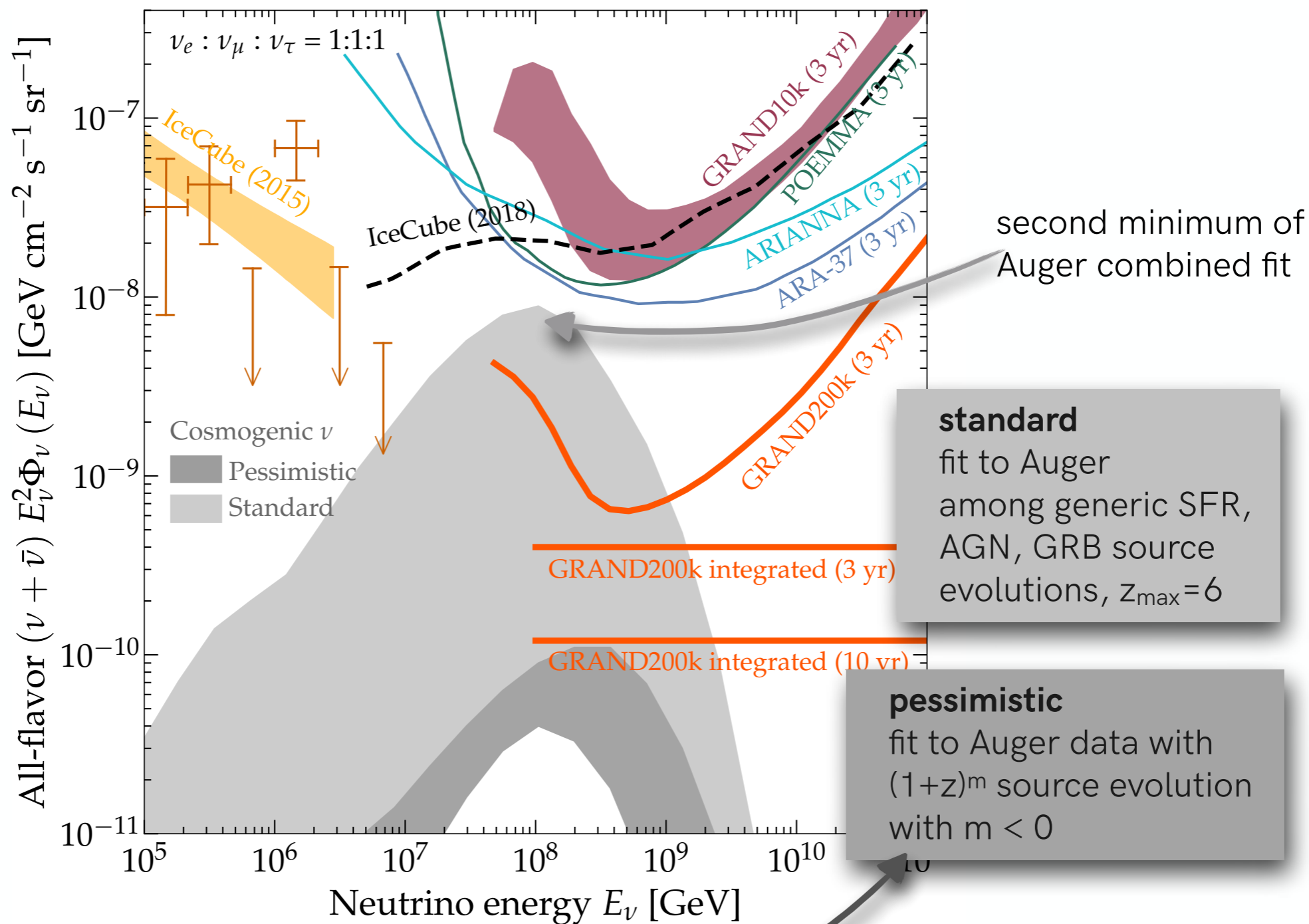
▶ depend strongly on observations of UHECRs

▶ less dependent but affects injection spectrum



Learning from secondary neutrinos?

Alves Batista, de Almeida, Lago, KK, 2018
 GRAND Science & Design, 2018
 KK, Allard, Olinto 2010
 Van Vliet et al. arXiv:1707.04511



second minimum of Auger combined fit

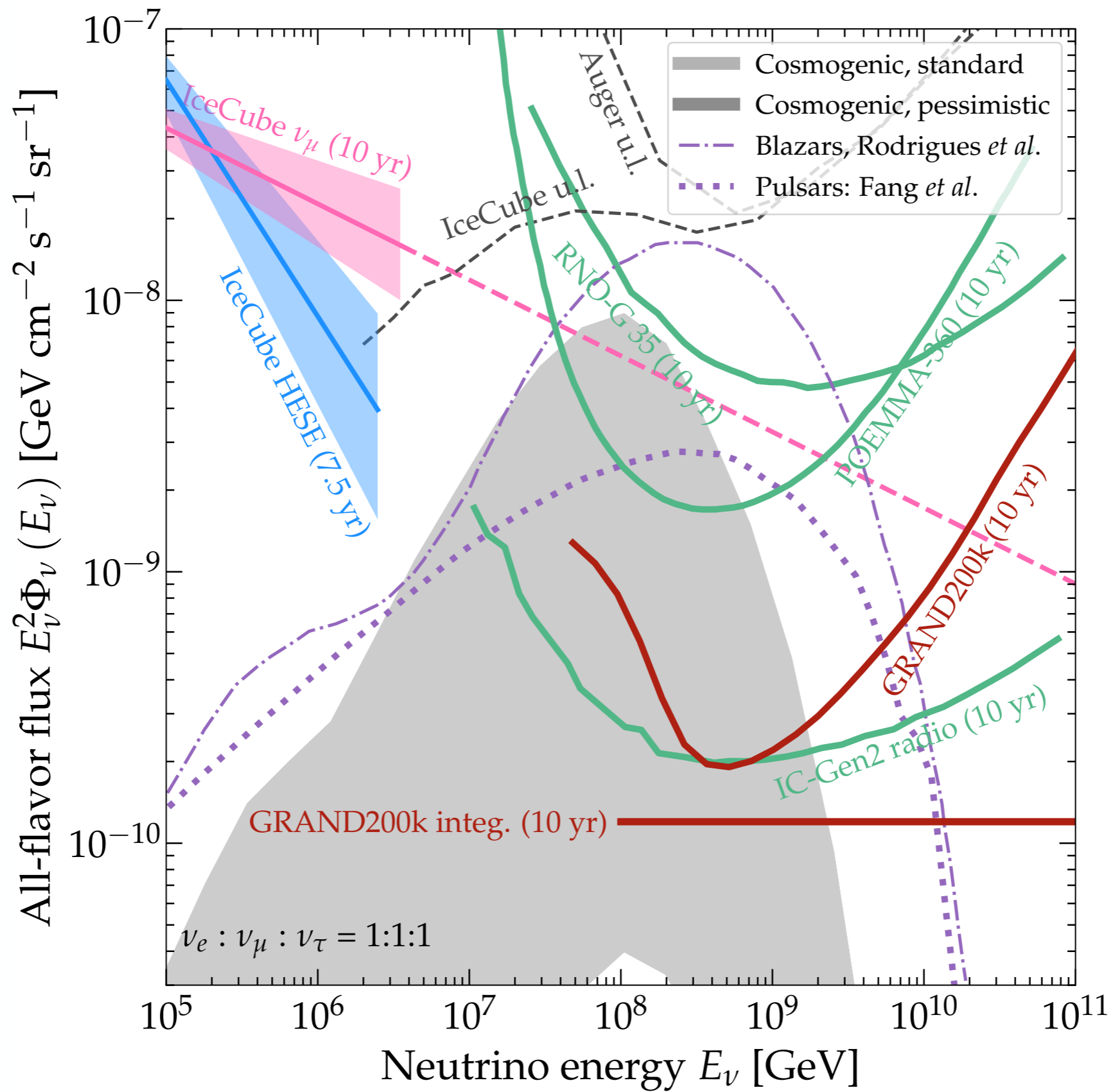
standard
 fit to Auger
 among generic SFR,
 AGN, GRB source
 evolutions, $z_{\max}=6$

pessimistic
 fit to Auger data with
 $(1+z)^m$ source evolution
 with $m < 0$

most pessimistic!

adding IGMF \rightarrow harder $\alpha \rightarrow$ increases neutrino flux
 alleviating simplifying assumption \rightarrow increases neutrino flux

Diffuse astrophysical & cosmogenic fluxes



courtesy M. Bustamante

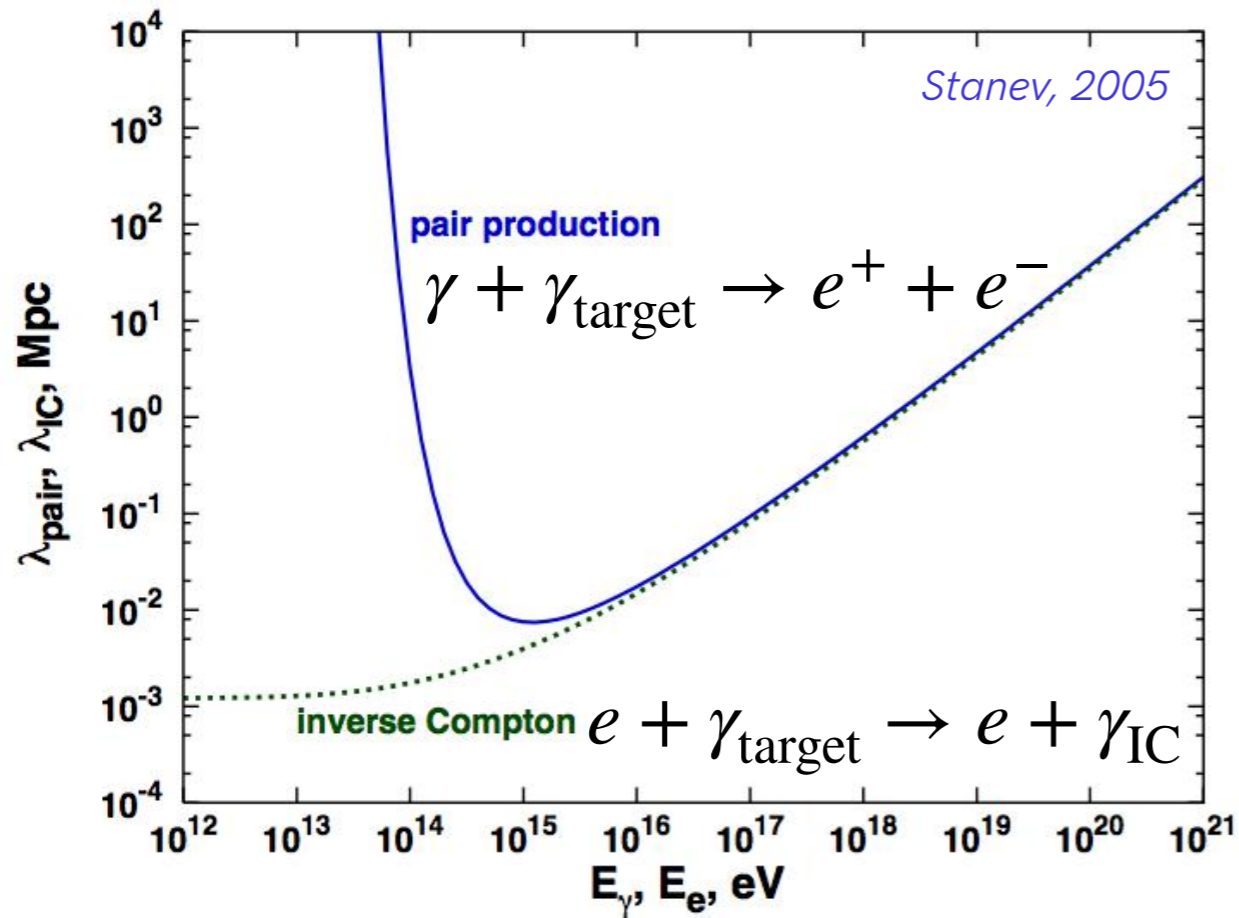
2. Tools for multi-messenger astrophysics

Specificities of gamma rays

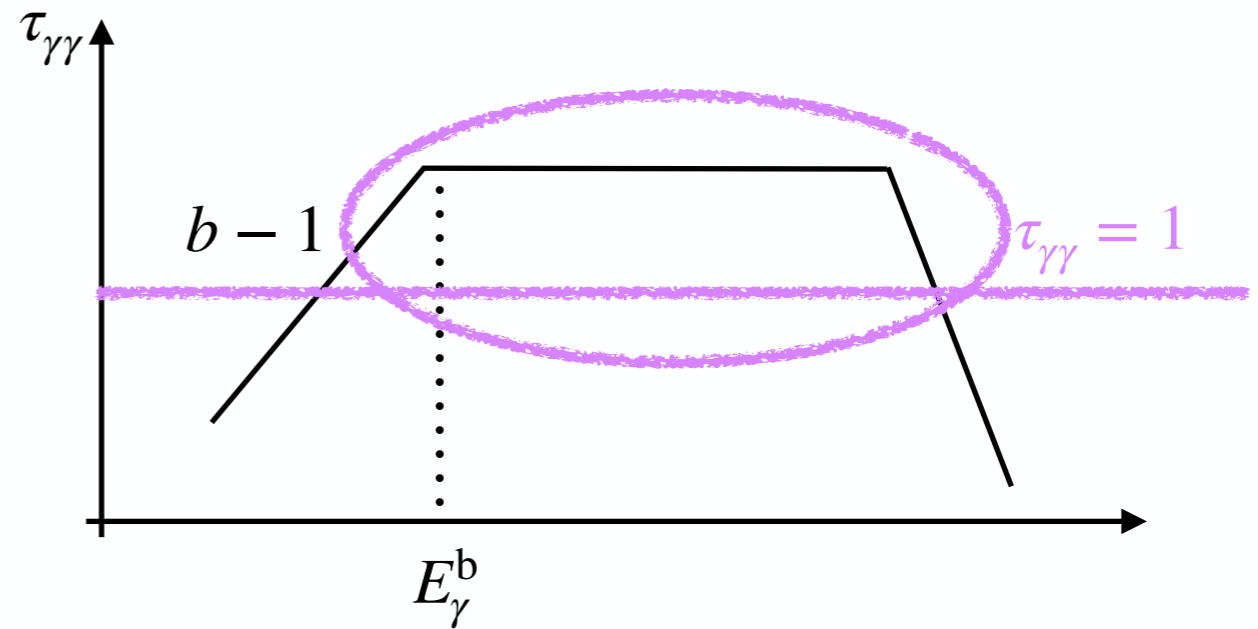
Gamma-ray cascades

$$p + \gamma_{\text{target}} \rightarrow \gamma, e^{\pm}, \dots$$

$$\gamma \rightarrow e \rightarrow \gamma \rightarrow e \dots$$



Gamma-ray attenuation at the source



these gamma rays cannot escape the source

pair production cross-section

$$\sigma_{\gamma\gamma}(s) = \frac{\pi r_e^2}{2} (1 - \beta_{\text{cm}}^2) \left[(3 - \beta_{\text{cm}}^4) \ln \left(\frac{1 + \beta_{\text{cm}}}{1 - \beta_{\text{cm}}} \right) - 2\beta_{\text{cm}} (2 - \beta_{\text{cm}}^2) \right]$$

gamma-ray absorption probability per unit length

$$\frac{d\tau_{\gamma\gamma}}{dx}(\epsilon_{\gamma}) = \frac{2}{\epsilon_{\gamma}^2} \int_{1/\epsilon_{\gamma}}^{\infty} \frac{d\epsilon}{\epsilon^2} \frac{dn_{\gamma}}{d\epsilon}(\epsilon) \int_1^{\epsilon\epsilon_{\gamma}} ds s \sigma_{\gamma\gamma}(s)$$

attenuation of intrinsic gamma-ray spectrum

$$\frac{dN}{dE}_{\text{observed}} = \frac{dN}{dE}_{\text{intrinsic}} \cdot e^{-\tau(E,z)}$$

Gamma-ray opacity $\tau_{\gamma\gamma}$ related to f_{mes}

$$\tau_{\gamma\gamma} \approx \frac{\eta_{\gamma\gamma} \sigma_{\gamma\gamma}}{\eta_{p\gamma} \hat{\sigma}_{p\gamma}} f_{\text{mes}}$$

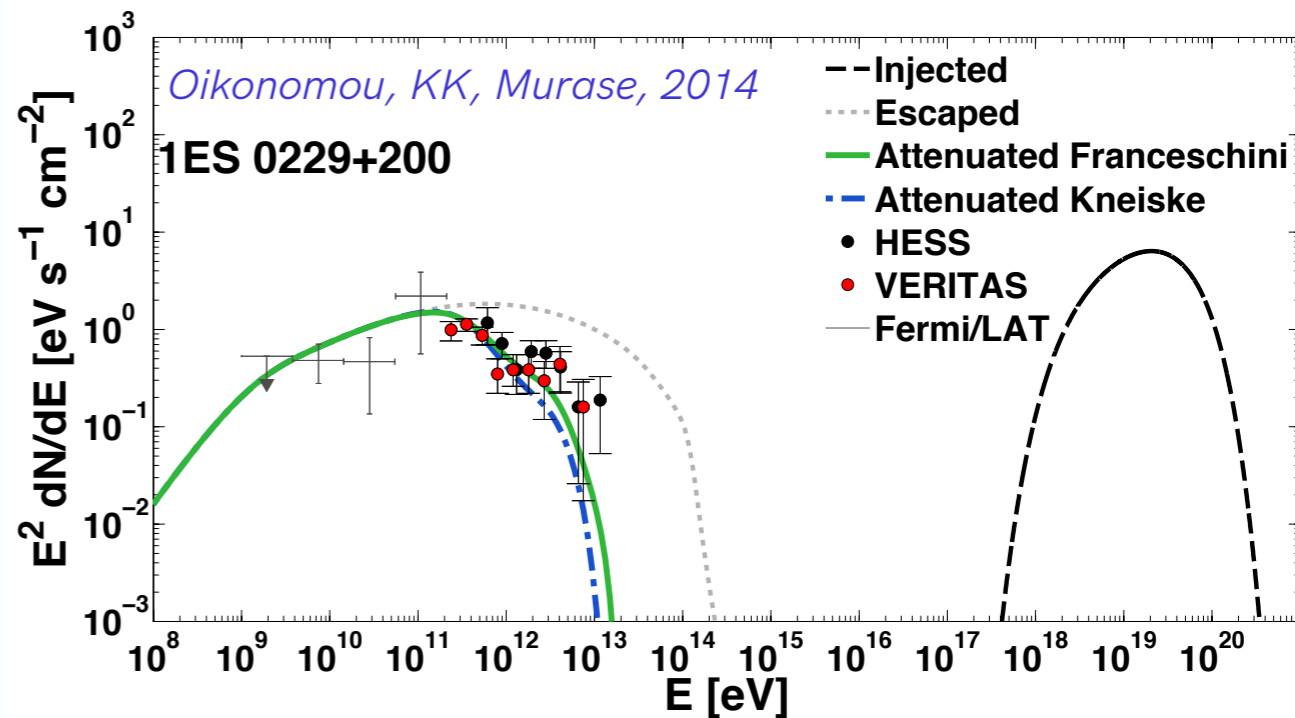
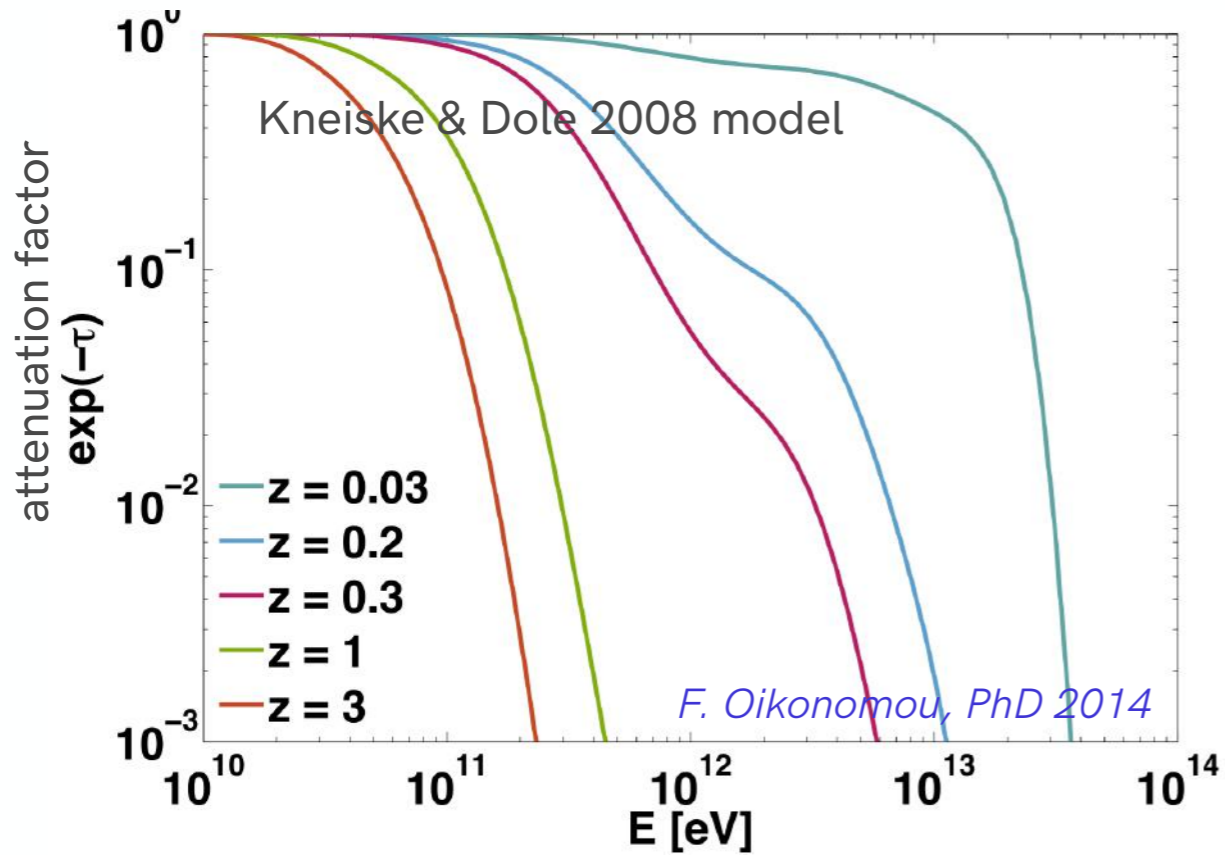
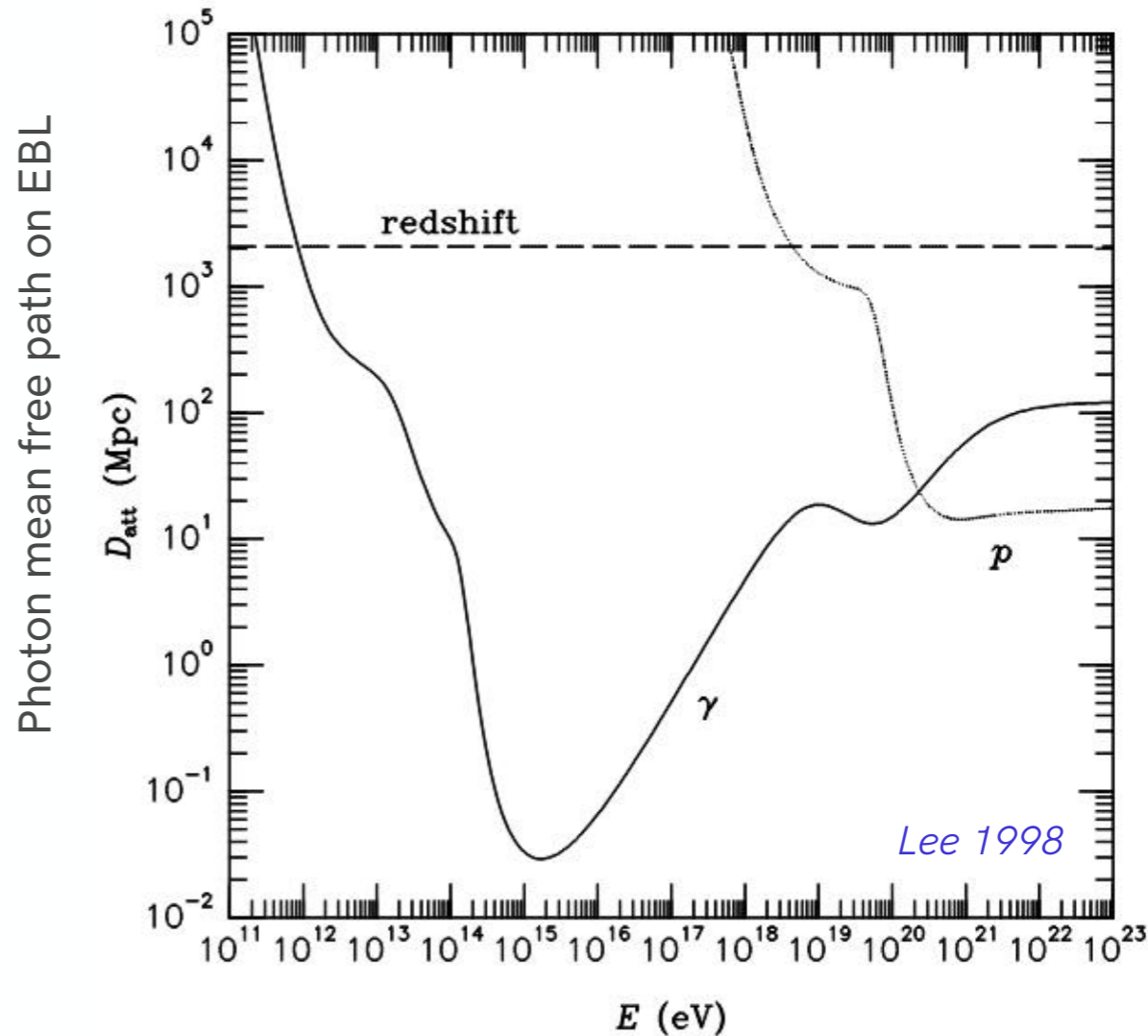
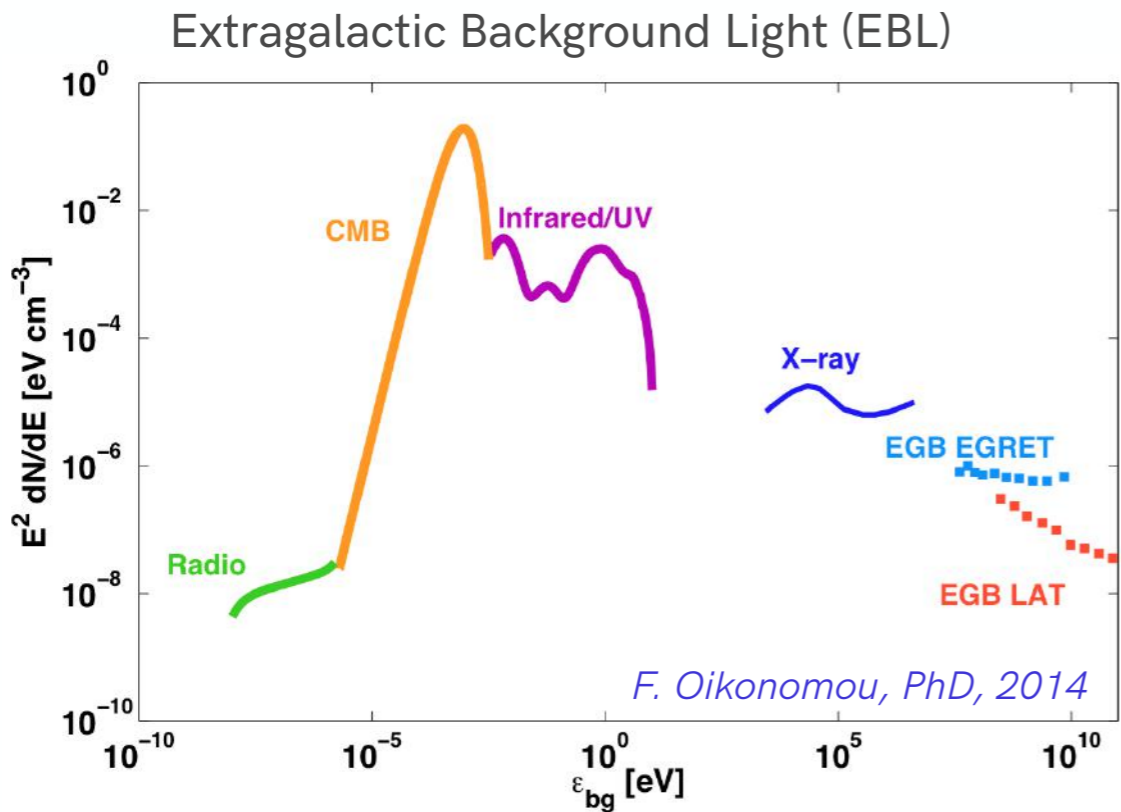
η factor depending on photon spectral slope

$$\sigma_{p\gamma} \kappa_{p\gamma}$$

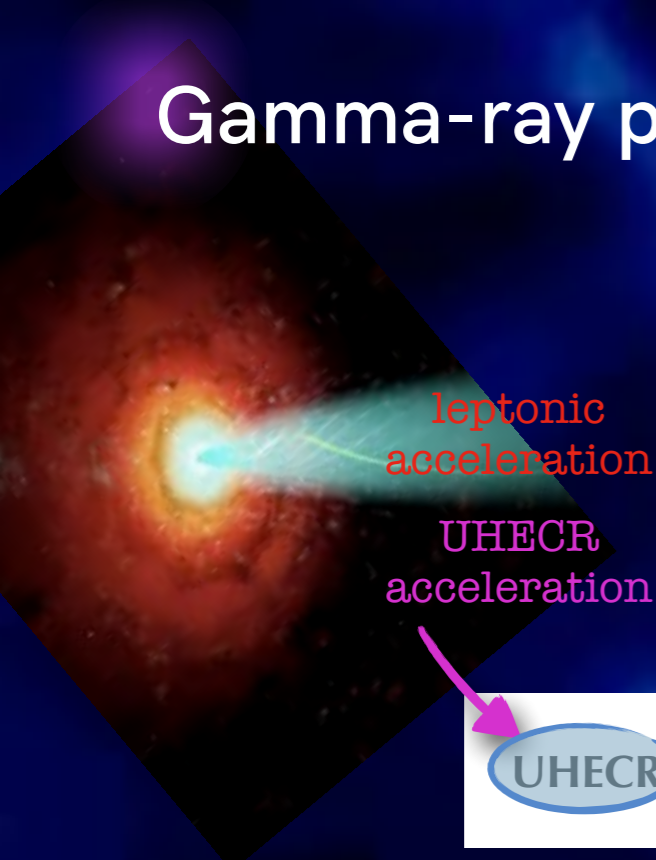
Murase et al., 2016

Gamma-ray cascades in the EBL

$$\frac{dN}{dE}_{\text{observed}} = \frac{dN}{dE}_{\text{intrinsic}} \cdot e^{-\tau(E,z)}$$



Gamma-ray propagation in the intergalactic medium

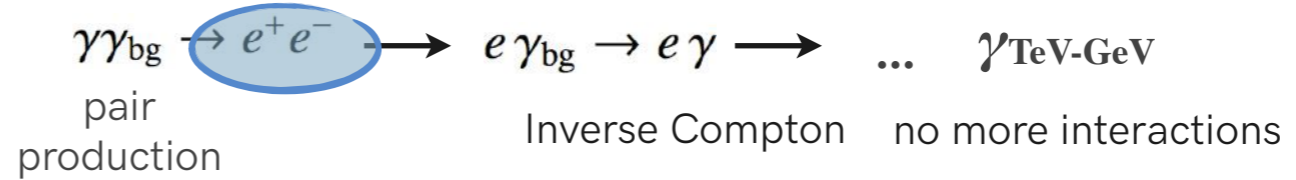


leptonic acceleration

UHECR acceleration

Cascade in IGM

e.g., Aharonian et al. 94,, 06, Coppi & Aharonian 97, Tavecchio et al. 11...



interactions with Extragalactic Background Light (EBL)



interactions with CMB/IR photons

Essey & Kusenko 10, 13, Essey et al. 10, 11, Murase et al. 12, Takami et al. 13

deflections
dilution of signal

Cosmic Magnetic fields

homogeneous B: flux completely diluted if $B_{\text{IGM}} > 3 \times 10^{-11} \text{G}$

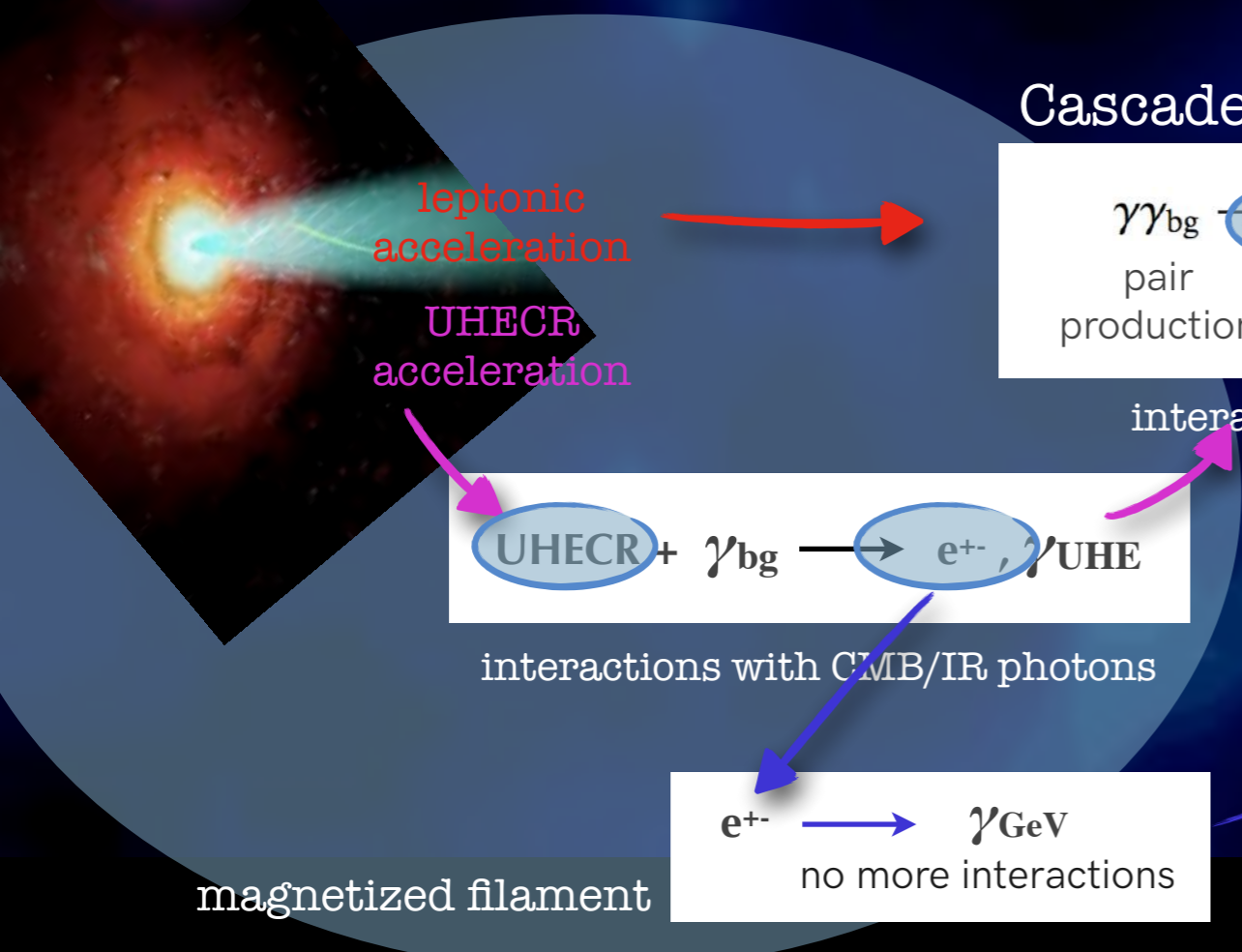
Protheroe 86, Protheroe & Stanev 93, Aharonian et al. 94

inhomogeneous B: flux dilution according to fraction of Universe where $B_{\text{IGM}} > 3 \times 10^{-11} \text{G}$

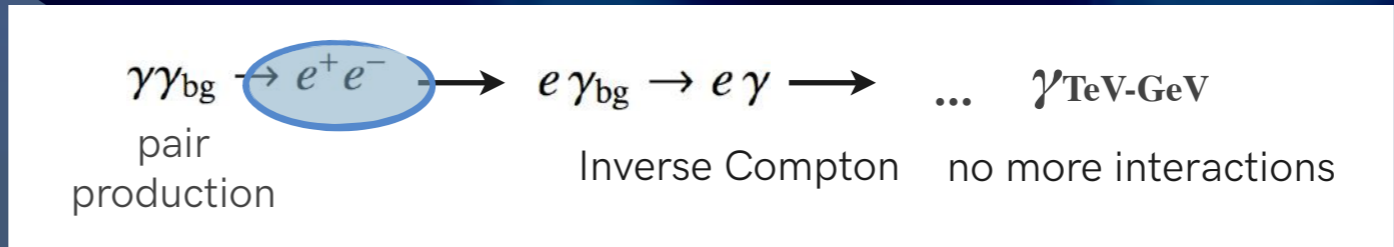
K.K., Allard & Lemoine 2010

$$E_\gamma^2 \frac{dN_\gamma}{dE_\gamma} \approx f_{\text{ld}}(< B_\theta) \frac{L_{\text{cr}}}{8\pi d^2} \left(\frac{E_\gamma}{E_{\gamma, \text{max}}} \right)^{1/2}$$

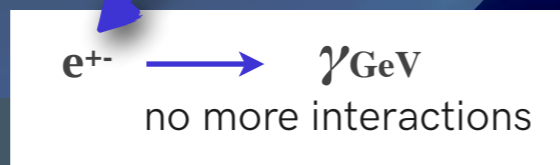
Gamma-ray propagation in the intergalactic medium



Cascade in IGM



interactions with Extragalactic Background Light (EBL)

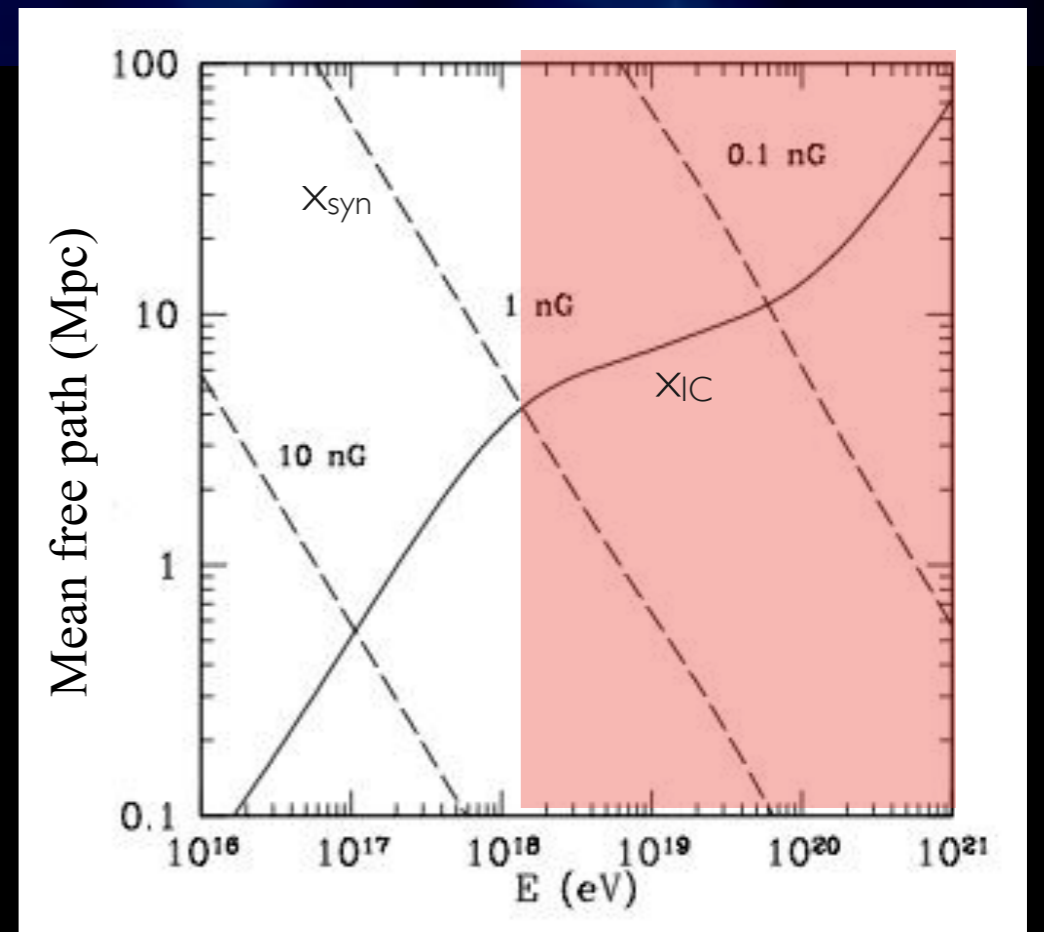


Synchrotron on B

NB: Confined UHECRs should produce UHE neutrals (e.g, photons) at source
(Murase 2009, Murase 2012, Dermer et al. 2012)

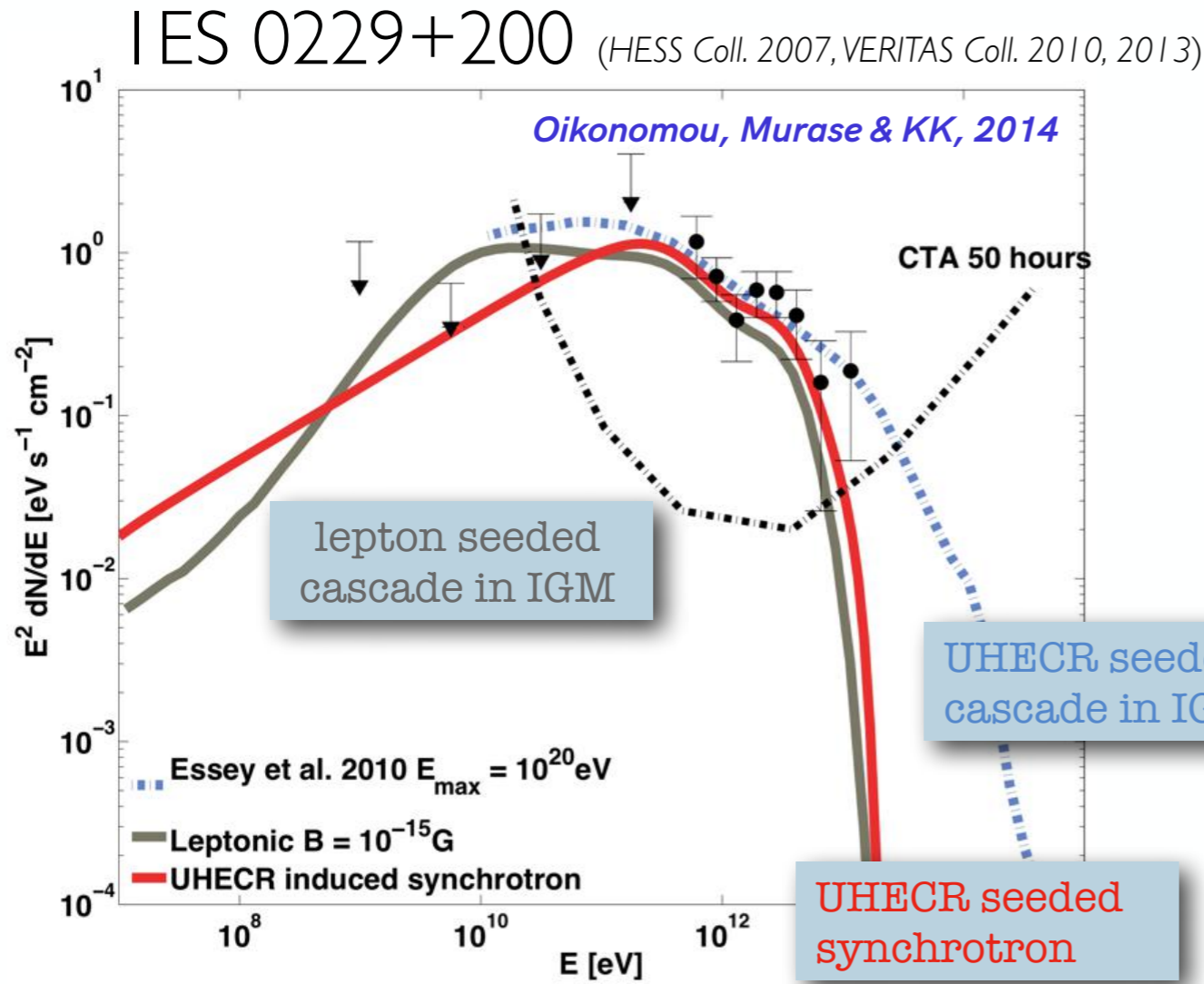
guaranteed if $\chi_{syn} > \chi_{IC}$

Gabici & Aharonian 06

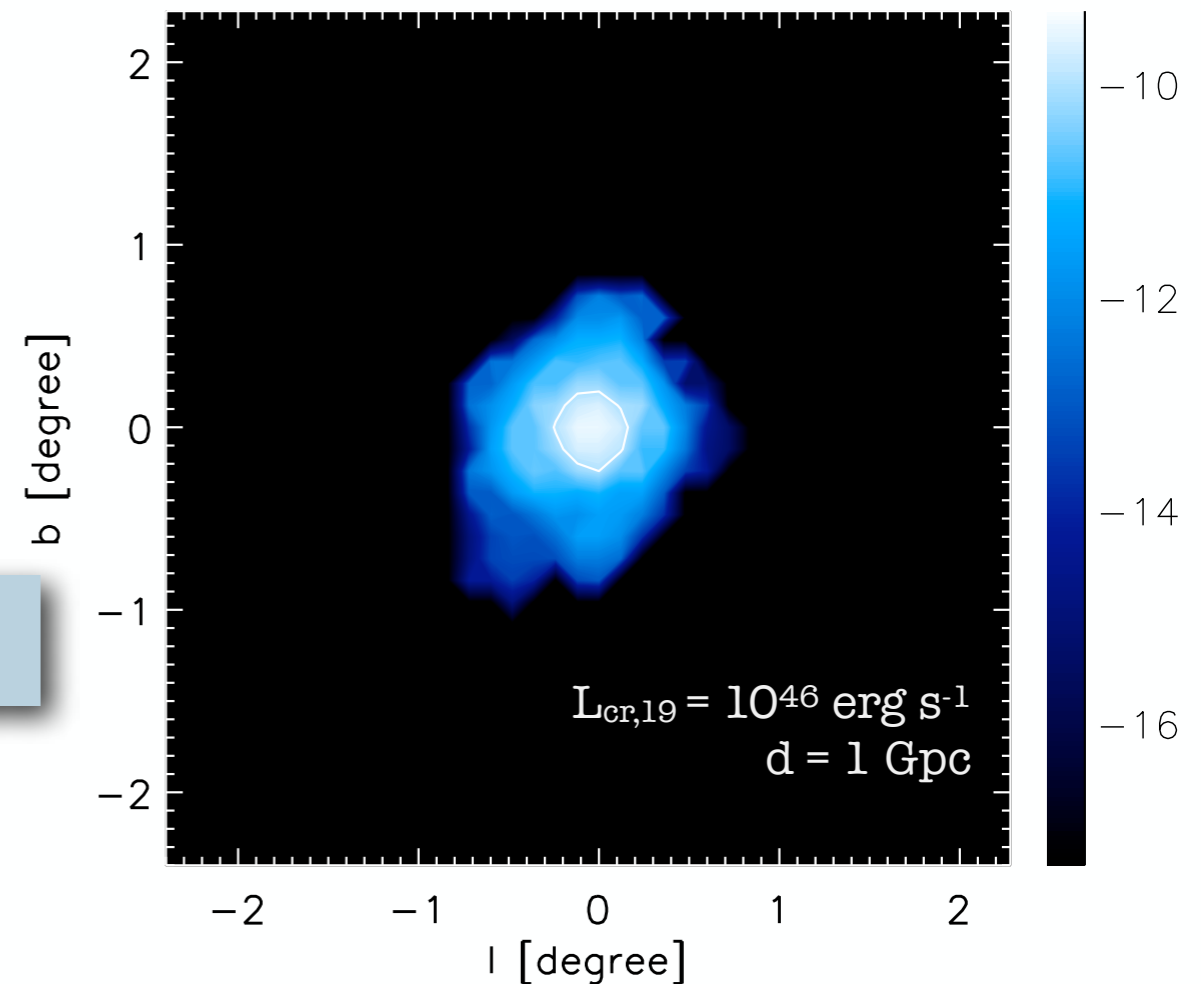


Learning from gamma rays: UHECR pair echoes/haloes

disentangling gamma-rays from leptons and cosmic rays



K.K., Allard & Lemoine 2010



Proton UHECRs
 $B_{3 \text{ Mpc}} = 316 \text{ nG}$
 Injection spectral index = 2 $E_{\text{MAX}} = 10^{21} \text{ eV}$
 $L_{\text{CR},j} = 10^{44.5} \text{ erg s}^{-1}$

also *Takami et al. 2013*

Fermi/CTA at 10 GeV:
 $\sim 10^{-10} \text{ GeV cm}^{-2} \text{ s}^{-1} (\theta_{\text{source}} / 1^\circ)$

spectra observation with CTA:
 disentangle UHECR cascade/leptonic
 but not UHECR synchrotron/leptonic



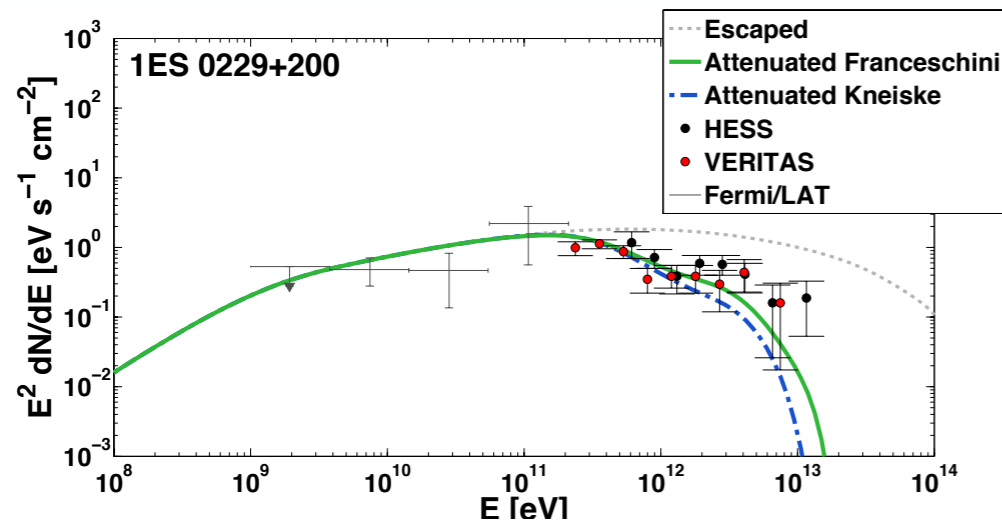
Synchrotron haloes around sources
 with strongly magnetized environ.
 for cosmic-ray scenarios

Pair echoes: time variabilities

$$\delta t \sim 2\theta_e^2 d / 2c \sim 0.3 \text{ yr } (E_{\text{syn}}/10^{2.5} \text{ GeV})(\min[d, \lambda_{\gamma\gamma}]/\text{Mpc})$$

deflection in B

$d = \text{magnetised region} \sim \text{few Mpc}, \lambda_{\gamma\gamma} \sim 2 \text{ Mpc}$



UHE photons

Injection spectral index = 1.5

$B_{3 \text{ Mpc}} = 316 \text{ nG}$

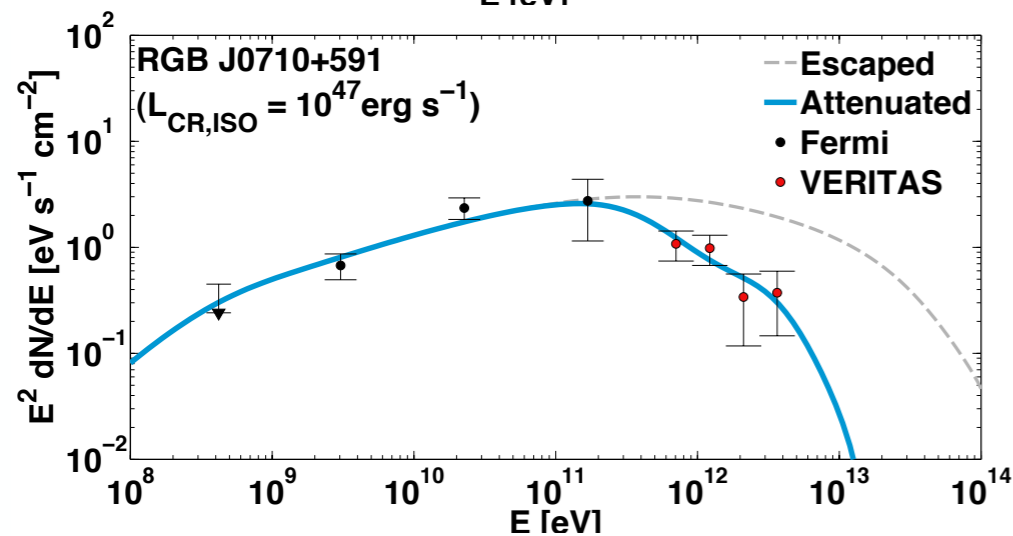
$E_{\gamma, \text{MAX}} = 10^{19.5} \text{ eV}$

$L_{\gamma} = 10^{45} \text{ erg s}^{-1}$

~ year? *Aliu et al 2014*

If confirmed:

- disfavors UHECR synchrotron cascade
- rules out UHECR IC cascade



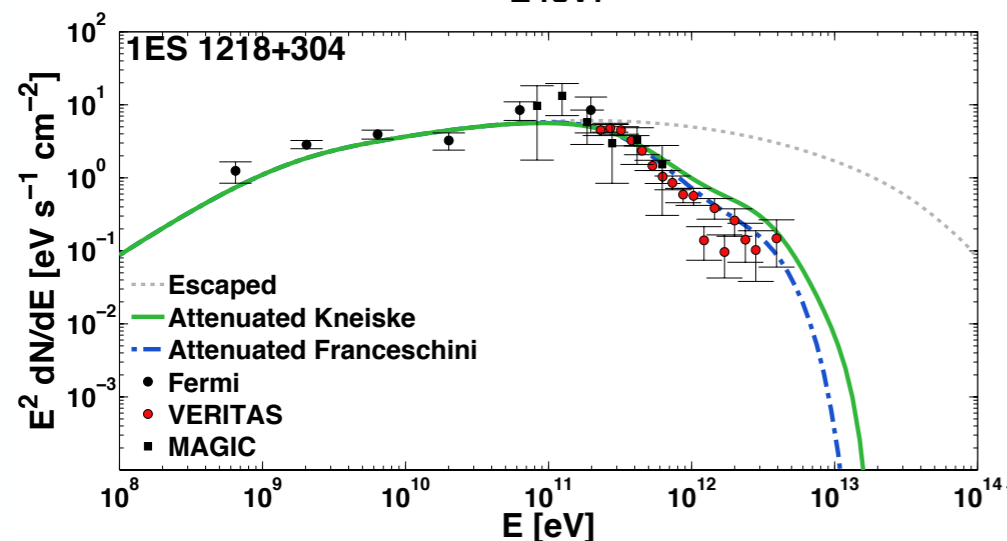
UHE protons

$B_{3 \text{ Mpc}} = 100 \text{ nG}$

Injection spectral index = 2

$E_{\text{MAX}} = 10^{20.5} \text{ eV}$

None



UHE photons

Injection spectral index = 1.5

$B_{3 \text{ Mpc}} = 100 \text{ nG}$

$E_{\gamma, \text{MAX}} = 10^{19.5} \text{ eV}$

$L_{\gamma} = 8 \times 10^{45} \text{ erg s}^{-1}$

~ day *Acciari et al 2010*

UHE neutrals could account for ~ day variability if emission region < pc size
detailed modeling needed

2. Tools for multi-messenger astrophysics

**Very quick
panorama of simulation tools**

Some public propagation and interaction codes

Cosmic-ray interstellar & intergalactic propagation tools

GALPROP
DRAGON
PICARD

propagation of cosmic ray densities at high energies treated by solving transport equations

...

CRPropa
SimProp

at UHE: numerical integration of the equation of motion of single particles
CRPropa: unify HE+UHE

...

Interaction codes/tables

SOPHIA

$p\gamma$

TALYS

$N\gamma$

EPOS/SIBYLL

hadronic

...

Gamma-ray cascades

CRPropa
ELMAG

...

Radiation from accelerated leptons & hadrons

AM3, ATHEvA, B13, LeHaParis...

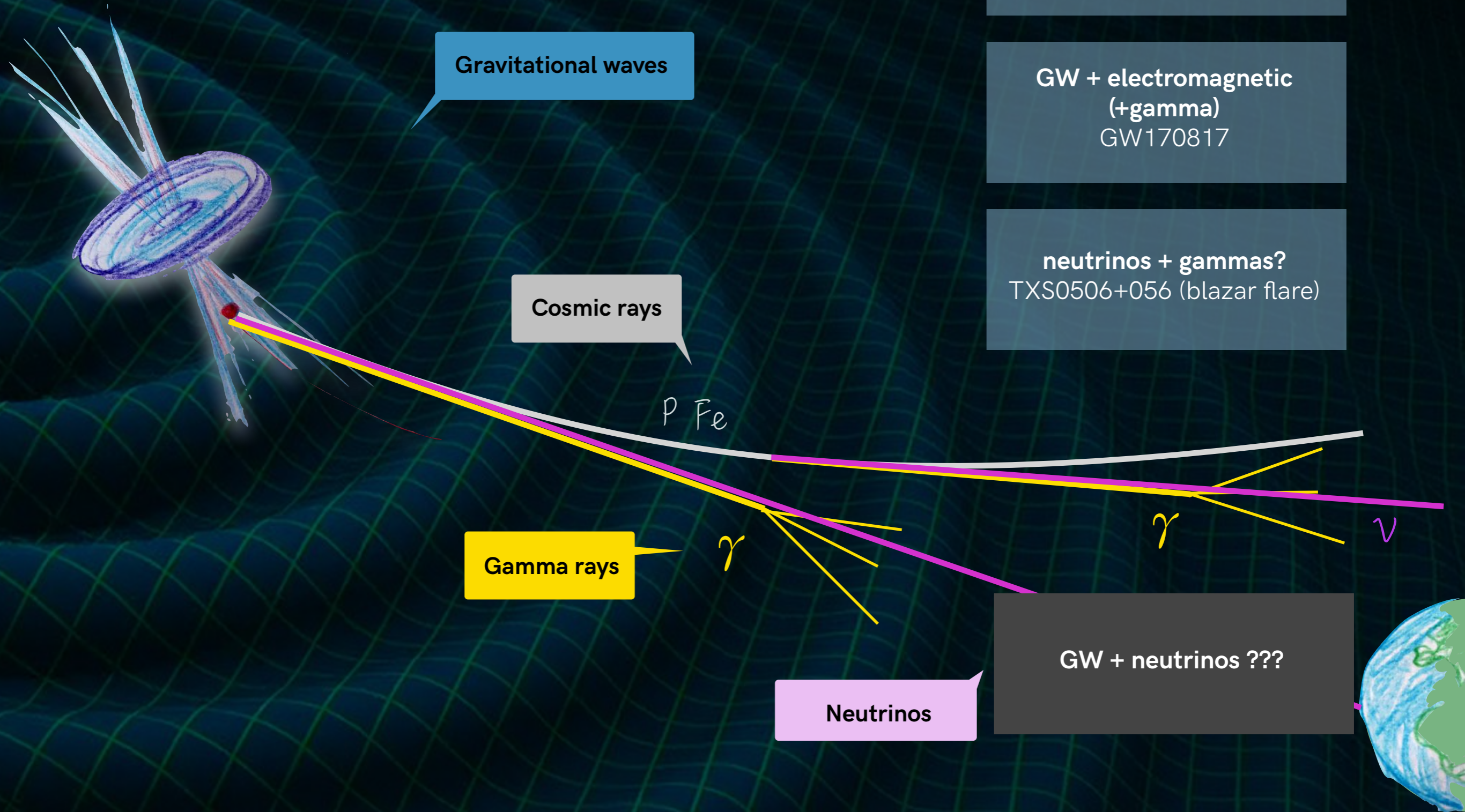
Challenges

- treatment of different scales (including microscopic & MHD processes)
- time-dependencies
- self-consistency (radiation production & impact)

3. Can we really do multi-messenger astrophysics?

GW-neutrino sources

Multi-messengers?



Gravitational waves

Cosmic rays

Gamma rays

Neutrinos

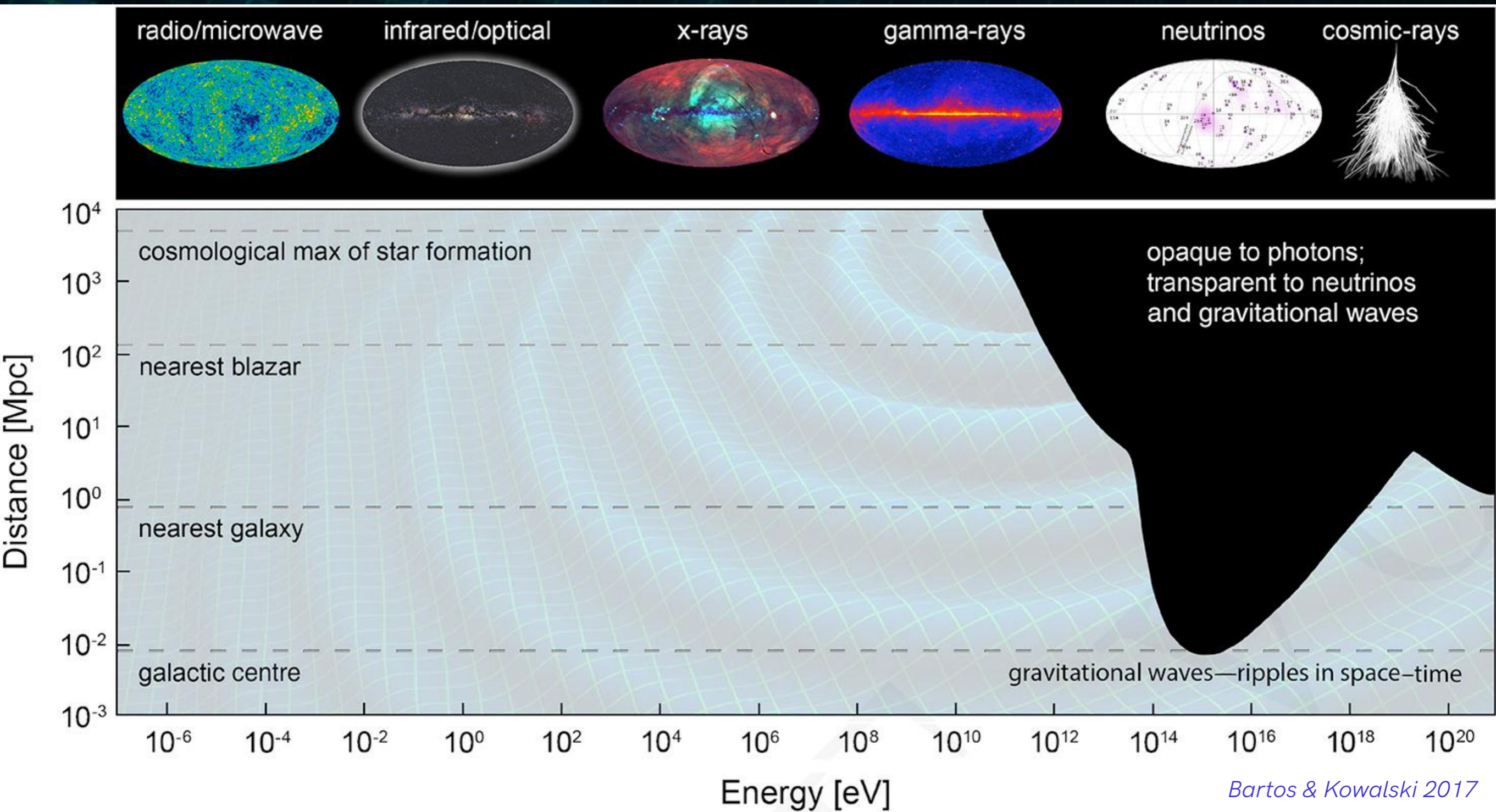
cosmic rays + others
—> temporal coincidence
impossible (deflections)
but studies of diffuse fluxes

GW + electromagnetic
(+gamma)
GW170817

neutrinos + gammas?
TXS0506+056 (blazar flare)

GW + neutrinos ???

Multi-messengers?



Possible gravitational wave sources

Murase & Bartos 2019
Guépin & KK 2017

e.g., Kimura et al. 2017, 2018
Biehl et al. 2018
Decoene, Guépin, Fang, KK,
Metzger, 2020
Ahlers & Halser 2020



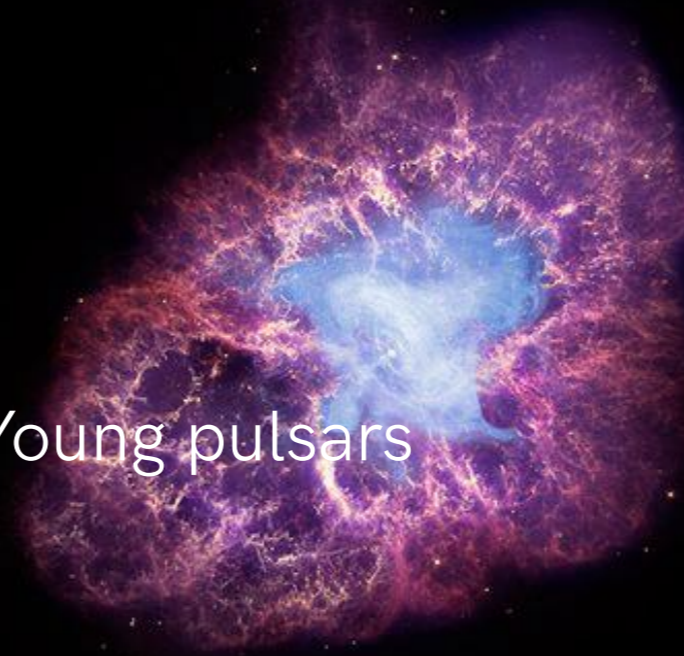
Neutron star
mergers

Fang & Metzger 2018

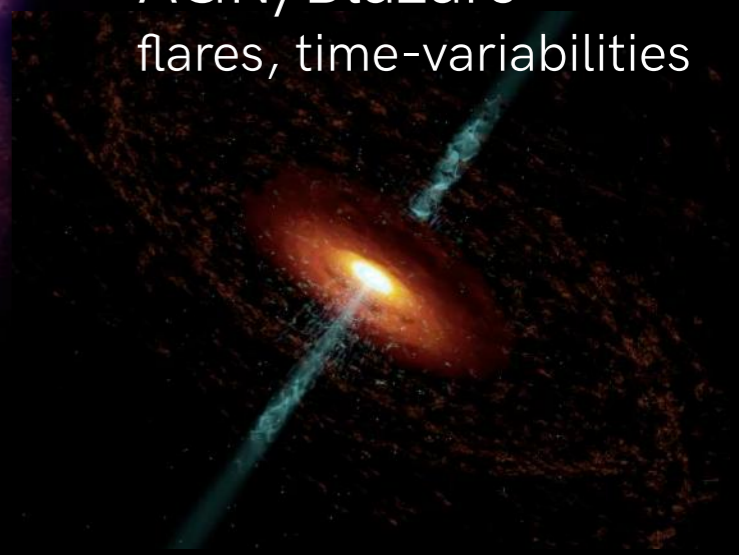


Magnetars
(AXP/SGR)

Young pulsars



AGN/Blazars
flares, time-variabilities



KK & Silk 2016
De Wasseige et al. 2019
Shi & Yuan 2020



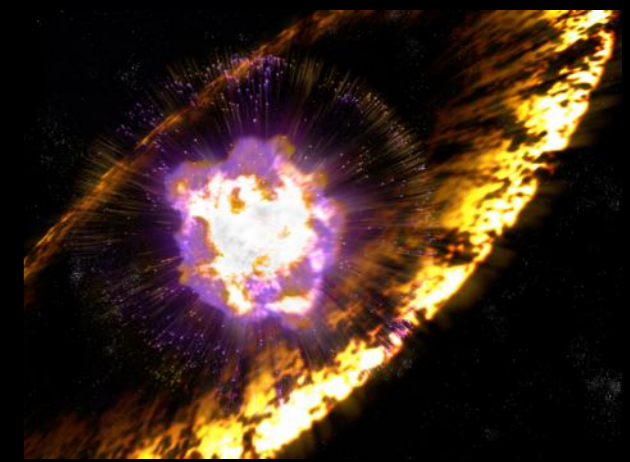
BH-BH and BH-
NS mergers



Long
Gamma Ray
Bursts



Tidal disruption
events



Superluminous
Supernovae

Black hole mergers as sources of UHECRs

KK & Silk 2016

- ▶ accretion to source BZ long enough,
- ▶ disk to anchor fields and do $\alpha\omega$ -dynamo to generate strong magnetic field



$$E_{\text{UHECR}} \gtrsim 3.2 \times 10^{53} \text{ erg} \left(\frac{\rho_0}{1 \text{ Gpc}^{-3} \text{ yr}^{-1}} \right)^{-1}$$

learnt from GW150914

- ▶ comfortable energetics:
 - ▶ $E_{\text{GW}} = 3.0 + 0.5 M_{\text{sun}} c^2 \sim 5.4 \times 10^{54} \text{ erg}$ per source
 - ▶ population rate $\rho_{\text{BH}} \sim 2 - 400 \text{ Gpc}^{-3} \text{ yr}^{-1}$
 - ▶ **efficiency** $< 3\%$ required in UHECRs per event per unit of GW energy release
- ▶ heavy composition possible:
 - ▶ iron-enriched residual debris around merging BHs

- ▶ luminosity extracted via Blandford-Znajek mechanism

$$L_{\text{BZ}} = \frac{(GM)^3 B^2}{c^5 R} \sim 3.2 \times 10^{46} \text{ erg s}^{-1} M_{100}^3 B_{11}^2 \frac{R_S}{R}$$

$$R_S = 2GM/c^2 \sim 3.0 \times 10^7 M_{100} \text{ cm}$$

- ▶ magnetic field strength via $\alpha\omega$ -dynamo

$$B \sim 10^{12} \text{ G} (P/300 \text{ ms})^{-1}$$

- ▶ luminosity has to last for 7 hours to 2 months to reach E_{UHECR}

- ▶ BZ timescale (as long as BH accretes after merger - sourced by debris)

$$t_{\text{BZ}} = Mc^2/L_{\text{BZ}} \sim 22 M_{100} B_{11}^{-2} (R_S/R)^2 \text{ yr}$$

High-energy neutrinos from binary neutron-star mergers

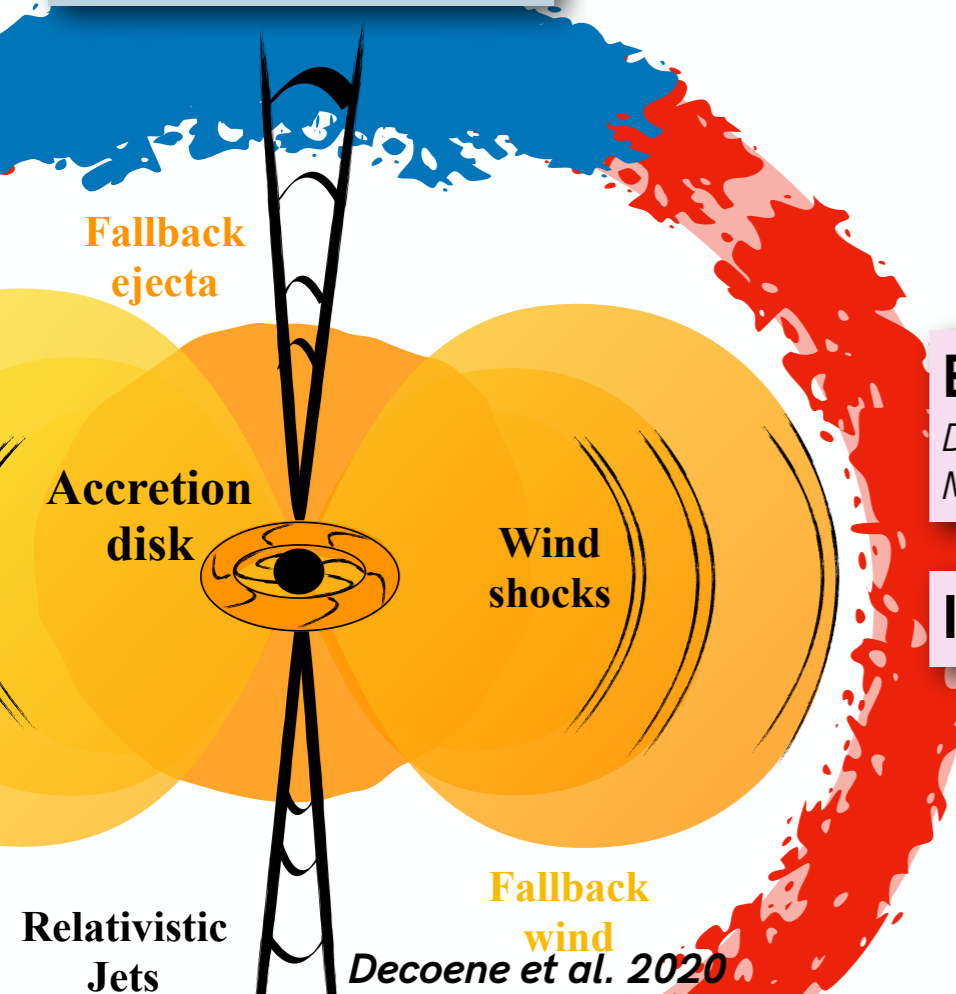
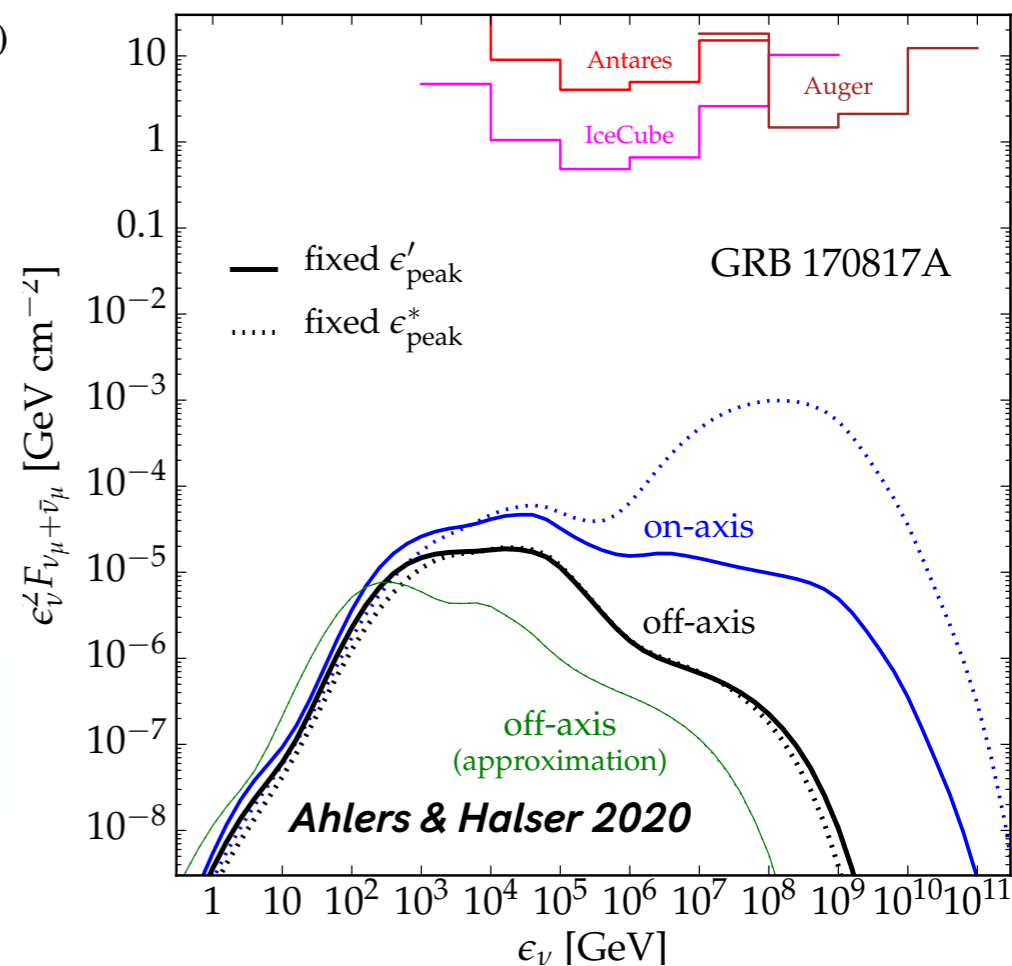
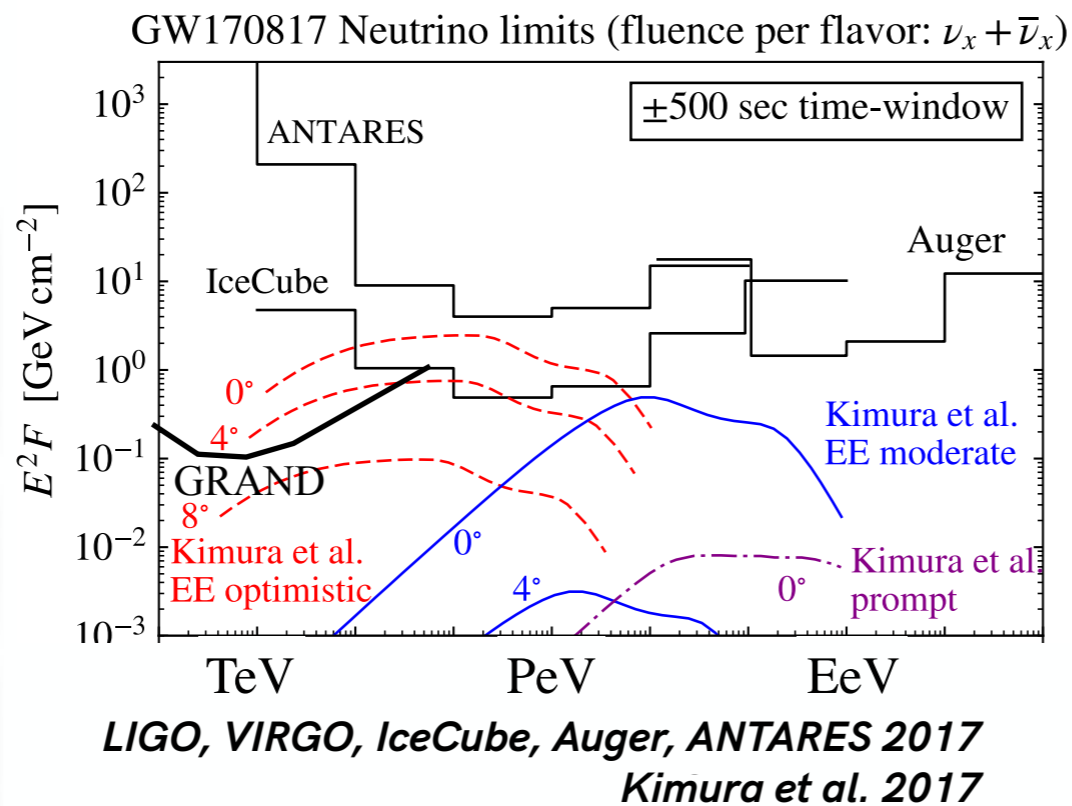
Successful jet

Kimura et al. 2017
Biehl et al. 2018
Ahlers & Halser 2020

Choked jet

Kimura et al. 2018

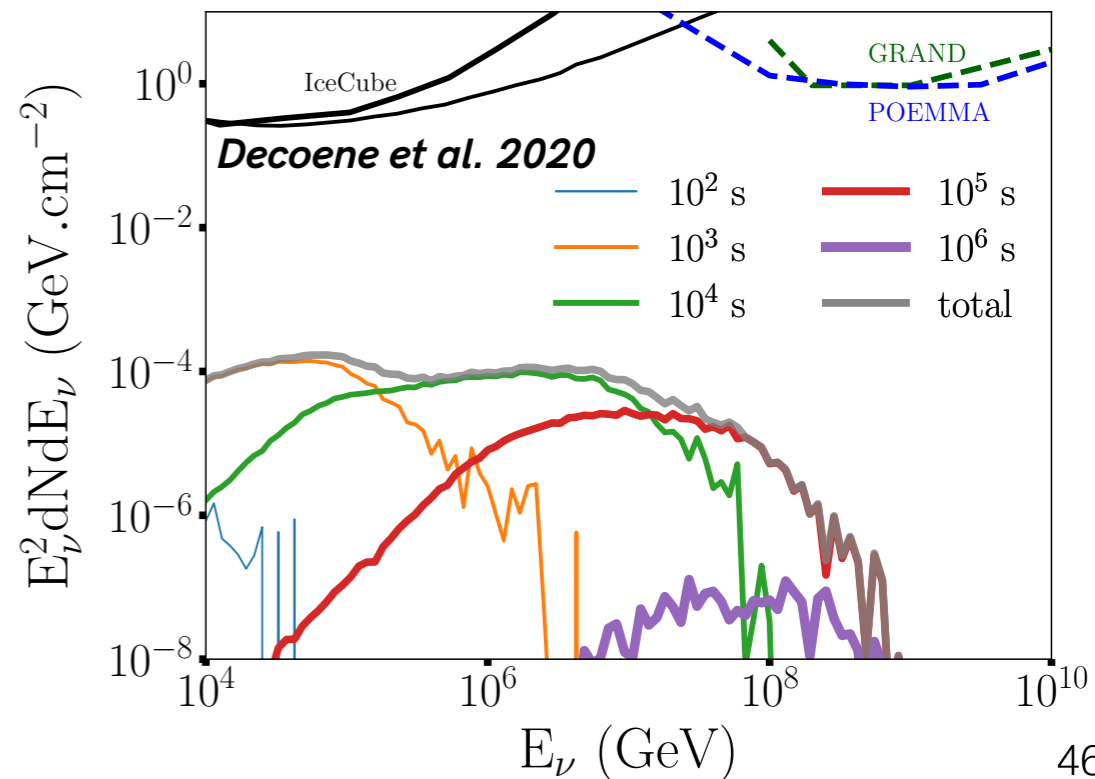
Beamed and intense emission



Equatorial emission

Decoene, Guépin, Fang, KK, Metzger, 2020

Isotropic emission



BNS: coincident detection with **gravitational waves**

Choked jet

Kimura et al. 2018

Optimistic model:
Coincident detection possible already with IceCube

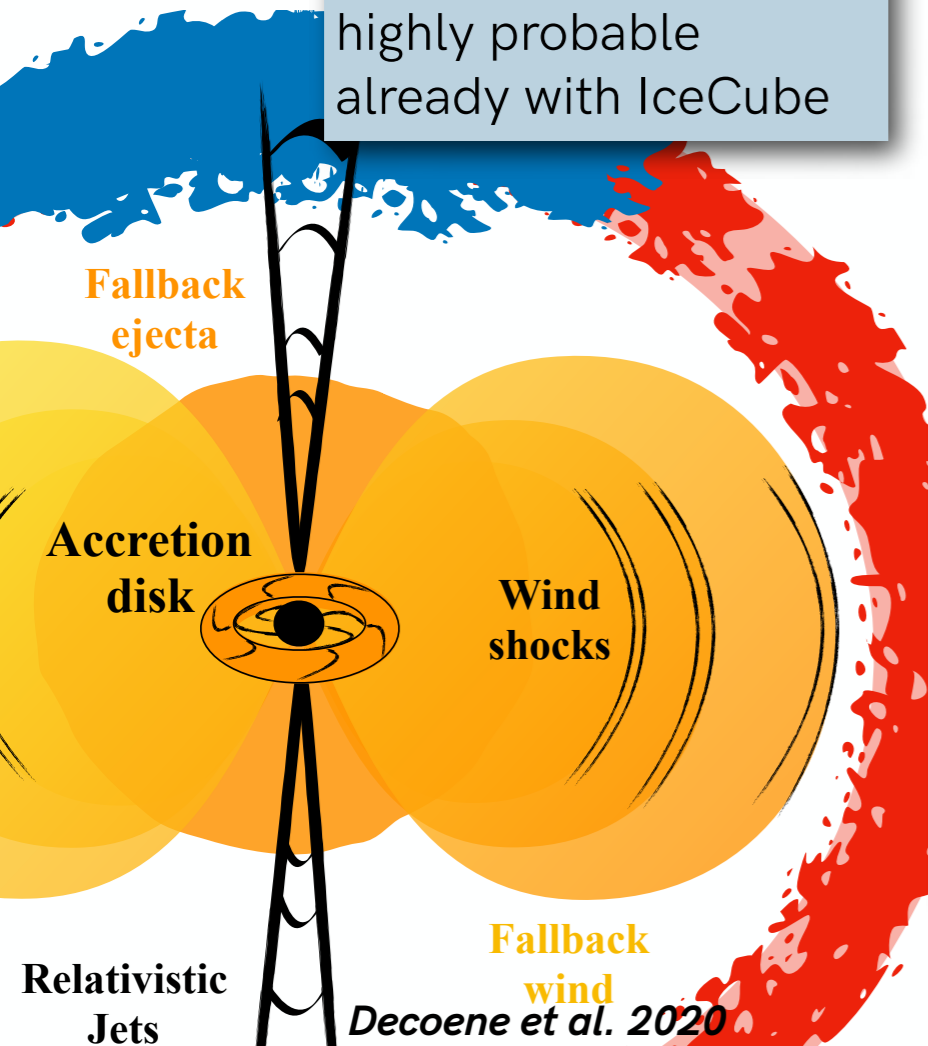
GW+neutrino detection rate [yr^{-1}]		
model	IceCube (up+hor+down)	Gen2 (up+hor)
A optimistic	0.38	1.2
B moderate	0.024	0.091

Successful jet

Kimura et al. 2017

Optimistic model:
Coincident detection highly probable already with IceCube

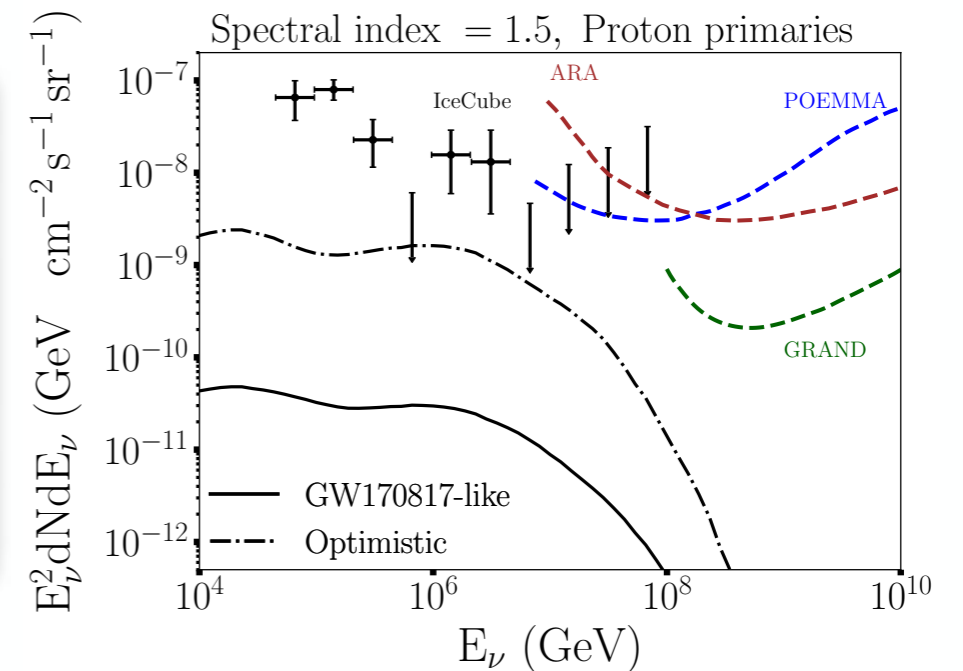
NS-NS ($\Delta T = 10 \text{ yr}$)	IC (all)	Gen2 (all)
EE-mod-dist-A	0.11 – 0.25	0.37 – 0.69
EE-mod-dist-B	0.16 – 0.35	0.44 – 0.77
EE-opt-dist-A	0.76 – 0.97	0.98 – 1.00
EE-opt-dist-B	0.65 – 0.93	0.93 – 1.00



Equatorial emission

Decoene, Guépin, Fang, KK, Metzger, 2020

Optimistic model:
10% of IceCube diffuse flux
Interesting for stacking and cross-correlation searches

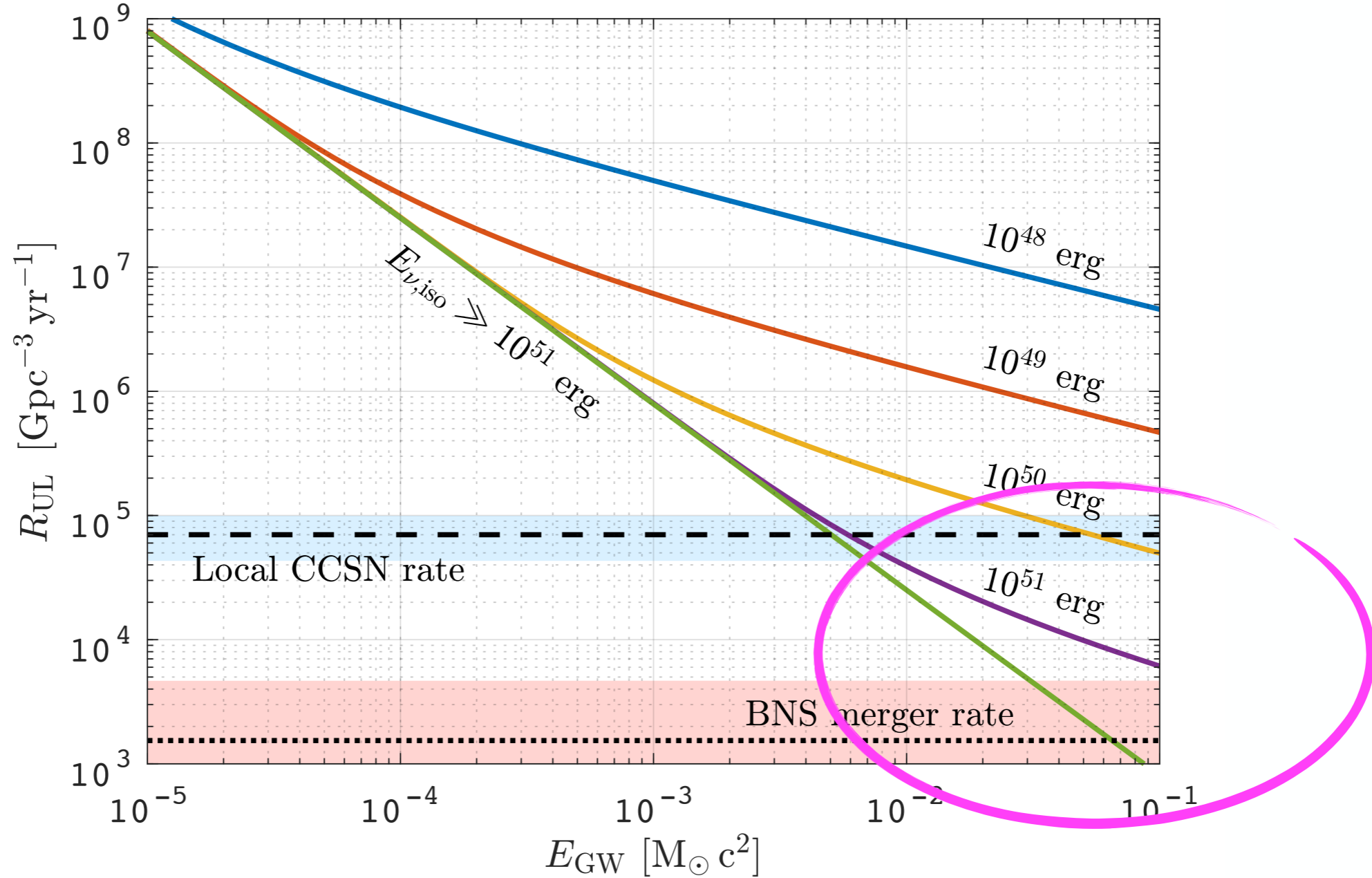


Population constraints from GW+neutrino non-detection

Advanced LIGO

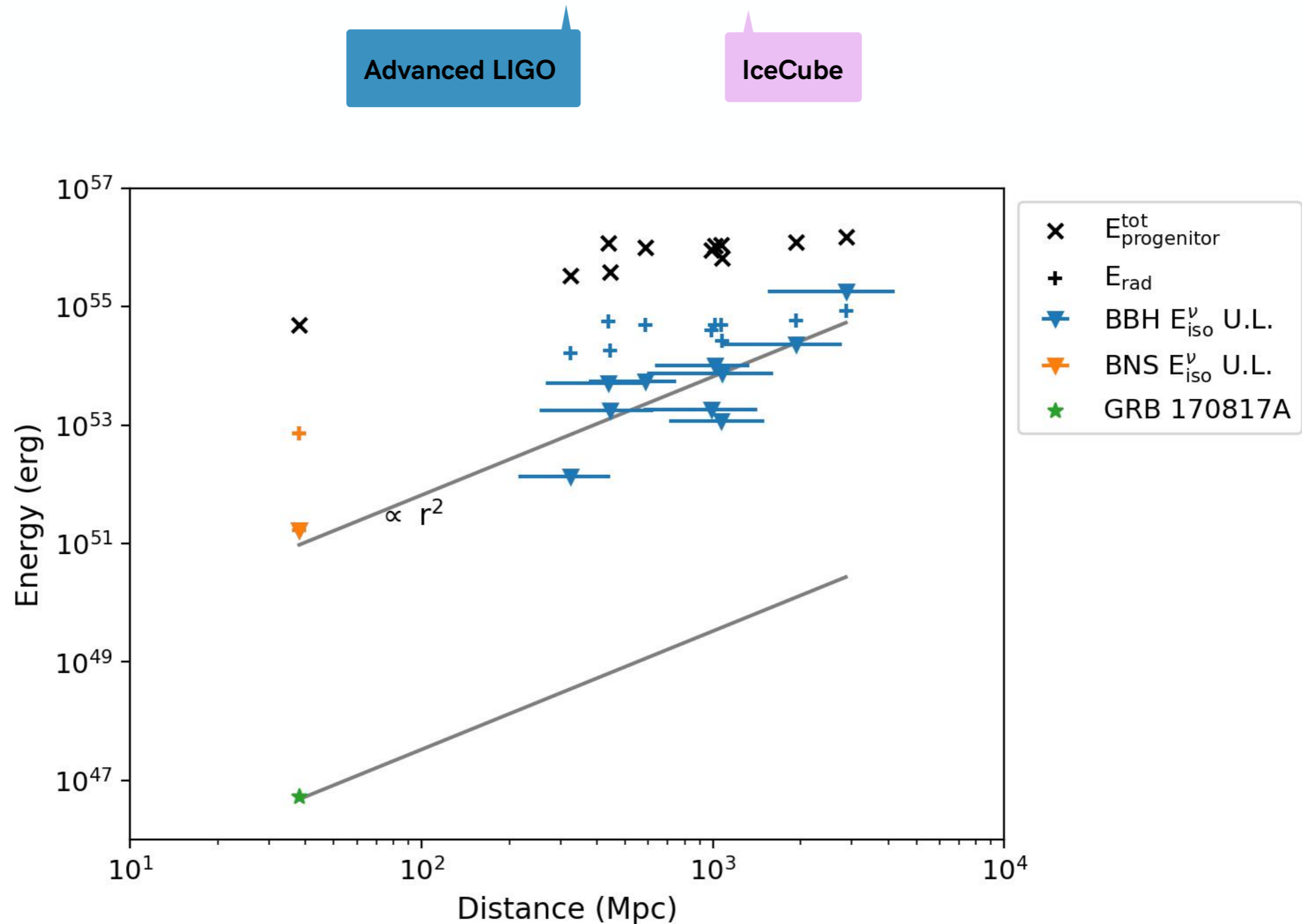
IceCube+ANTARES

Upper limits on rate density of GW+neutrino sources



Albert et al. 2019 ApJ 870 134

Population constraints from GW+neutrino non-detection



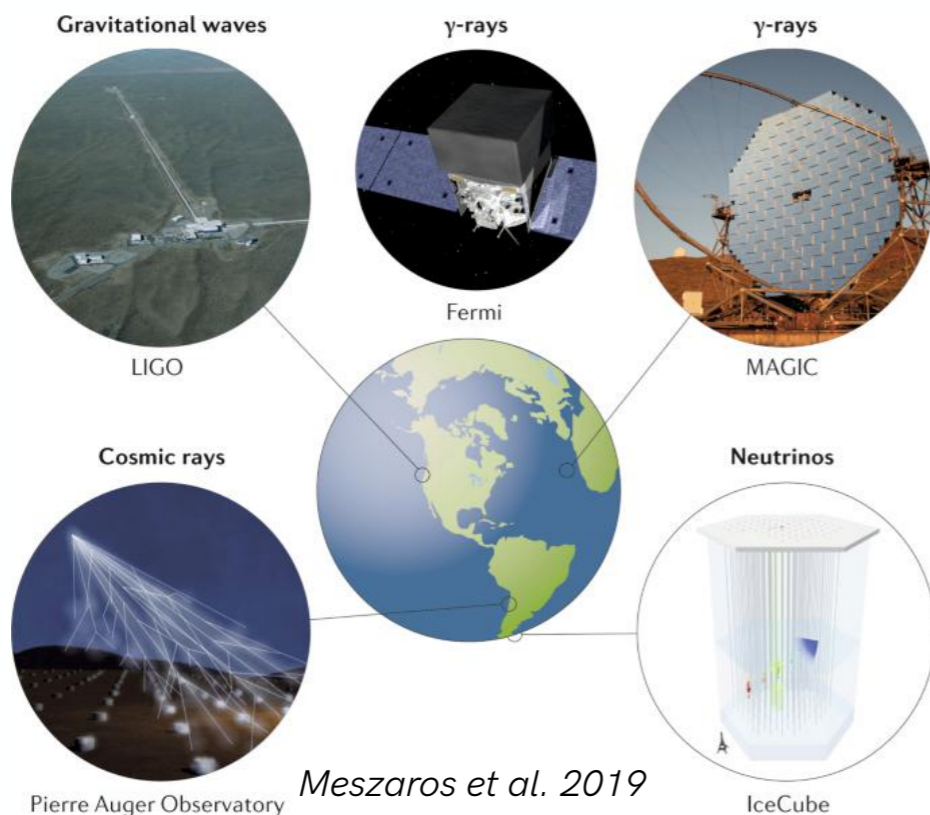
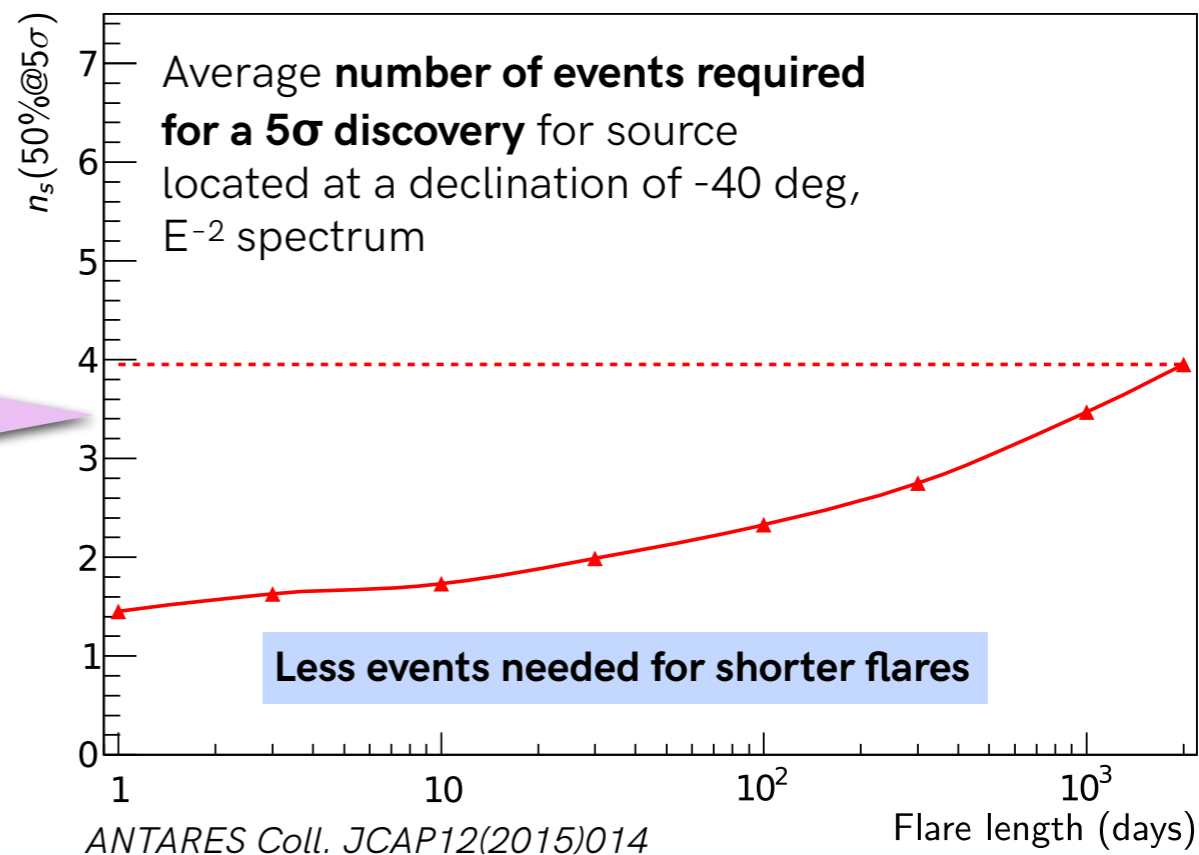
No significant neutrino coincidence is seen by either search during the first two observing runs of the LIGO-Virgo detectors. Upper limits on the time-integrated neutrino emission within the 1000 second window for each of the 11 GW events.

3. Can we really do multi-messenger astrophysics?

Focus on neutrinos from transients sources

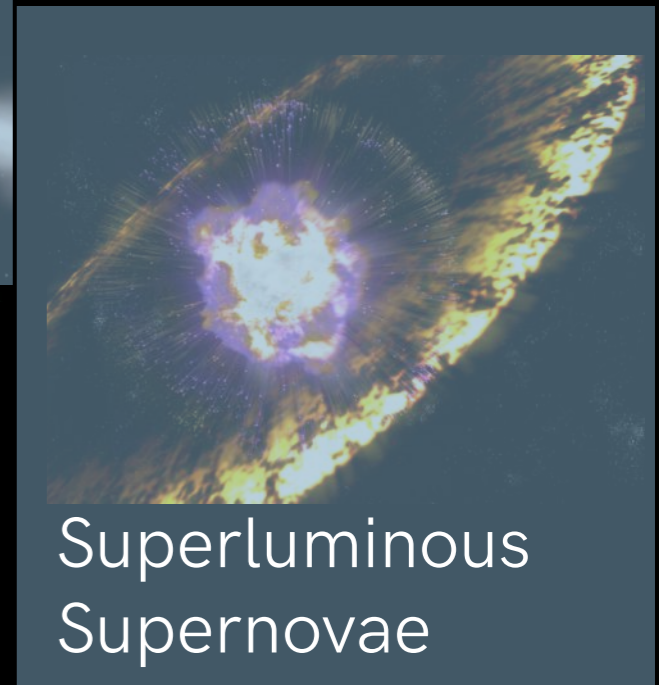
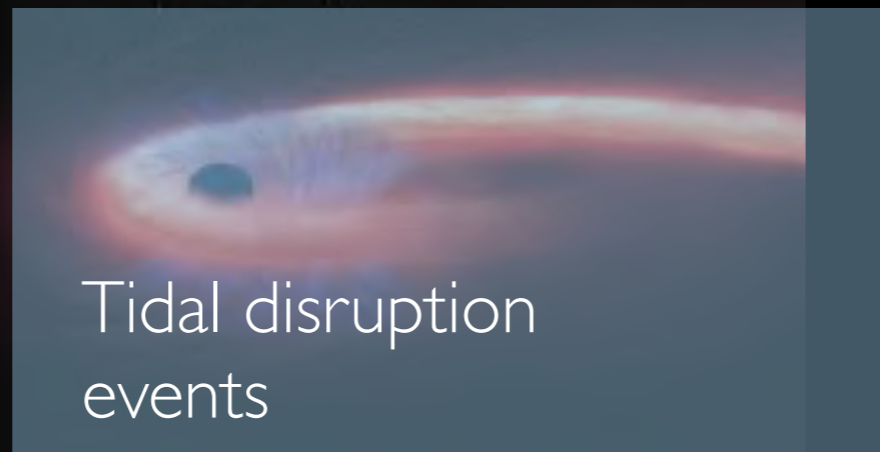
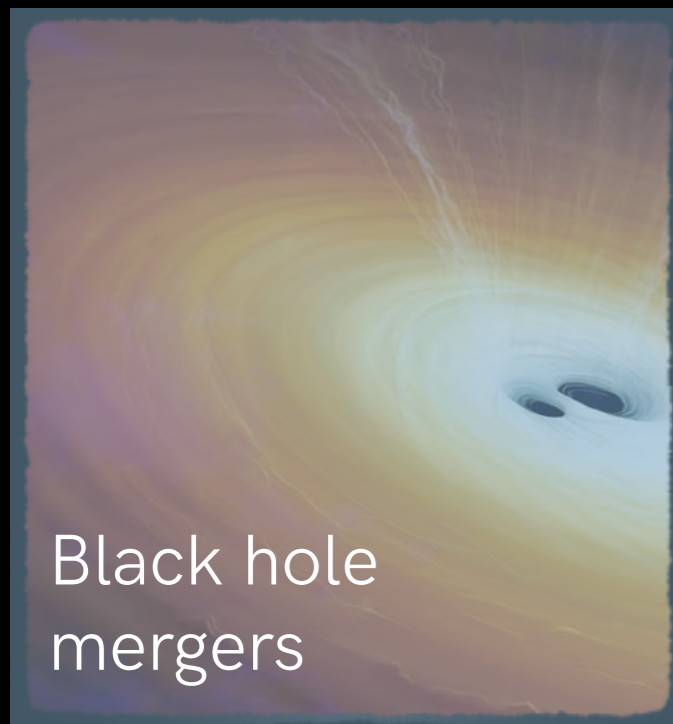
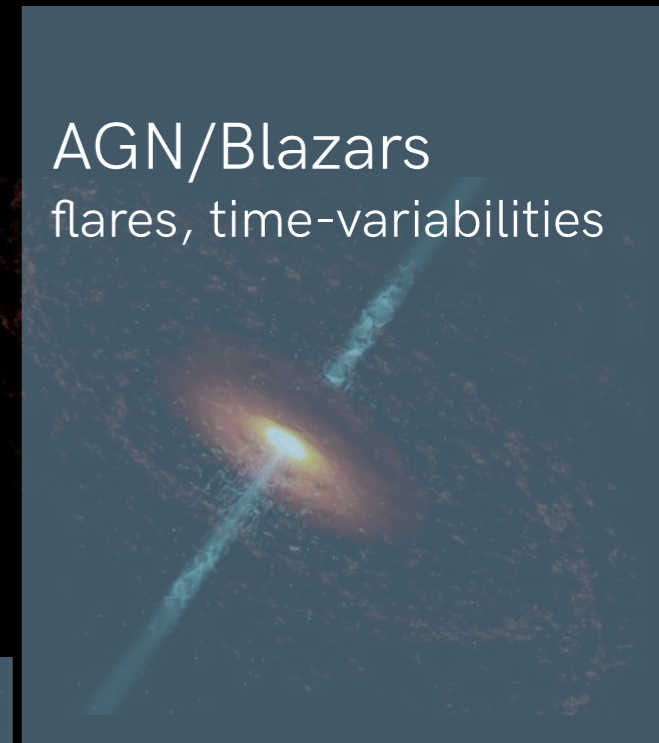
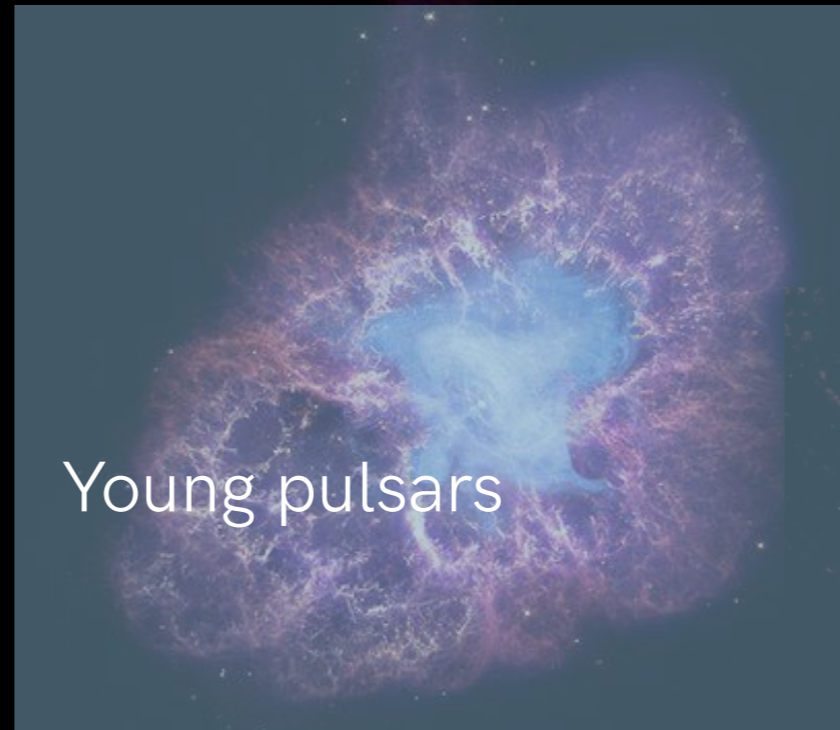
Why focus on transient sources?

time-dependent neutrino searches **reduce the background** for sub-PeV energies (atmospheric neutrinos+muons)



Real-time analysis + multi-messenger follow-up on alerts increase statistical significance of signals

The new high-energy transient zoo





AGN/Blazars

Source	Rate density [Gpc ⁻³ yr ⁻¹]	EM Luminosity [erg s ⁻¹]	Duration [s]	Typical Counterpart
Blazar flare ^a	10 – 100	10 ⁴⁶ – 10 ⁴⁸	10 ⁶ – 10 ⁷	broadband
Tidal disruption event	0.01 – 0.1 100 – 1000	10 ⁴⁷ – 10 ⁴⁸ 10 ^{43.5} – 10 ^{44.5}	10 ⁶ – 10 ⁷ > 10 ⁶ – 10 ⁷	jetted (X) tidal disruption event (optical,UV)
Long GRB	0.1 – 1	10 ⁵¹ – 10 ⁵²	10 – 100	prompt (X, gamma)
Short GRB	10 – 100	10 ⁵¹ – 10 ⁵²	0.1 – 1	prompt (X, gamma)
Low-luminosity GRB	100 – 1000	10 ⁴⁶ – 10 ⁴⁷	1000 – 10000	prompt (X, gamma)
GRB afterglow		< 10 ⁴⁶ – 10 ⁵¹ ,	> 1 – 10000	afterglow (broadband)
Supernova (II)	10 ⁵	10 ⁴¹ – 10 ⁴²	> 10 ⁵	supernova (optical)
Supernova (Ibc)	3 × 10 ⁴	10 ⁴¹ – 10 ⁴²	> 10 ⁵	supernova (optical)
Hypernova	3000	10 ⁴² – 10 ⁴³	> 10 ⁶	supernova (optical)
NS merger	300 – 3000	10 ⁴¹ – 10 ⁴² 10 ⁴³	> 10 ⁵ > 10 ⁷ – 10 ⁸	kilonova (optical/IR) radio flare (broadband)
BH merger	10 – 100	?	?	?
WD merger	10 ⁴ – 10 ⁵	10 ⁴¹ – 10 ⁴²	> 10 ⁵	merger nova (optical)

^aBlazar flares such as the 2017 flare of TXS 0506+056 are assumed for the demonstration.

Abbreviations: BH, black hole; EM, electromagnetic; GRB, gamma-ray burst; NS, neutron star; WD, white dwarf.

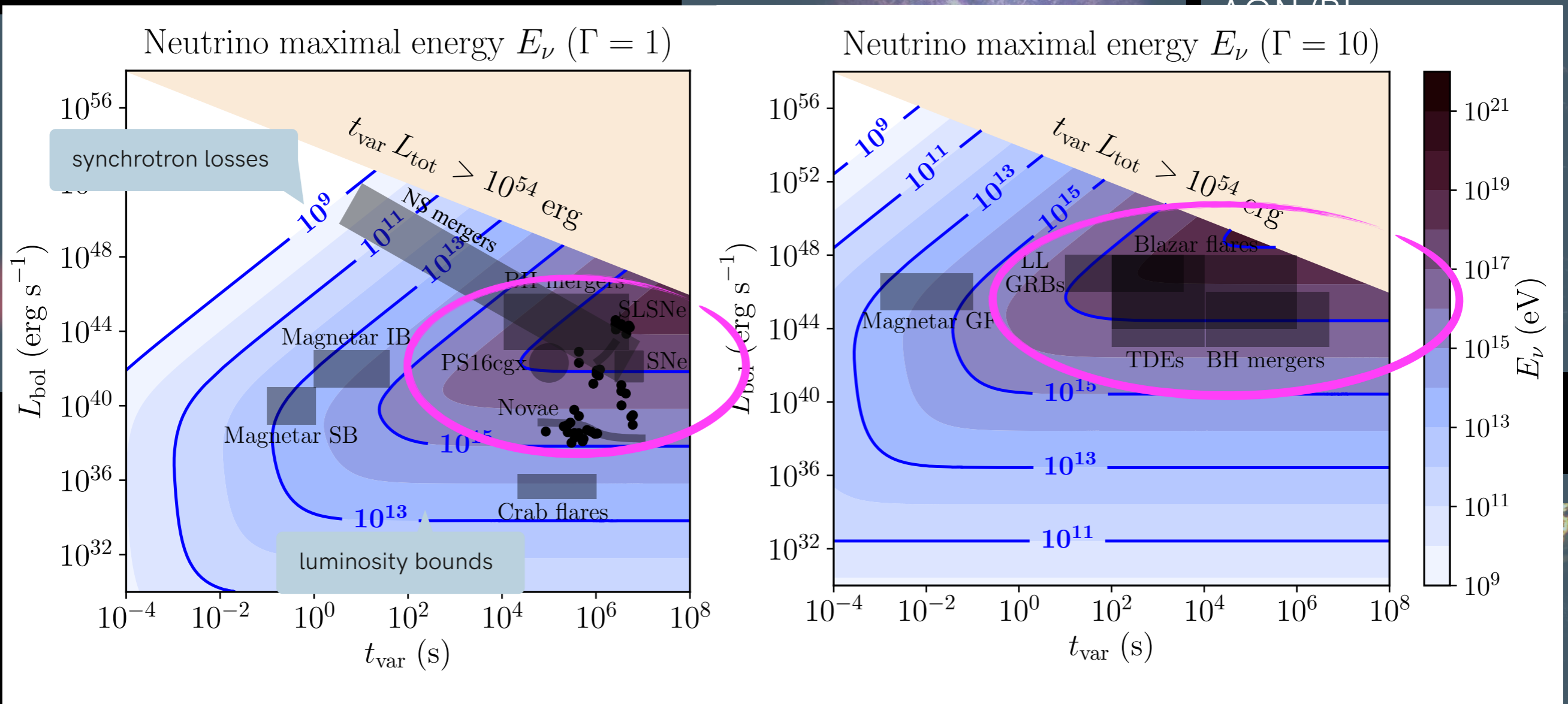
Black hole mergers

Tidal disruption events

Superluminous Supernovae

A "Hillas diagram" for high-energy neutrino transients

Guépin & KK 2017



Black hole mergers

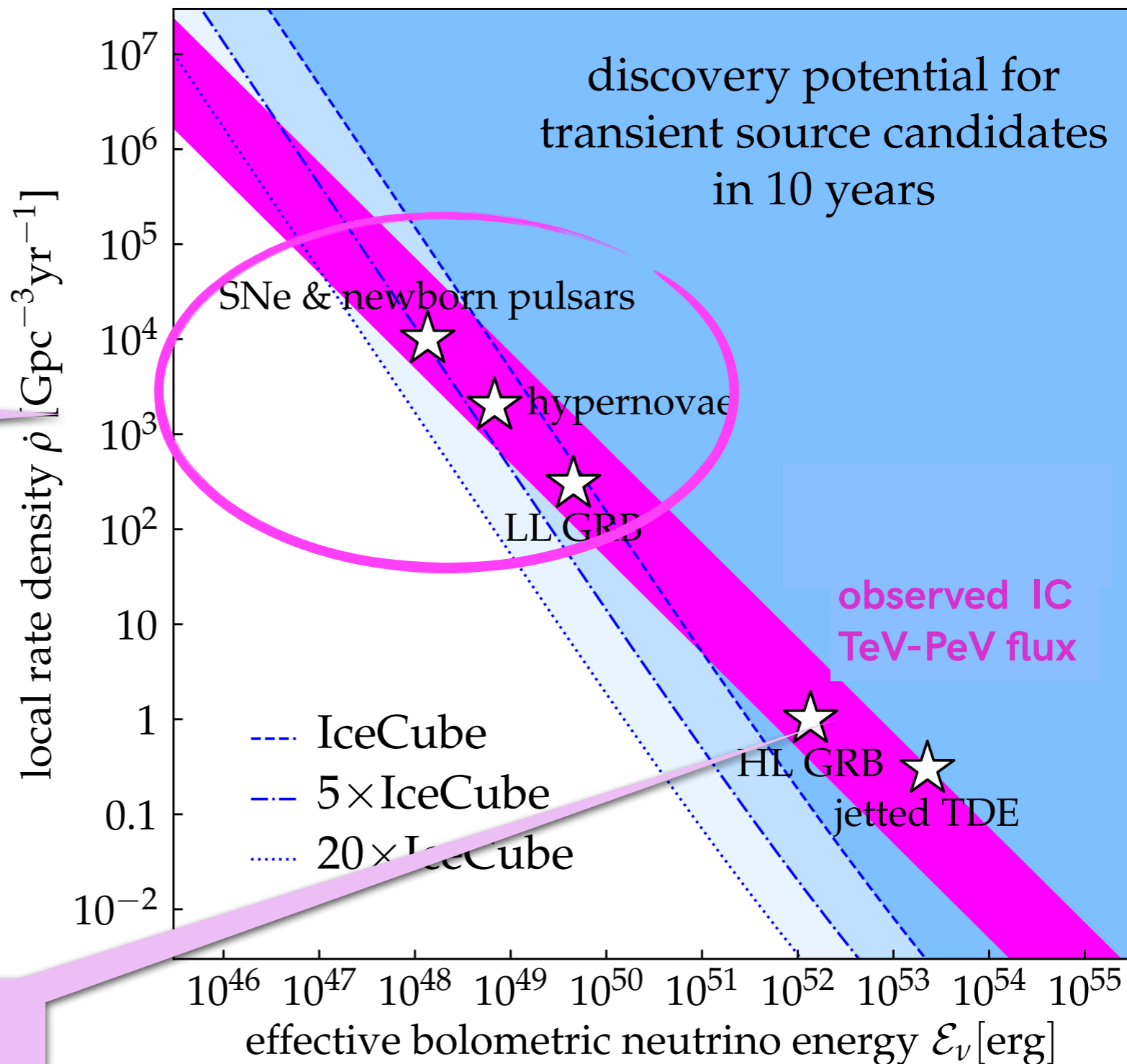
Tidal disruption events

Superluminous Supernovae

IceCube neutrinos: soon to be probed transients

Detection of **multiplets** depends on number density of sources

Could be probed in the next decade

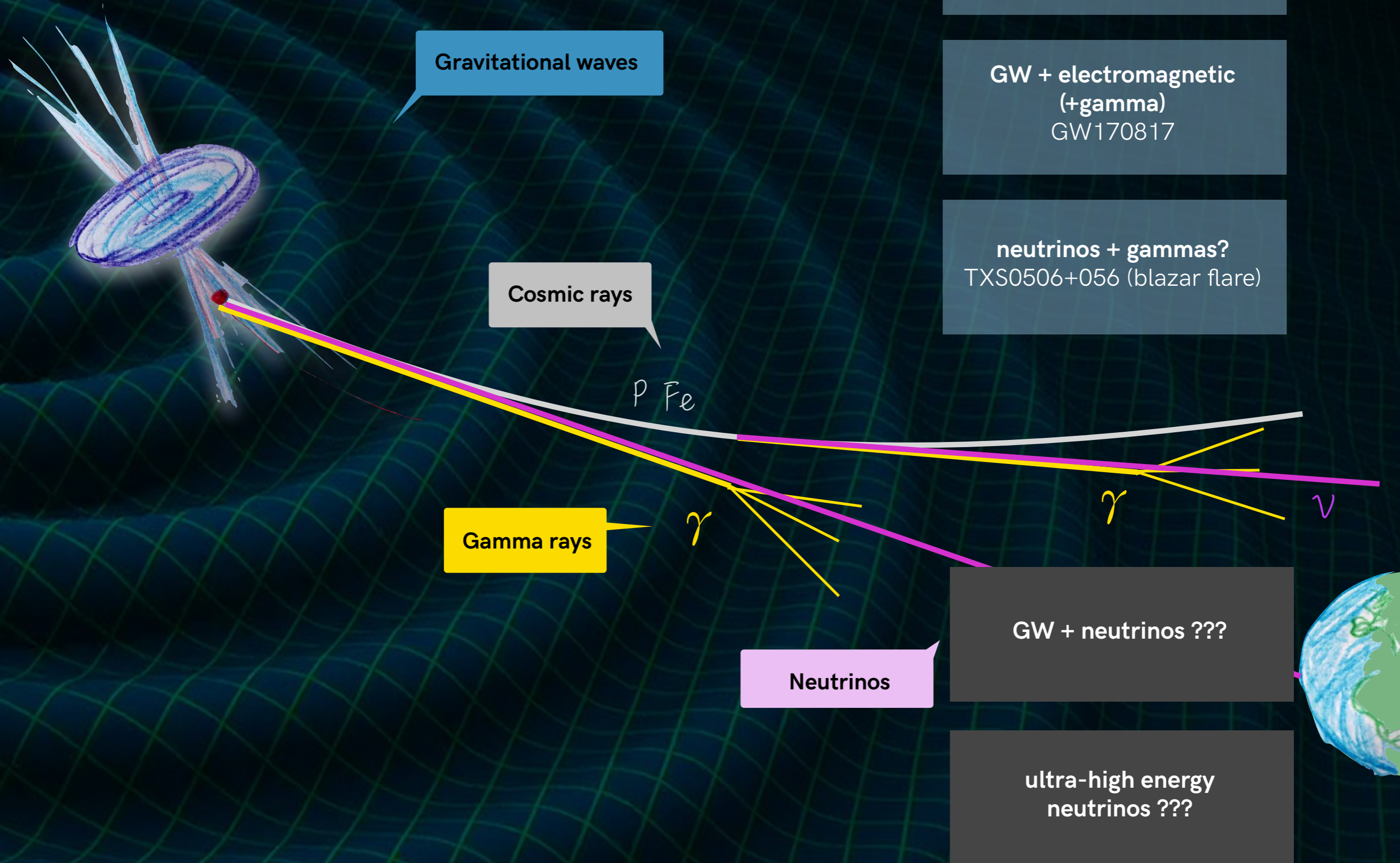


Rare powerful sources are excluded

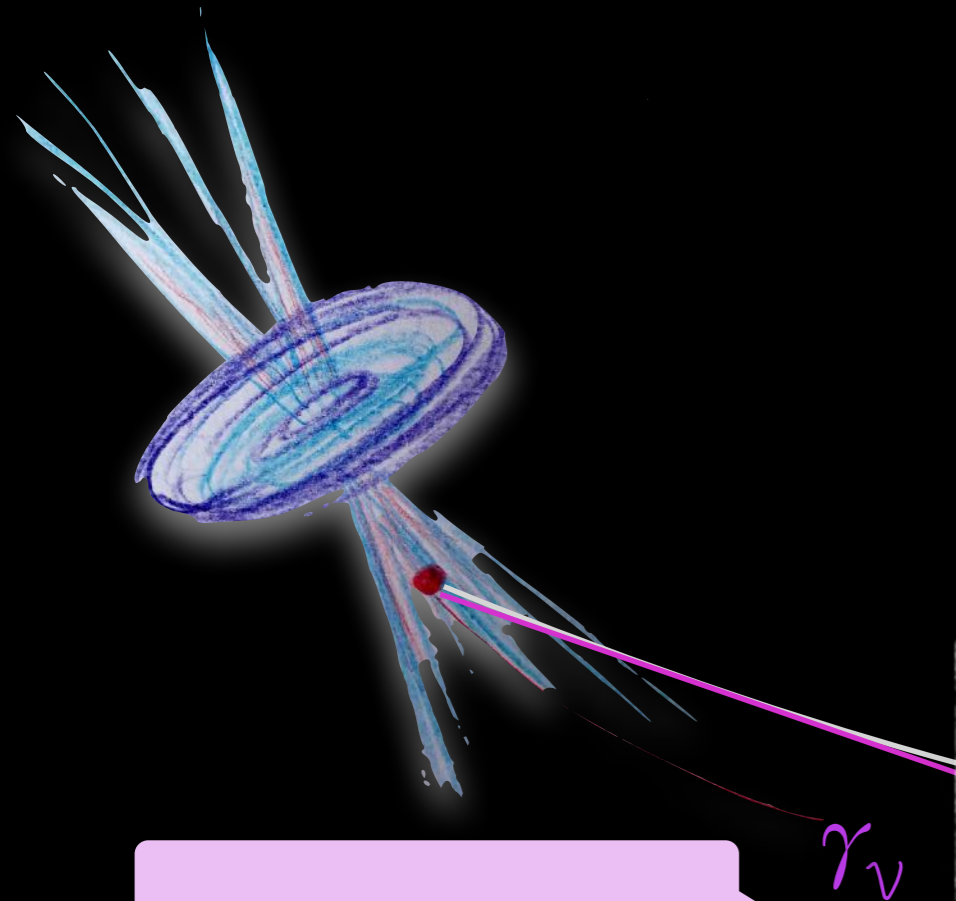
3. Can we really do multi-messenger astrophysics?

Opening the UHE neutrino window

Multi-messengers!



Current multi-messenger data: useful to understand UHECRs?



Cosmic backgrounds

interactions on CMB, UV/opt/IR photons

cosmogenic neutrino and gamma-ray production

Backgrounds

- radiative? baryonic?
- evolution, density?
- magnetic field: deflections?

associated neutrino and gamma-ray production

Secondaries take up 5-10% of parent cosmic-ray energy

$$E_\nu \sim 5\% E_{CR}$$

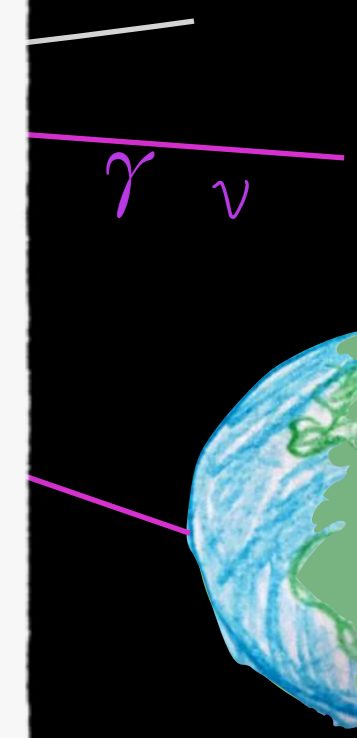
$$E_\gamma \sim 10\% E_{CR}$$

$$E_{CR} > 10^{18} \text{ eV}$$

$$E_\nu > 10^{16} \text{ eV}$$

IceCube neutrinos do not directly probe UHECRs

Actually, none of the current multi-messenger data (except UHECR data) can directly probe UHECRs ... but they help :-)

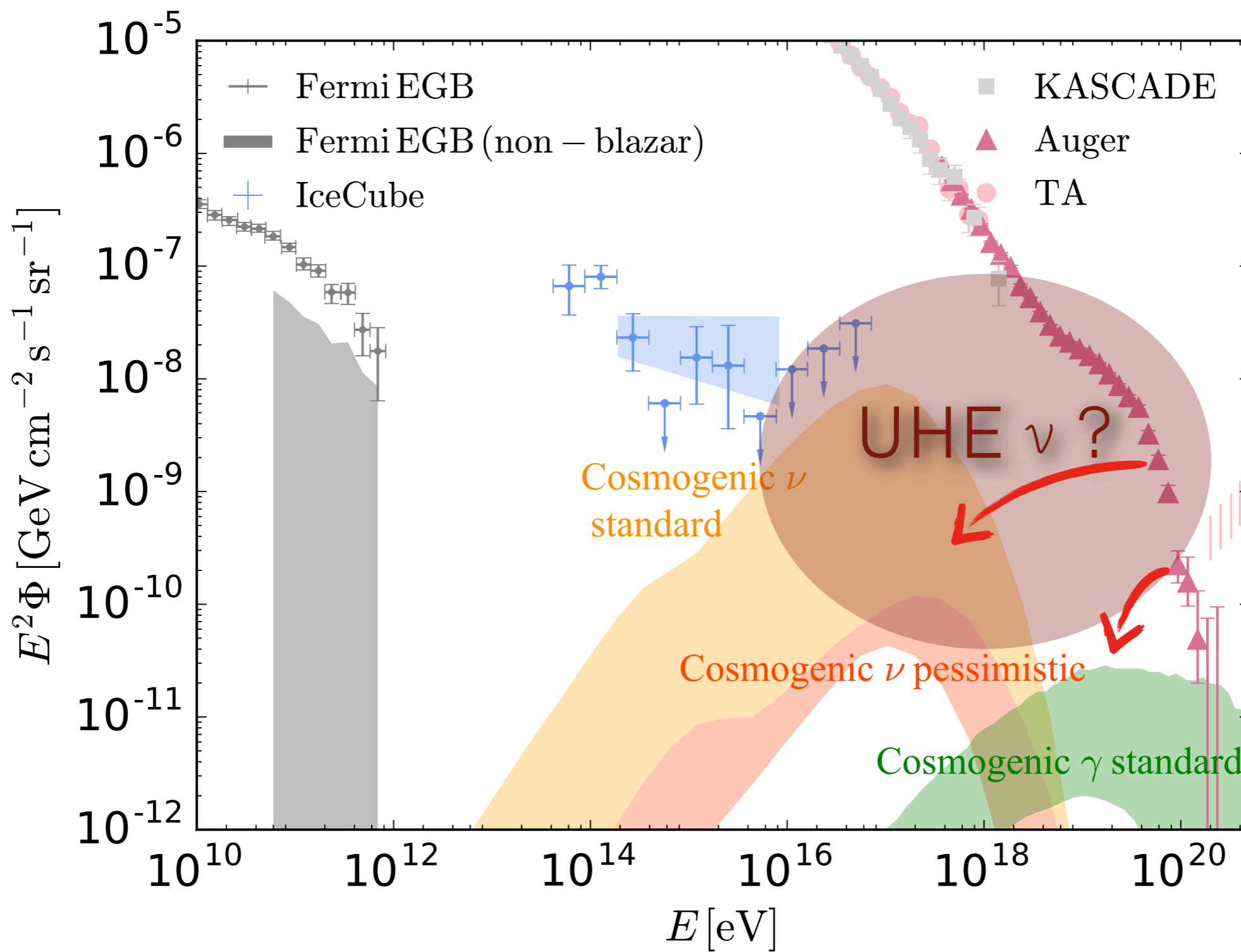


UHE neutrinos: a challenging no-man's land

Alves Batista, de Almeida, Lago, KK, 2018

GRAND Science & Design, 2018

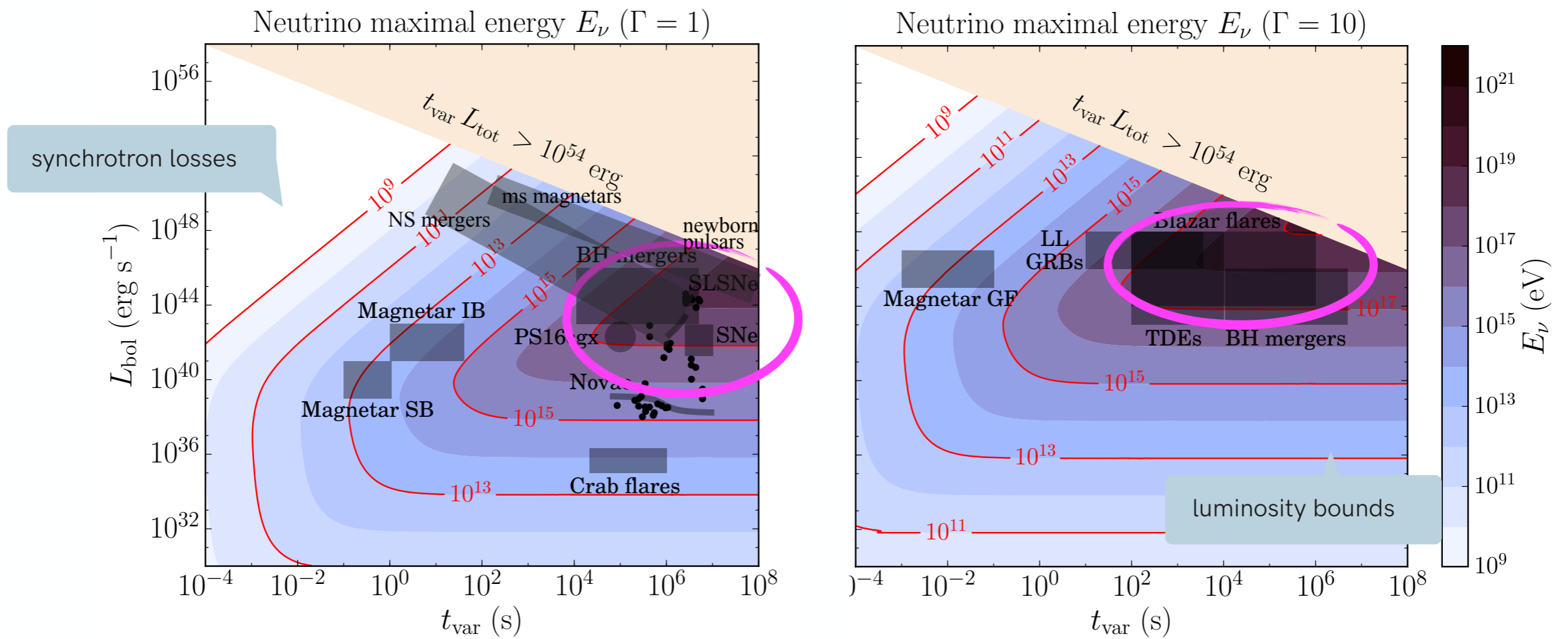
KK, Allard, Olinto 2010



UHE neutrino production for transients

many transient sources could make it

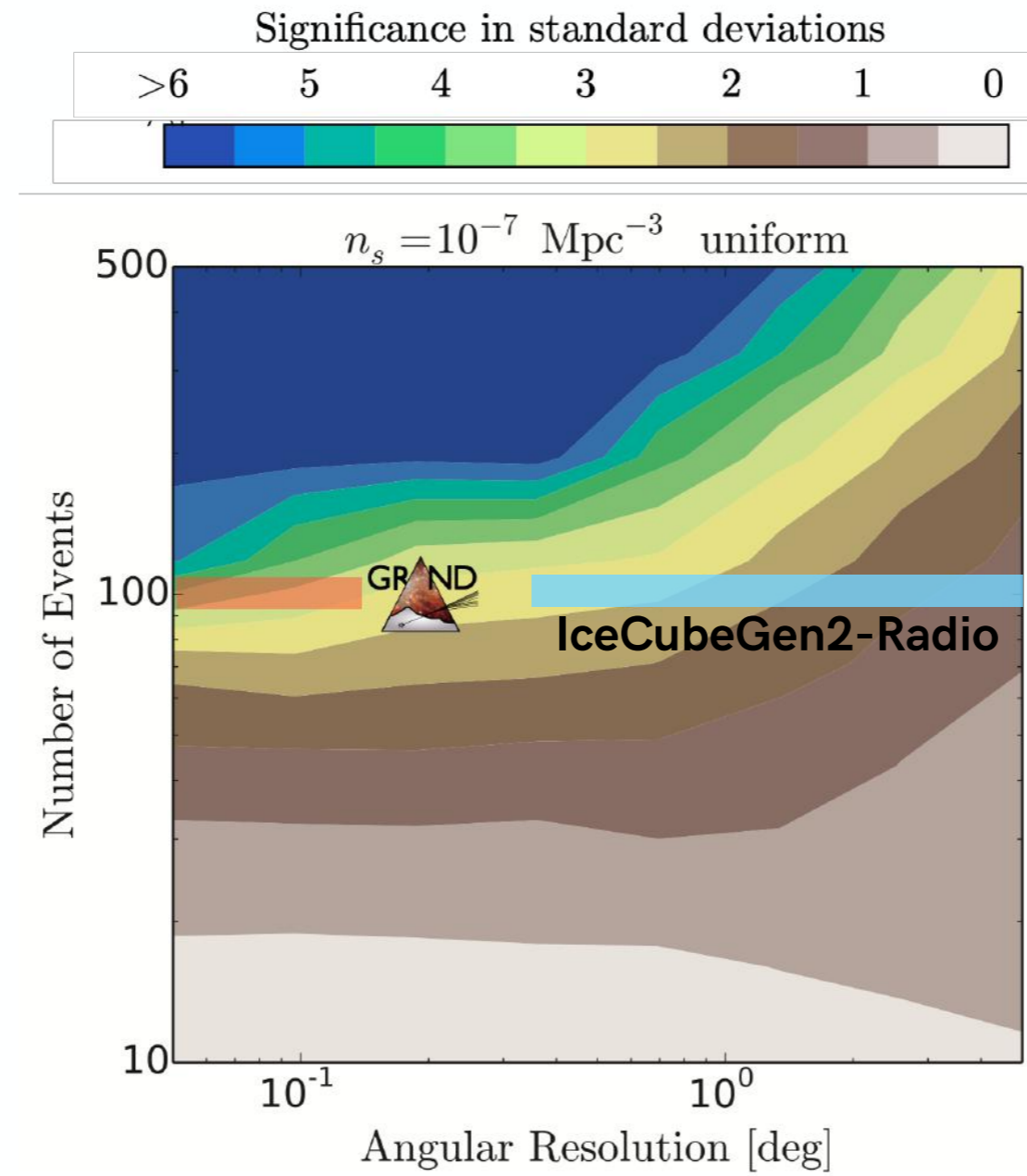
Guépin & KK 2016



Can we hope to detect very high-energy neutrino sources?

Neutrinos don't have a horizon: won't we be polluted by background neutrinos?

Fang, KK, Miller, Murase, Oikonomou JCAP 2016



boxes for experiments assuming neutrino flux: $10^{-8} \text{ GeV cm}^{-2} \text{ s}^{-1}$

YES if

- ▶ good angular resolution (< fraction of degree)
- ▶ number of detected events > 100s

Towards UHE multi-messenger astronomy

What will we need?

- ✓ Excellent sensitivity
- ✓ Sub-degree angular resolution
- ✓ Wide instantaneous field of view

The angular resolution is key for multi-messenger networks

- development of MM-networks, of EM instruments
—> false associations will be extremely common
- skim interesting events + narrow down search area
—> requires angular resolution

2021	2025	>2030	Diff. sens. lim. in $\text{GeV cm}^{-2} \text{s}^{-1} \text{sr}^{-1}$	iFoV in sky %	ang. res.
	PUEO		4.2×10^{-10}	?	2.8°
ARA			3×10^{-10}	?	2.8°
RNO-G			8×10^{-10}	?	2.8°
	ARIANNA-200		3×10^{-10}	?	2.8°
	RET-N		3×10^{-10}	?	2.8°
	IceCube-Gen2 Radio		4×10^{-10} in 5 yr	43	$2^\circ \times 10^\circ$
	BEACON		1.2×10^{-8} in 5 yr	6	$0.3^\circ - 1^\circ$
	GRAND10k		1×10^{-8} in 5 yr	6	0.1°
	GRAND		4×10^{-10} in 5 yr	45	0.1°
Auger			$[1.5 \times 10^{-8} (2019)]$	30	$< 1^\circ$
	TAMBO		?	27	1°
	POEMMA Cerenkov		7×10^{-8} in 5 yr	0.6	0.4°
	Trinity		1×10^{-10} in 5 yr	6	$< 1^\circ$
	Ashra-NTA		2×10^{-10} in 5 yr	30	0.1°

difficult to reach sub-degree resolution for in-ice instruments

	2021	2025	>2030	FoV	ang. res.
gamma	LHAASO			2 sr	0.3°
		CTA		$10-20^\circ$	$< 0.15^\circ$
	HAWC			2 sr	0.1°
	H.E.S.S.			5°	0.1°
	MAGIC			3.5°	0.07°
	VERITAS			3.5°	0.1°
	Fermi LAT			2.4 sr	0.15°
	GBM			9 sr	10°
X	INTEGRAL	IBIS		64 deg^2	0.2°
		SPI-ACS		4π	-
	XMM-Newton			0.5°	$6''$
multi		Athena-WFI		0.4 deg^2	$< 5''$
	Swift	BAT		1.4 sr	0.4°
		XRT		0.1 deg^2	$18''$
		UVOT		0.1 deg^2	$2.5''$
		SVOM	ECLAIRs	2 sr	$< 0.2^\circ$
			MXT	1 deg^2	$13''$
IR/optical/UV		VT		0.2 deg^2	$< 1''$
	ASAS-SN			72 deg^2	$7.8''$
	ATLAS			29 deg^2	$2''$
	Pan-STARRS			14 deg^2	$1.0-1.3''$
	ZTF			47 deg^2	$2''$
		Vera Rubin Obs. (LSST)		9.6 deg^2	$0.7''$
	MASTER-II(VWF)			$8(400) \text{ deg}^2$	$1.9'' (22'')$
	TAROT			4 deg^2	$3.5''$
	GEMINI (GMOS)			$30.23'^2$	$0.07''/\text{pix}$
	GTC (OSIRIS)			0.02 deg^2	$0.127''/\text{pix}$
	Keck (LRIS)			$46.8'^2$	$0.135''/\text{pix}$
radio	VLT (X-shooter)			$2.2'^2$	$0.173''/\text{pix}$
	VLA			0.16 deg^2	$0.12''$
	MWA			610 deg^2	$0.9'$
		SKA1(2)-MID		$1(10) \text{ deg}^2$	$0.04^\circ-0.7^\circ$

adapted from Guépin, KK, Oikonomou, Nature Phys. Rev. subm.

Some references (a personal selection)

General perspectives and ideas

Alves Batista et al., Front. Astron. Space Sci. (2019)

Halzen & Kheirandish, Front. Astron. Space Sci. (2019)

Bartos & Murase, ARAA (2020)

Guépin, KK, Oikonomou, Nature Phys. Rev. (subm.)

Specific calculations

Dermer & Menon, Princeton University Press (2009)

KK, Allard, Olinto, JCAP (2010)

Guépin & KK, Phys. Rev. D (2017)

absolutely NOT exhaustive!