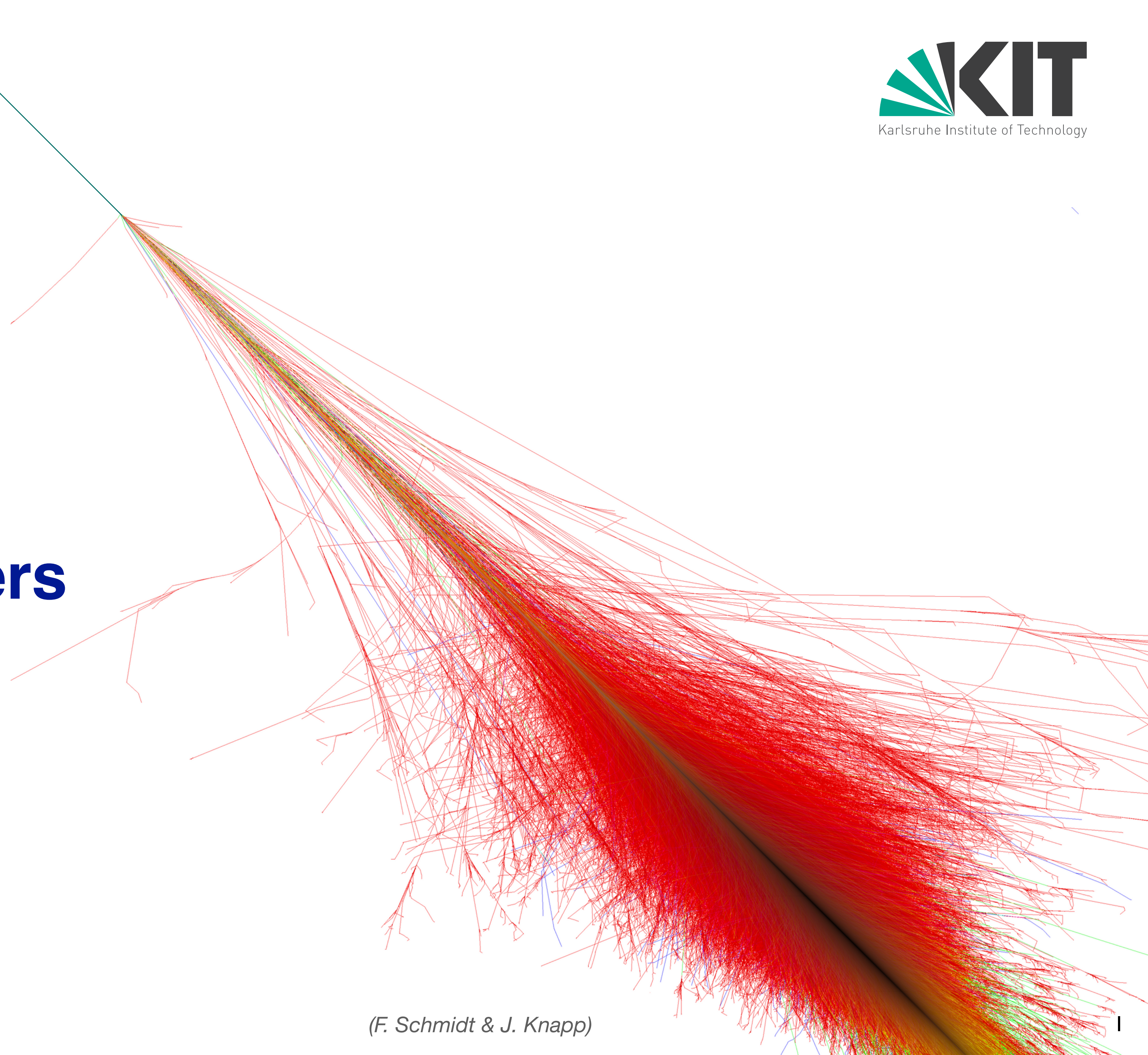


Physics of High-Energy Showers

Lecture 2

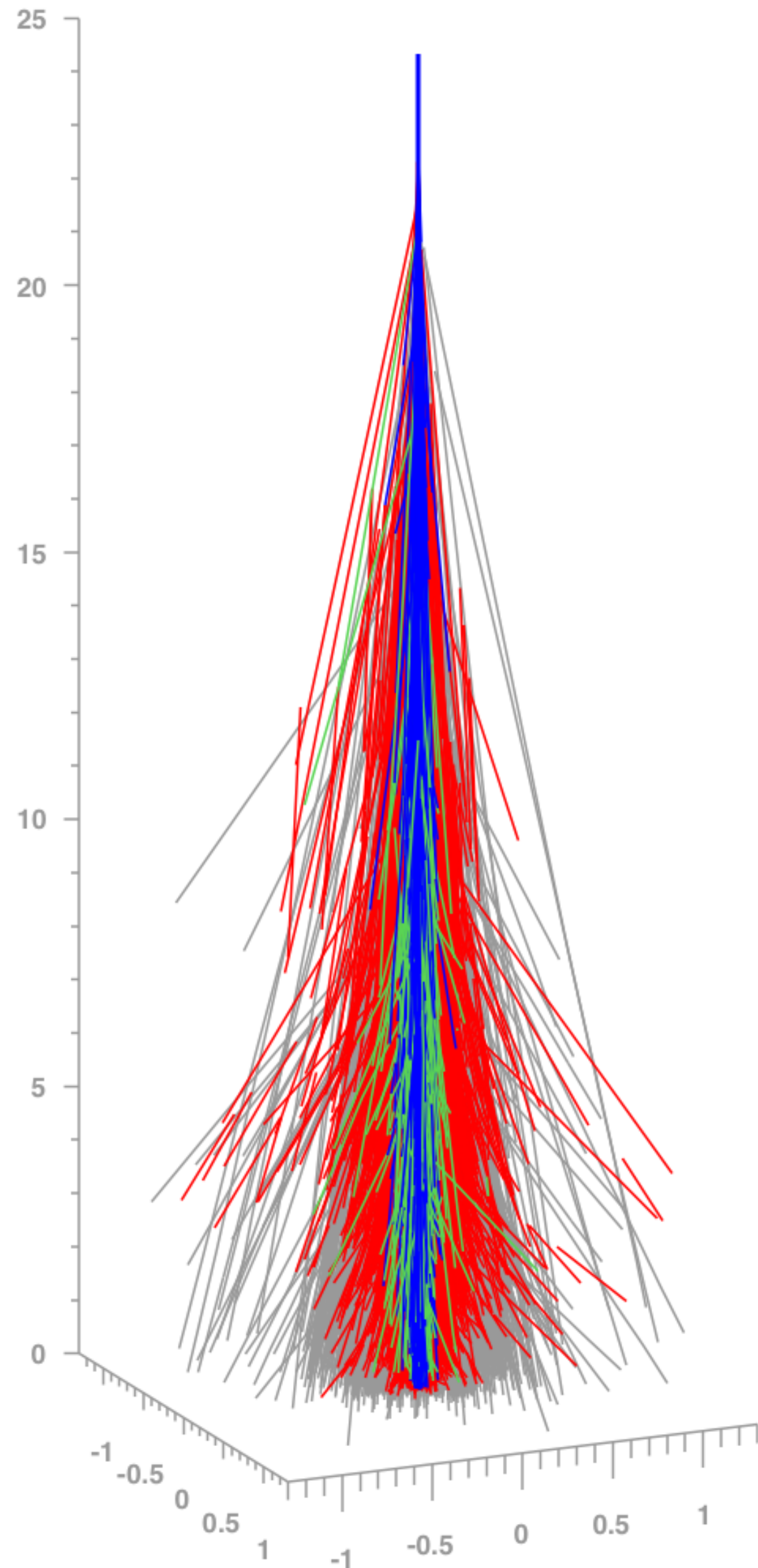
Ralph Engel

Karlsruhe Institute of Technology (KIT)

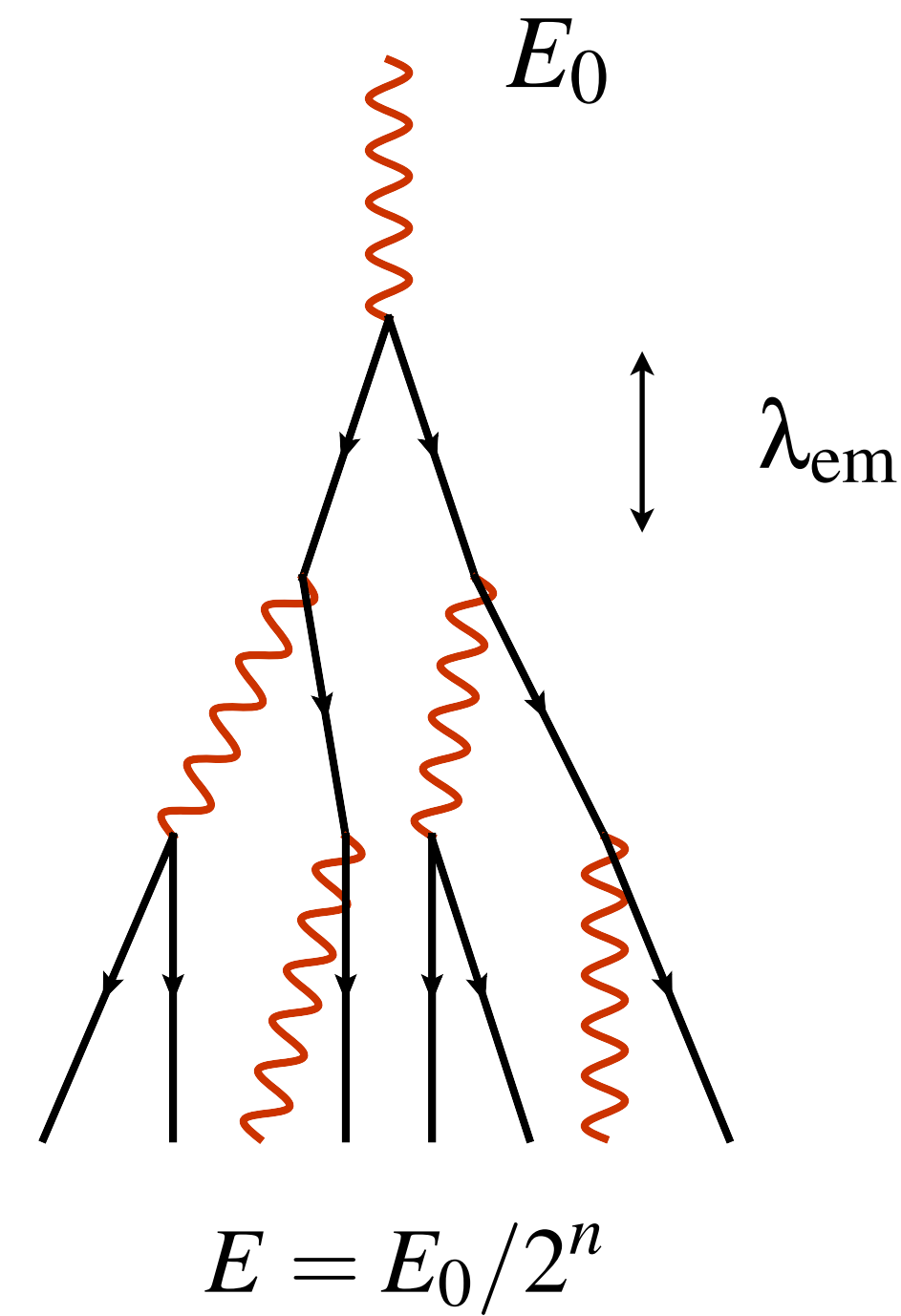
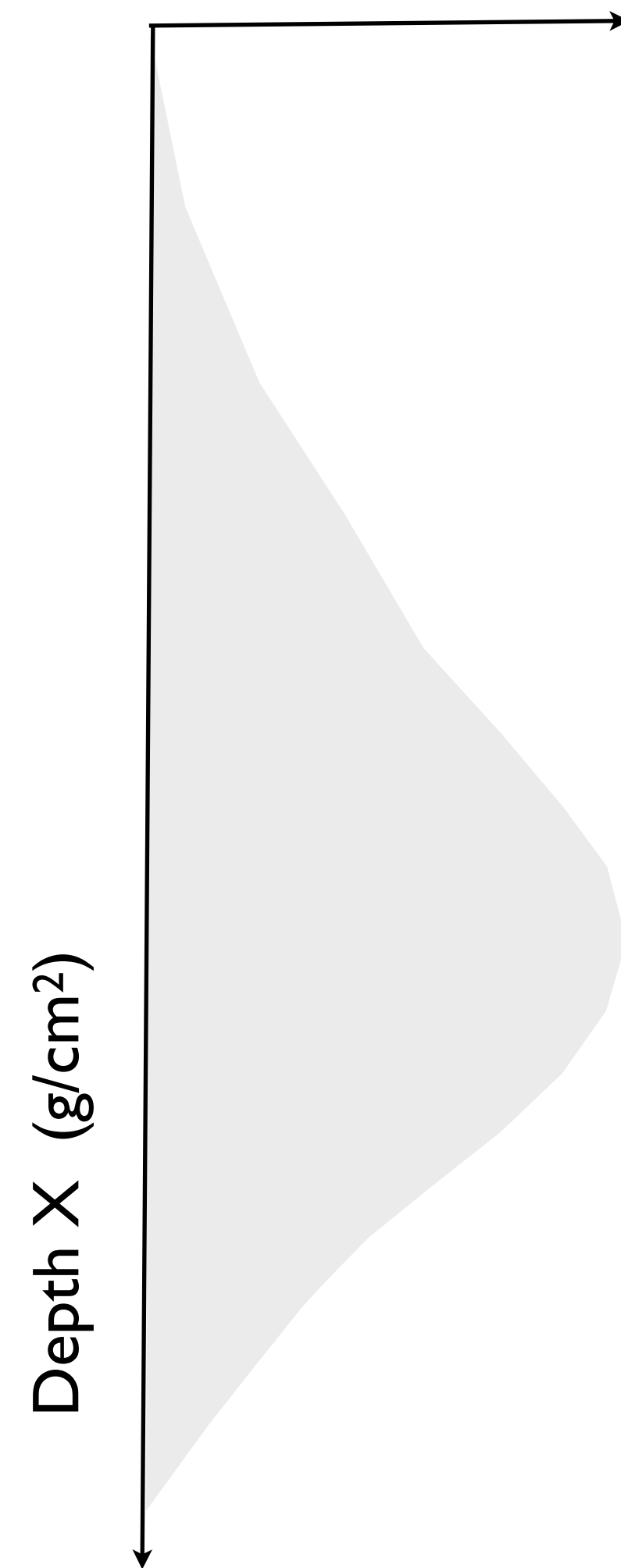


1. Recap of last lecture

Qualitative approach: Heitler model



Number of charged particles



$$X = n \lambda_{em}$$

Shower maximum: $E = E_c$

$$N_{\max} = E_0/E_c$$

$$X_{\max} \sim \lambda_{em} \ln(E_0/E_c)$$

Electromagnetic shower theory

Energy loss of electron: $\frac{dE}{dX} = -\alpha - \frac{E}{X_0}$

Critical energy: $E_c = \alpha X_0 \sim 85 \text{ MeV}$

Radiation length: $X_0 \sim 36 \text{ g/cm}^2$

$$\lambda_{\text{pair}} = \frac{\langle m_{\text{air}} \rangle}{\sigma_{\text{pair,tot}}} = \frac{9}{7} X_0$$

Longitudinal profile (Greisen formula)

$$N_e(X) \approx \frac{0.31}{[\ln E_0/E_c]^{1/2}} \exp \left\{ \frac{X}{X_0} \left(1 - \frac{3}{2} \ln s \right) \right\}$$

Shower age

$$s = \frac{3X}{X + 2X_{\text{max}}}$$

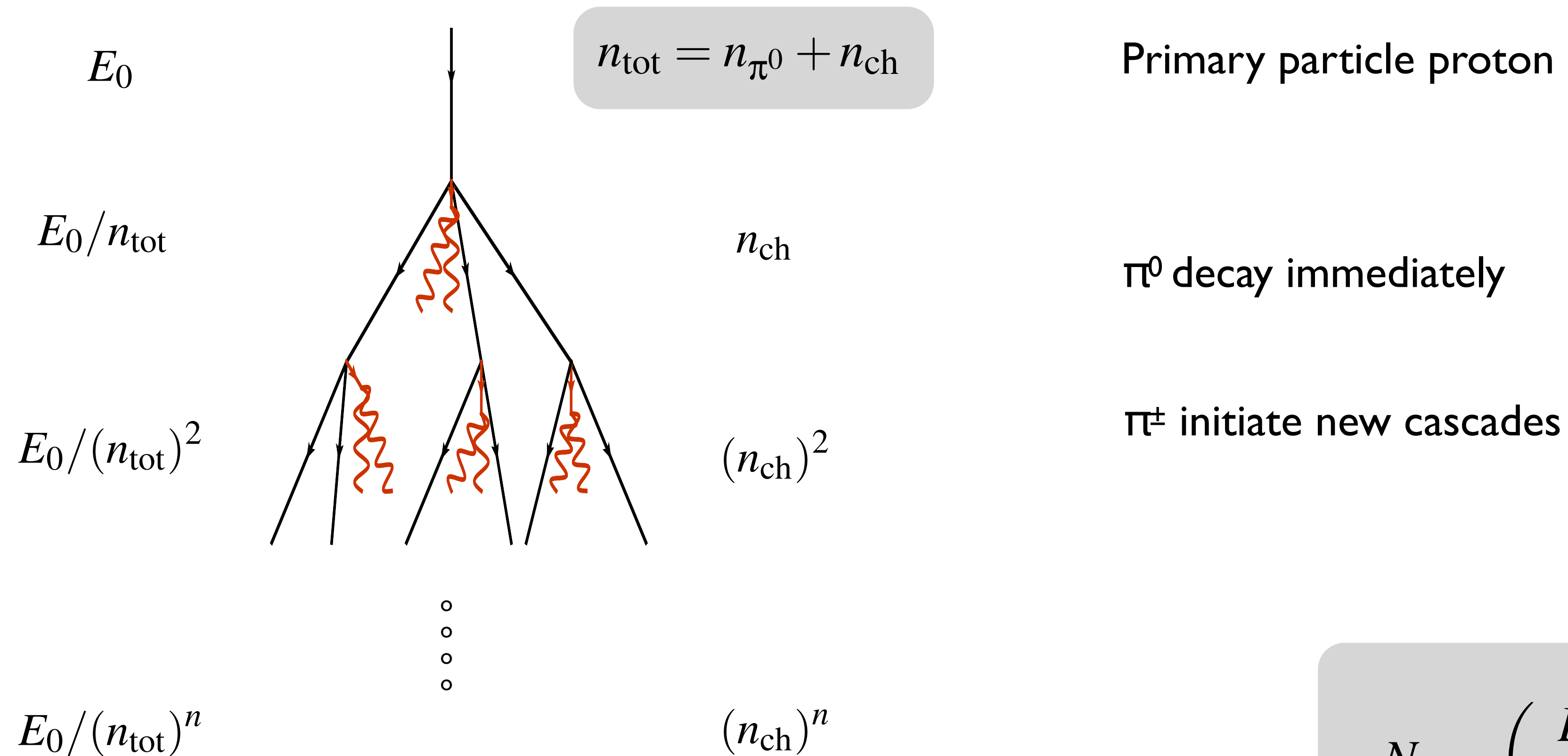
Energy spectrum particles

$$\frac{dN_e}{dE} \sim \frac{1}{E^{1+s}}$$

$$X_{\text{max}} \approx X_0 \ln \left(\frac{E_0}{E_c} \right)$$

$$N_{\text{max}} \approx \frac{0.31}{\sqrt{\ln(E_0/E_c) - 0.33}} \frac{E_0}{E_c}$$

Qualitative approach: Heitler-Matthews model



Assumptions:

- cascade stops at $E_{\text{part}} = E_{\text{dec}}$
- each hadron produces one muon

(Matthews, *Astropart.Phys.* 22, 2005)

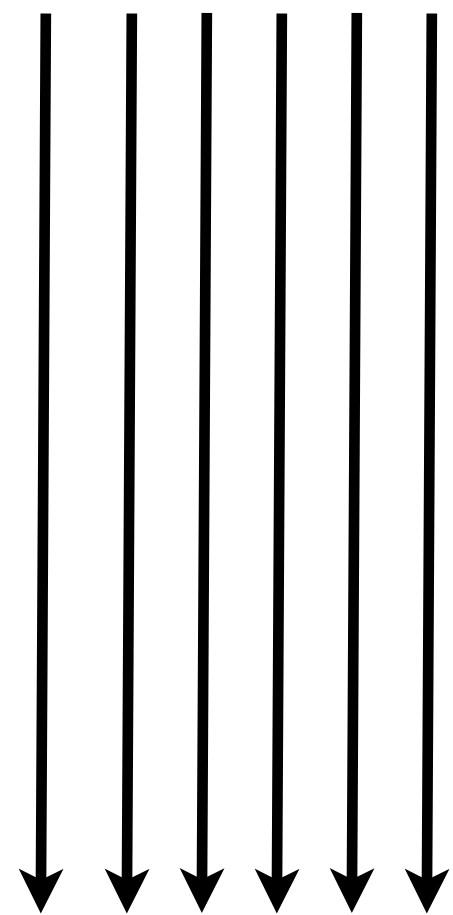
$$N_\mu = \left(\frac{E_0}{E_{\text{dec}}} \right)^\alpha$$

$$\alpha = \frac{\ln n_{\text{ch}}}{\ln n_{\text{tot}}} \approx 0.82 \dots 0.95$$

Superposition model

Nucleus

$$E_i = E_0/A$$



Target ●

Proton-induced shower

$$N_{\max} \sim E_0/E_c$$

$$X_{\max} \sim \lambda_{\text{eff}} \ln(E_0)$$

$$N_{\mu} = \left(\frac{E_0}{E_{\text{dec}}} \right)^{\alpha} \quad \alpha \approx 0.9$$

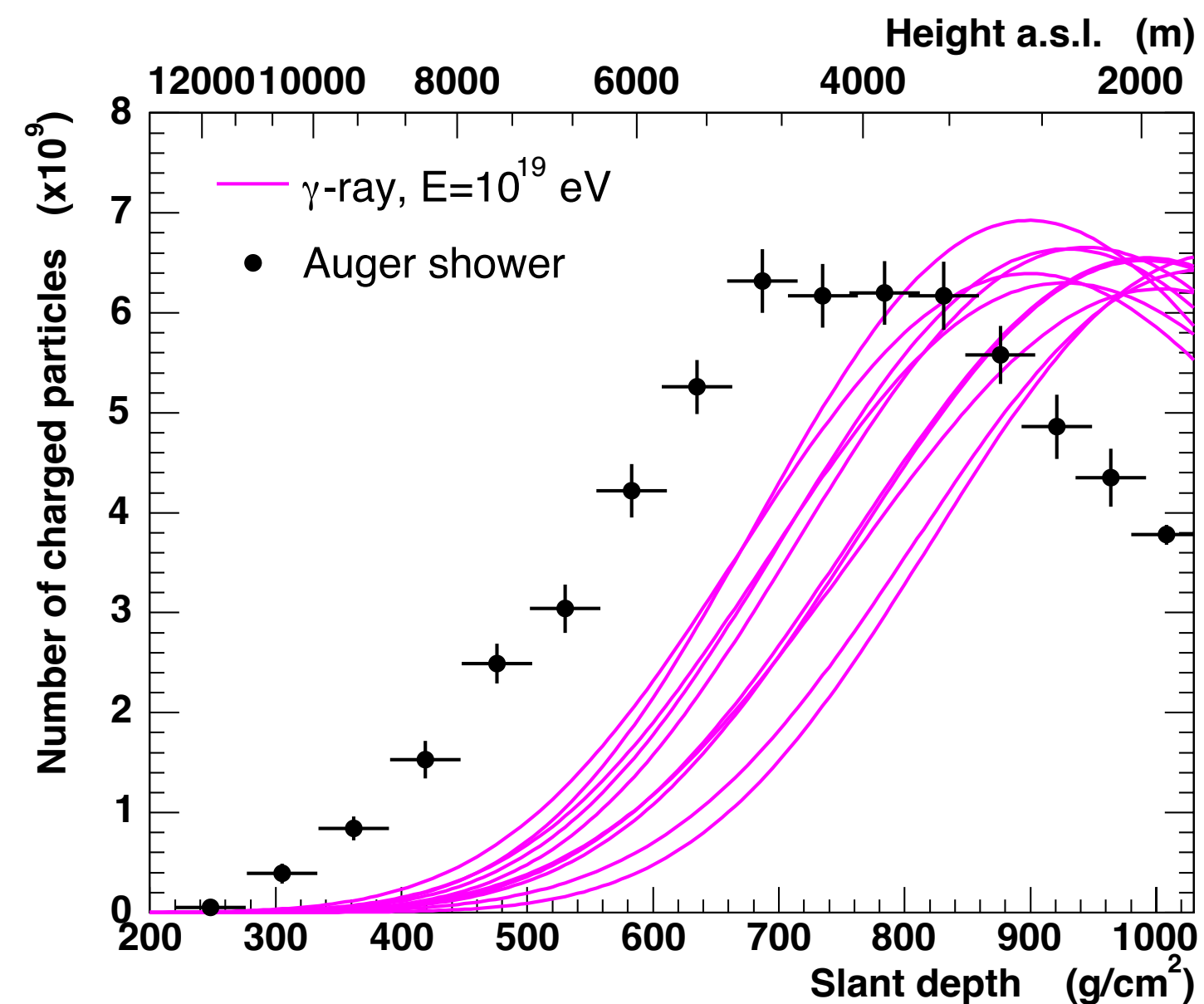
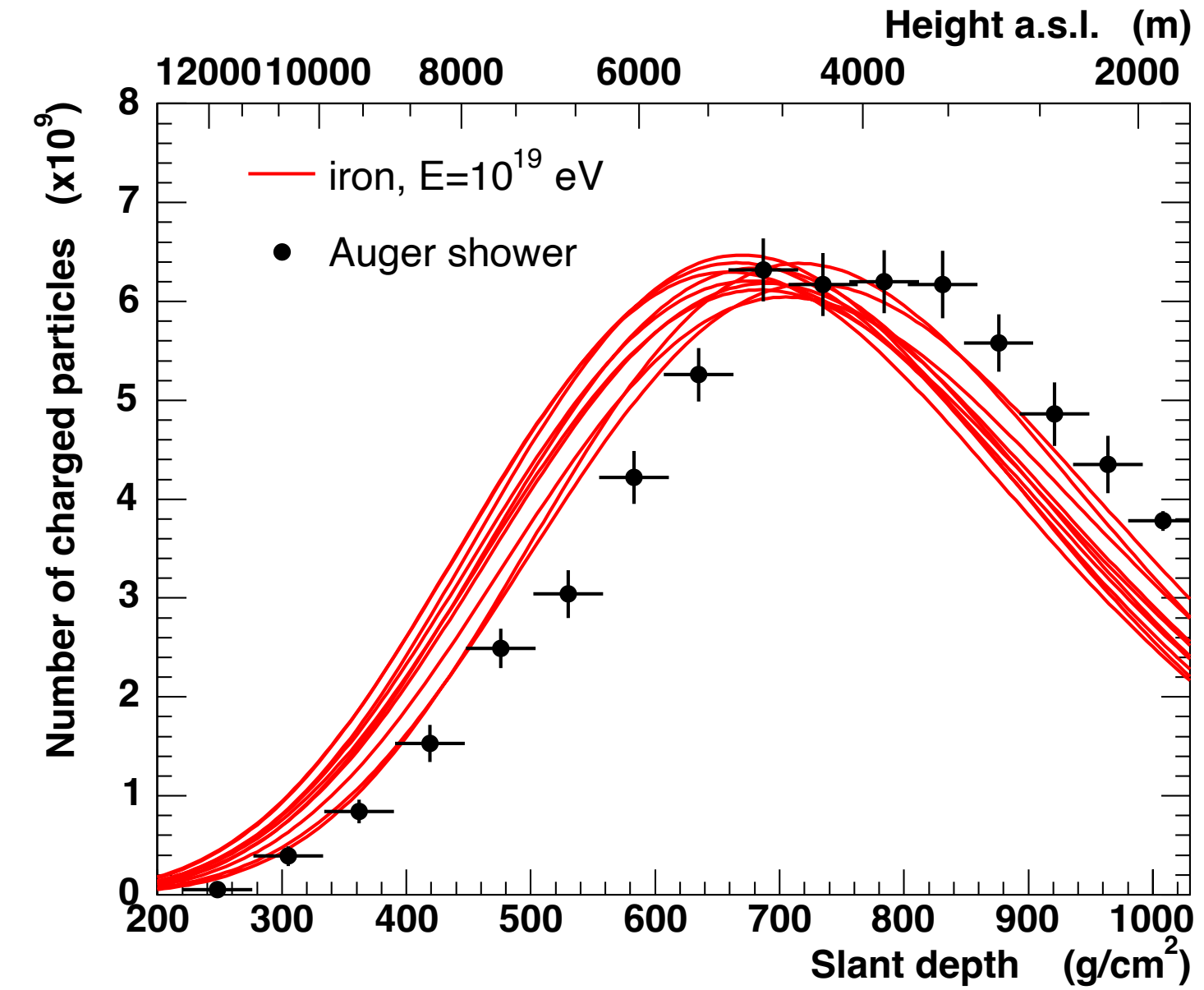
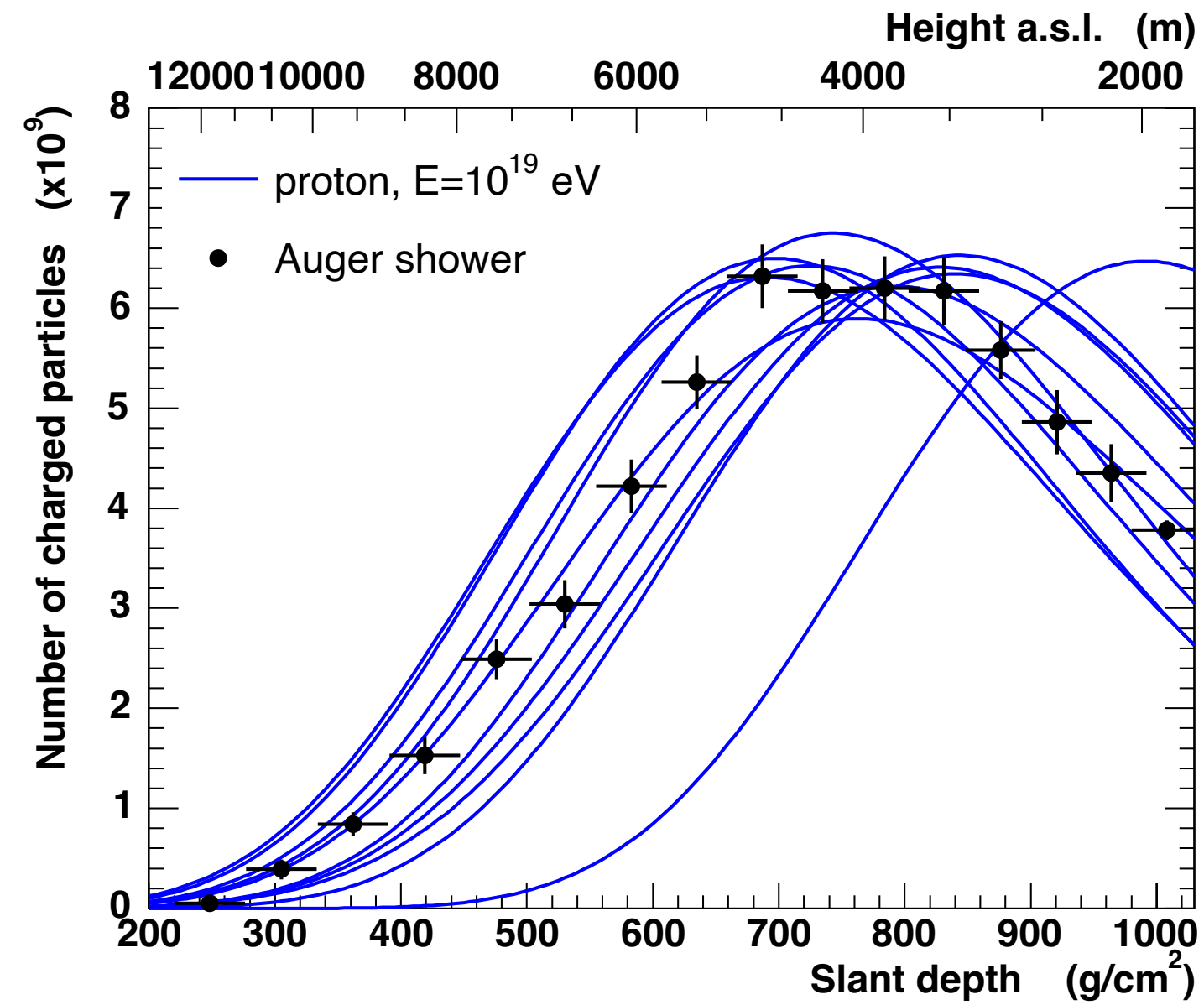
Assumption: nucleus of mass A and energy E_0 corresponds to A nucleons (protons) of energy $E_n = E_0/A$

$$N_{\max}^A \sim A \left(\frac{E_0}{AE_c} \right) = N_{\max}$$

$$X_{\max}^A \sim \lambda_{\text{eff}} \ln(E_0/A)$$

$$N_{\mu}^A = A \left(\frac{E_0}{AE_{\text{dec}}} \right)^{\alpha} = A^{1-\alpha} N_{\mu}$$

Longitudinal shower profiles: simulations and data



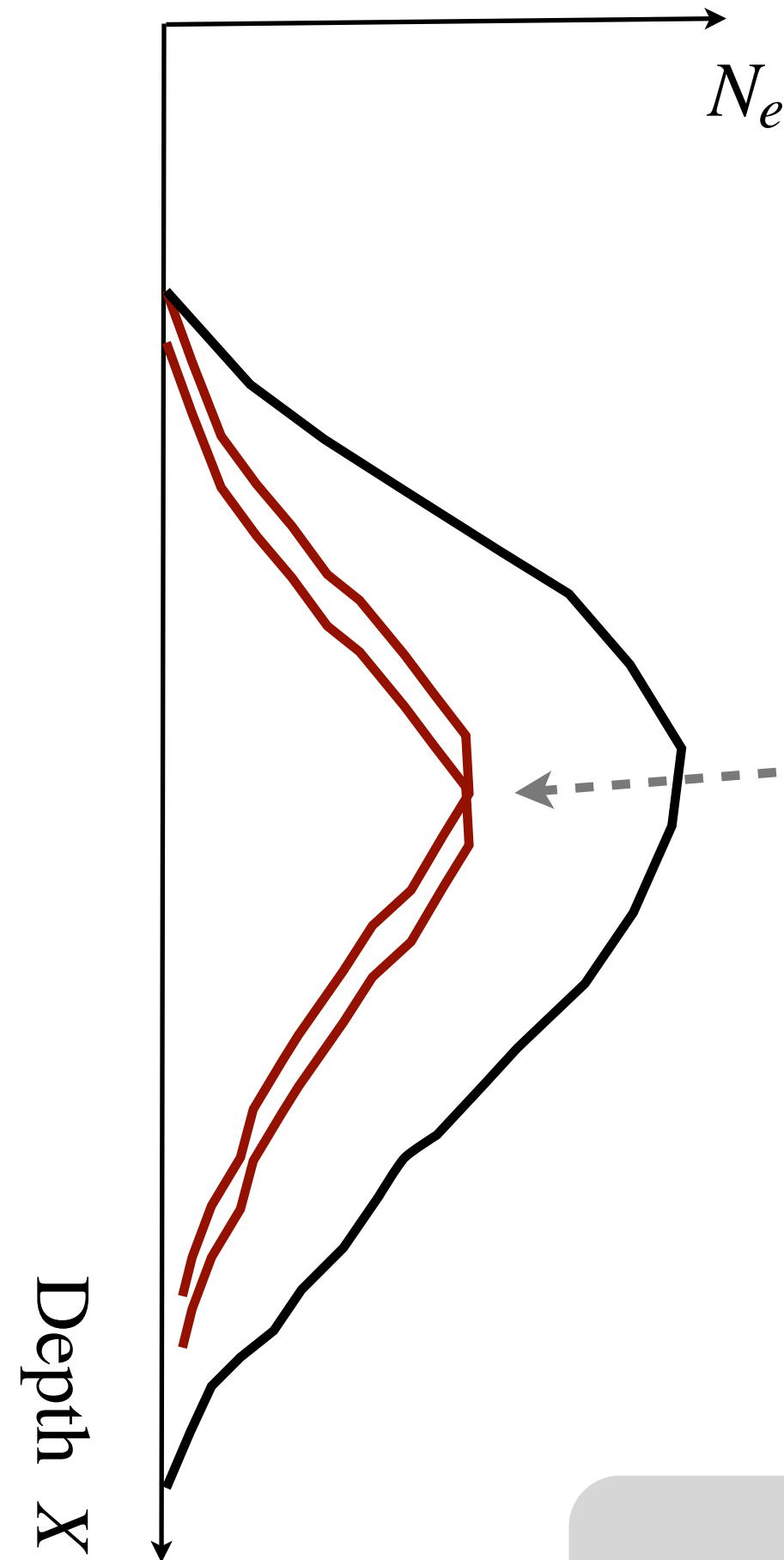
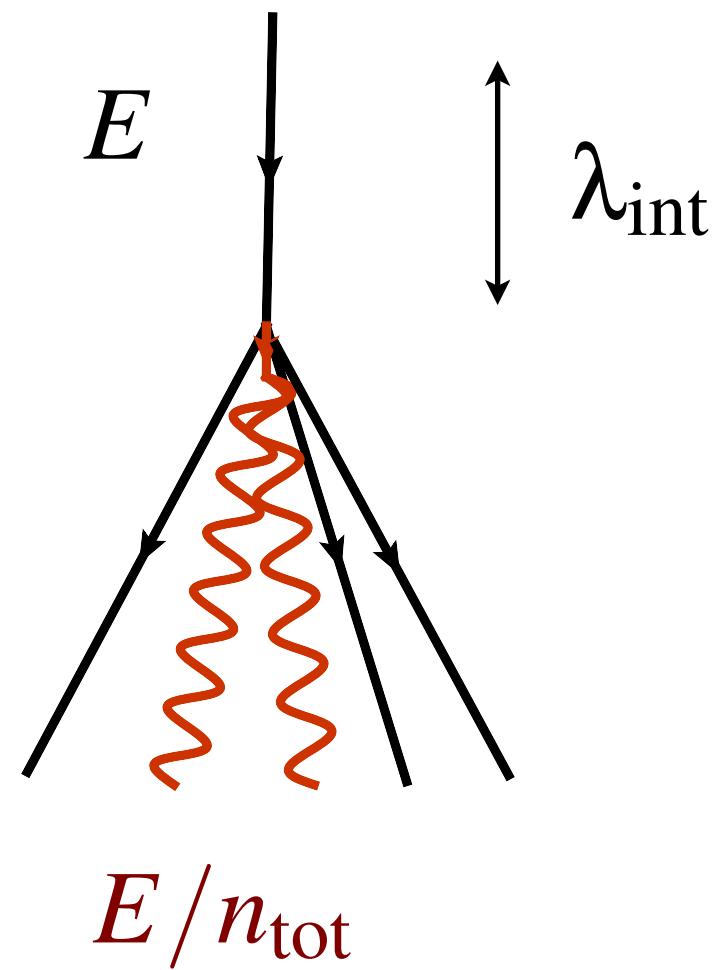
$$N_{\max} = E_0 / E_c$$

$$X_{\max} \sim D_e \ln(E_0 / E_c)$$

Superposition model:

$$X_{\max}^A \sim D_e \ln(E_0 / A E_c)$$

Derivation of elongation rate theorem



$$\langle X_{\max}(E) \rangle = \langle X_{\max}^{\text{em}}(E/n_{\text{tot}}) \rangle + \lambda_{\text{int}}$$

em. cascade theory

$$\langle X_{\max}^{\text{em}} \rangle \sim X_0 \ln(E/n_{\text{tot}})$$

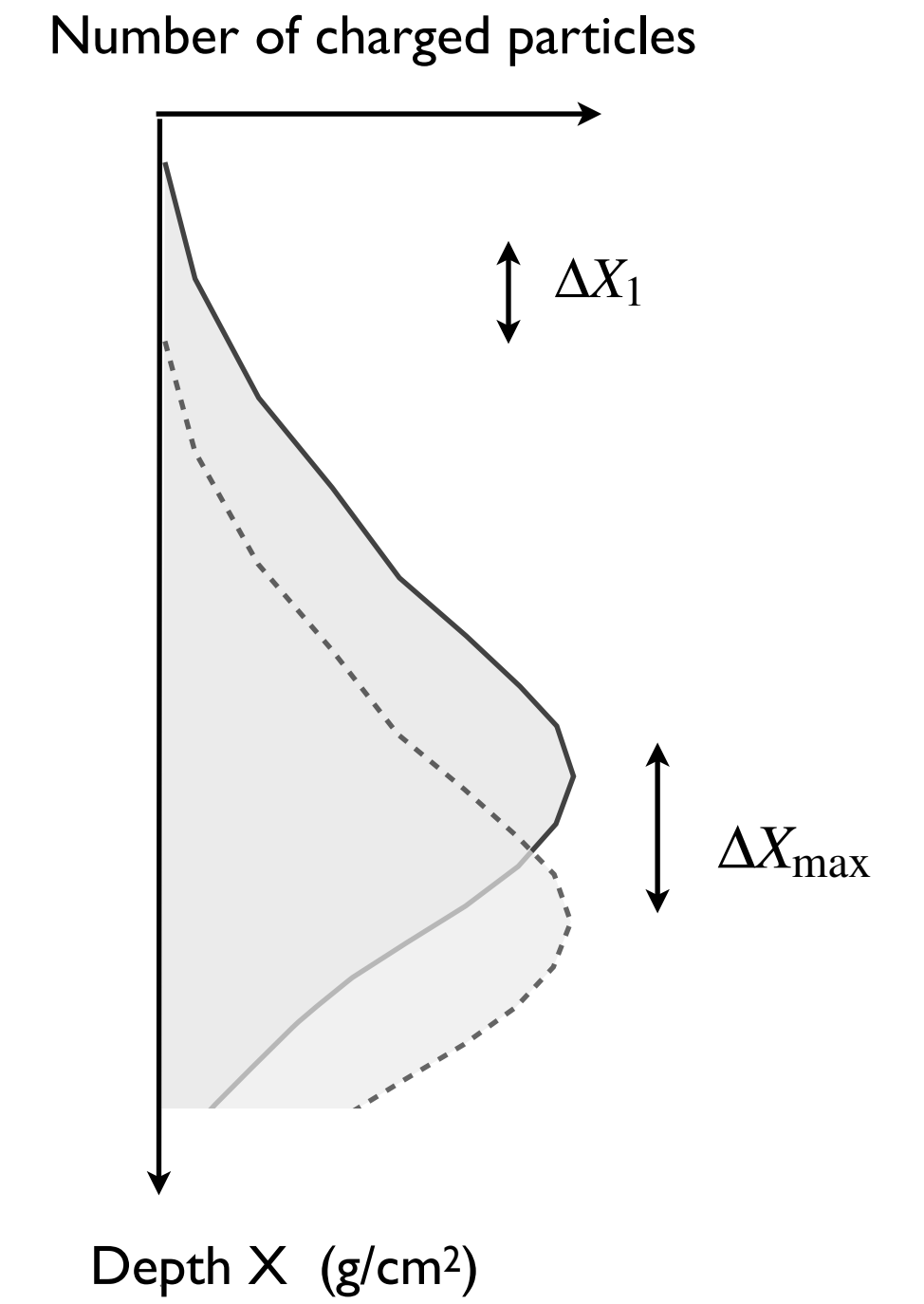
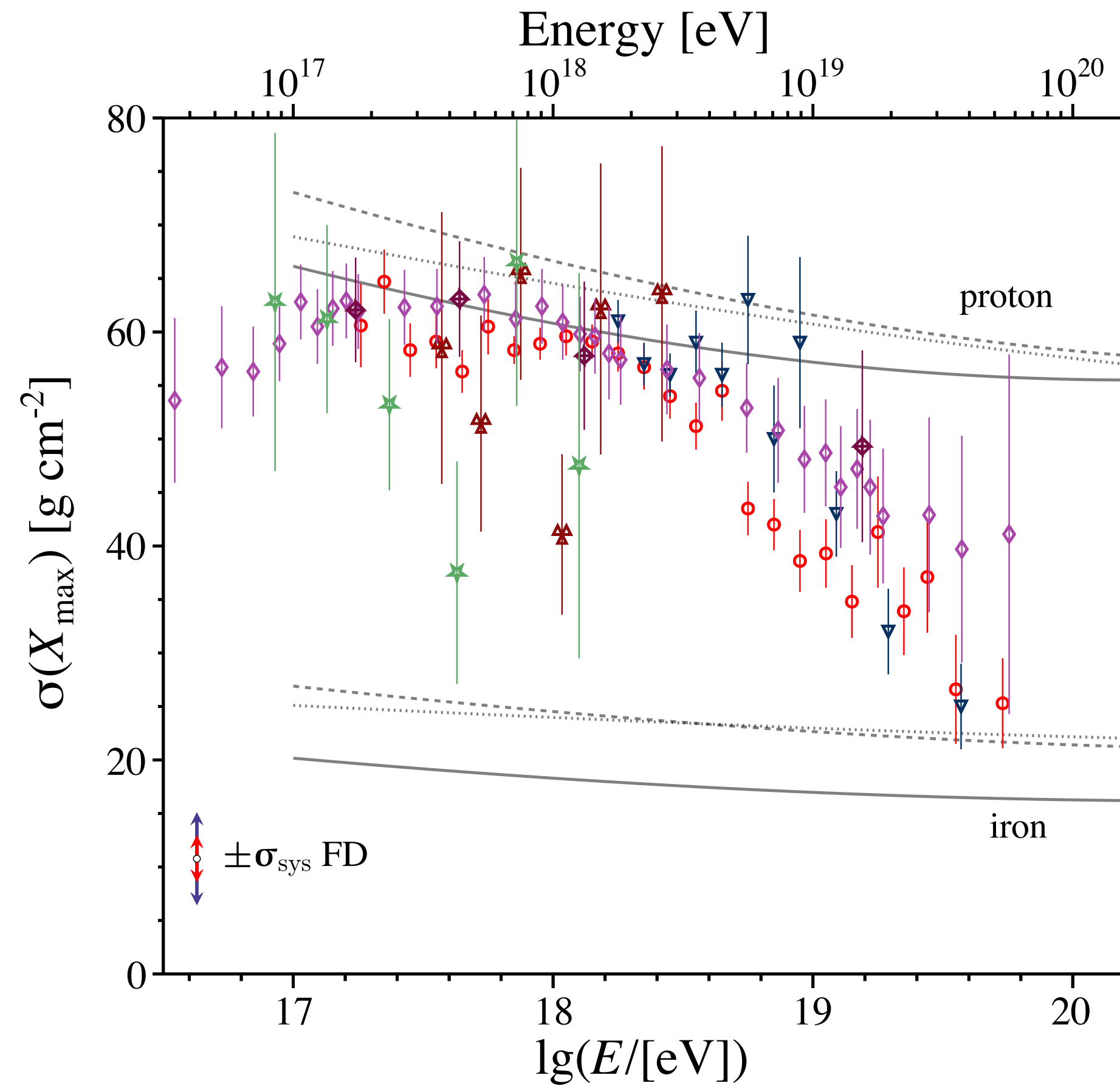
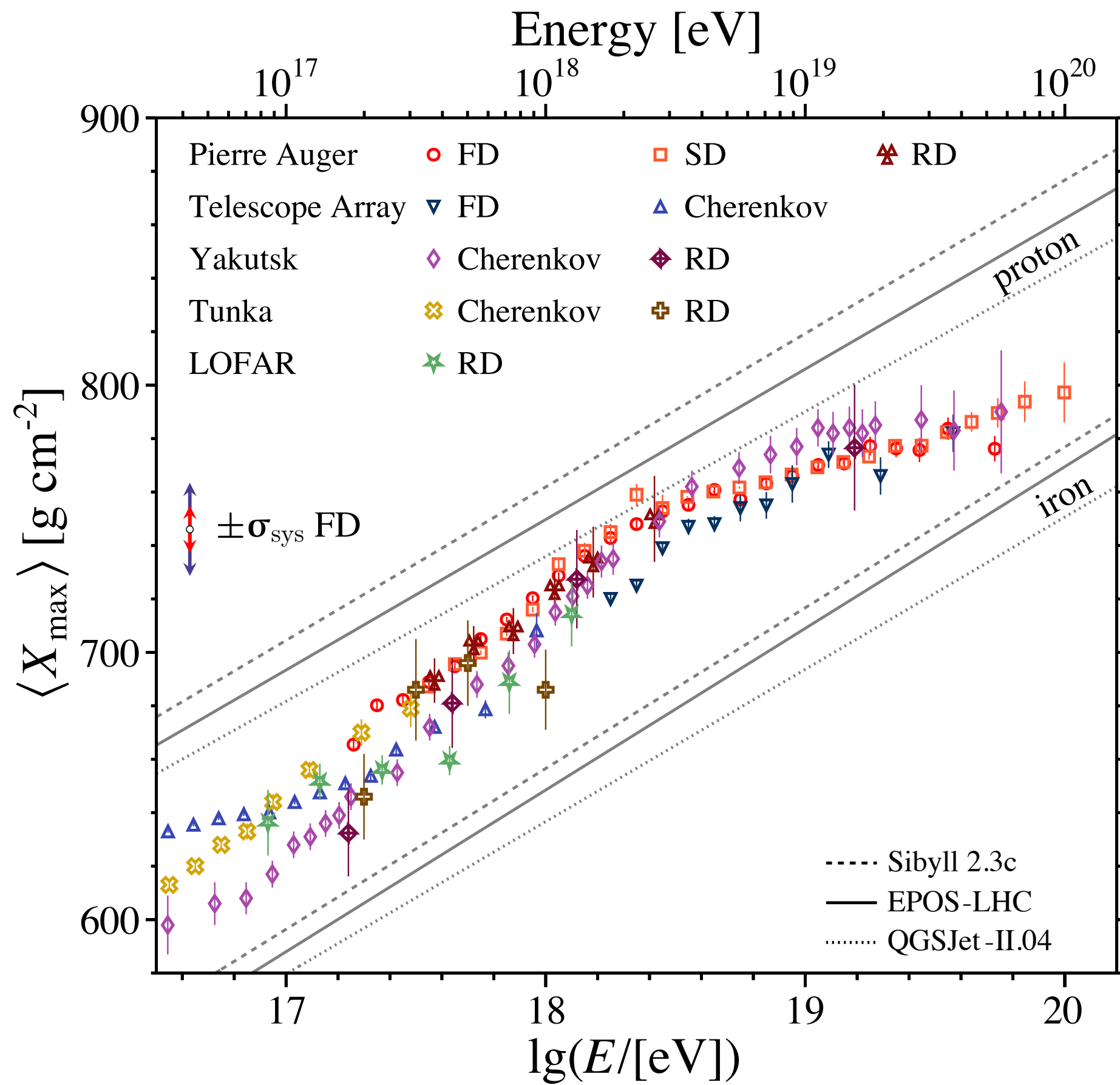
$$\langle X_{\max}(E) \rangle = X_0 \ln(E/n_{\text{tot}}) + c + \lambda_{\text{int}}$$

taking derivative $\log E$

$$D_e = \frac{d\langle X_{\max}(E) \rangle}{d \ln E} \leq X_0 - X_0 \frac{d \ln n_{\text{tot}}}{d \ln E} + \frac{d \lambda_{\text{int}}}{d \ln E}$$

Elongation rate of em. shower

Mass composition results – world data



$$\frac{dP}{dX_1} = \frac{1}{\lambda_{\text{int}}} e^{-X_1/\lambda_{\text{int}}}$$

Important: LHC-tuned interaction models used for interpretation

$$\sigma_{X_1,p} \sim 45 - 55 \text{ g/cm}^2$$

$$\sigma_{X_1,Fe} \sim 10 \text{ g/cm}^2$$

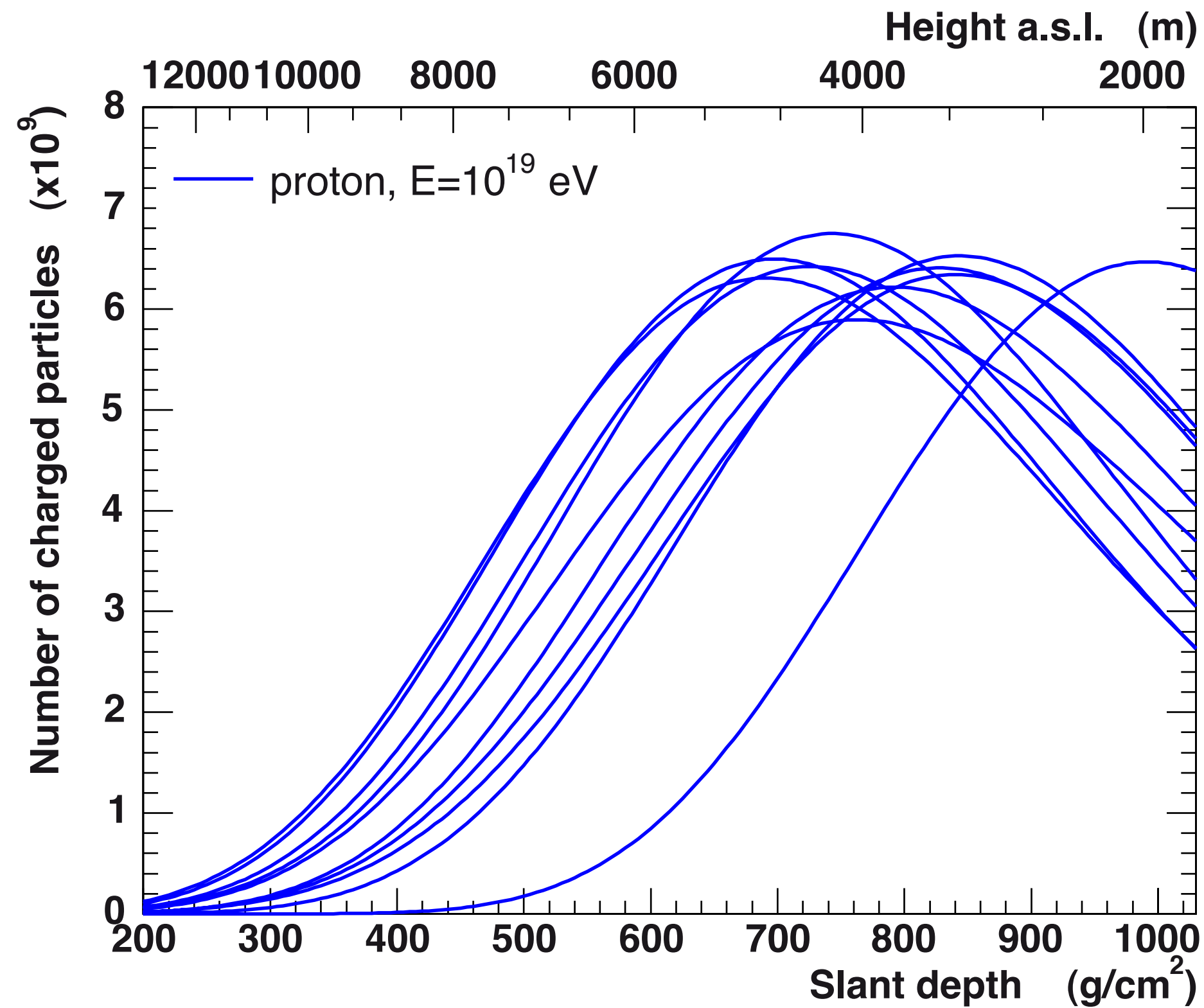
(Snowmass report UHECR composition, 2022)

(Phys. Rev. D96 (2017), 122003)

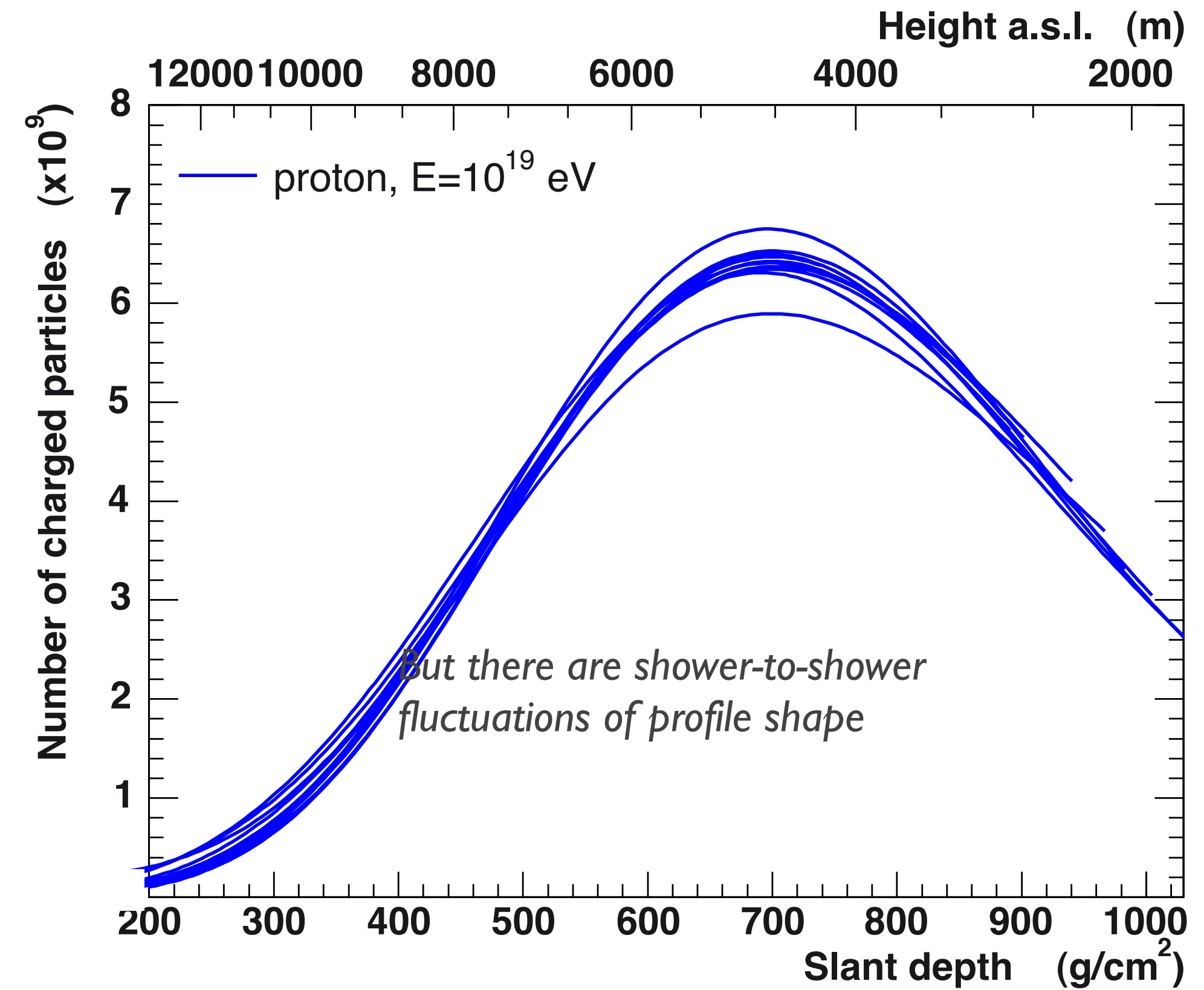
($E \sim 10^{18}$ eV)

Universality features of high-energy shower profiles

Simulated shower profiles

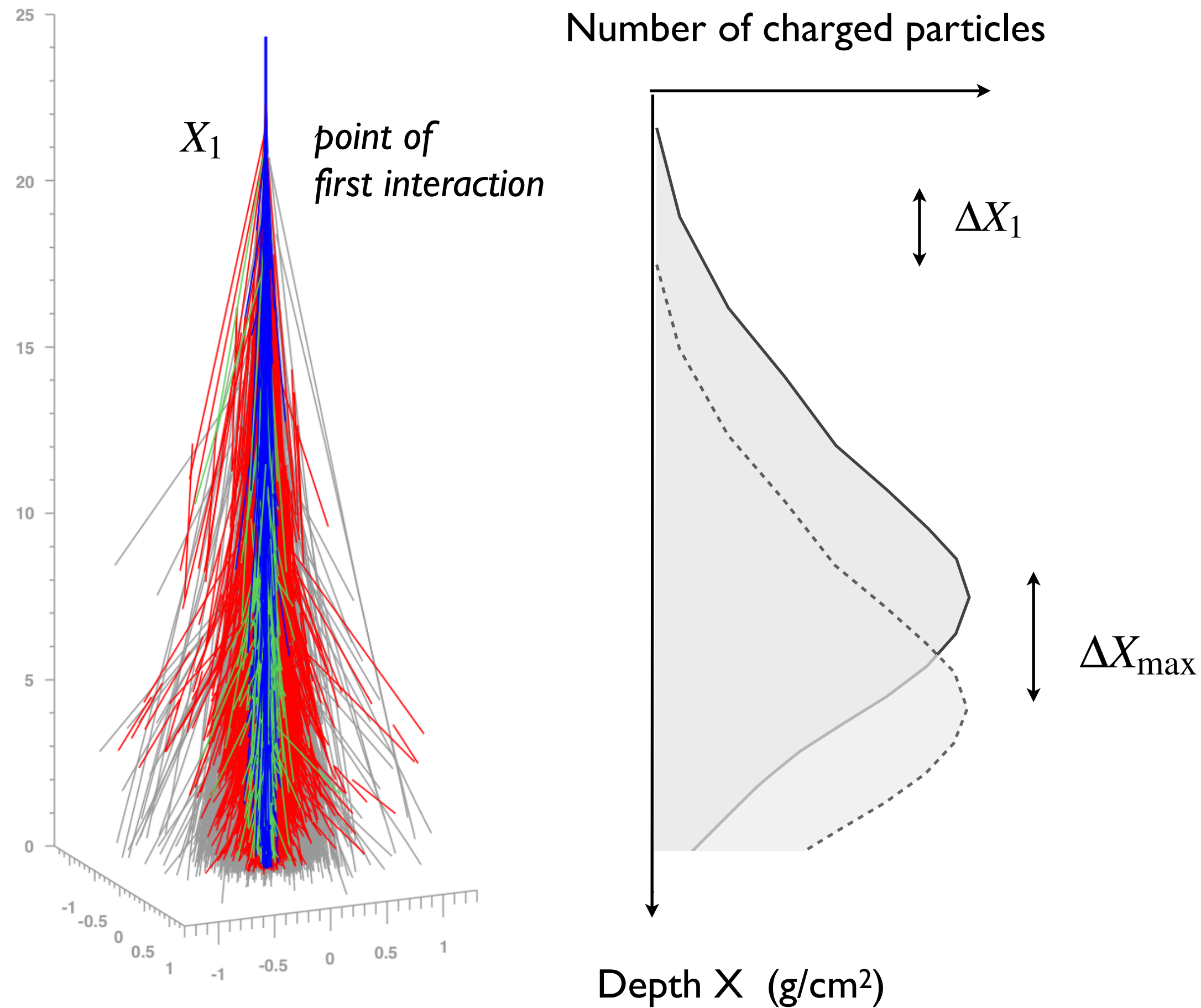


Profiles shifted in depth



Depth of first interaction X_I and X_{max} strongly correlated, use X_{max} for analysis

Measurement of proton-air cross section

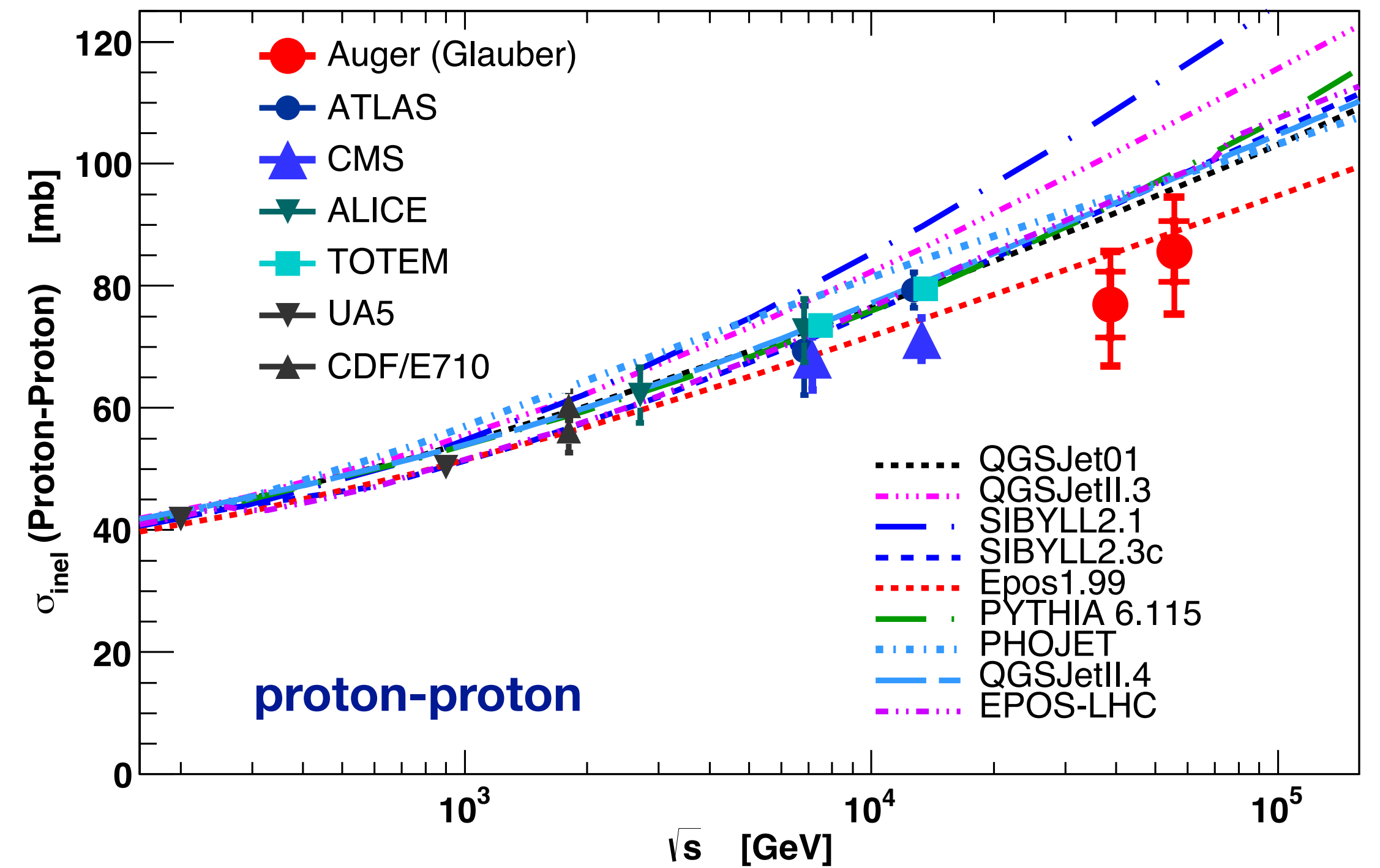


$$\frac{dP}{dX_1} = \frac{1}{\lambda_{\text{int}}} e^{-X_1/\lambda_{\text{int}}}$$

$$\sigma_{\text{p-air}} = \frac{\langle m_{\text{air}} \rangle}{\lambda_{\text{int}}}$$

Difficulties

- mass composition
- fluctuations in shower development (model needed for correction)



Electromagnetic energy and energy transfer

Hadronic energy

$$\frac{2}{3}E_0$$

$$\frac{2}{3} \left(\frac{2}{3}E_0 \right)$$

⋮

$$E_{\text{had}} = \left(\frac{2}{3} \right)^n E_0$$

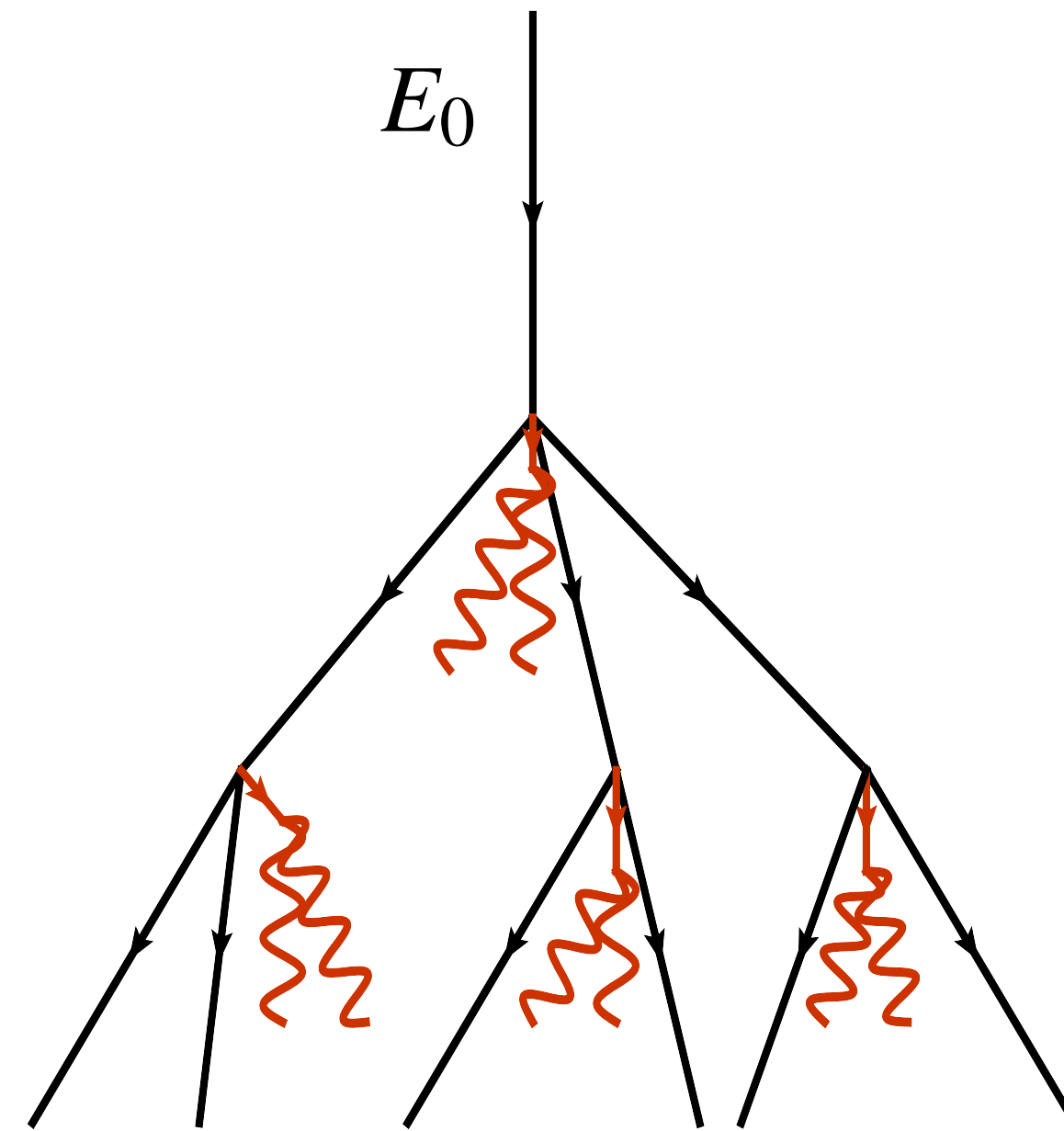
Electromagnetic energy

$$\frac{1}{3}E_0$$

$$\frac{1}{3}E_0 + \frac{1}{3} \left(\frac{2}{3}E_0 \right)$$

⋮

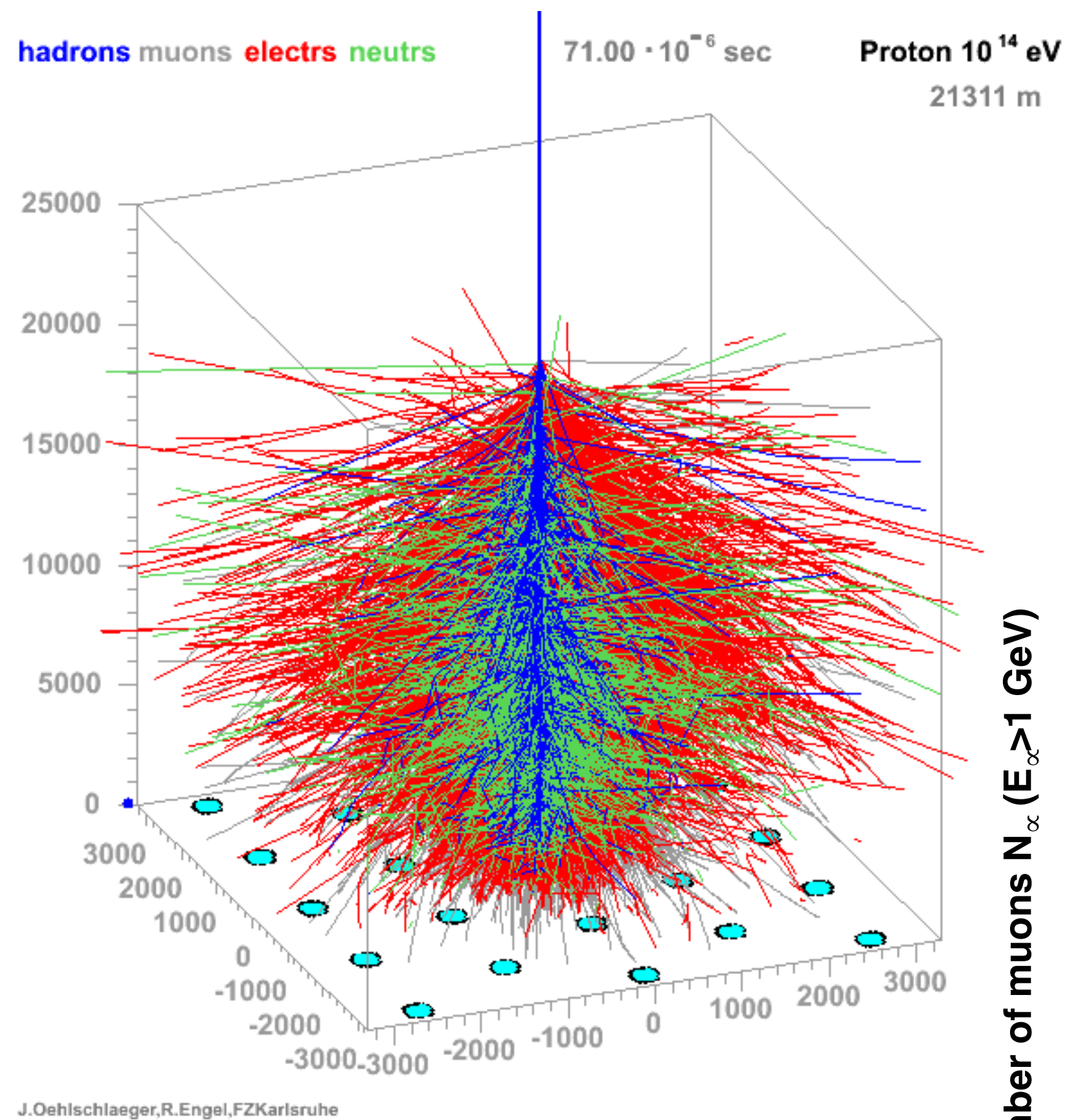
$$E_{\text{em}} = \left[1 - \left(\frac{2}{3} \right)^n \right] E_0$$



After n generations ...

$$\begin{aligned} n = 5, & \quad E_{\text{had}} \sim 12\% \\ n = 6, & \quad E_{\text{had}} \sim 8\% \end{aligned}$$

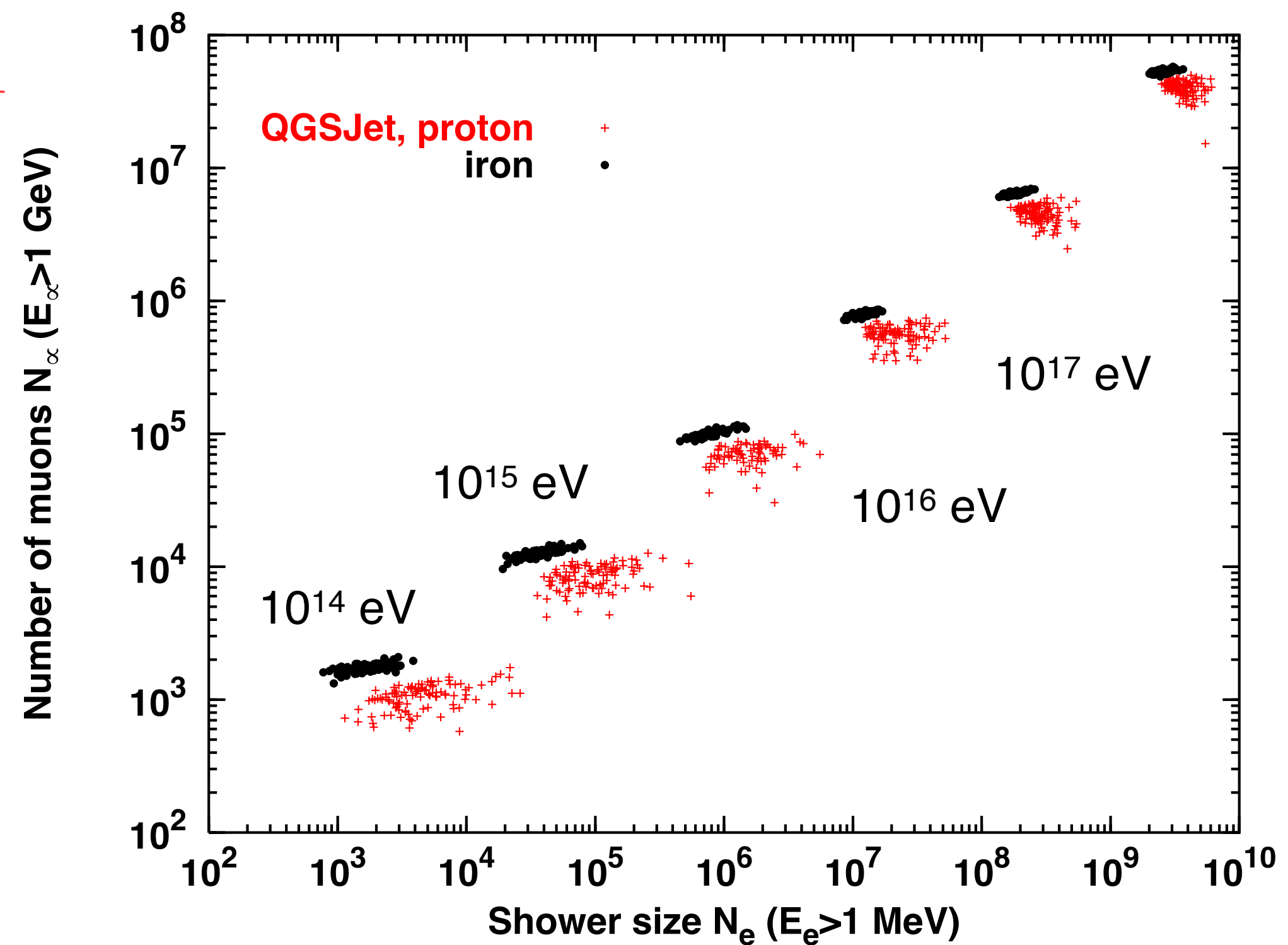
Air shower ground arrays: N_e and N_μ



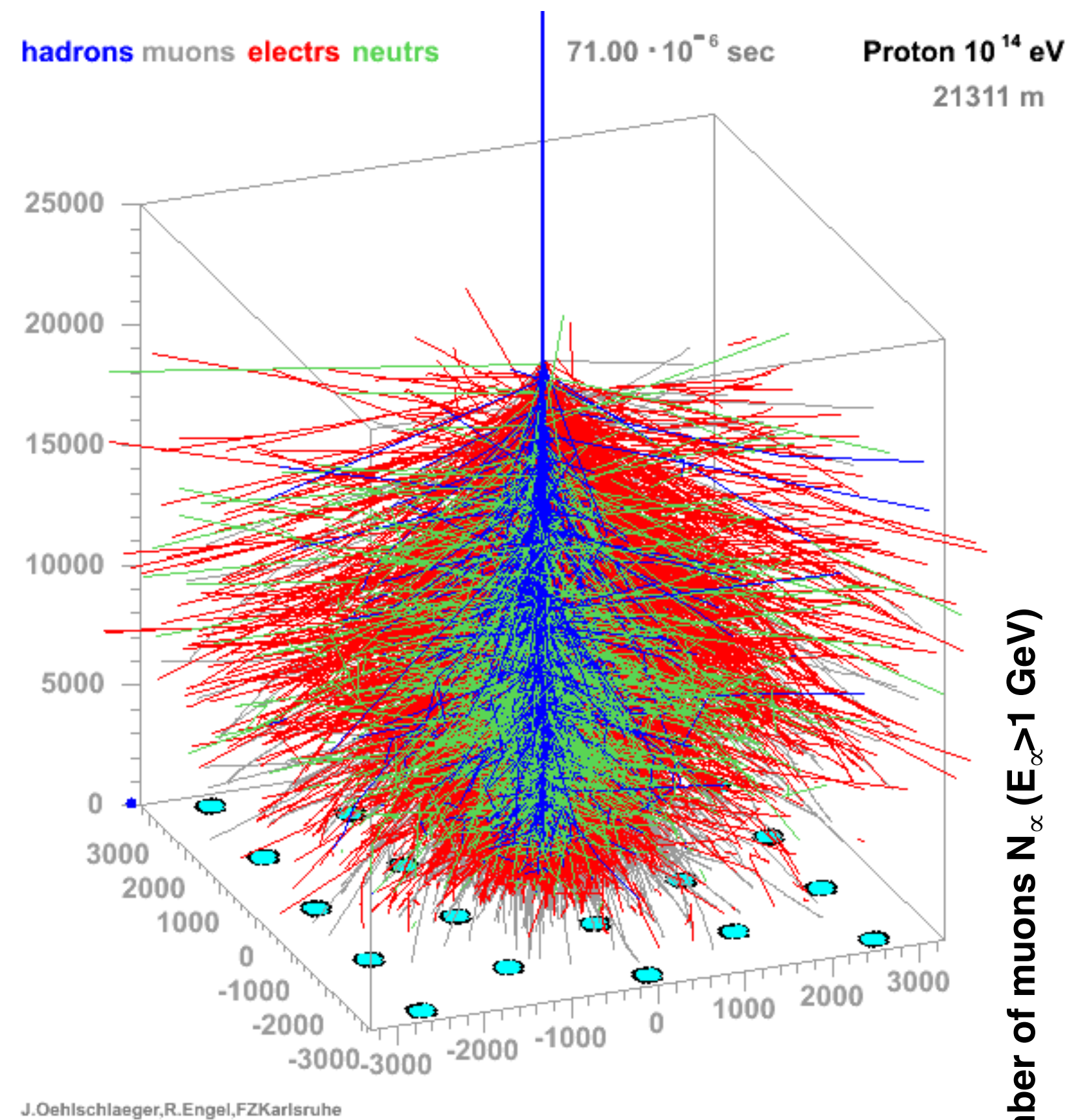
KASCADE and KASCADE-Grande

Energy conservation

$$\ln E = a \cdot \ln N_e + b \cdot \ln N_\mu$$



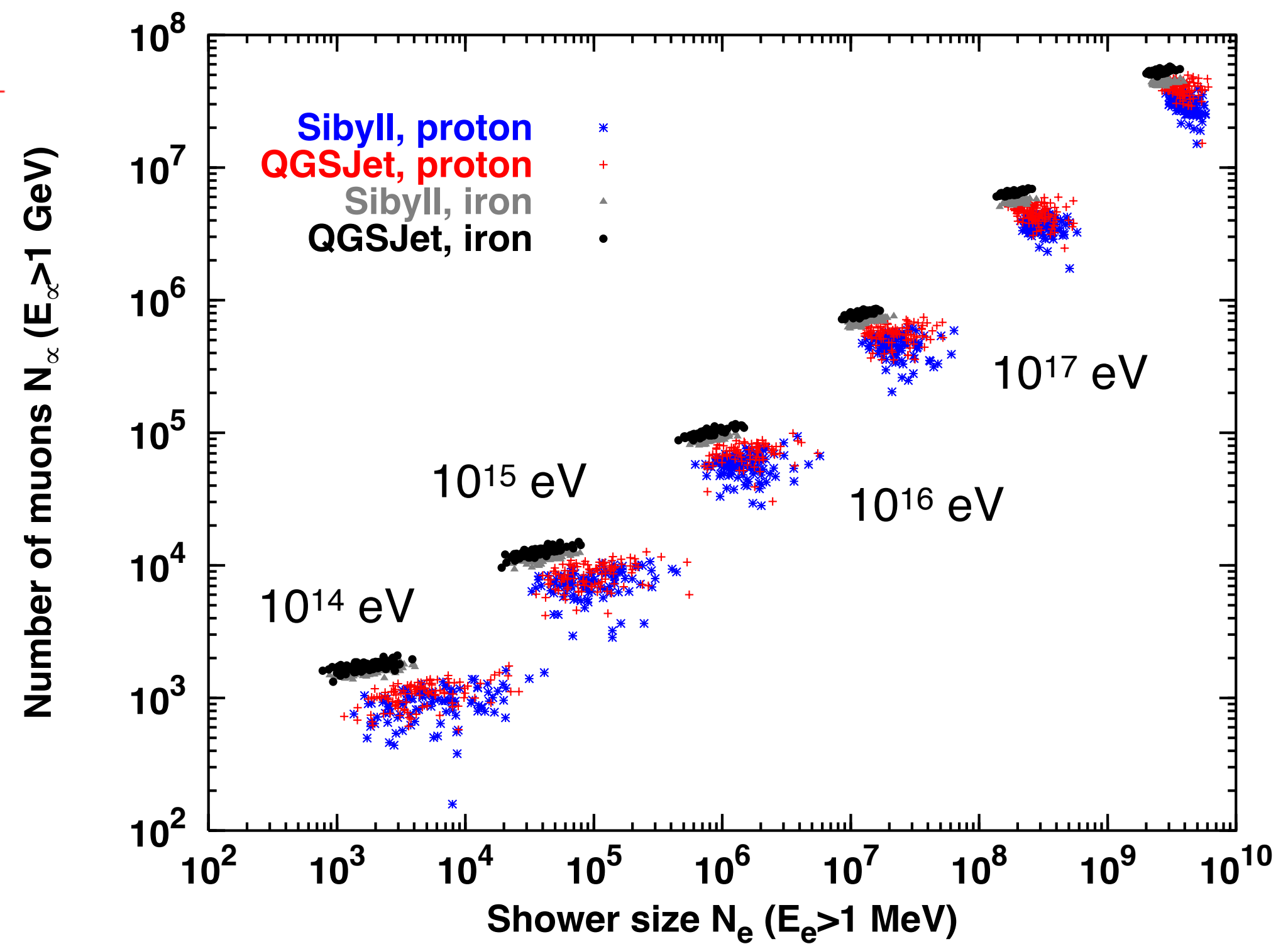
Air shower ground arrays N_μ



KASCADE and KASCADE-Grande

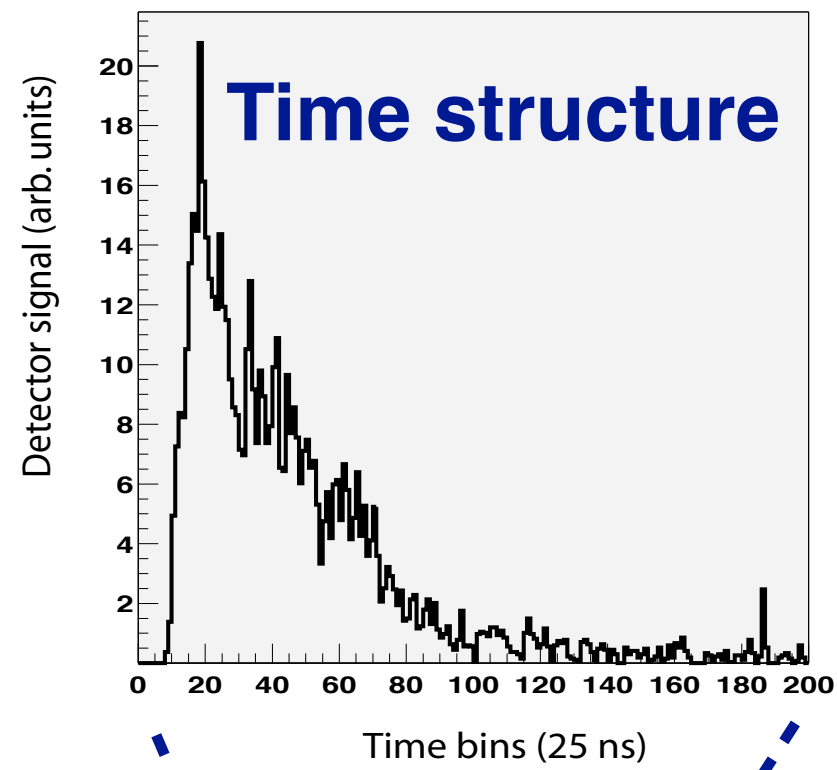
Energy conservation

$$\ln E = a \cdot \ln N_e + b \cdot \ln N_\mu$$

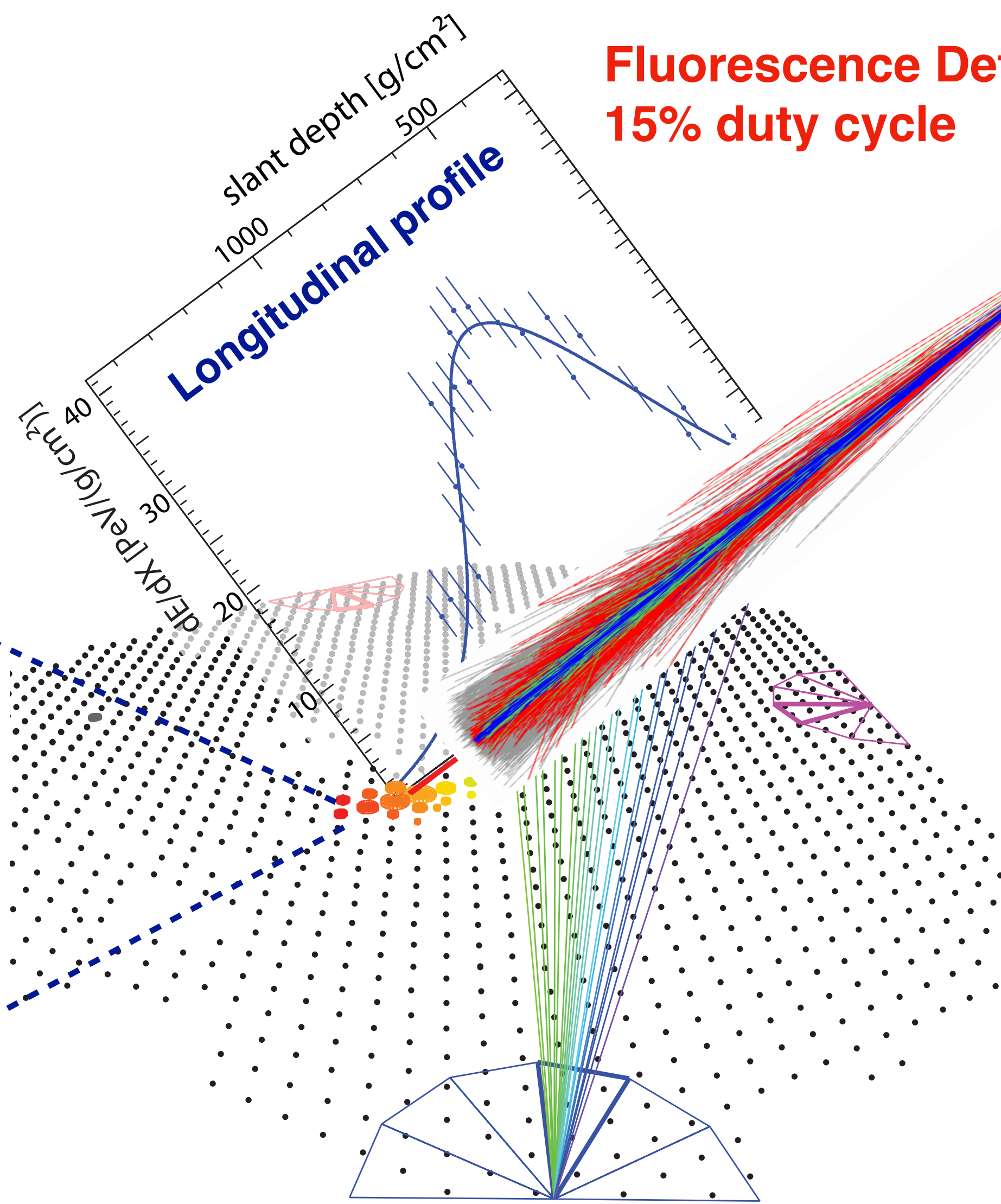
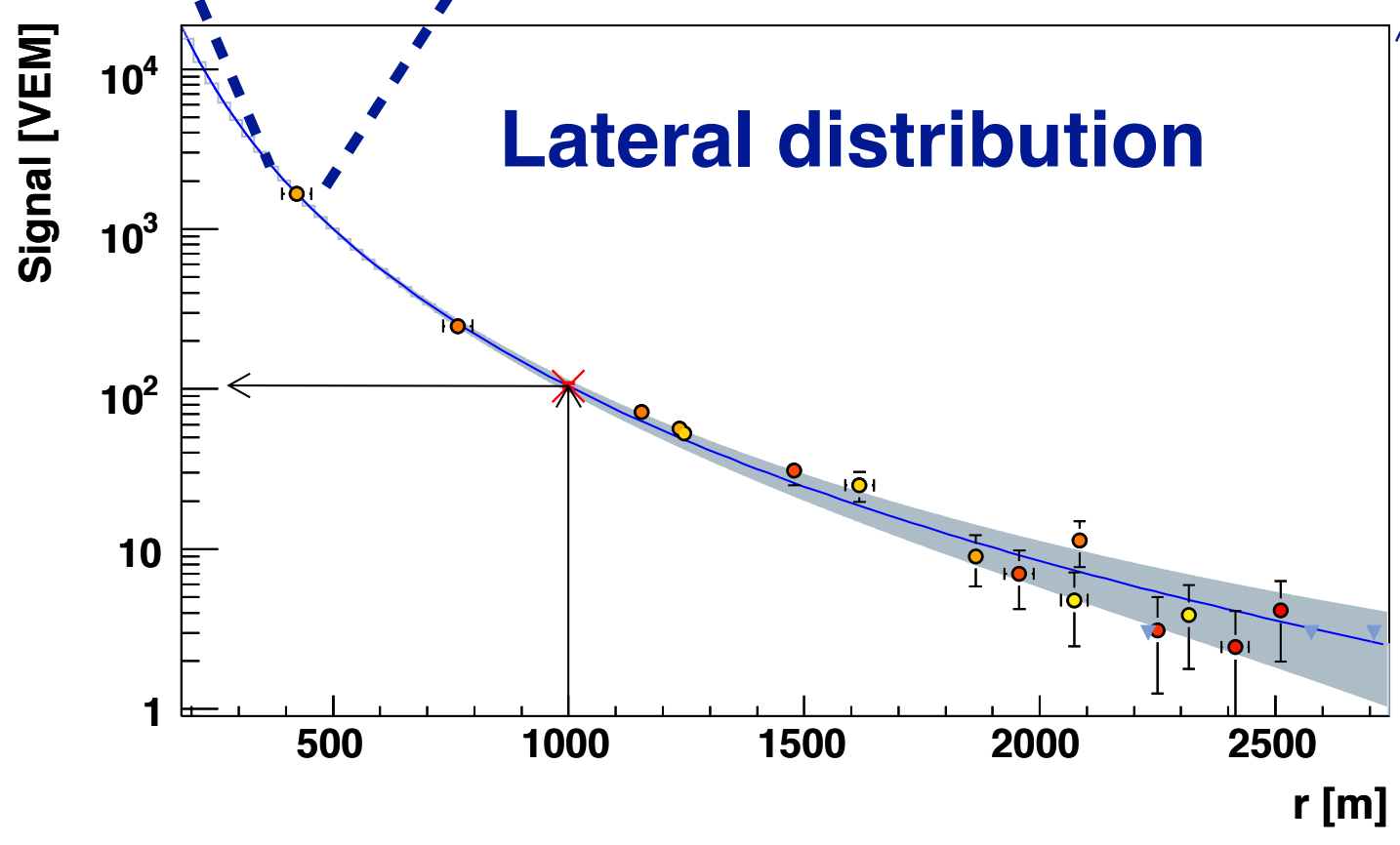


2. Overall description of air shower data

Air shower observables (Auger hybrid observation)



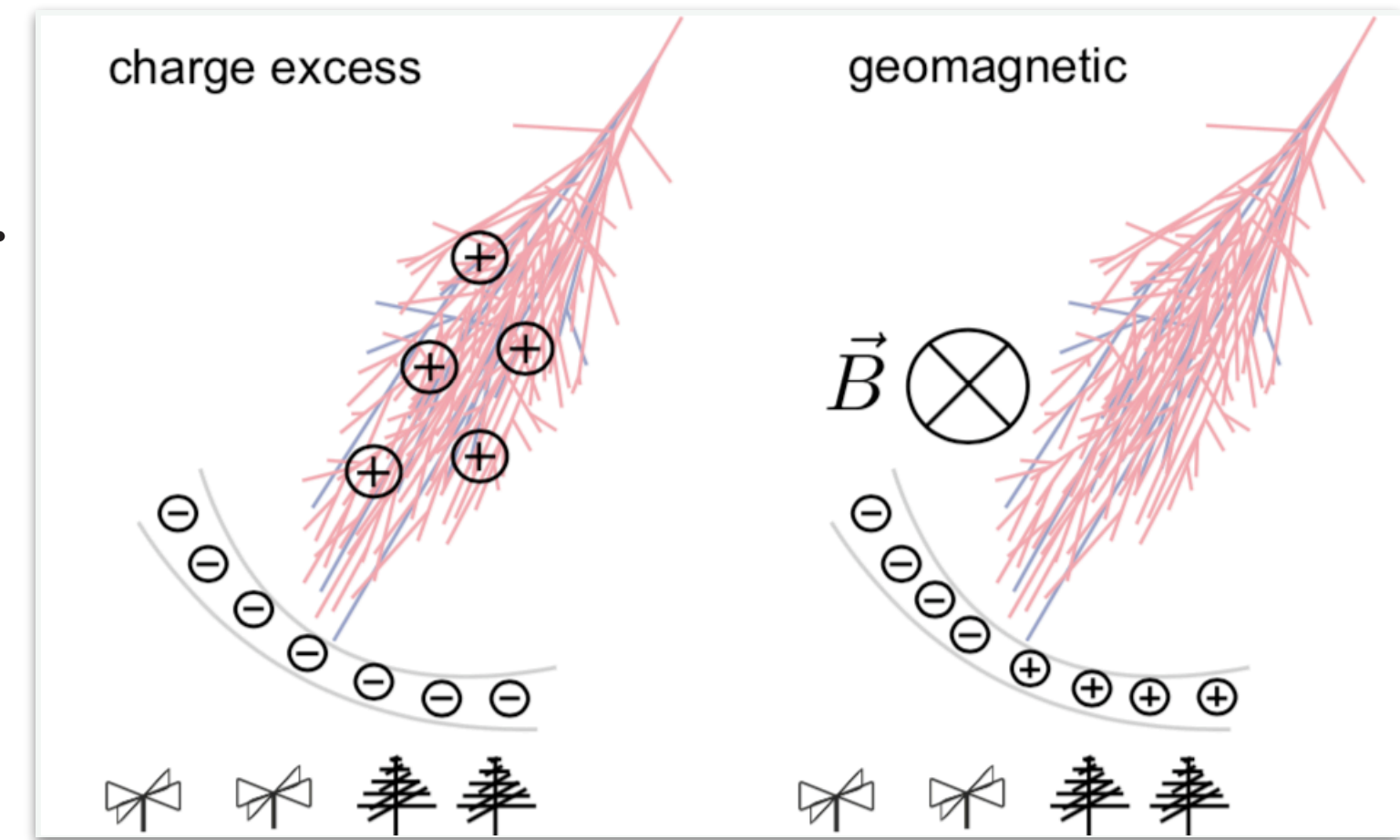
$$E_{\text{rec}} = f(S_{1000}, \theta)$$



Fluorescence Detector (FD):
15% duty cycle

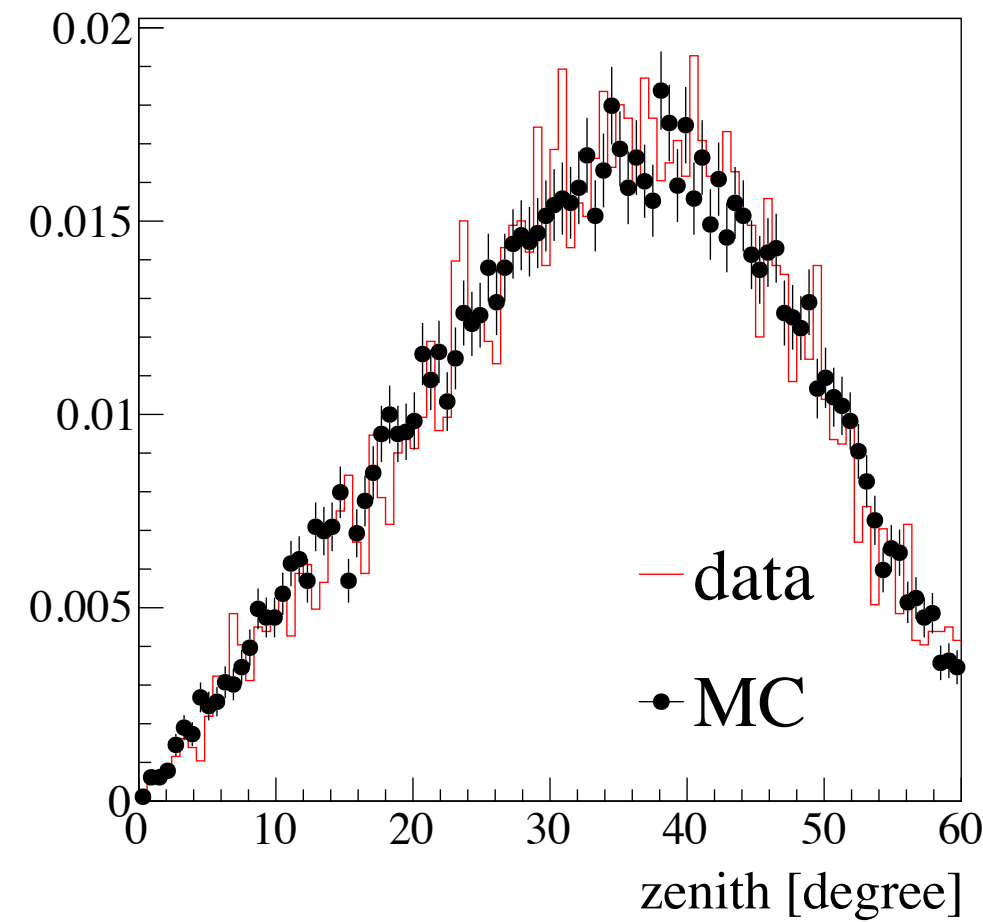
$$E_{\text{cal}} = \int_0^\infty \left(\frac{dE}{dX} \right)_{\text{obs}} dX$$

Radio Detector (RD):
100% duty cycle

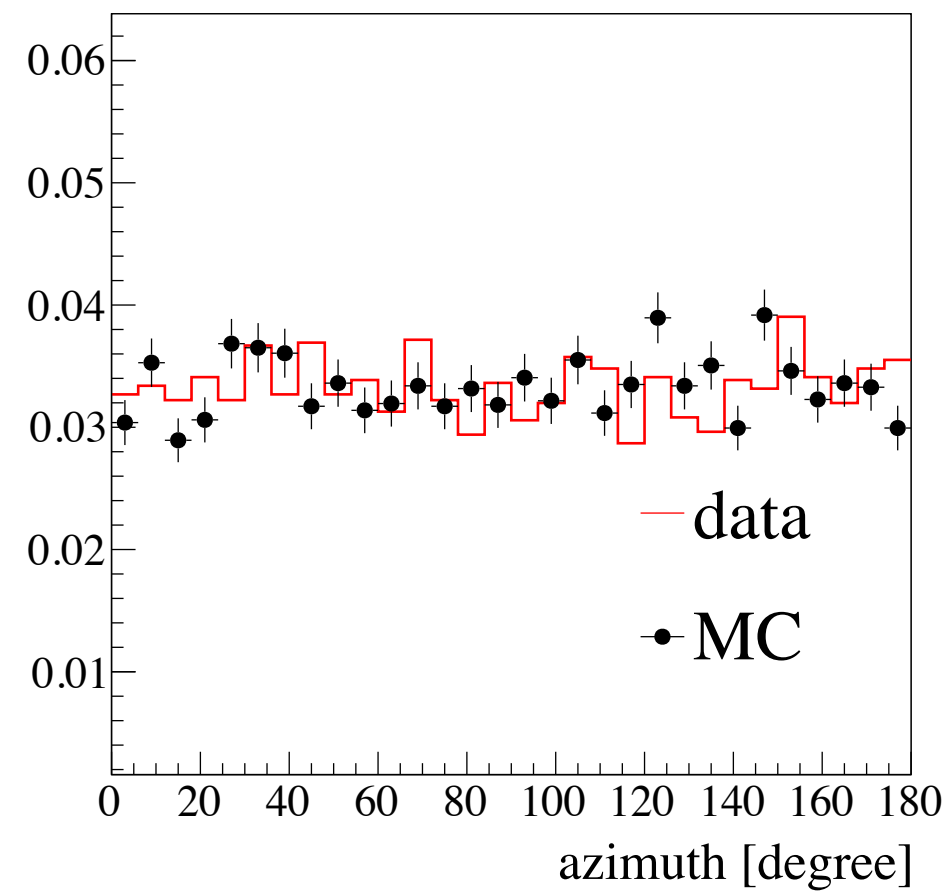


Surface Detector (SD)
100% duty cycle

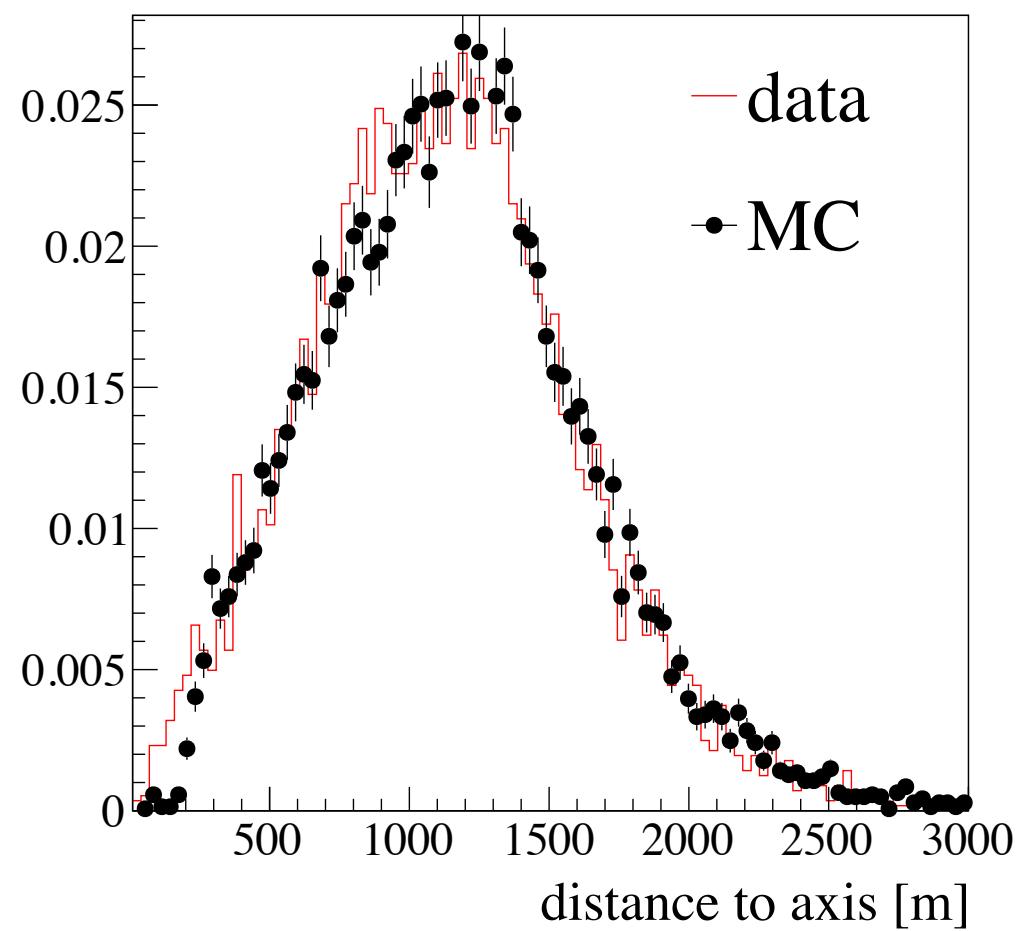
Auger event simulation for surface array



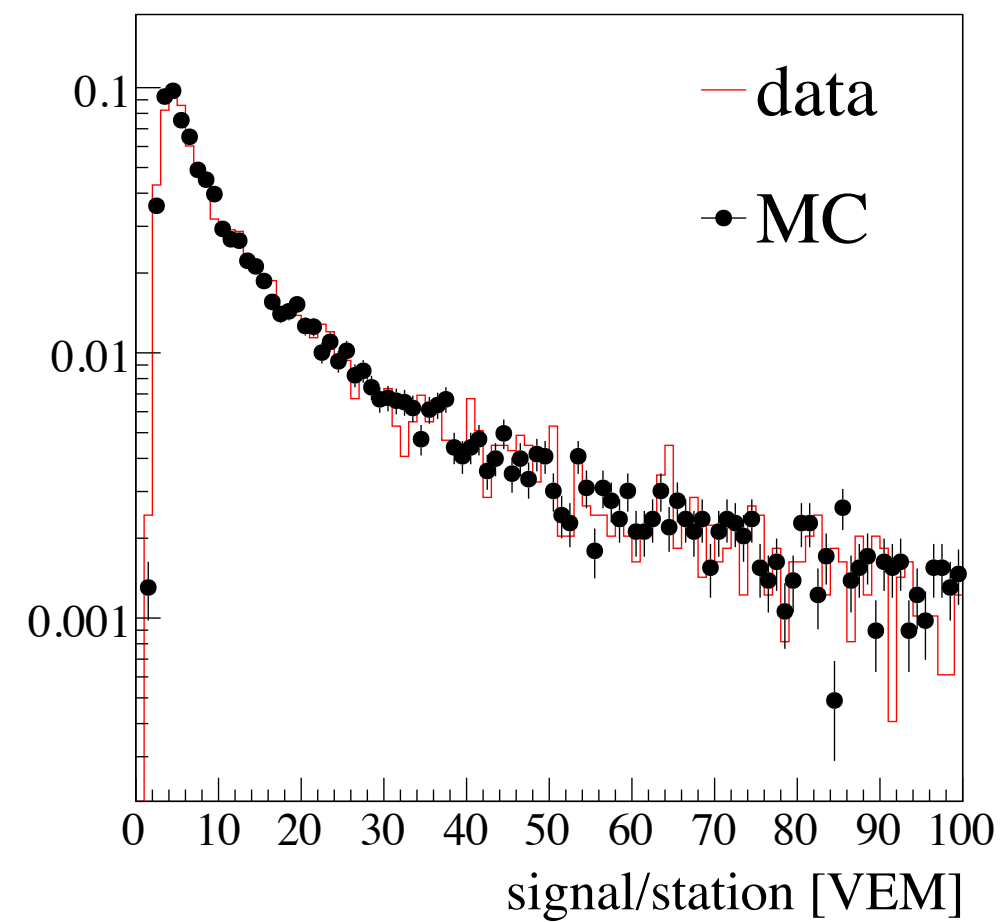
Zenith angle



Azimuth angle

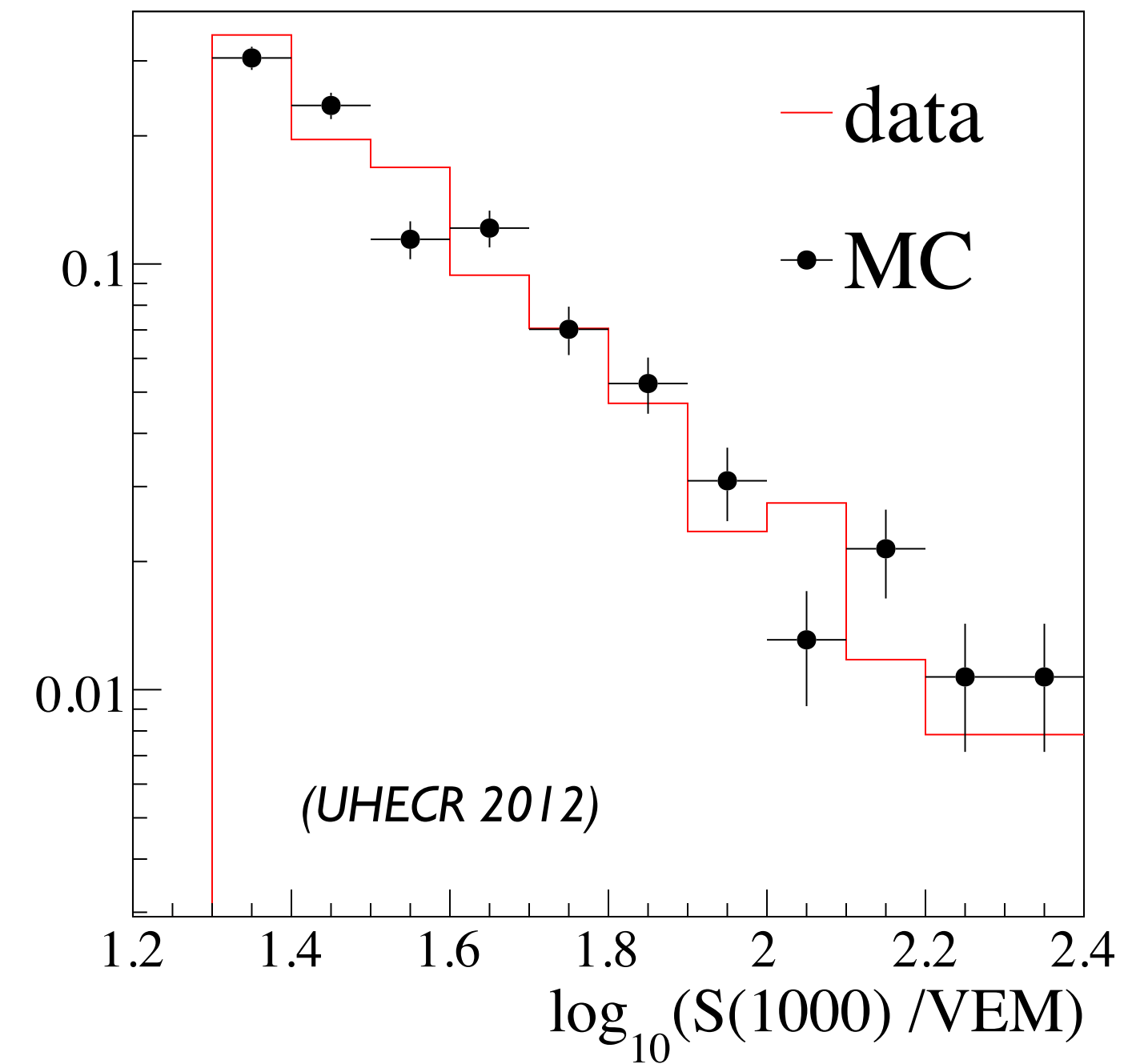


Distance of triggered stations



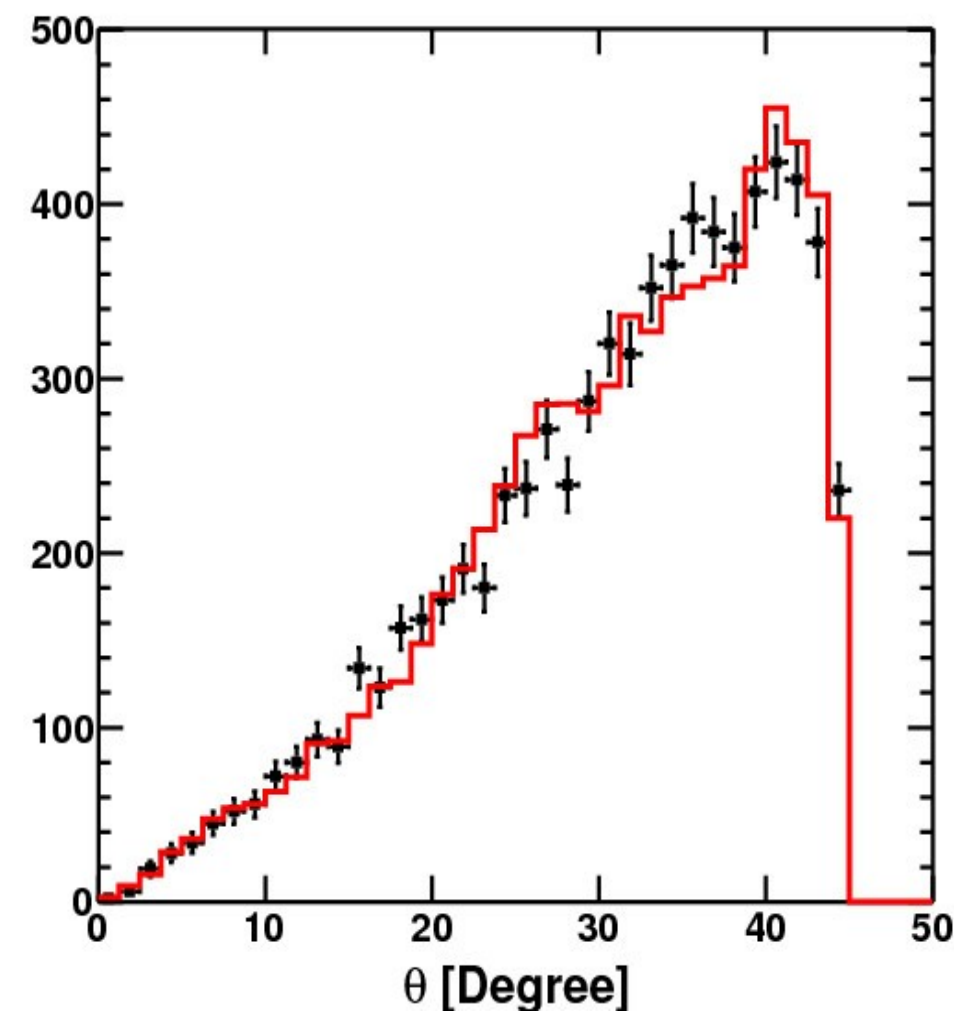
Signal per station

CORSIKA + full detector simulation
(50% p + 50% Fe)

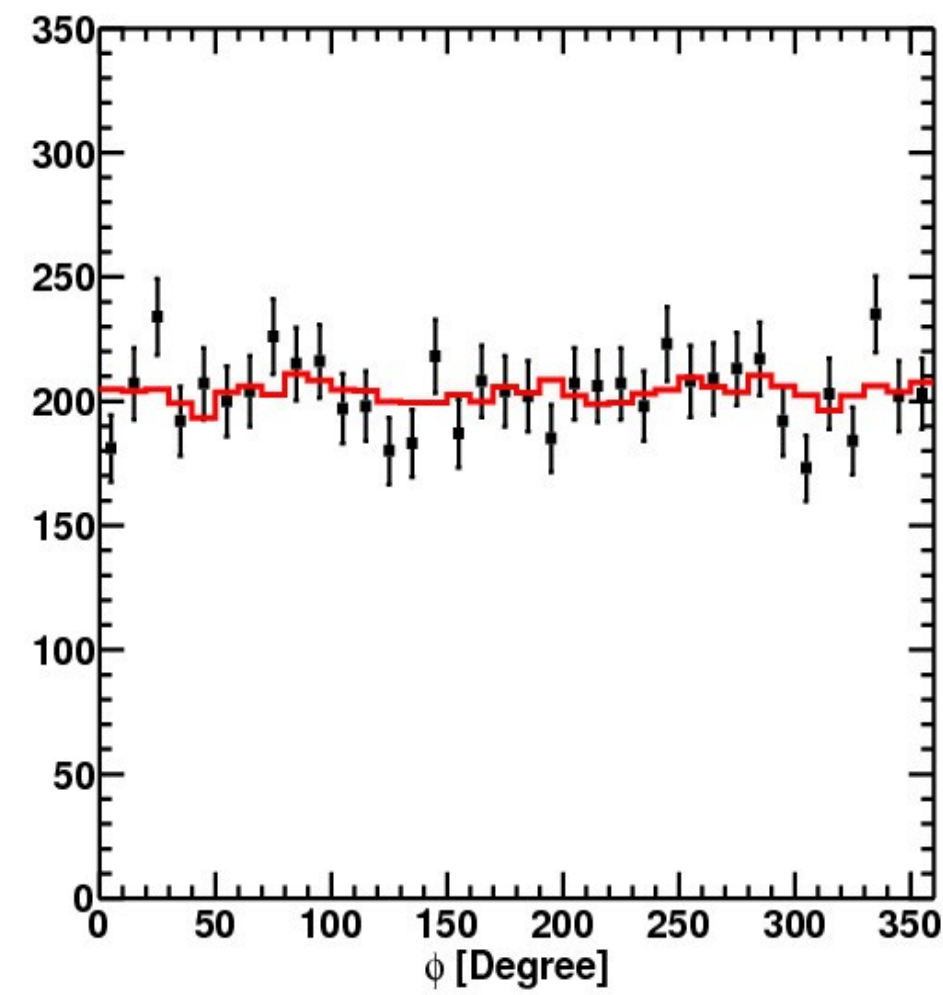


Very good agreement

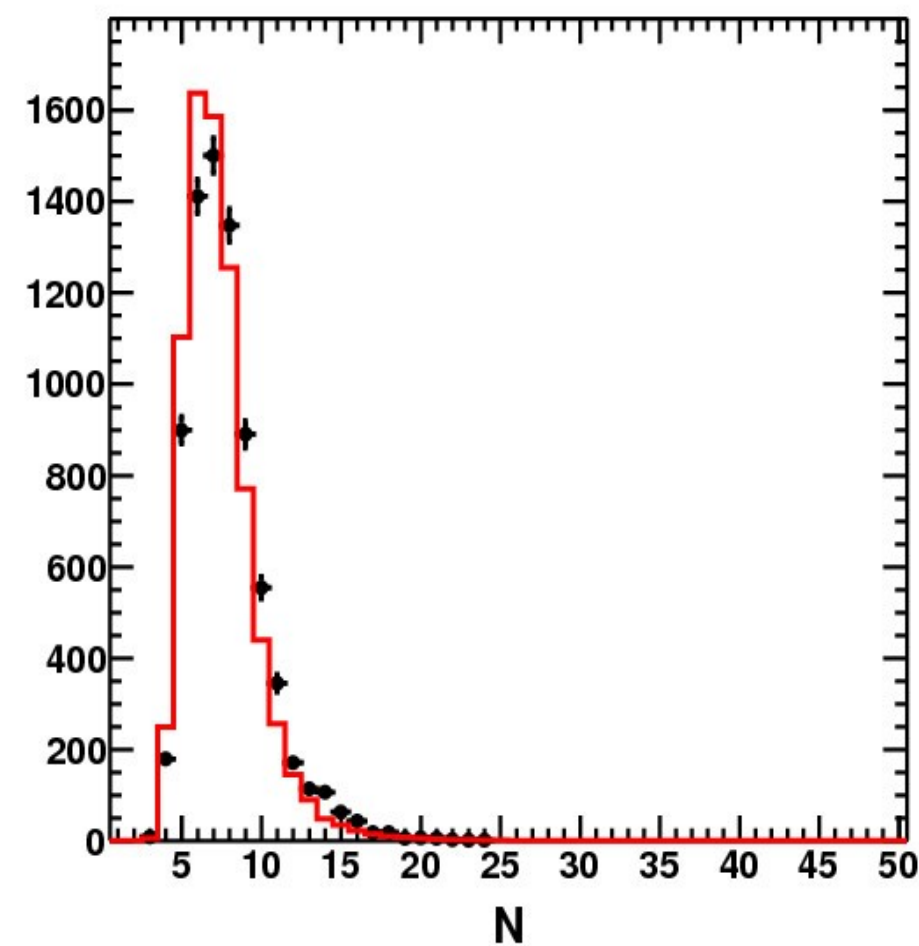
Telescope Array event simulation for surface array



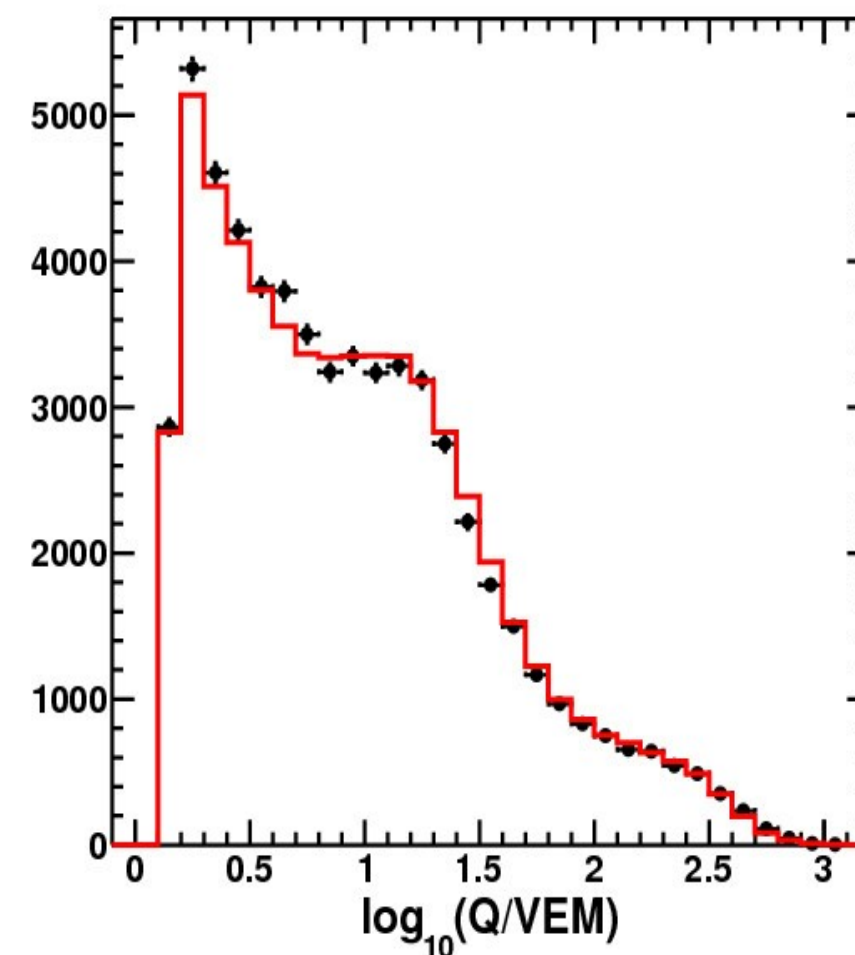
Zenith Angle



Azimuth Angle

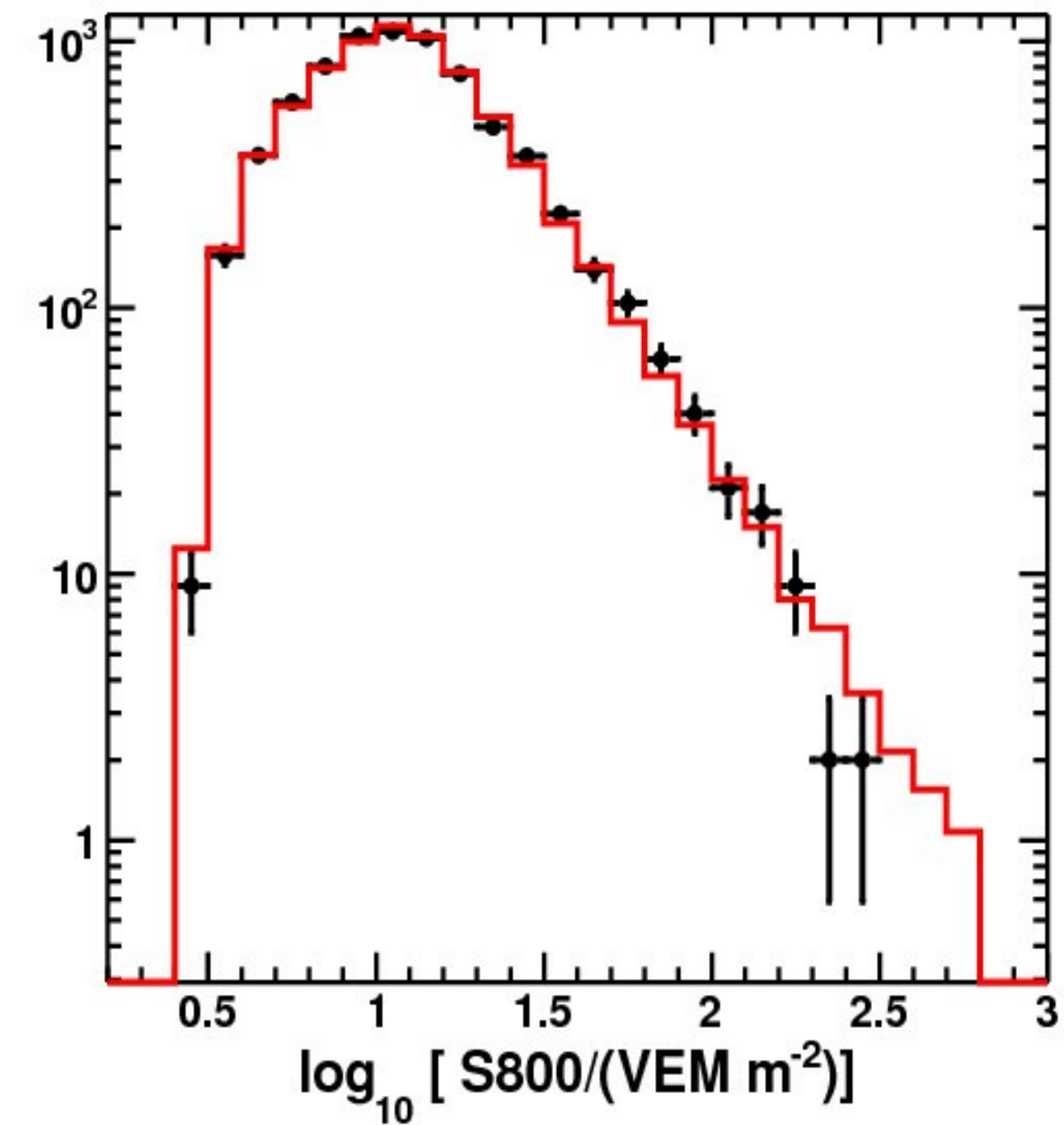


Number of Good Counters/Event



Charge/Counter/Event

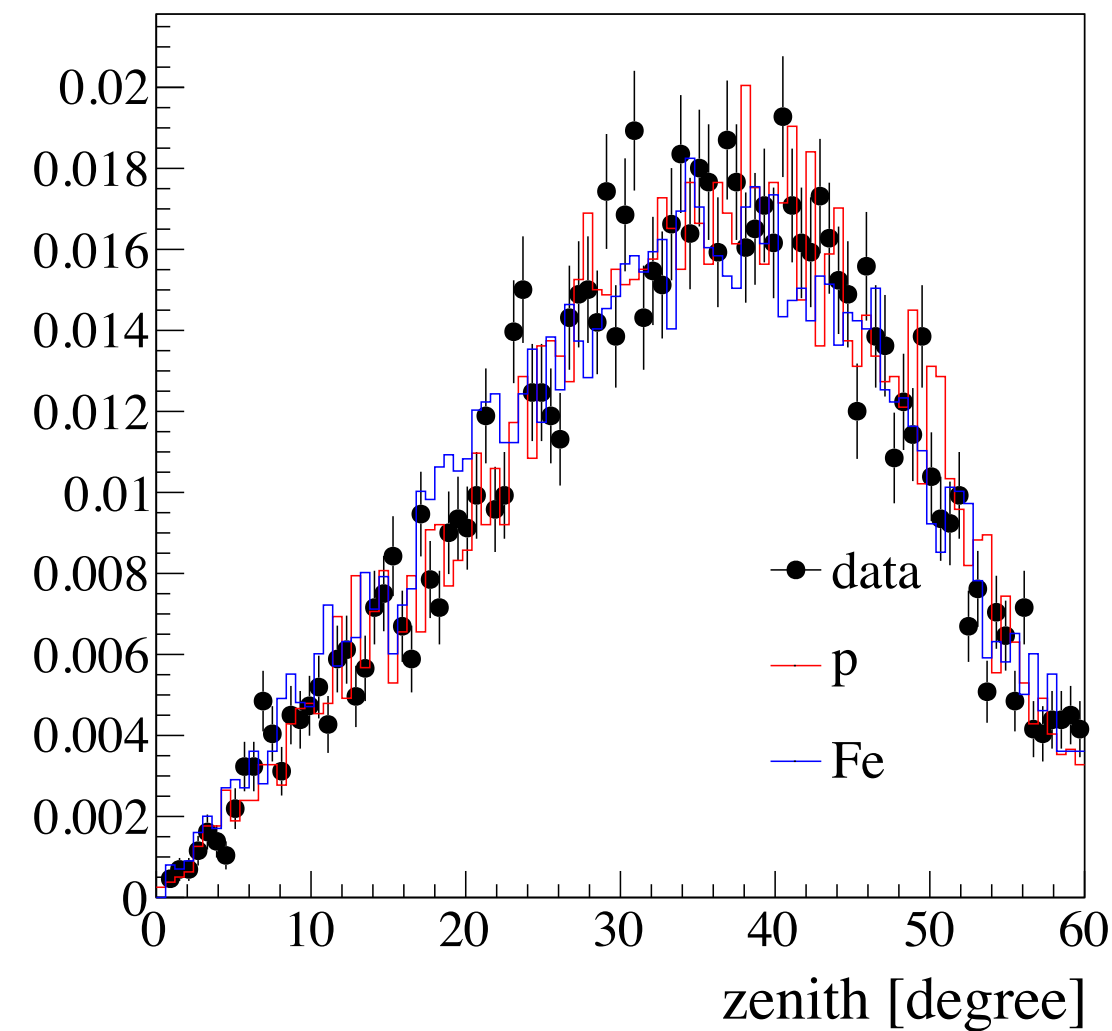
CORSIKA + full detector simulation
(proton primaries)



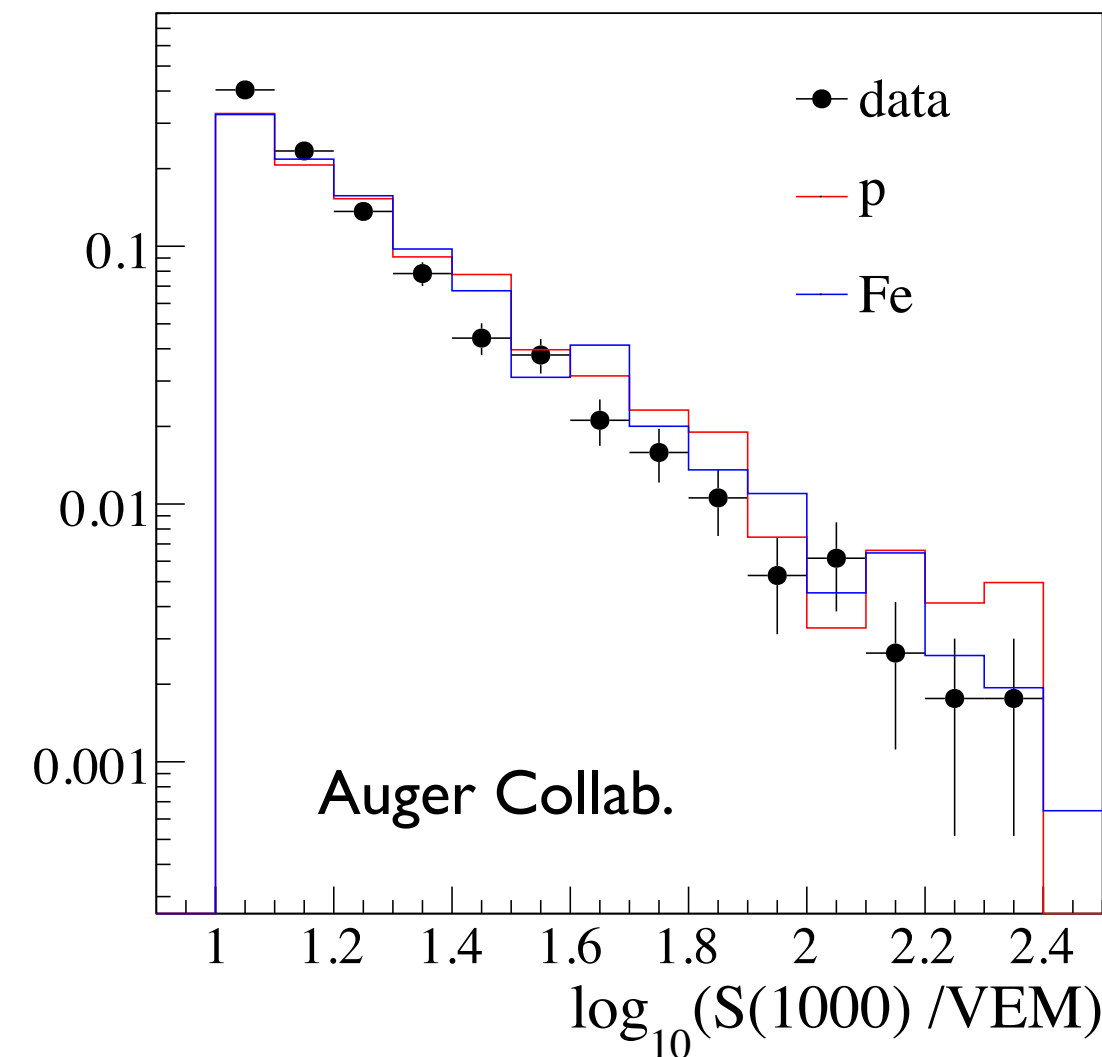
(UHECR 2012)

Very good agreement

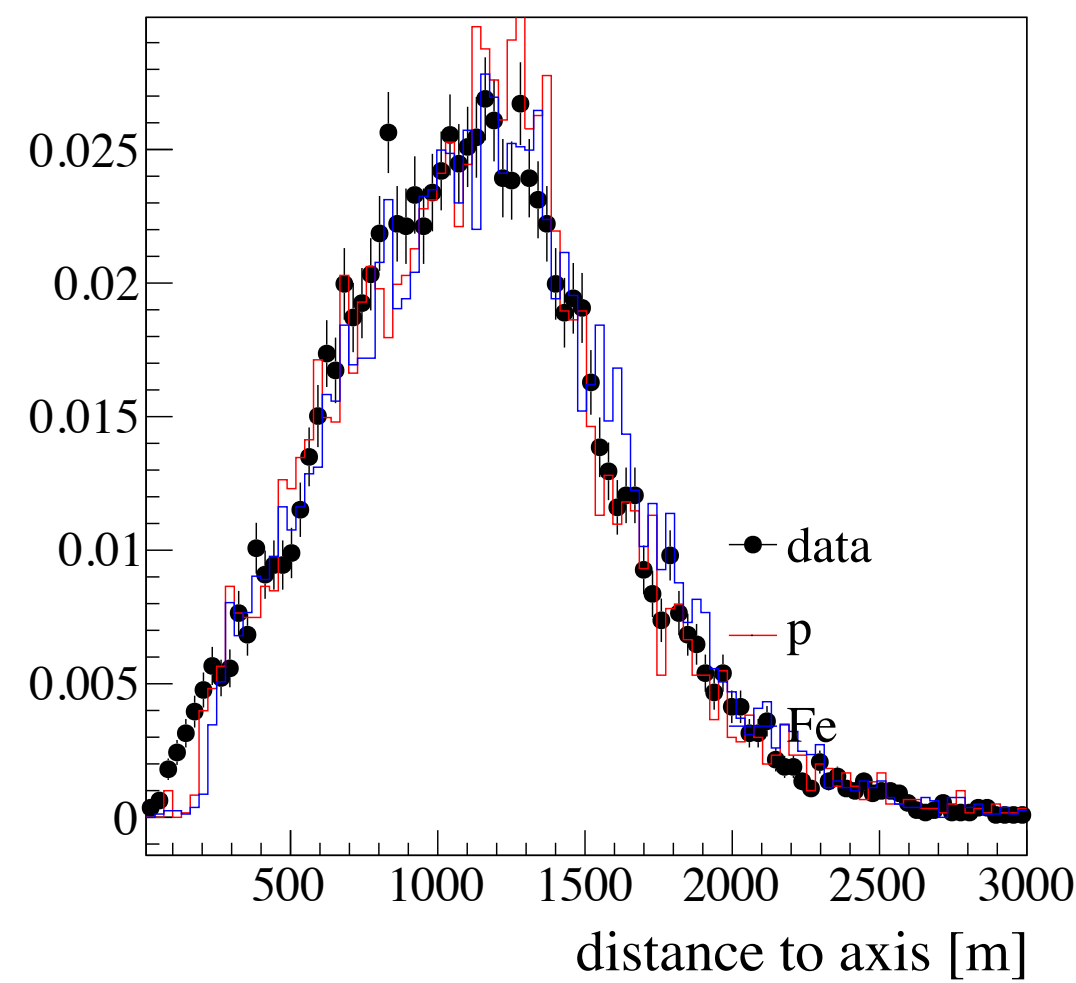
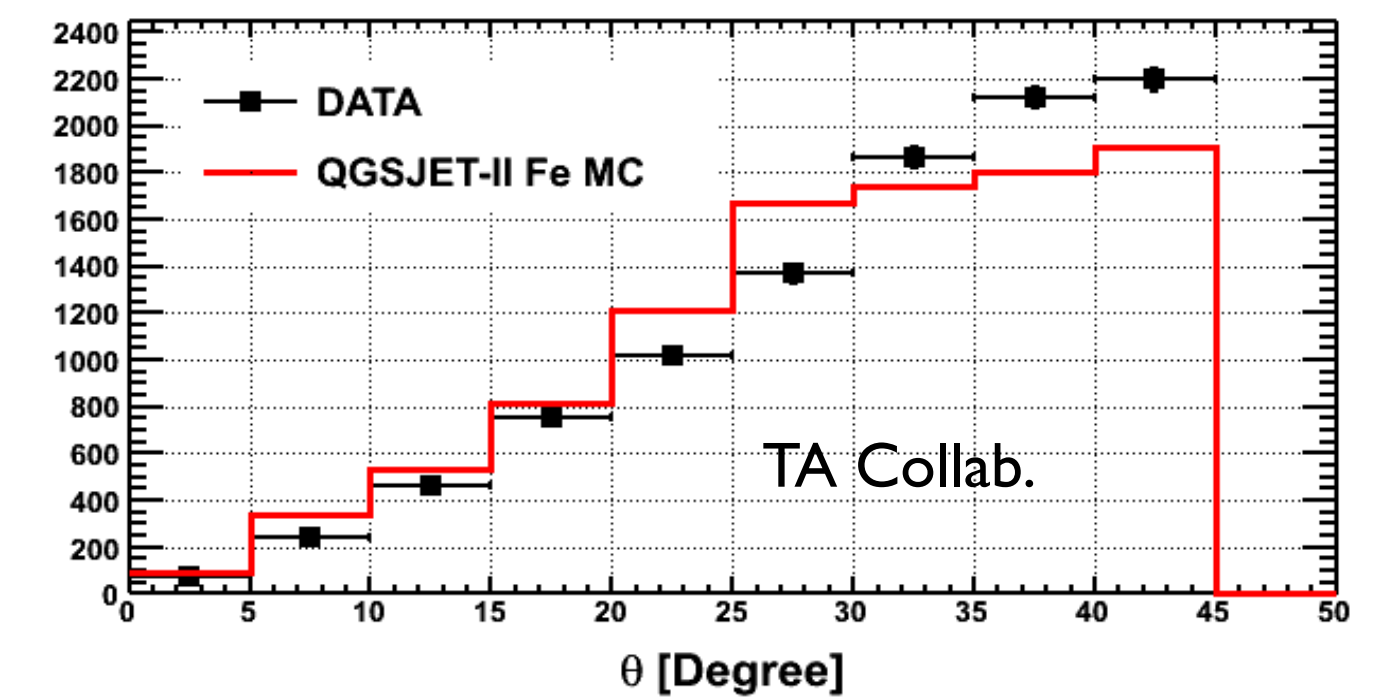
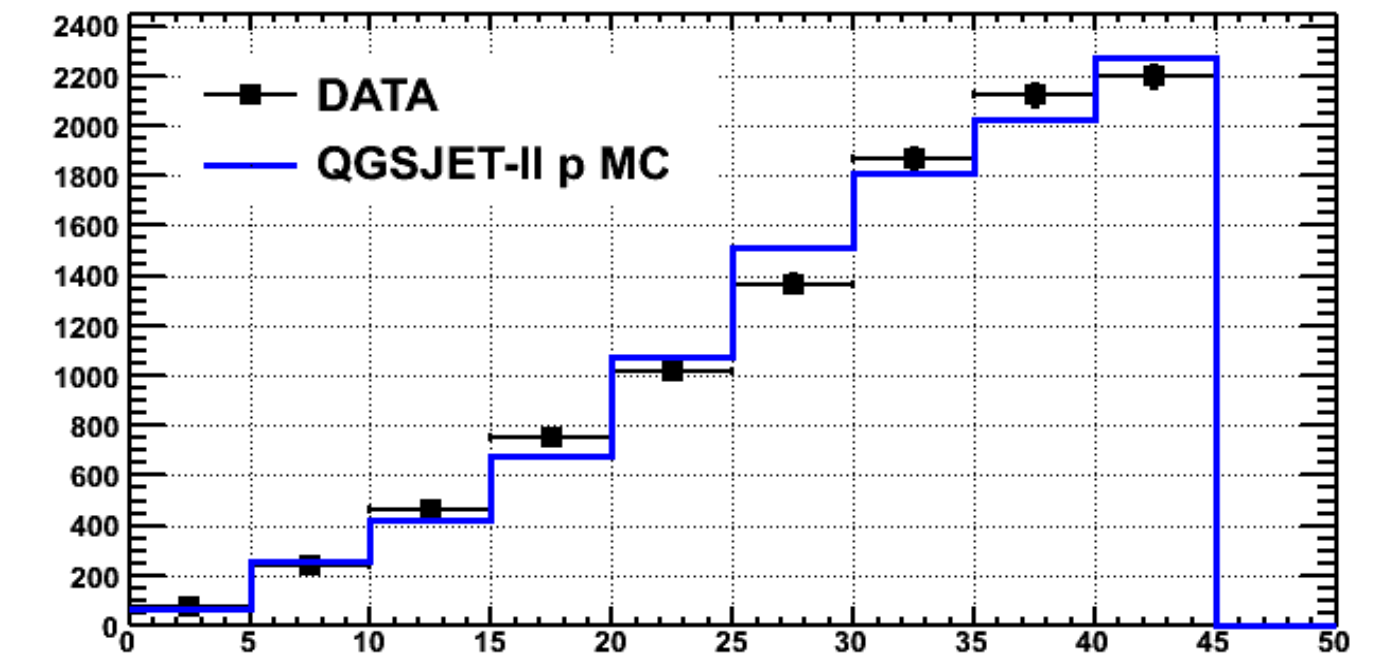
Composition sensitivity of data description?



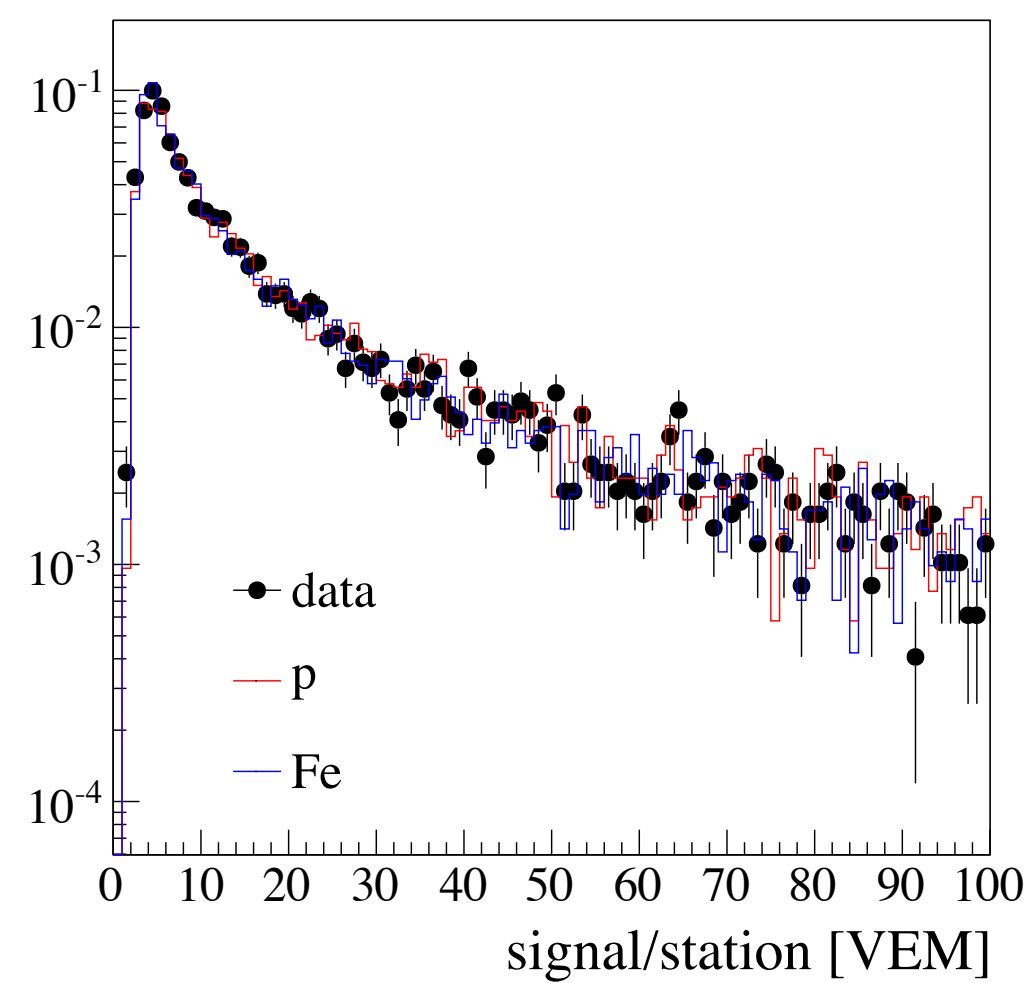
Zenith angle



Auger Collab.



Distance of triggered stations

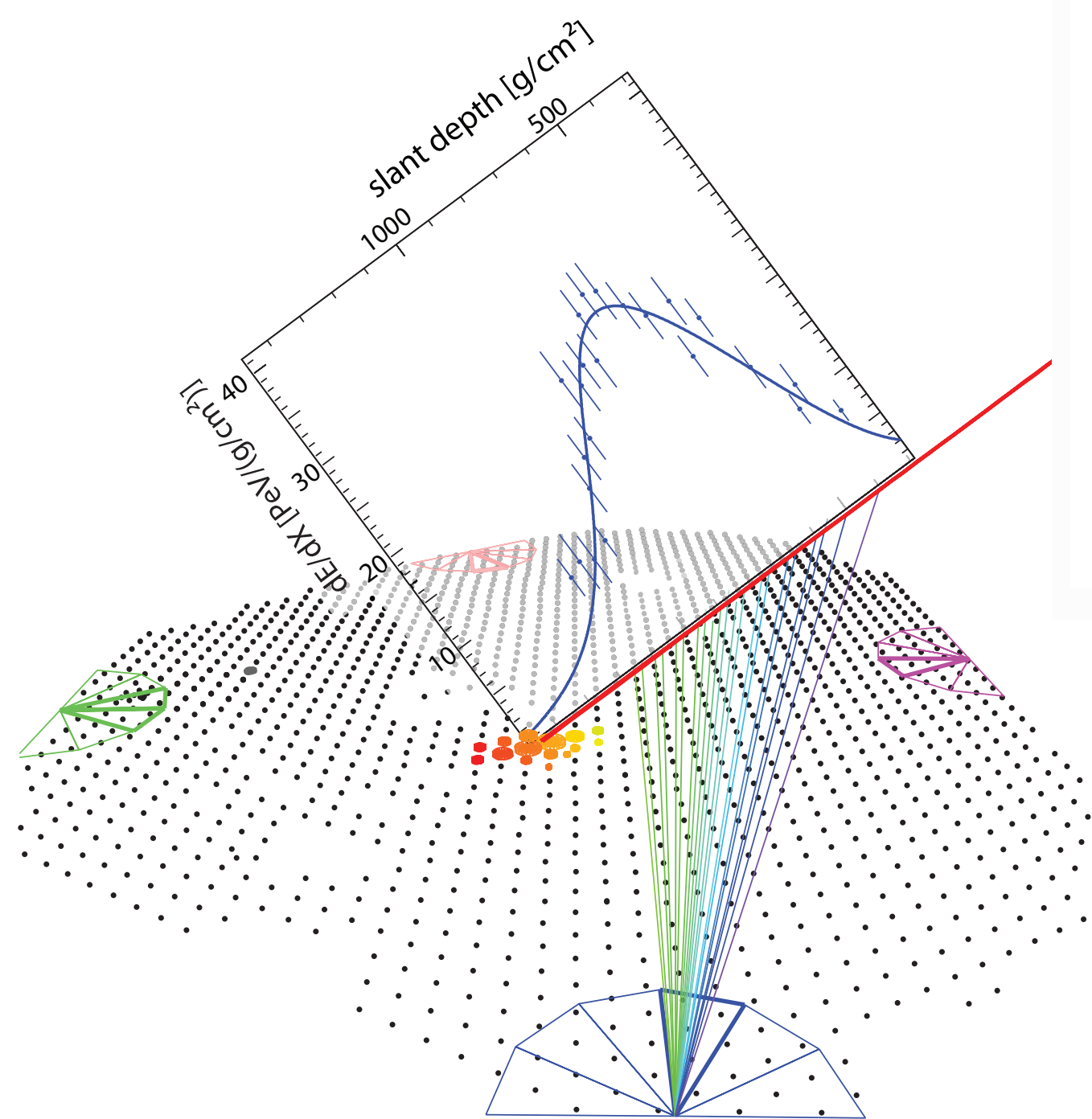


Signal per station

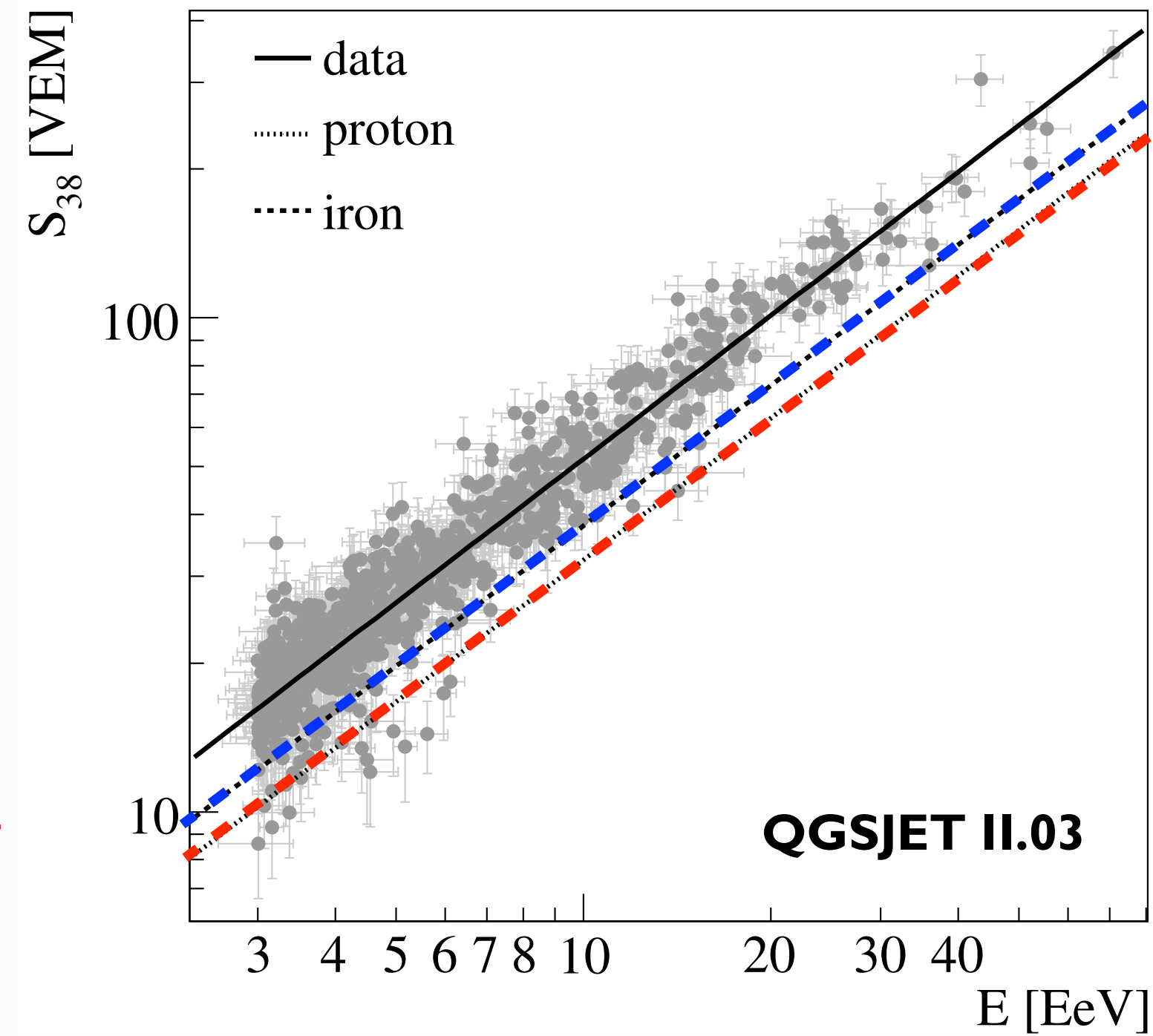
Most observables not very sensitive to details of shower simulation

Auger Observatory: comparison of surface detector signals

Subset of data with full hybrid observation



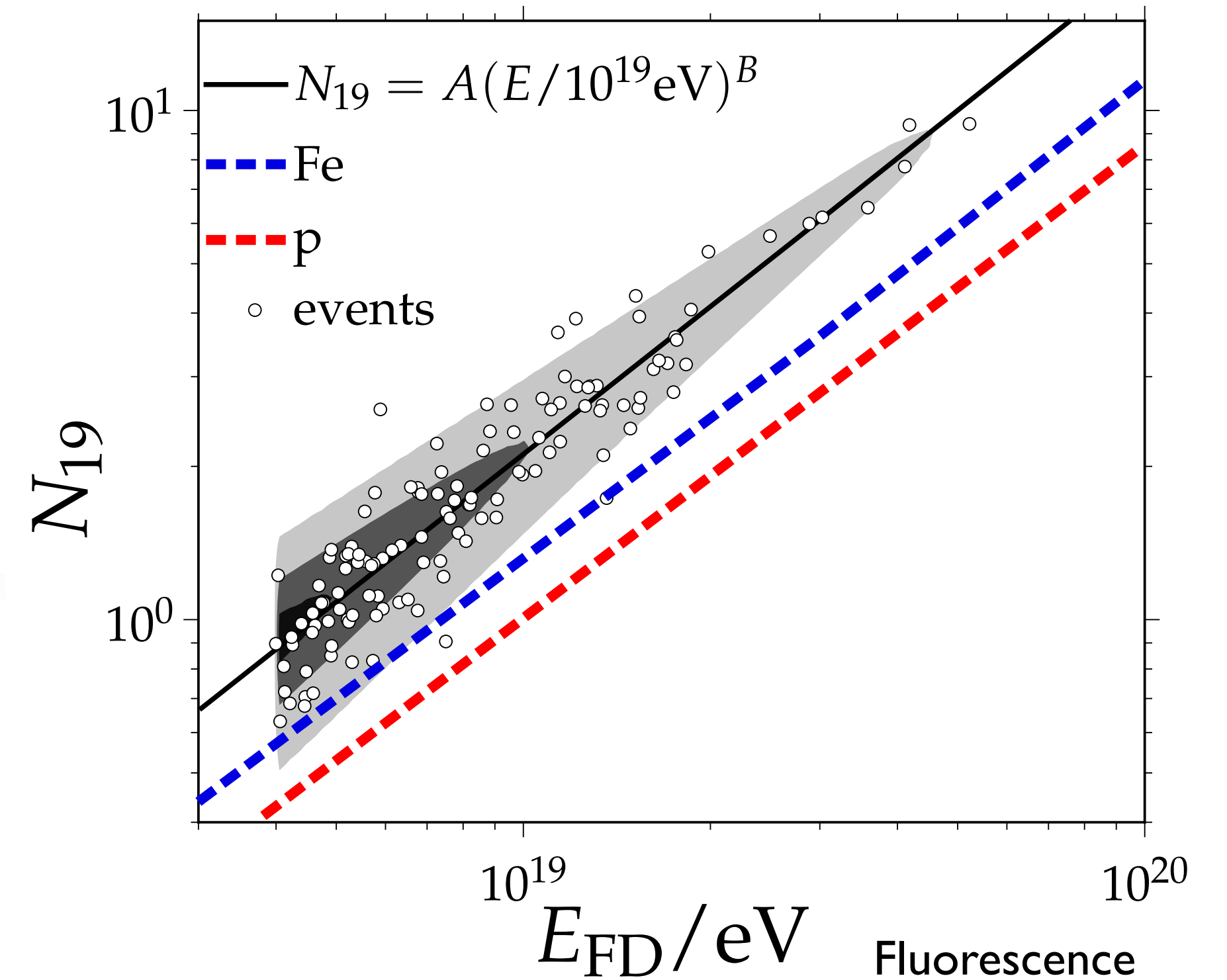
Showers up to 60° zenith angle



Fluorescence

(HadInt Working Group, UHECR 2012)

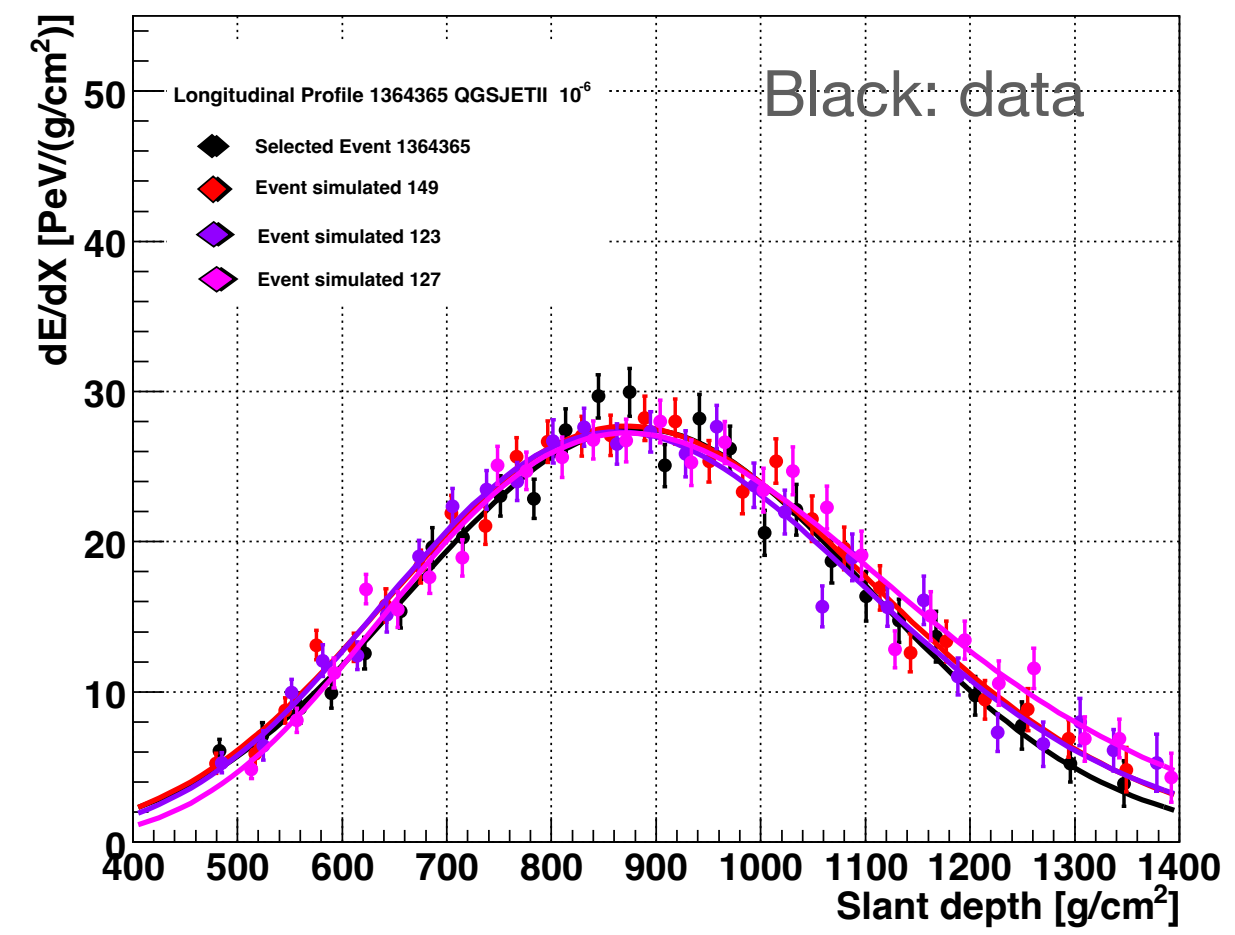
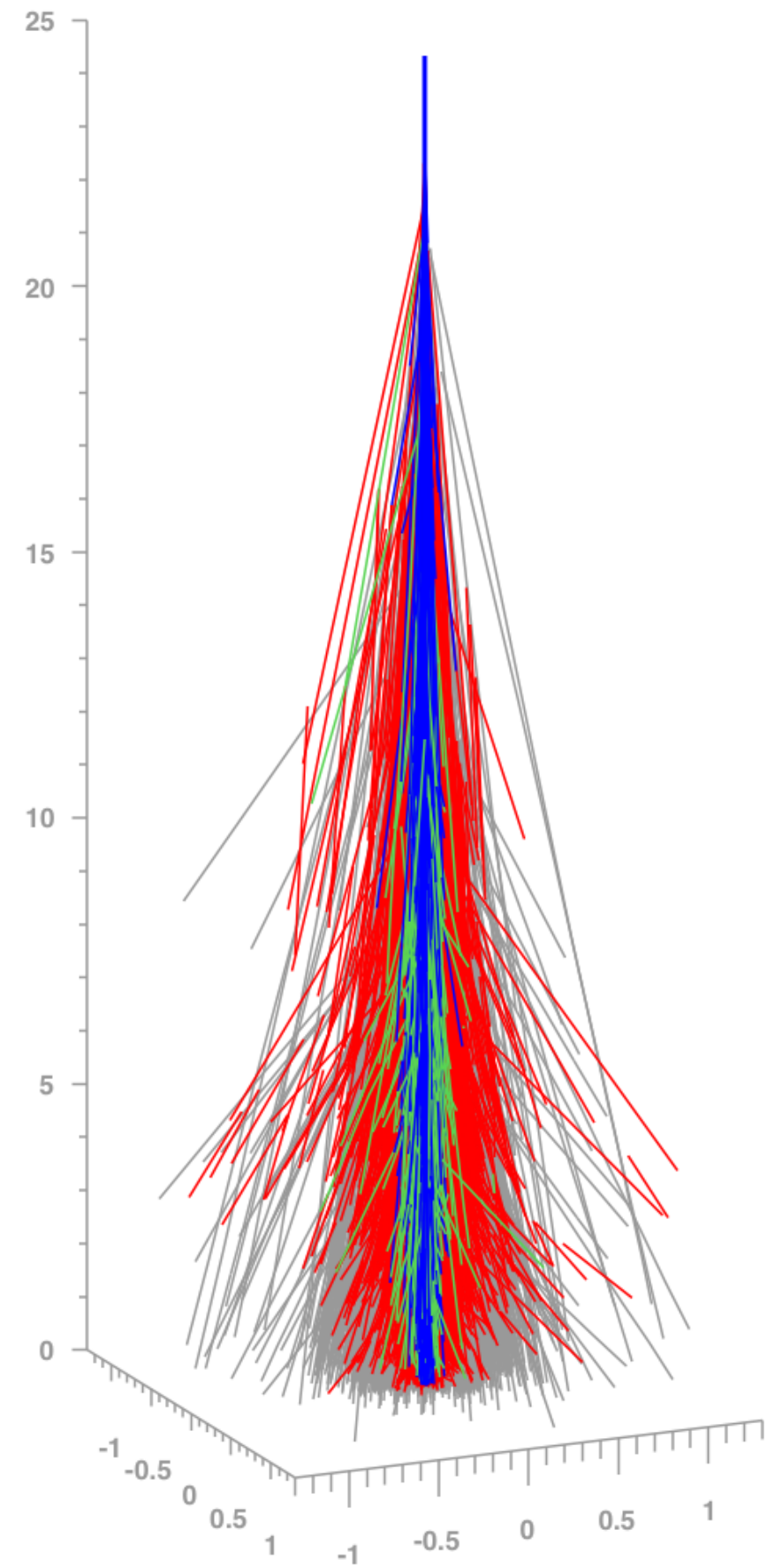
Inclined showers (muon dominated)



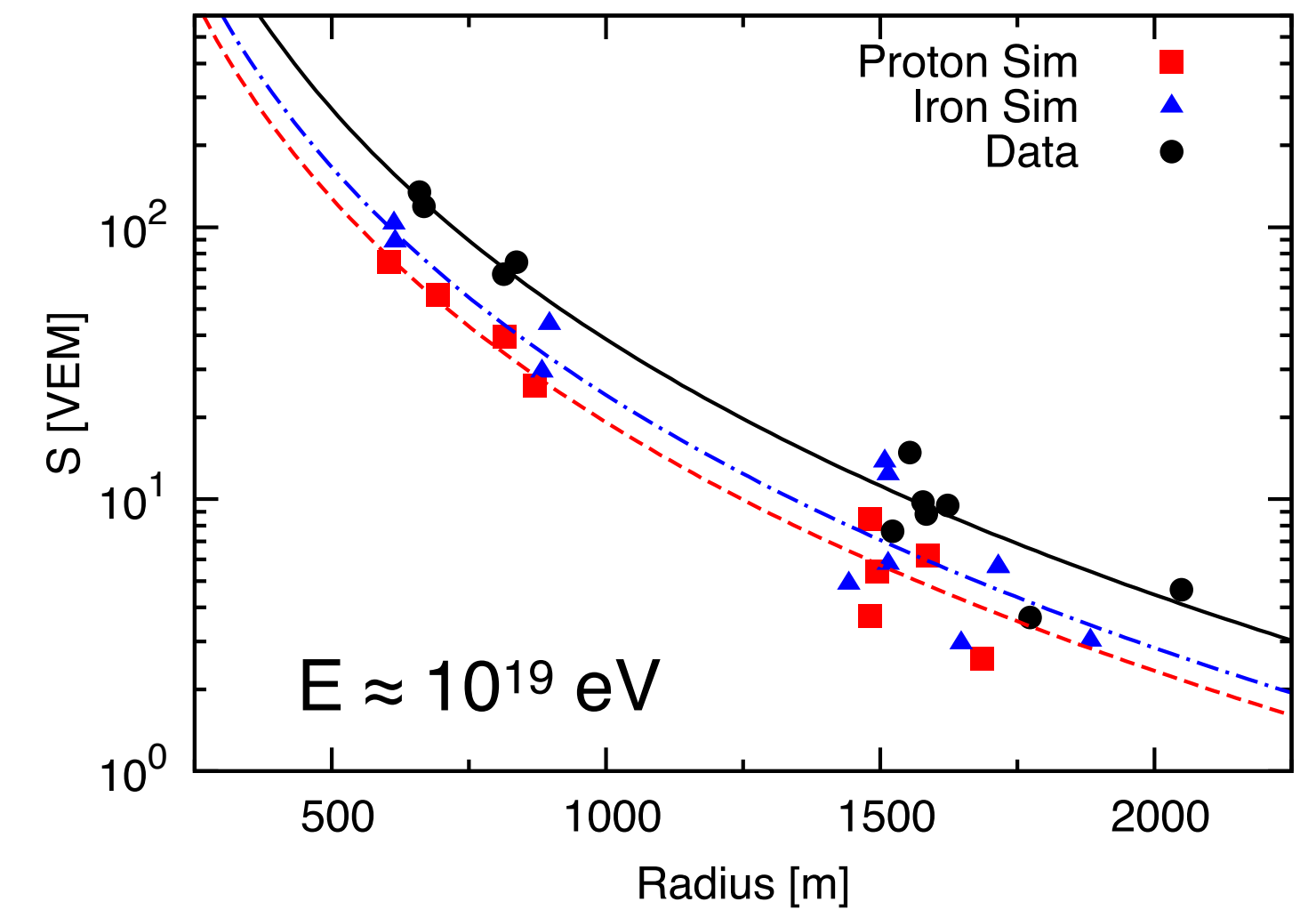
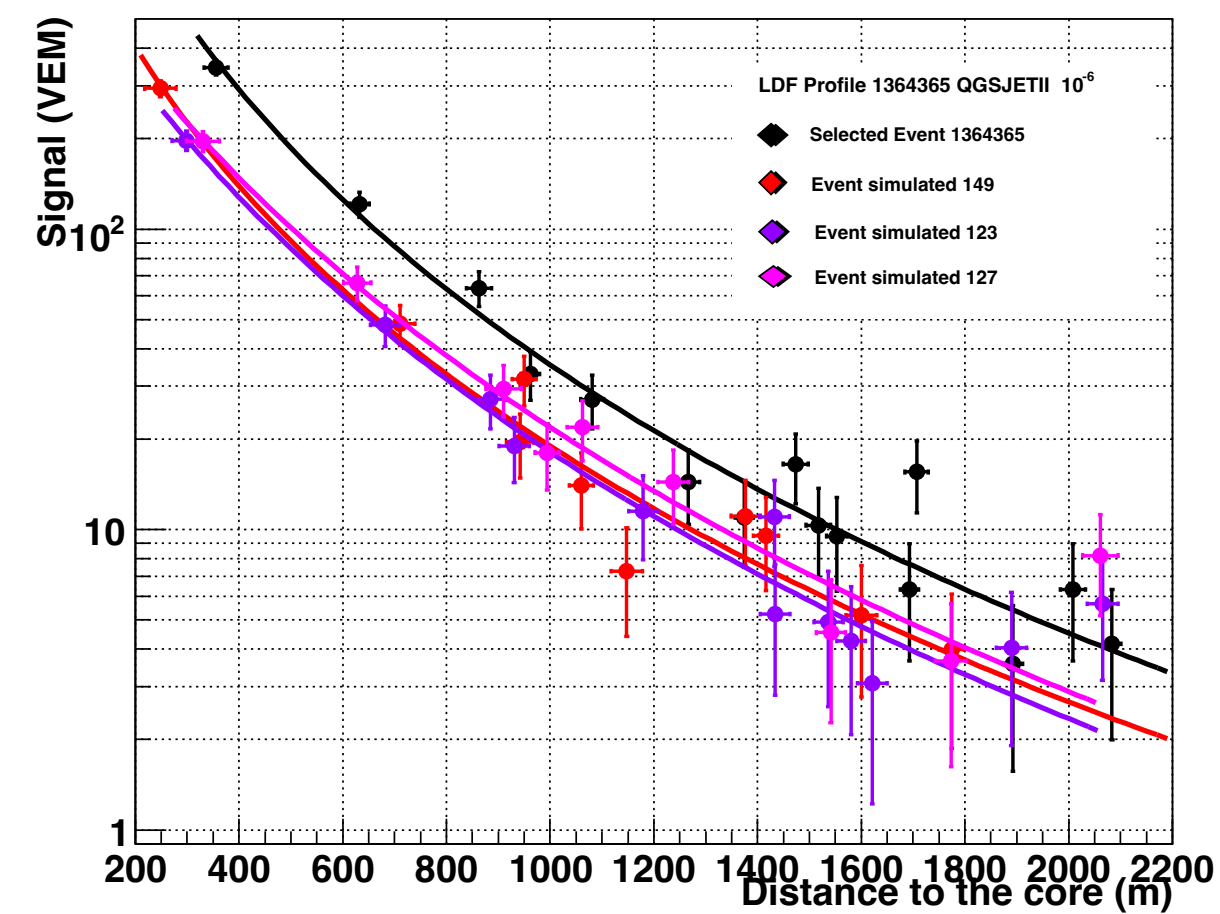
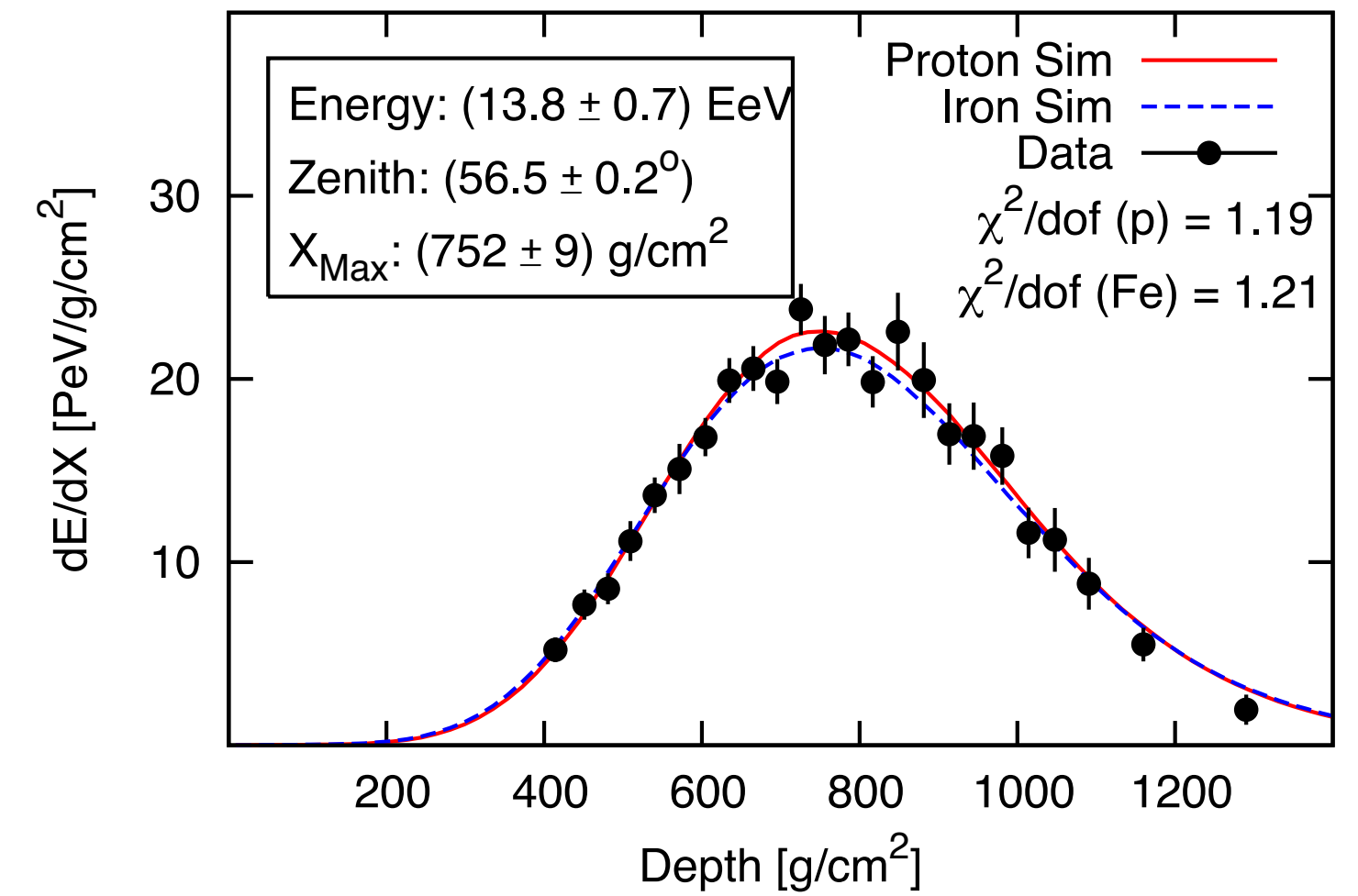
3. The muon puzzle

Comparison of longitudinal and lateral shower profiles (i)

Several simulated showers

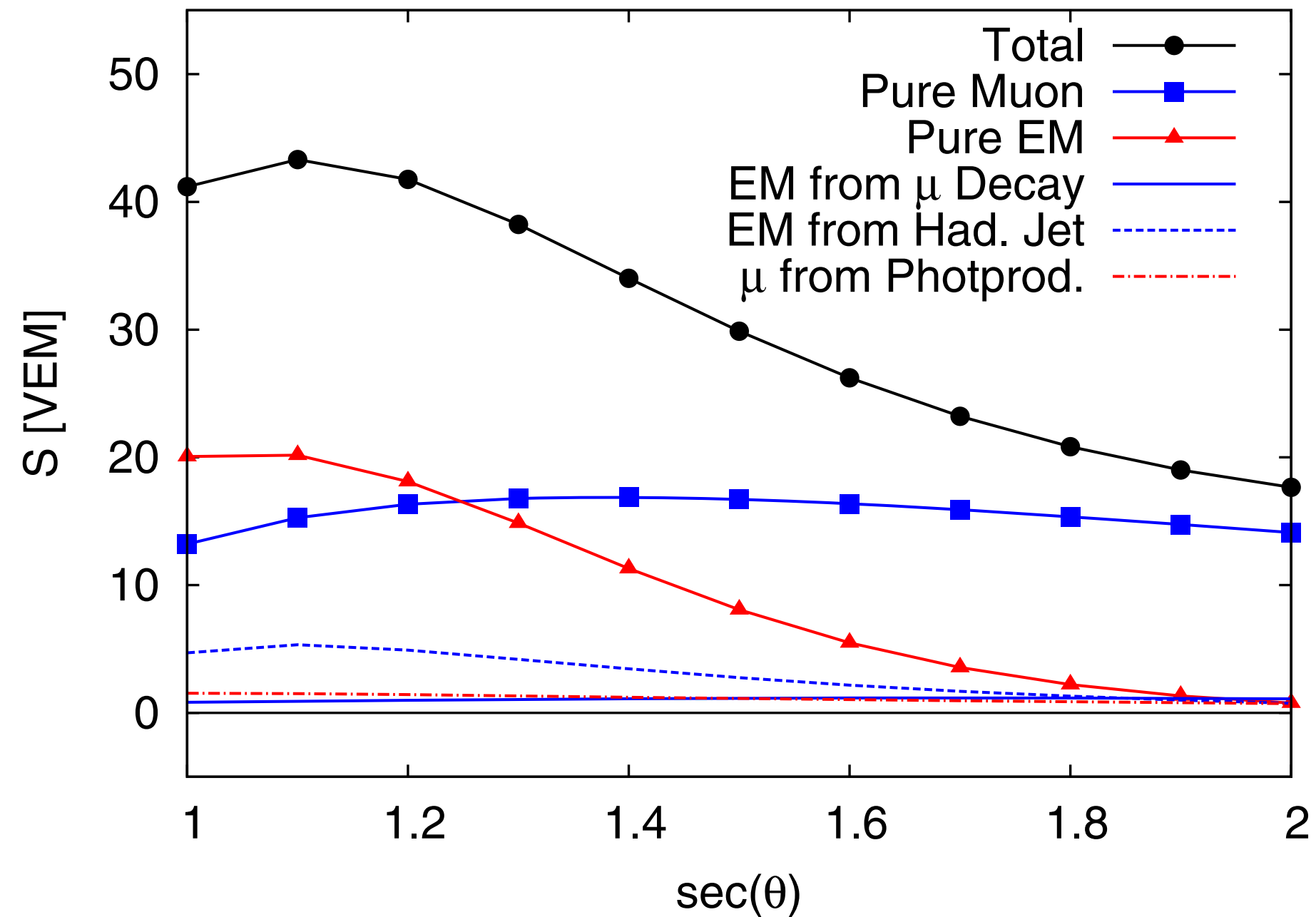


Different primary masses



Comparison of longitudinal and lateral profiles (ii)

Shower signal at 1000 m from core



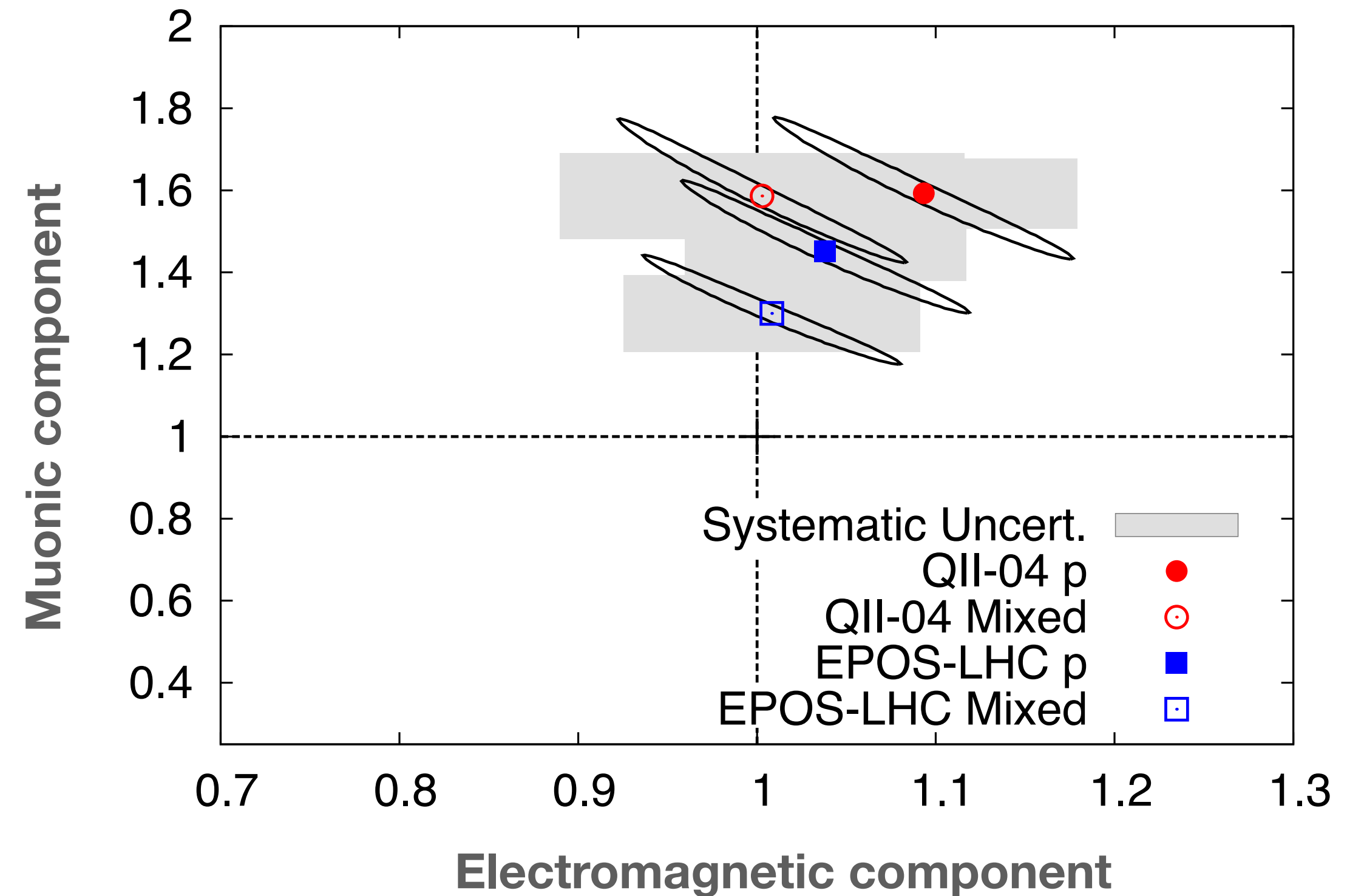
Energy scaling: em. particles and muons

Muon scaling: hadronically produced muons and muon interaction/decay products

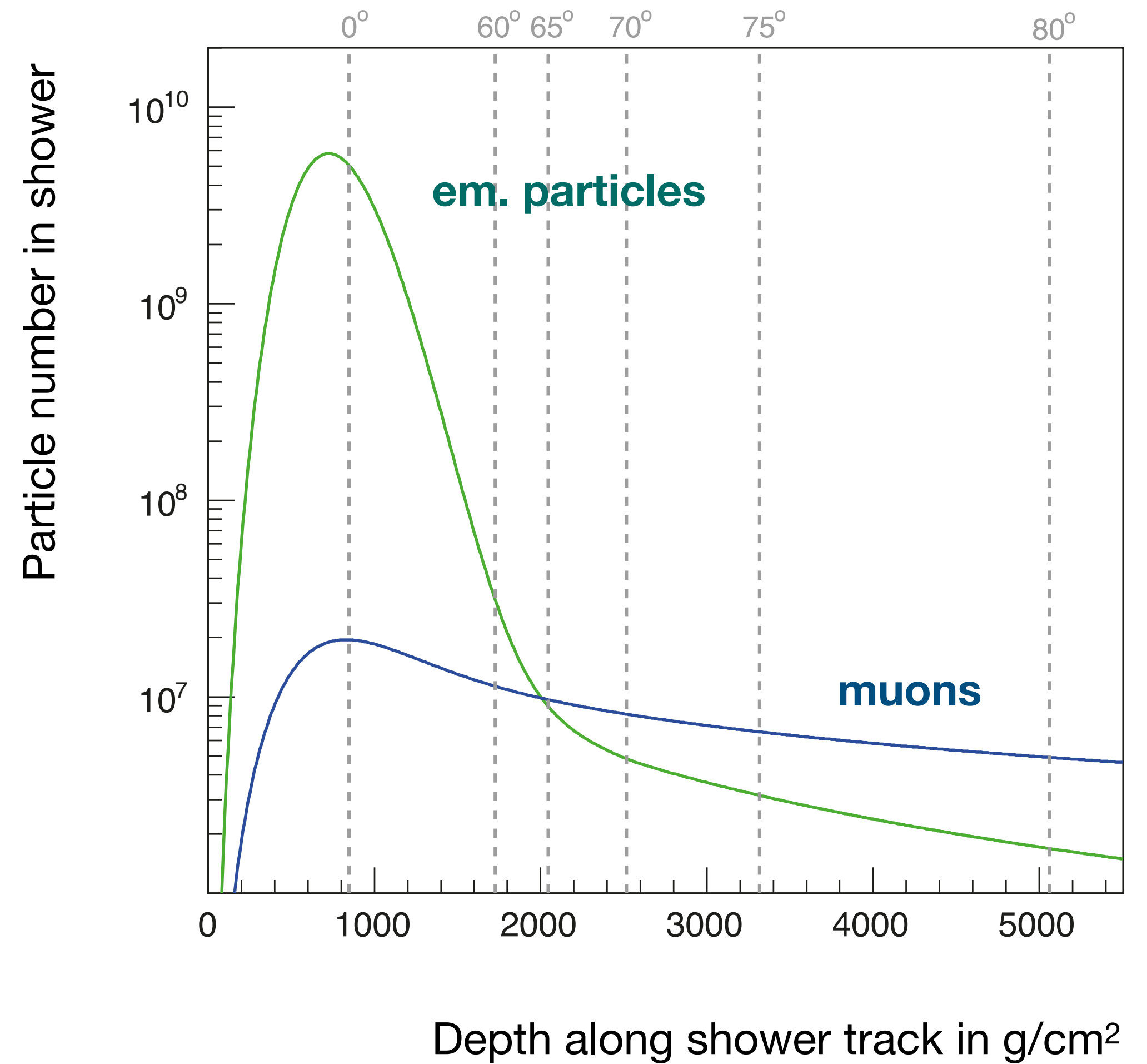
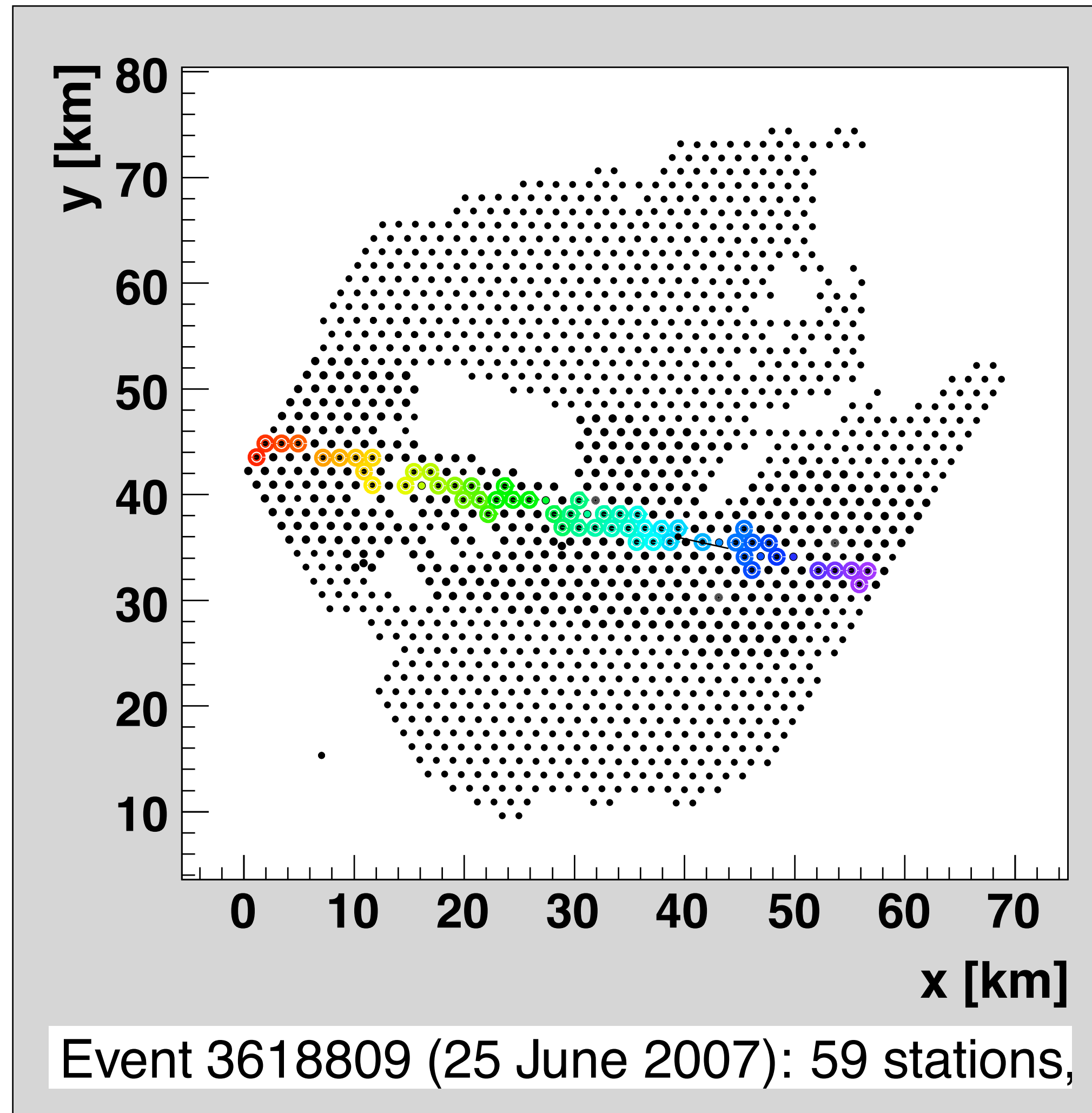
Full detector simulation after re-scaling

Phenomenological model ansatz

Needed rescaling factors for correcting average signal at ground

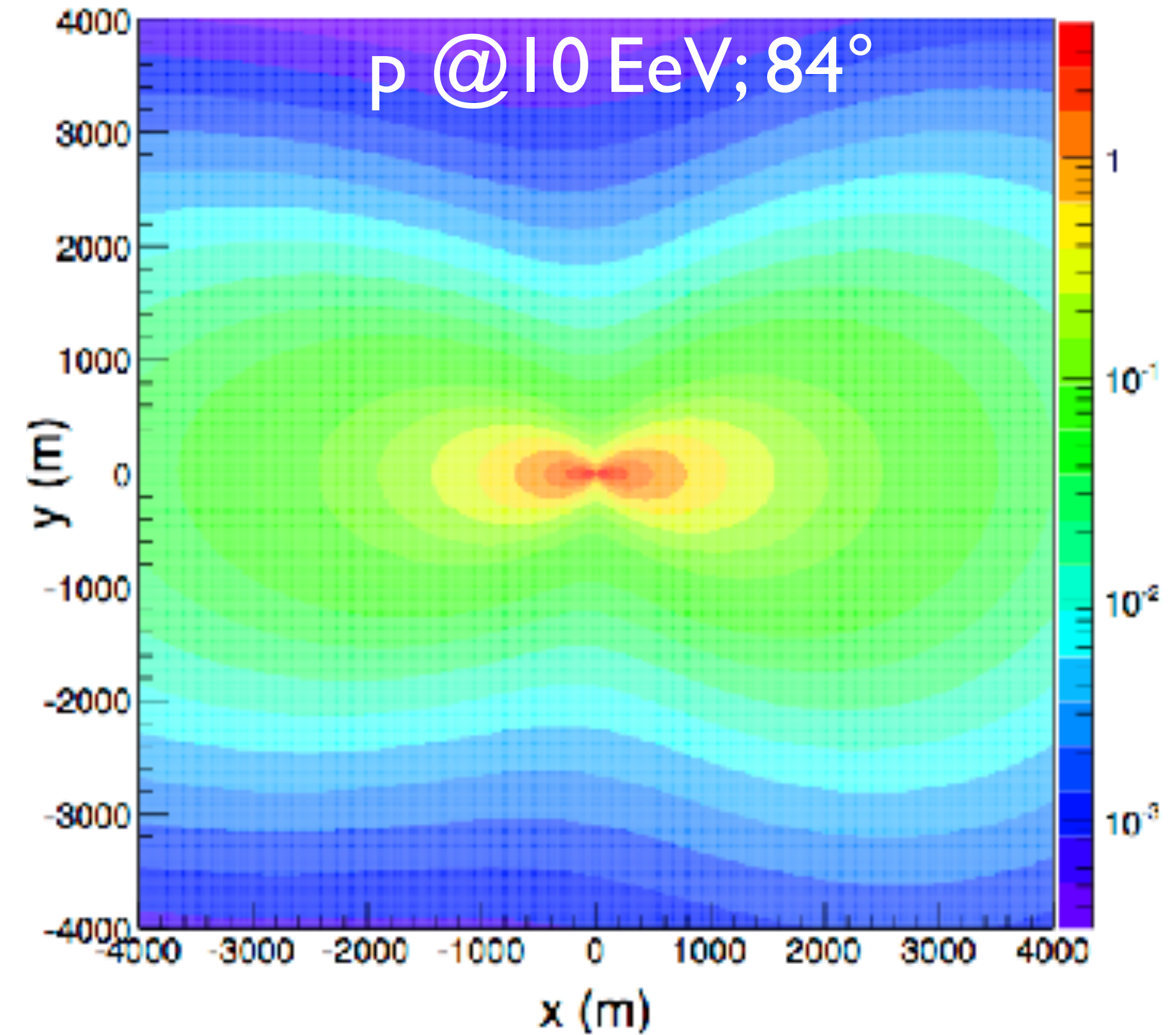
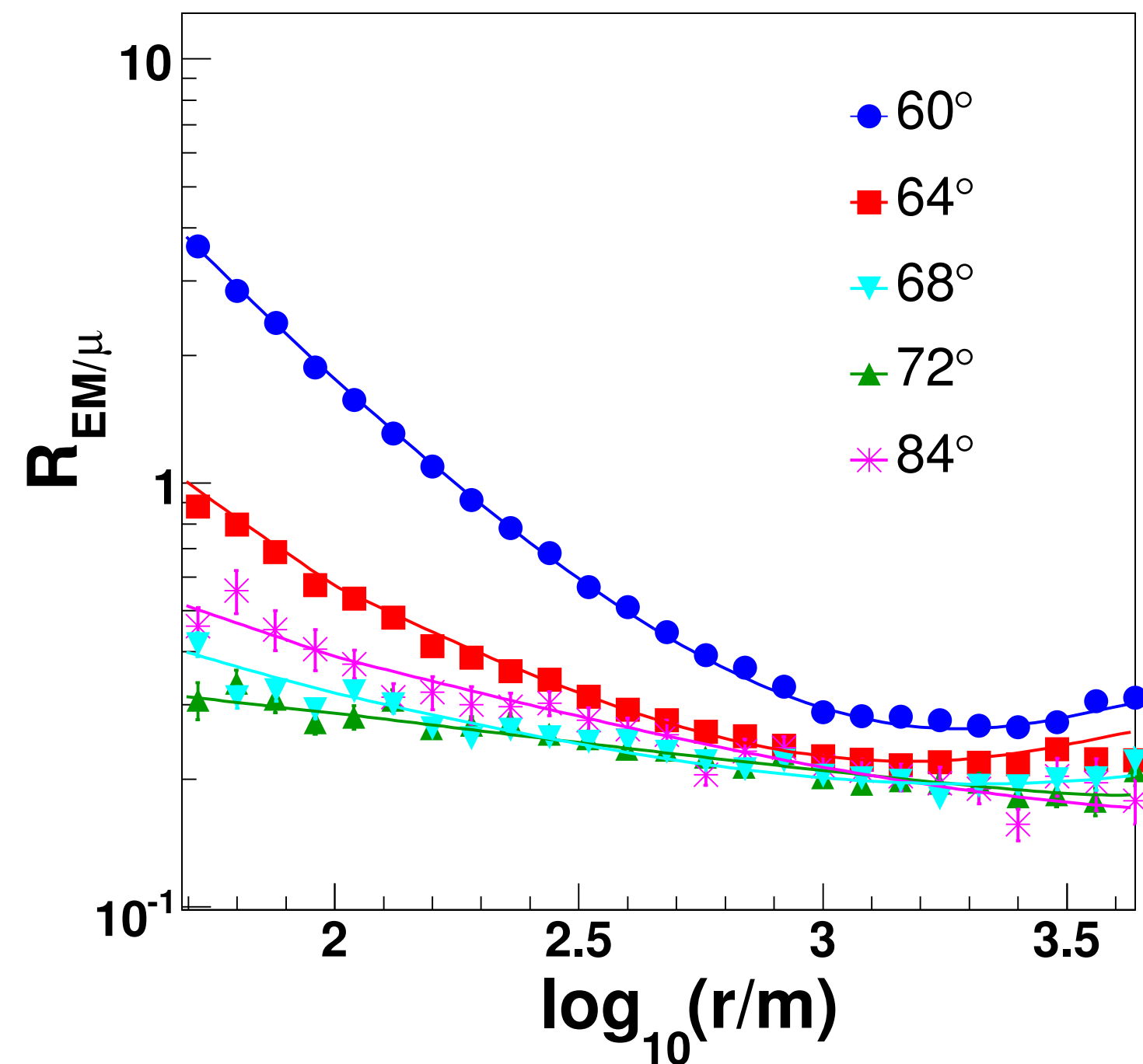


Inclined showers ($\theta > 60^\circ$), em. component absorbed



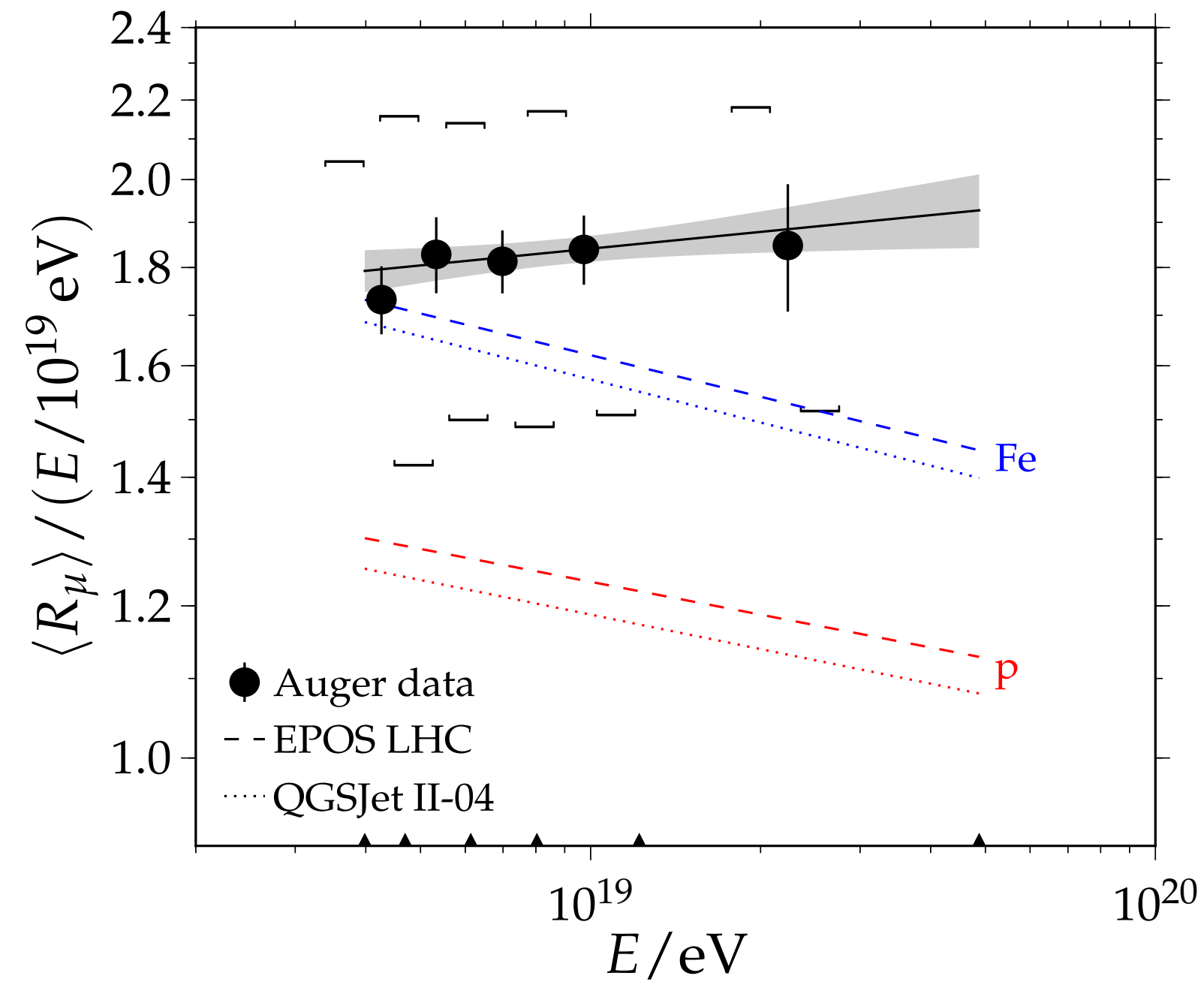
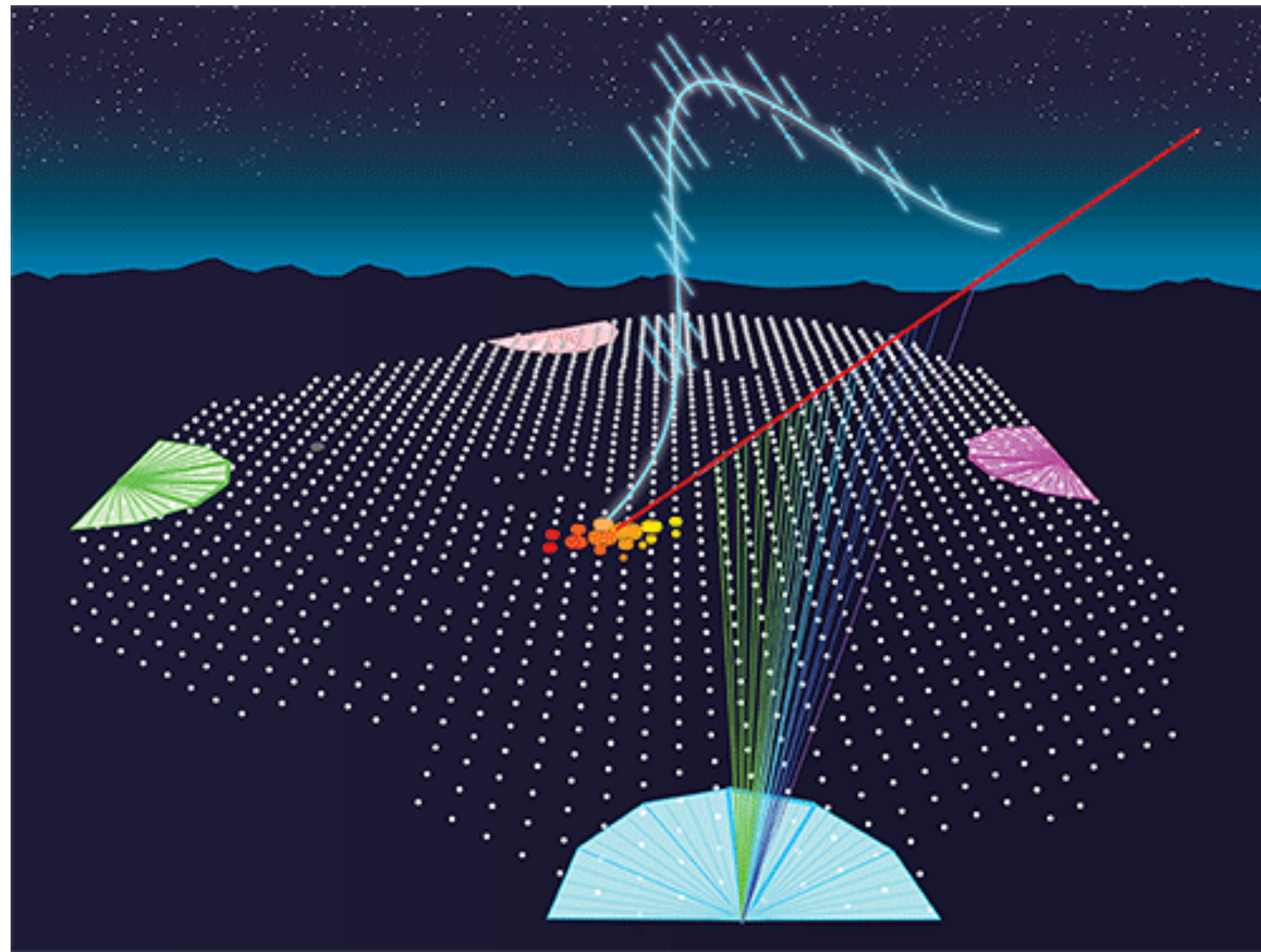
Hybrid events: N_{19} used for muon counting

- Muonic component dominates
 - ($\approx 20\%$ residual e.m. component)
- Energy estimator N_{19} :
$$N_{19} = \rho_{\mu} / \rho_{\mu, 19}(x, y, \theta, \phi)$$
- zenith angle independent

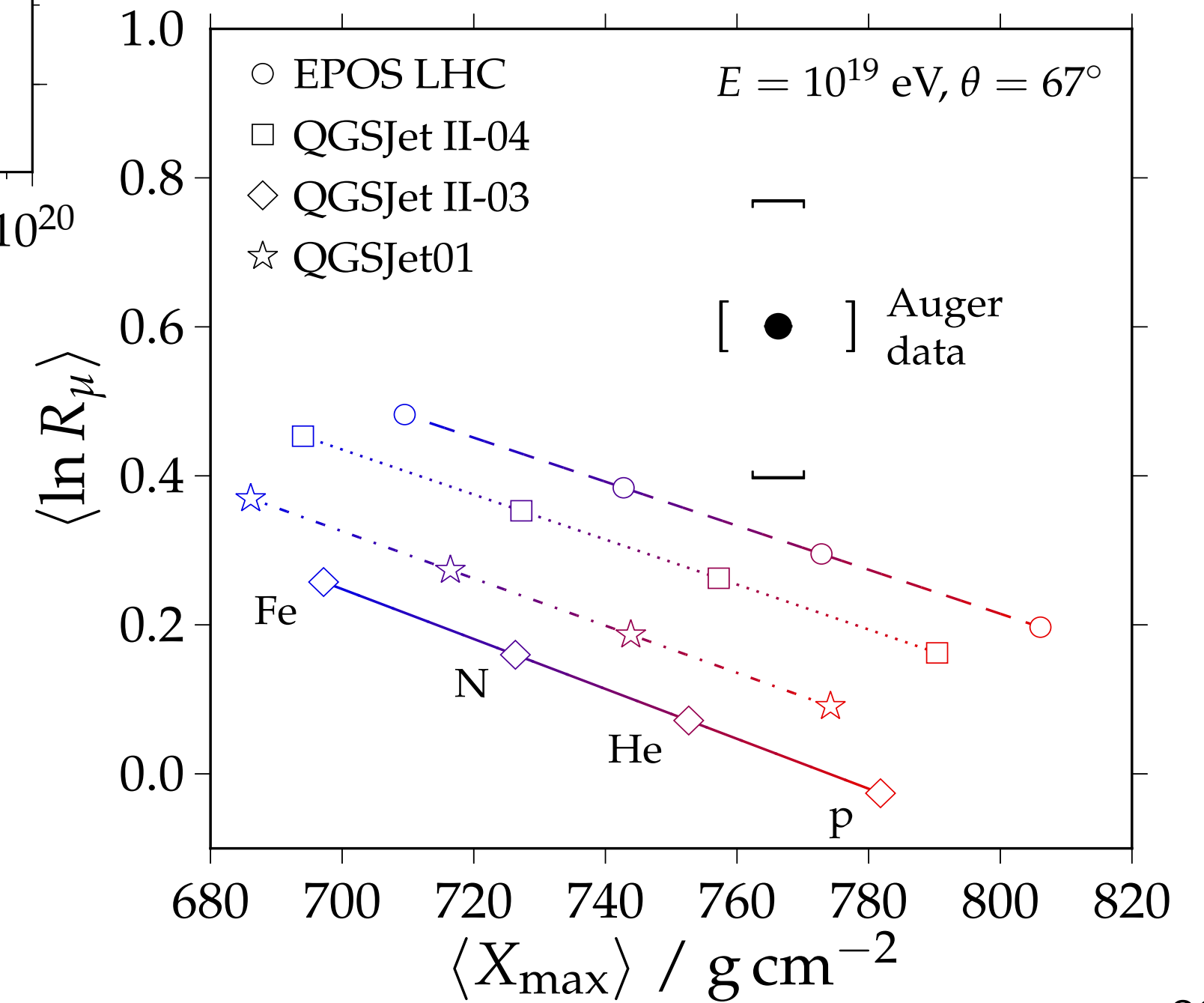


Simulated muon maps (magnetic deflection)

Muon number in inclined showers (nearly background-free)



Relative number of muons
in showers with $\theta > 60^\circ$



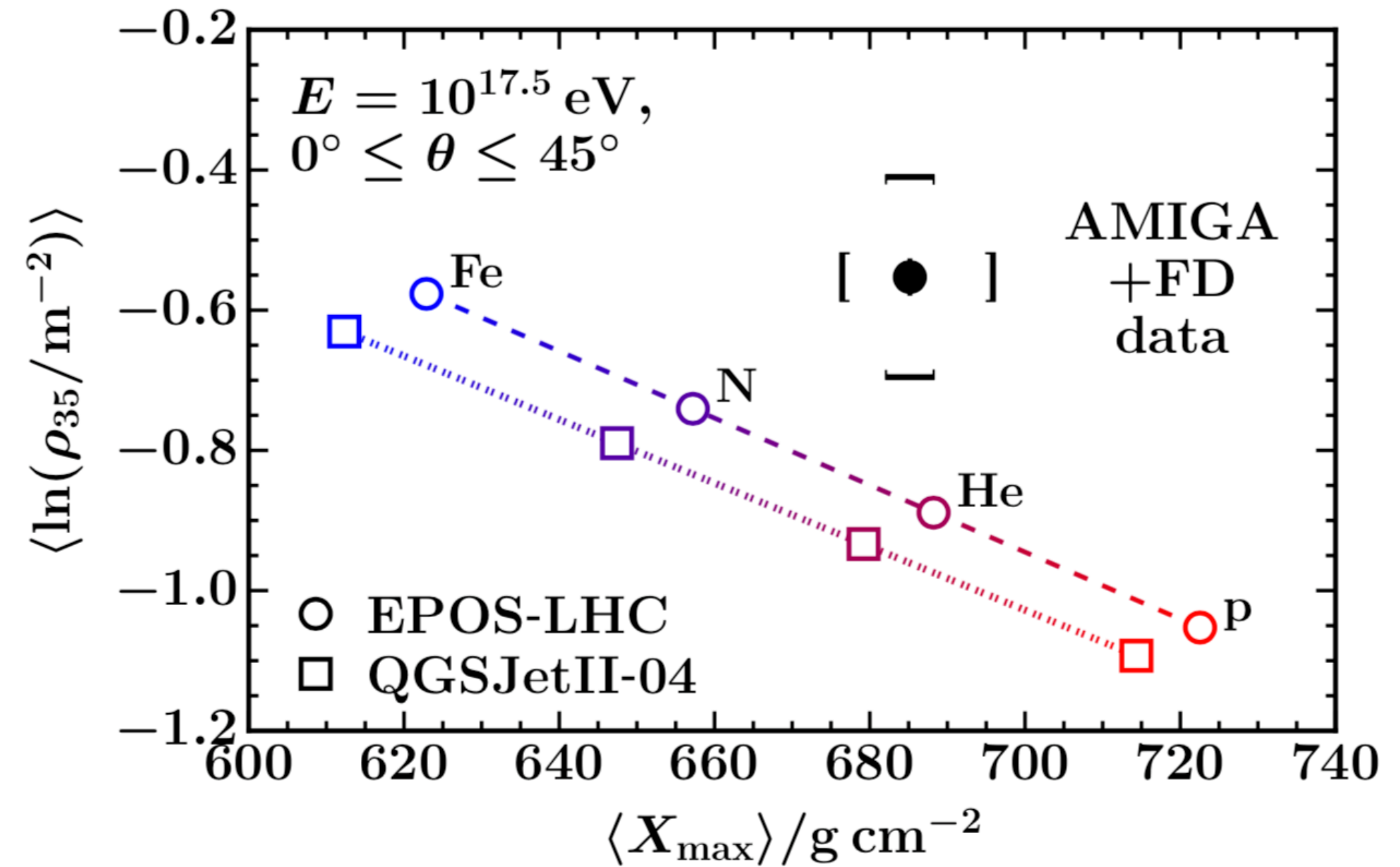
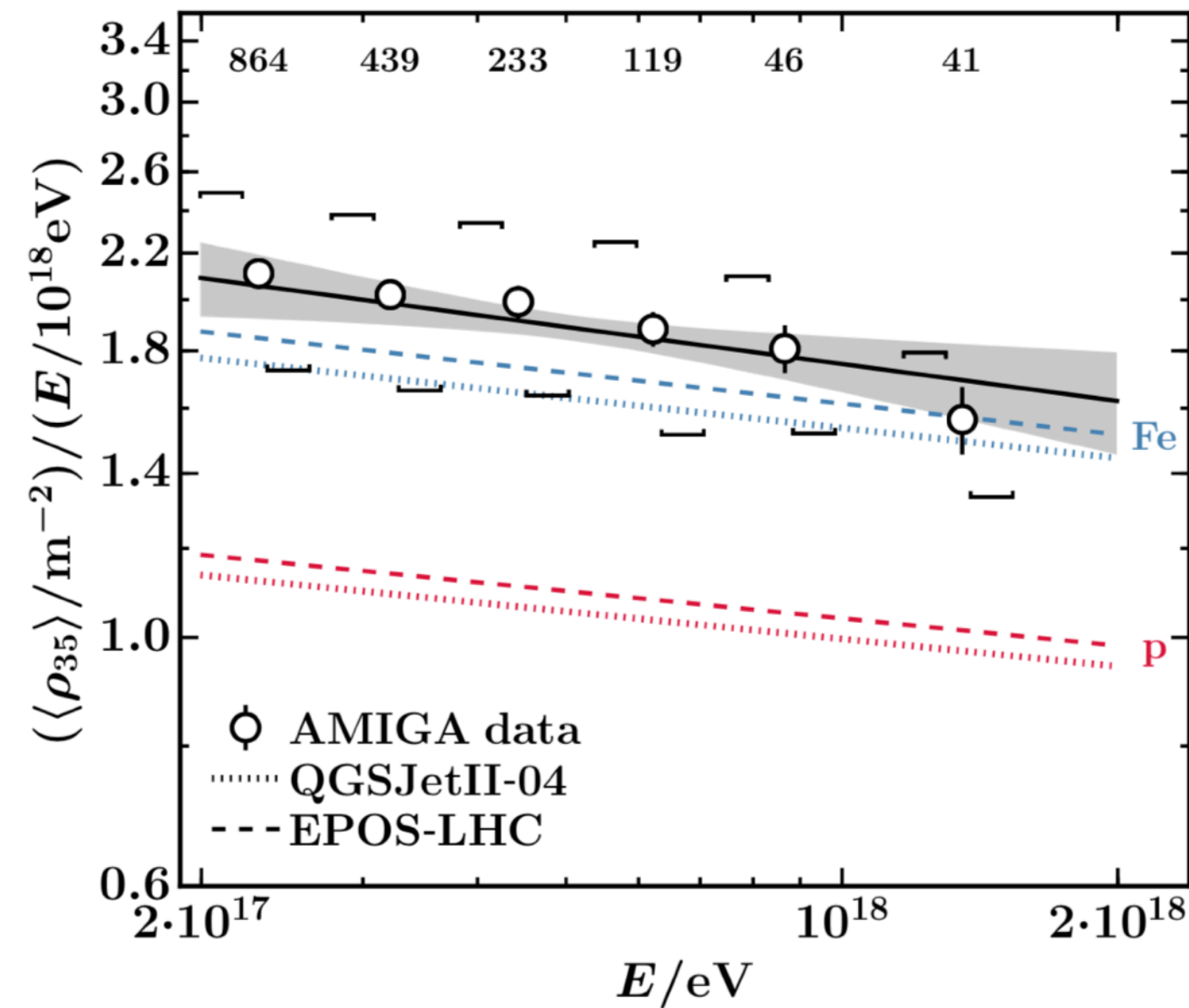
Muon discrepancy confirmed

(Auger, *Phys. Rev. Lett.* 117 (2016) 192001,
*Phys. Rev. D*91 (2015) 032003)

Direct measurement of muons at lower energy



Underground muon detectors
(2.3 m soil for shielding)

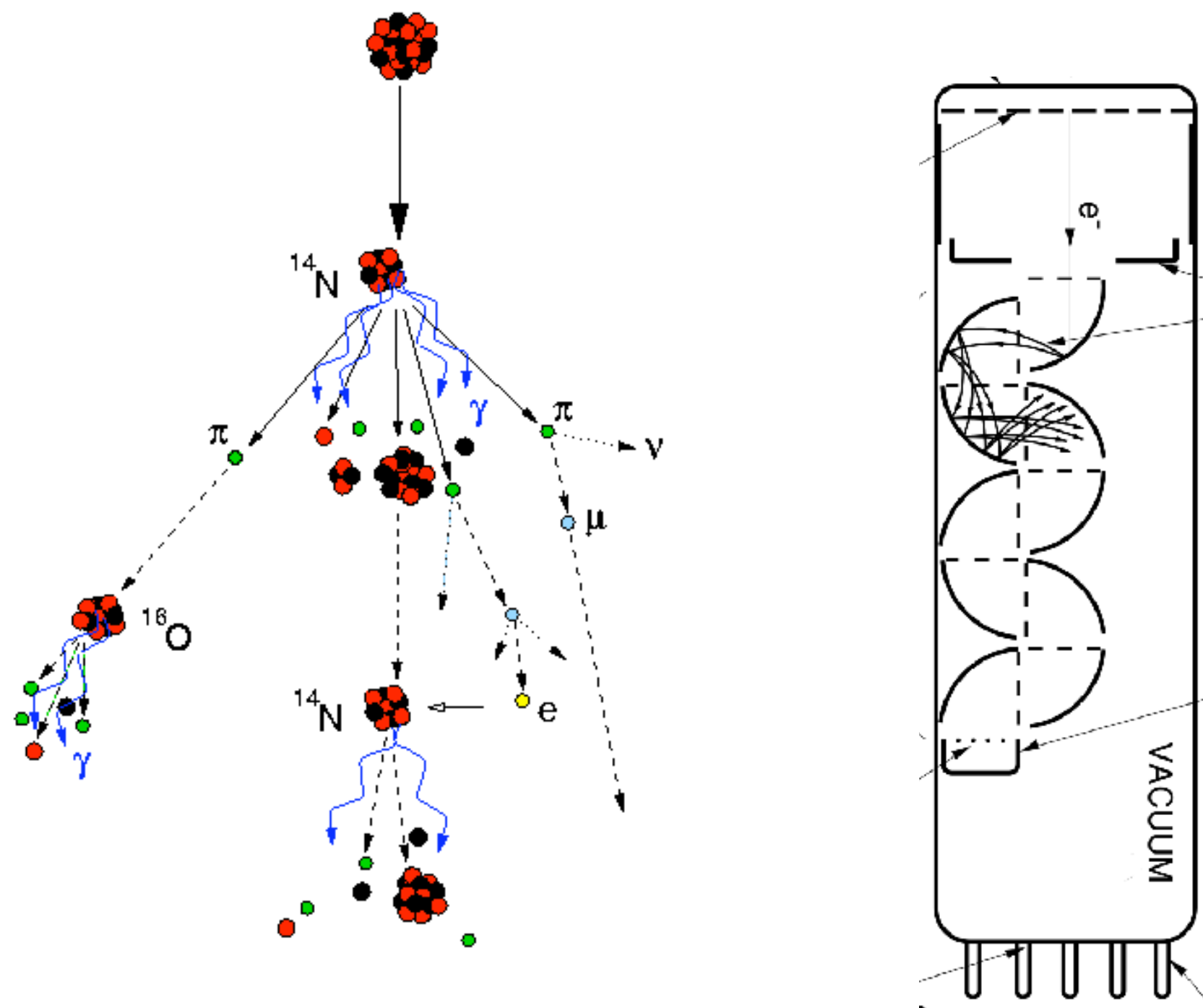


**In range 3×10^{17} eV to 2×10^{18} eV simulations don't reproduce muon densities
40% (50%) increase in $\langle N_\mu \rangle$ at 10^{18} eV needed for EPOS-LHC (QGSJetII-04)**

Note: this is in energy range of LHC

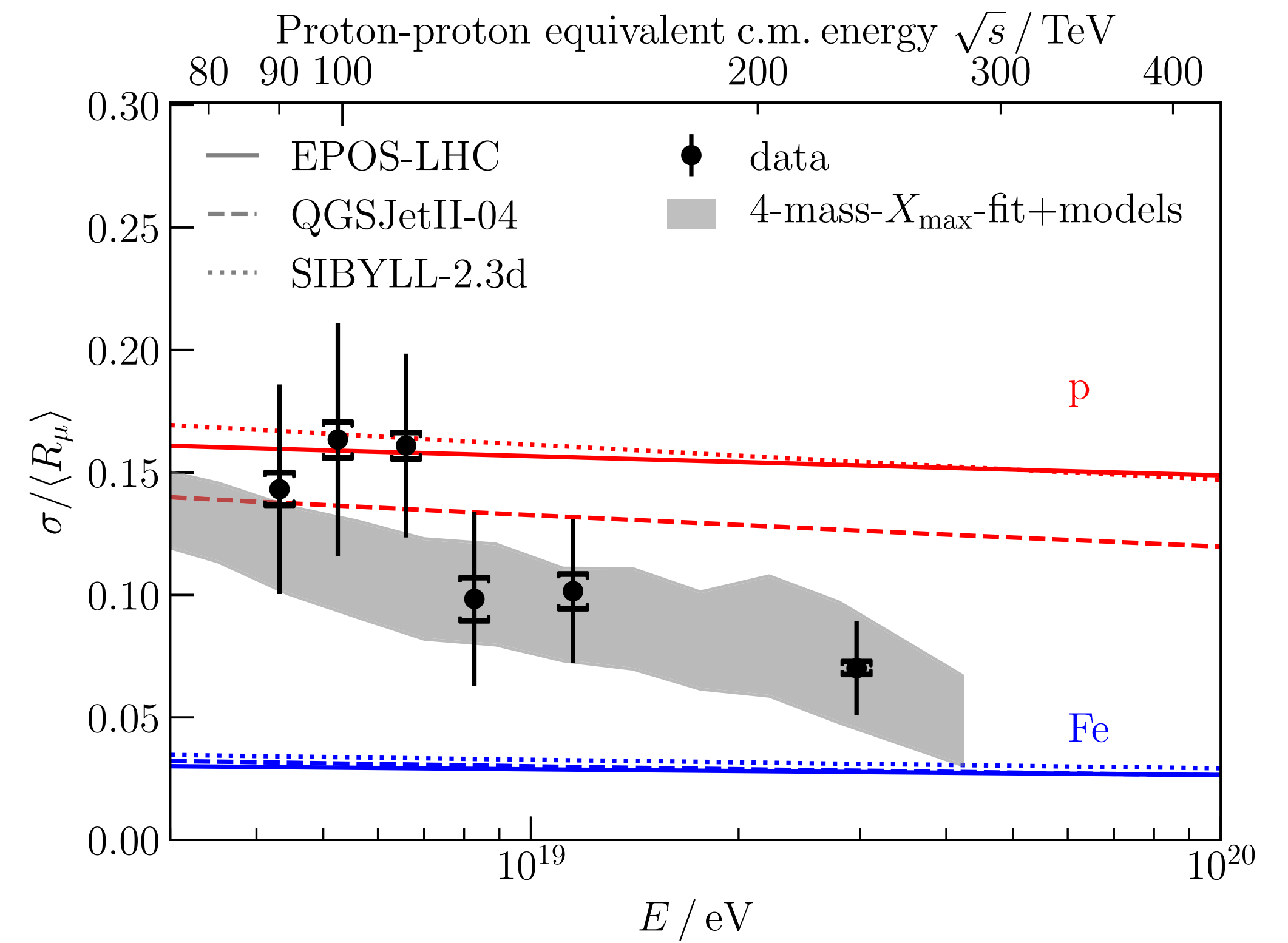
Muon number fluctuations in inclined showers ($\theta > 60^\circ$)

Hybrid events and inclined showers



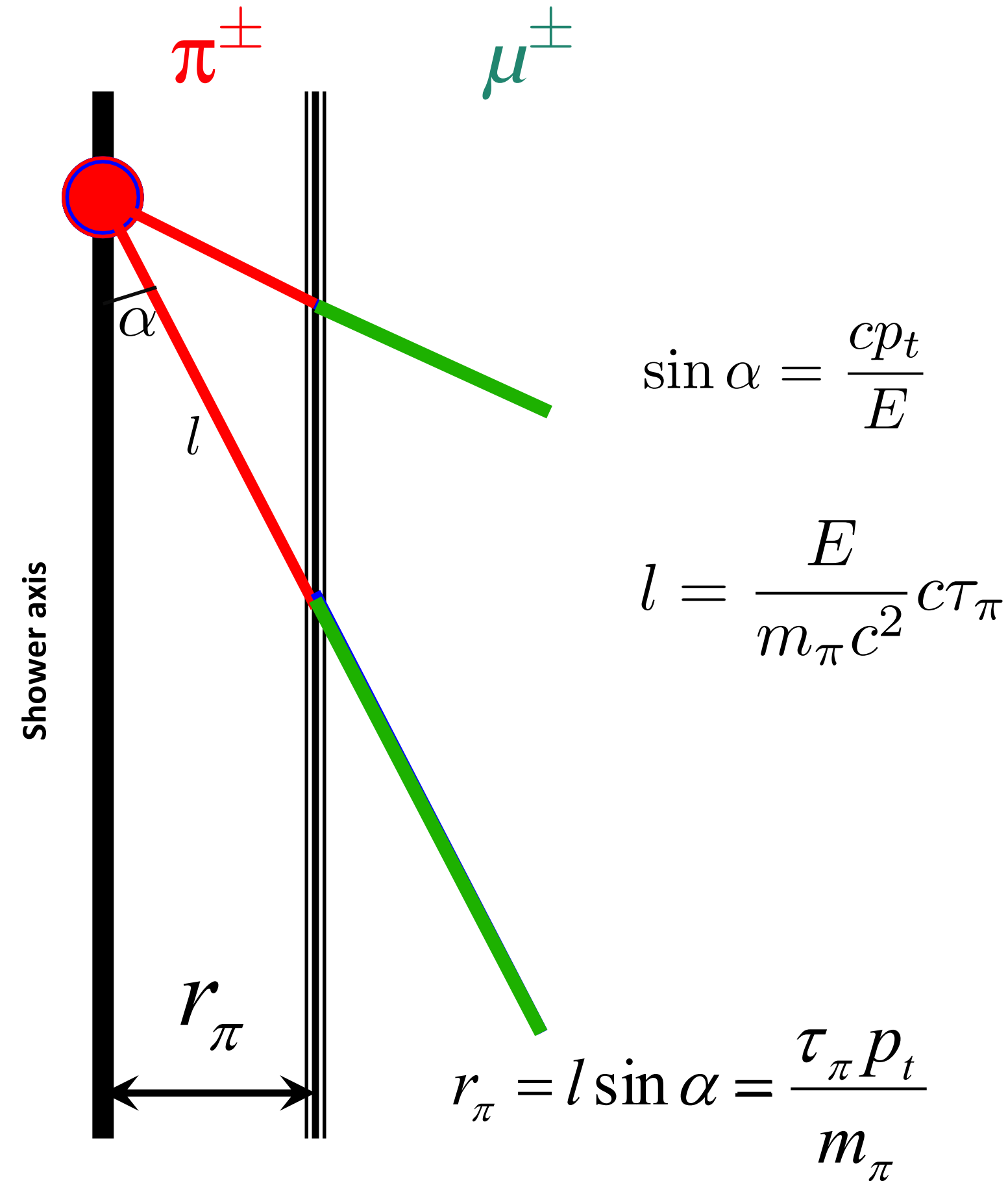
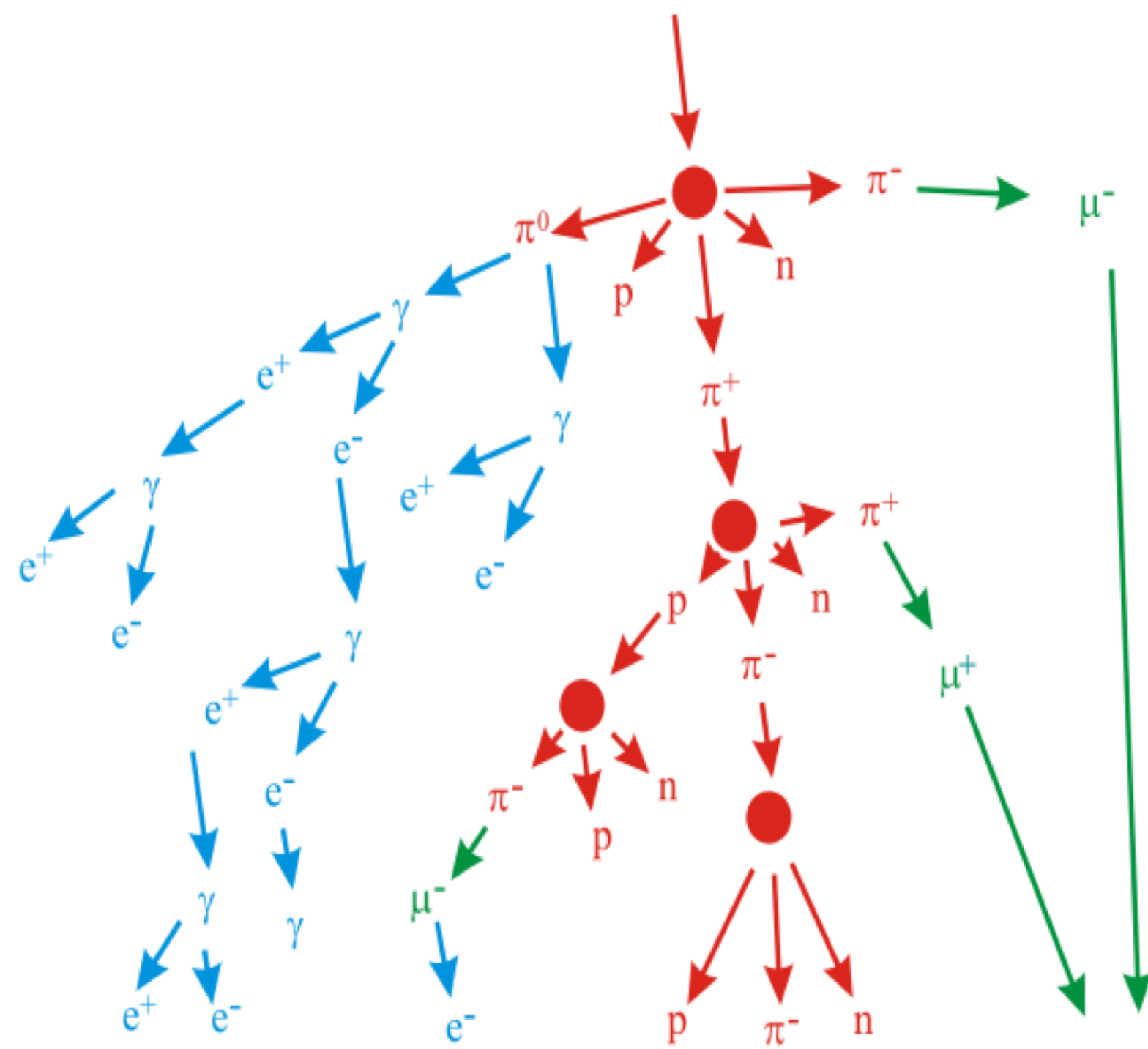
PMT analogy of air shower

Muon fluctuations driven by first interactions



Size of fluctuations as expected

Physics of muon production and number fluctuations



Lorenzo Cazon et al.
Astropart. Phys. 36 (2012) 211
Phys. Lett. B 784 (2018) 68

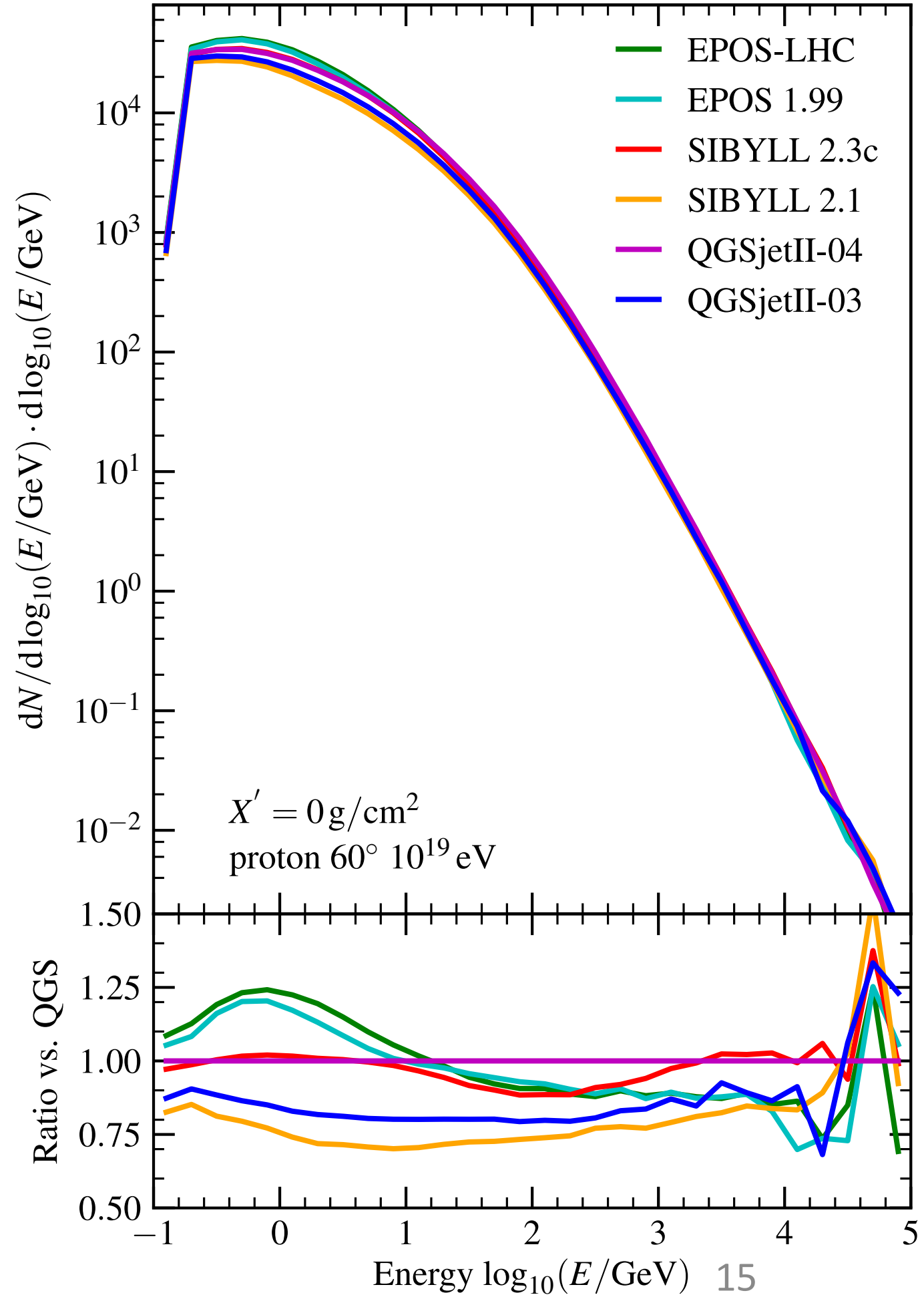
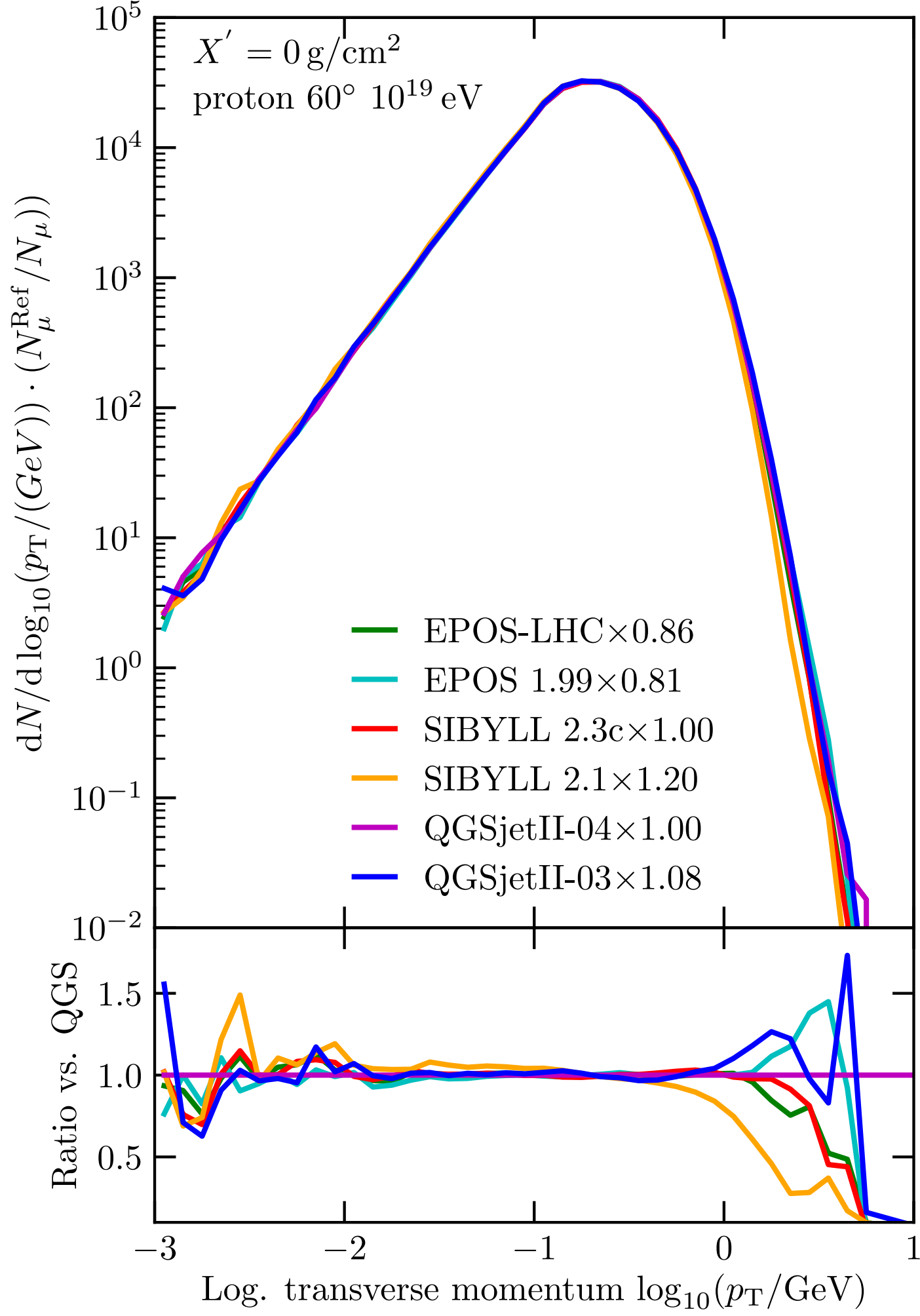
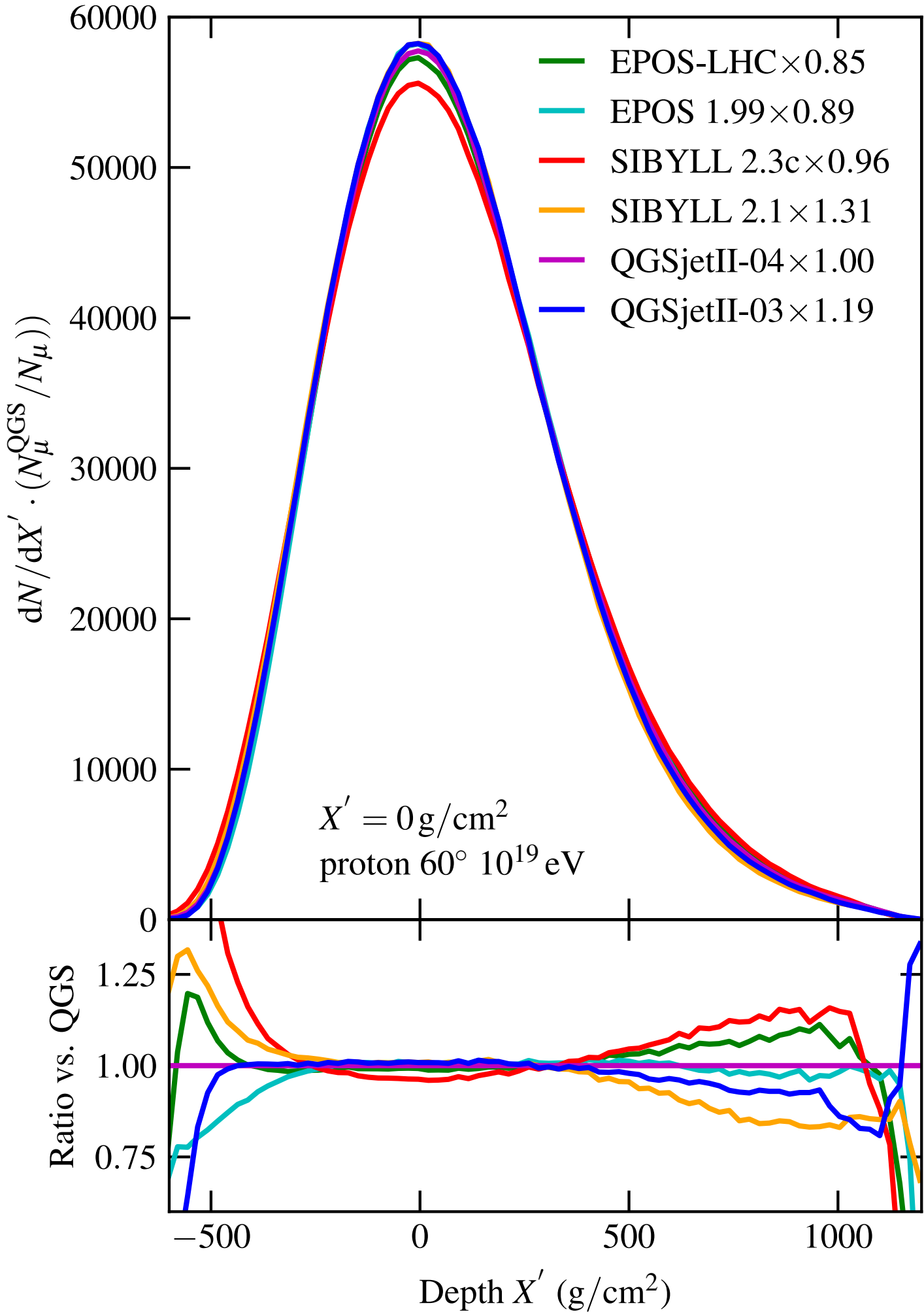
**Lateral distance
 59% of all muons**

$r_\pi < 22 \text{ m}$

70% of fluctuations from first interaction

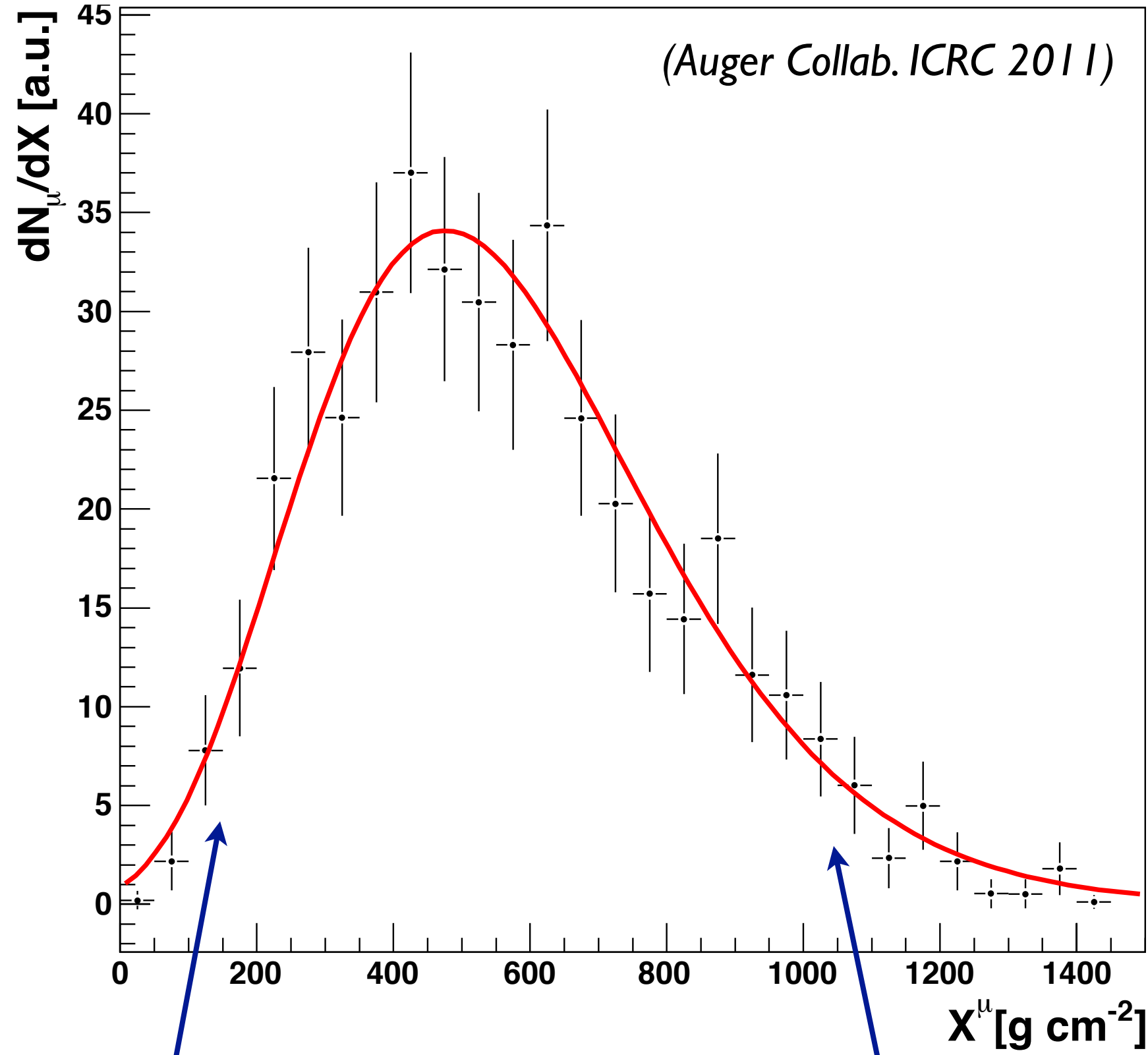
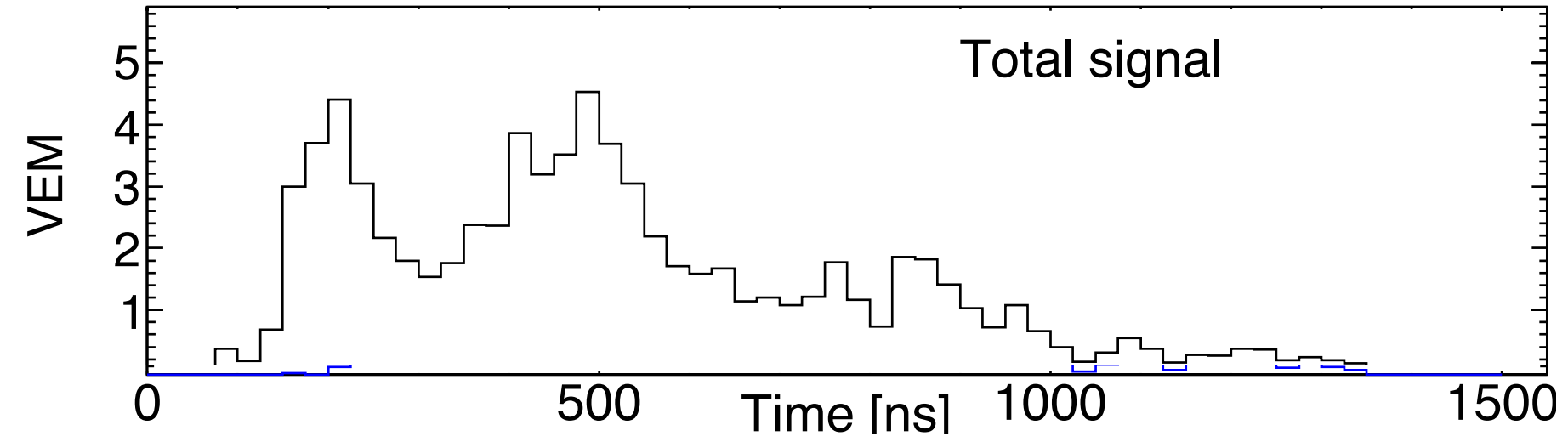
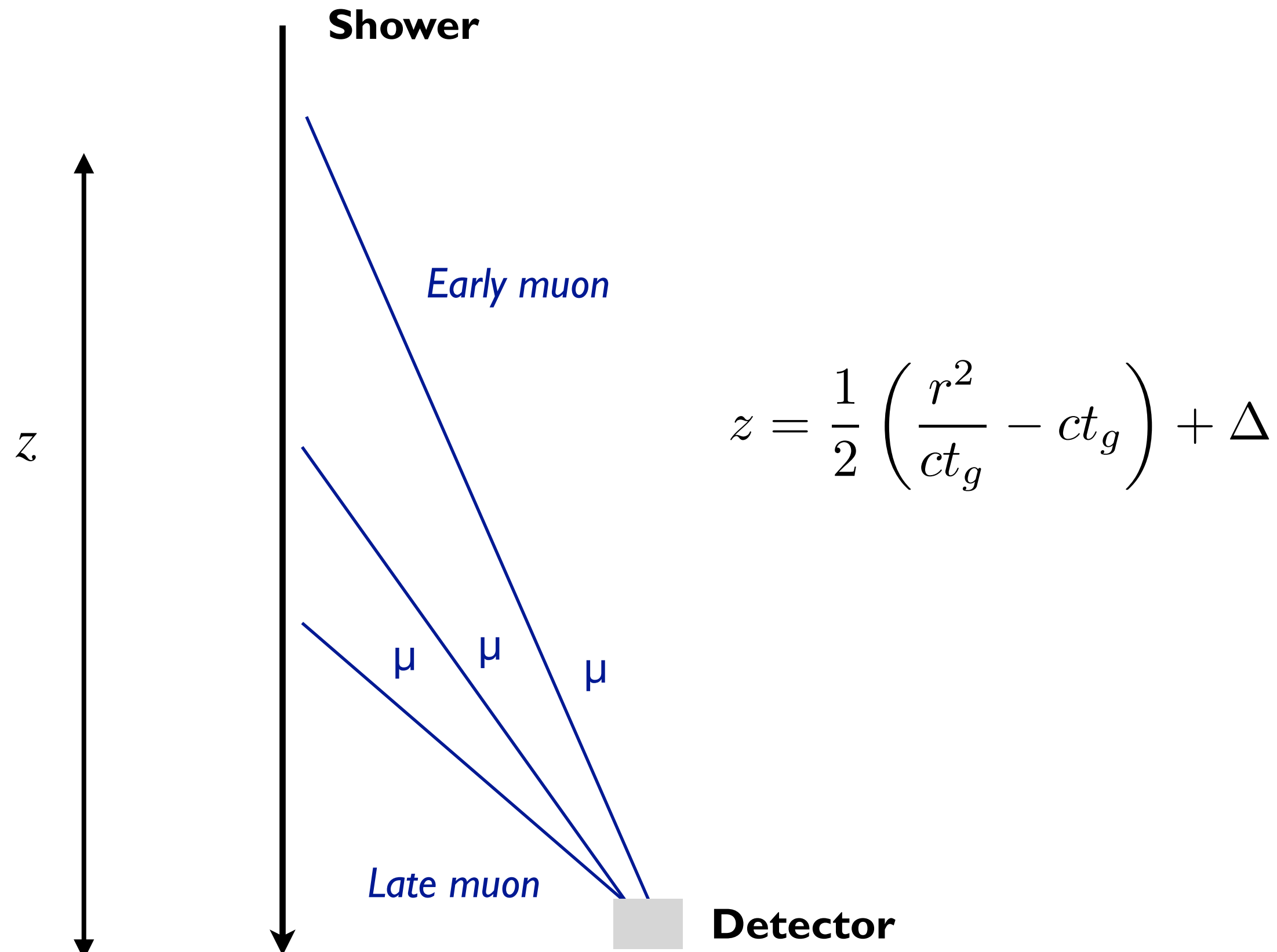
$$\left(\frac{\sigma(N_\mu)}{N_\mu} \right)^2 \simeq \left(\frac{\sigma(\alpha_1)}{\alpha_1} \right)^2 + \left(\frac{\sigma(\alpha_2)}{\alpha_2} \right)^2 + \dots + \left(\frac{\sigma(\alpha_c)}{\alpha_c} \right)^2$$

Universality features of muon production



(Cazon, Epiphany Conference 2022)

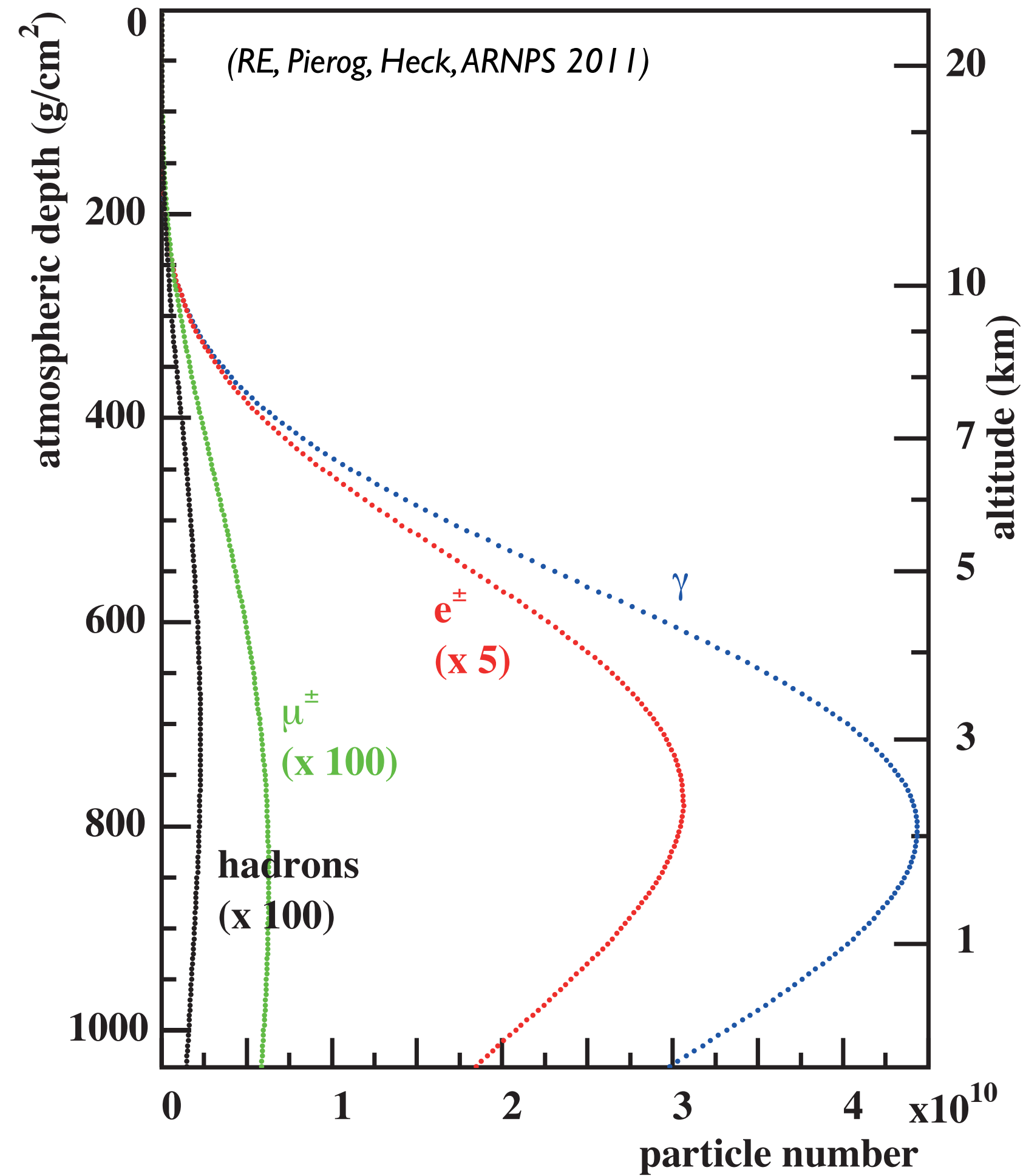
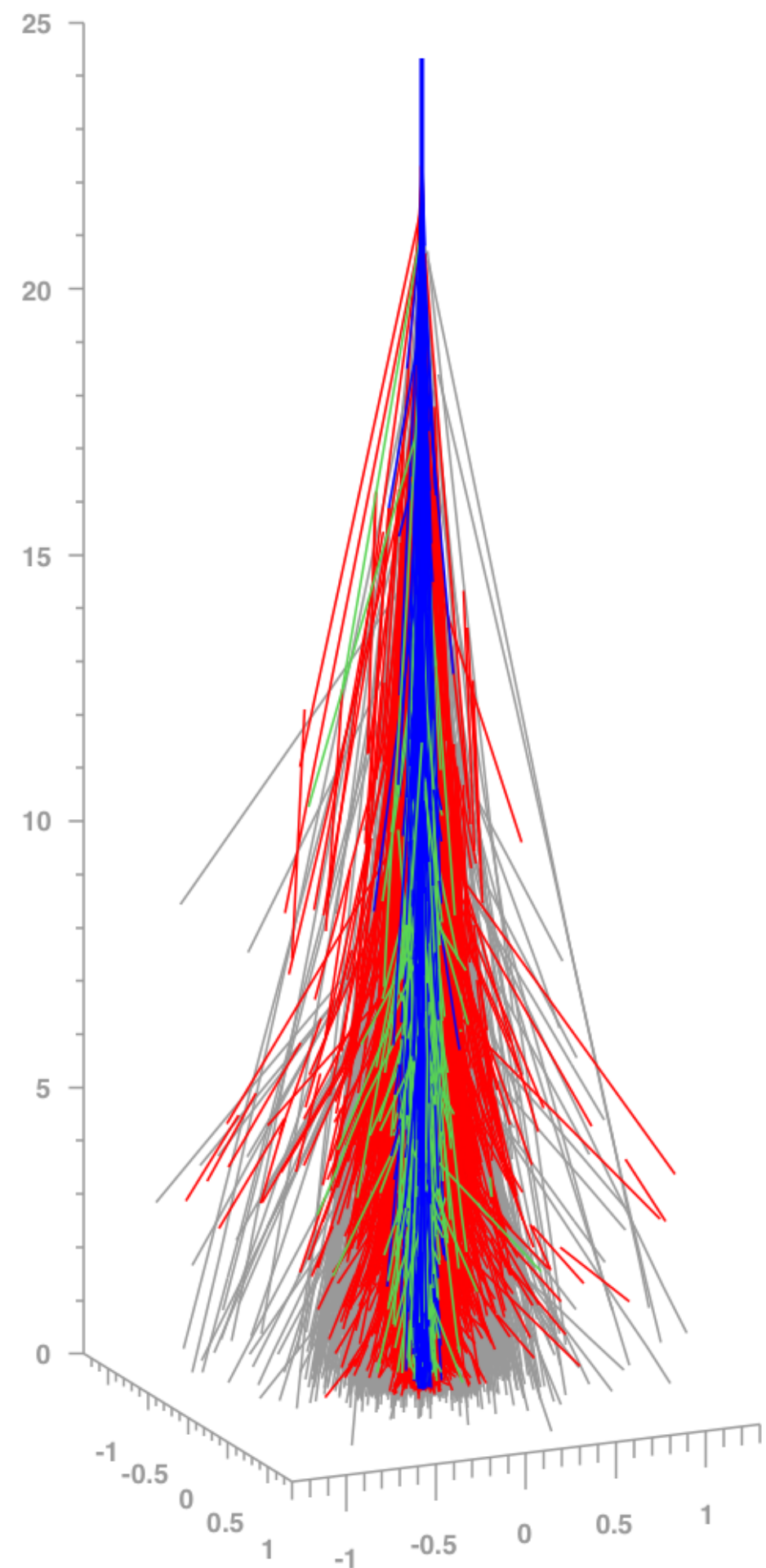
Muon production depth



Muons from high-energy interactions

Muons from low-energy interactions

Expectation from simulations

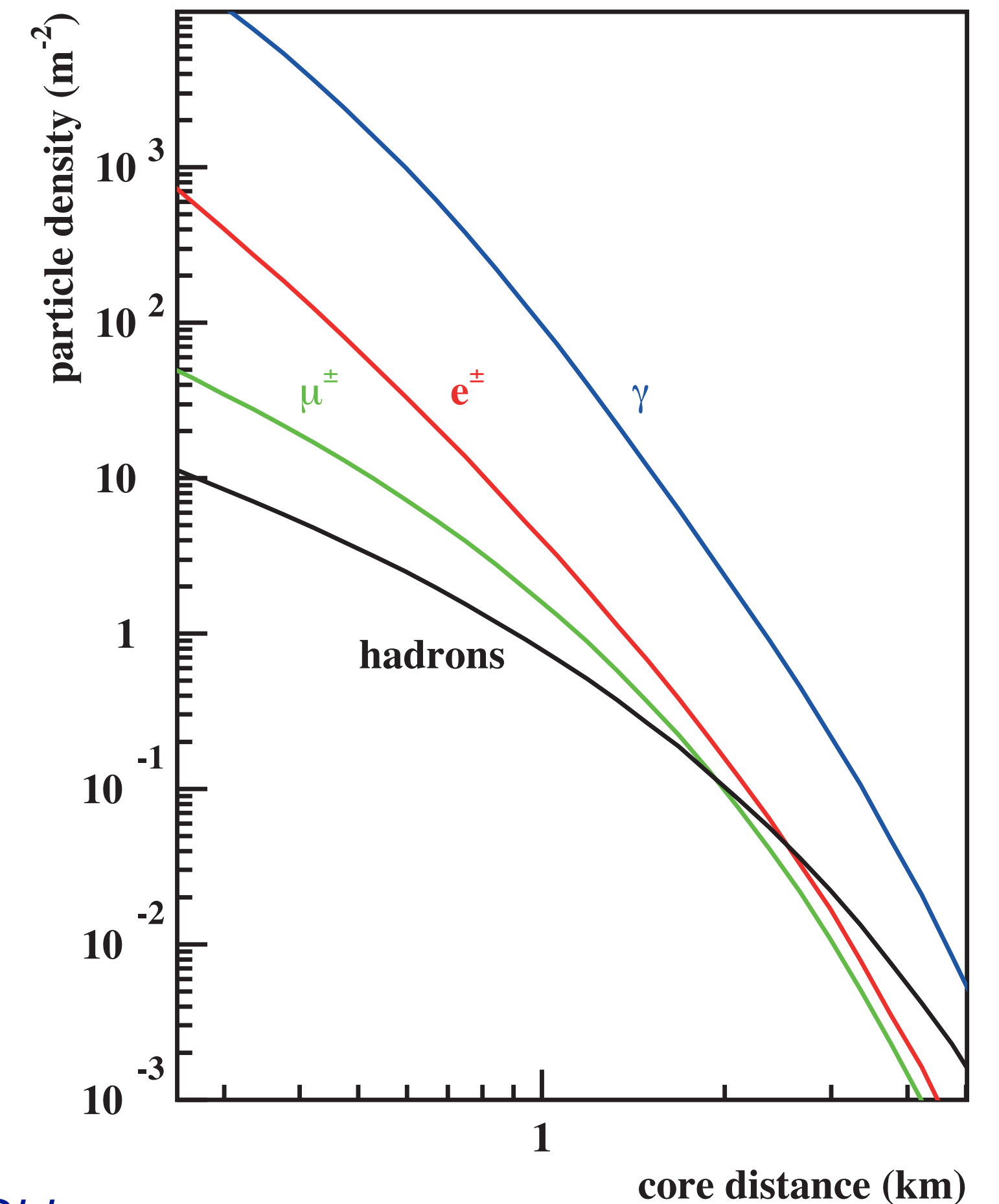


Longitudinal profile:

Cherenkov light
 Fluorescence light
 (bulk of particles measured)

Lateral profiles:

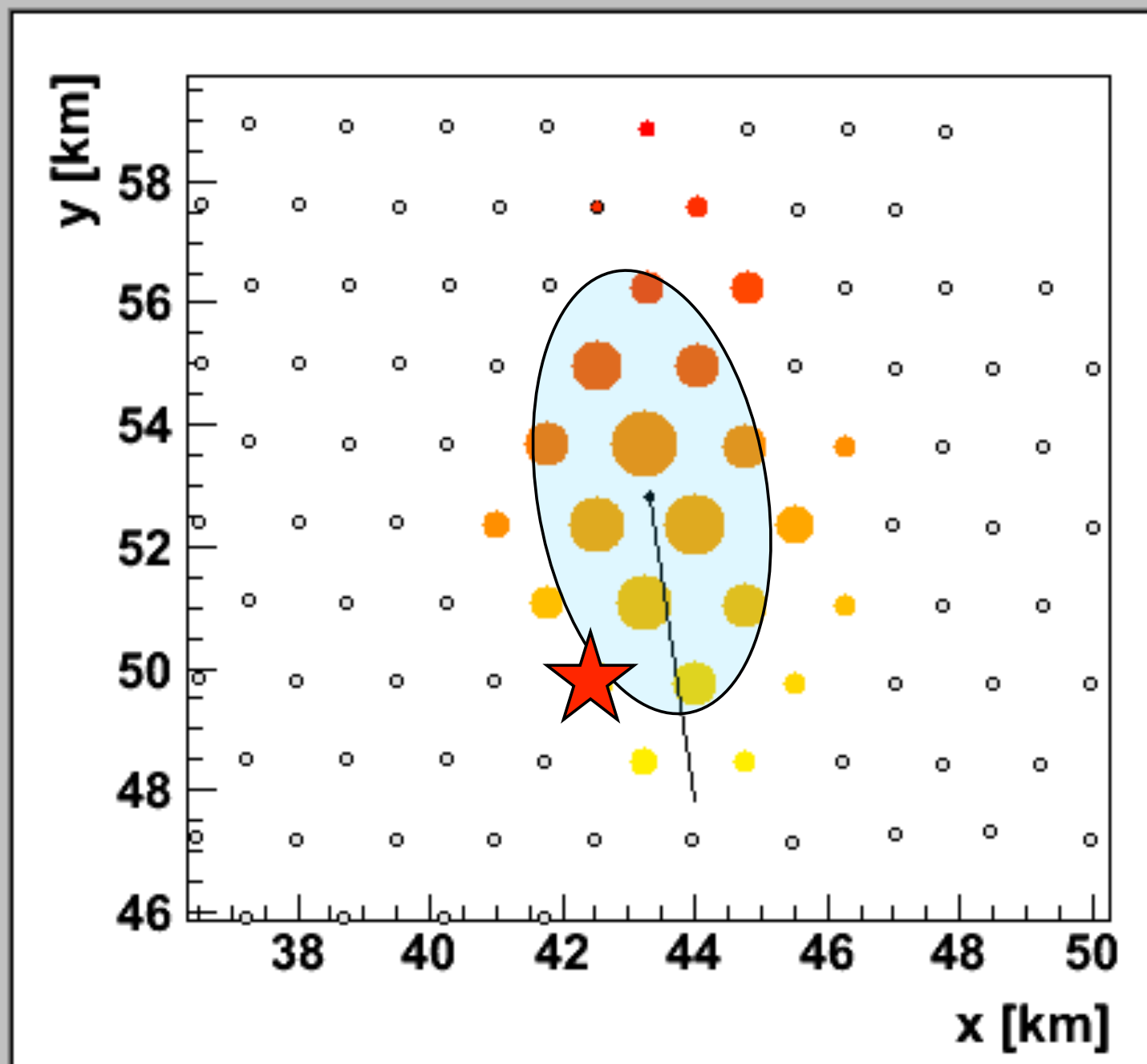
particle detectors at ground
 (very small fraction of particles sampled)



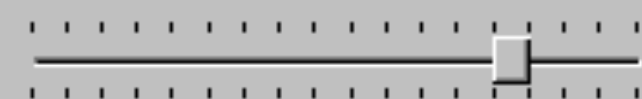
See talk by Piera Ghia

Event Info | MC info

Event 8123914 :-)
 Time 933708755 s 768757000 ns
 3TOT & 4C1; T5
 Candidate stations: 24(20 acc)
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 $R = 20.59 \pm 0.57$ km
 $r_{\text{opt}} = 1109.4$ m

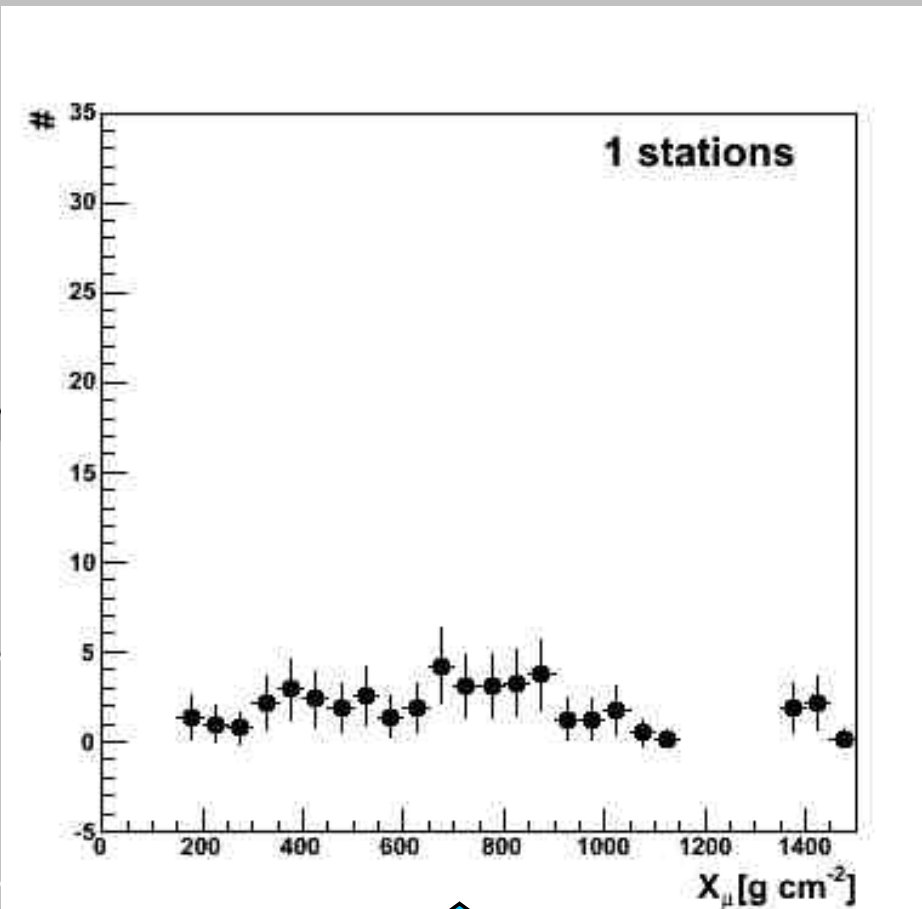


1398 TOT 898.1(1091.9) VEM
1522 TOT 365.1 VEM
1396 TOT 207.4 VEM
1523 TOT 179.7 VEM
1391 TOT 81.1 VEM
1390 TOT 56.1 VEM
1386 TOT 45.5 VEM
1520 TOT 42.2 VEM
1305 TOT 40.0 VEM
1456 TOT 37.1 VEM
1533 TOT 23.9 VEM
1498 TOT 18.6 VEM

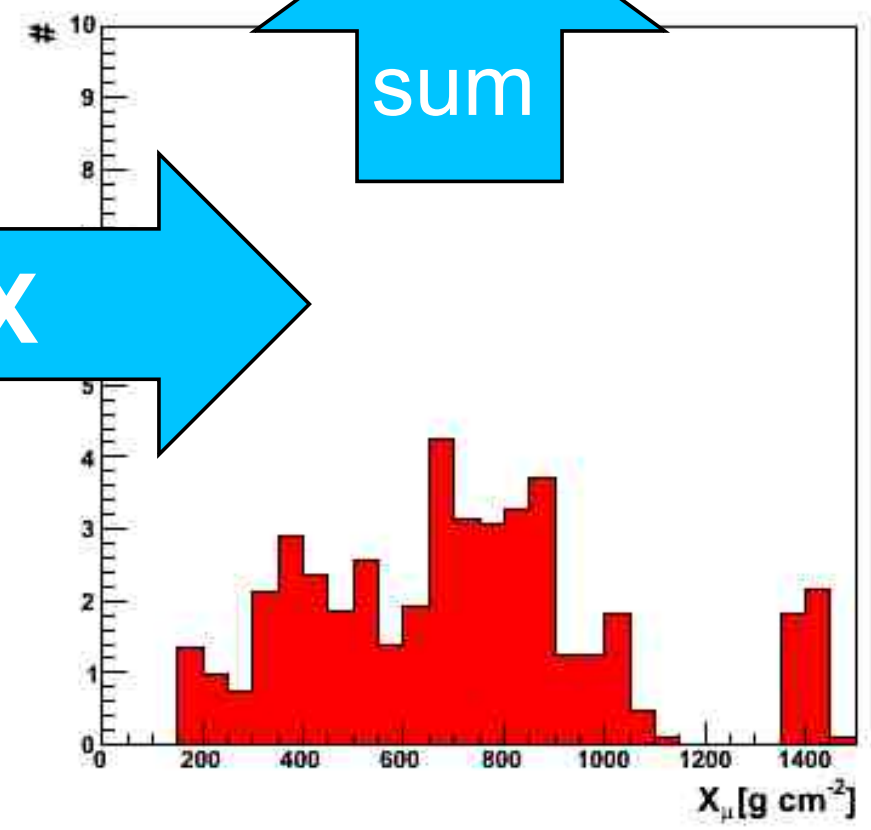
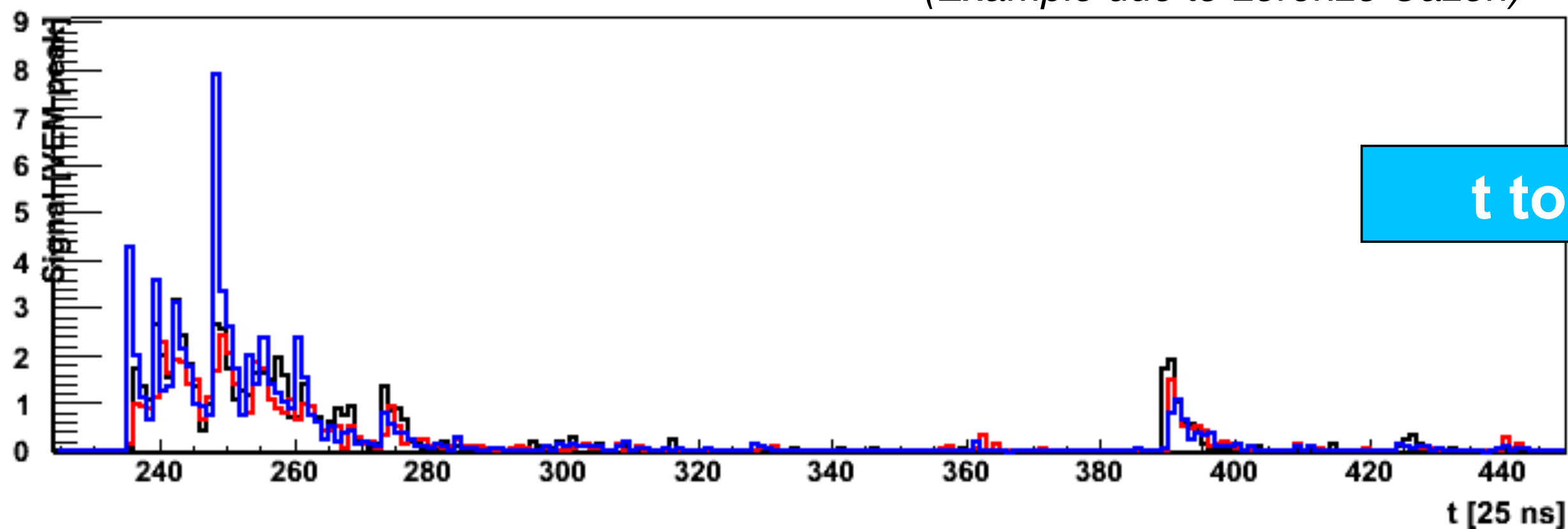


LDF LDF Res

LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)



(Example due to Lorenzo Cazon)

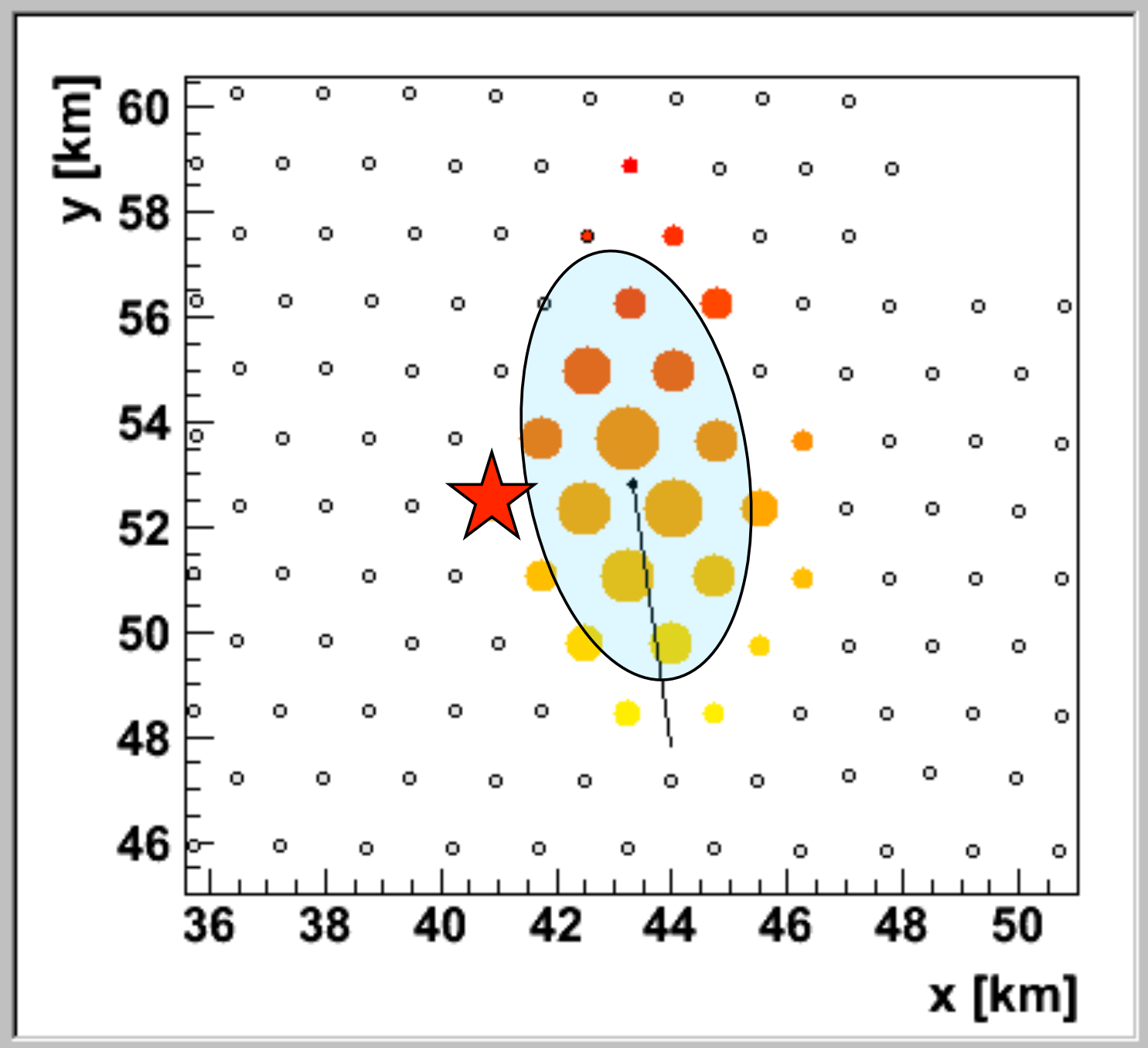


t to X

sum

Event Info | MC info

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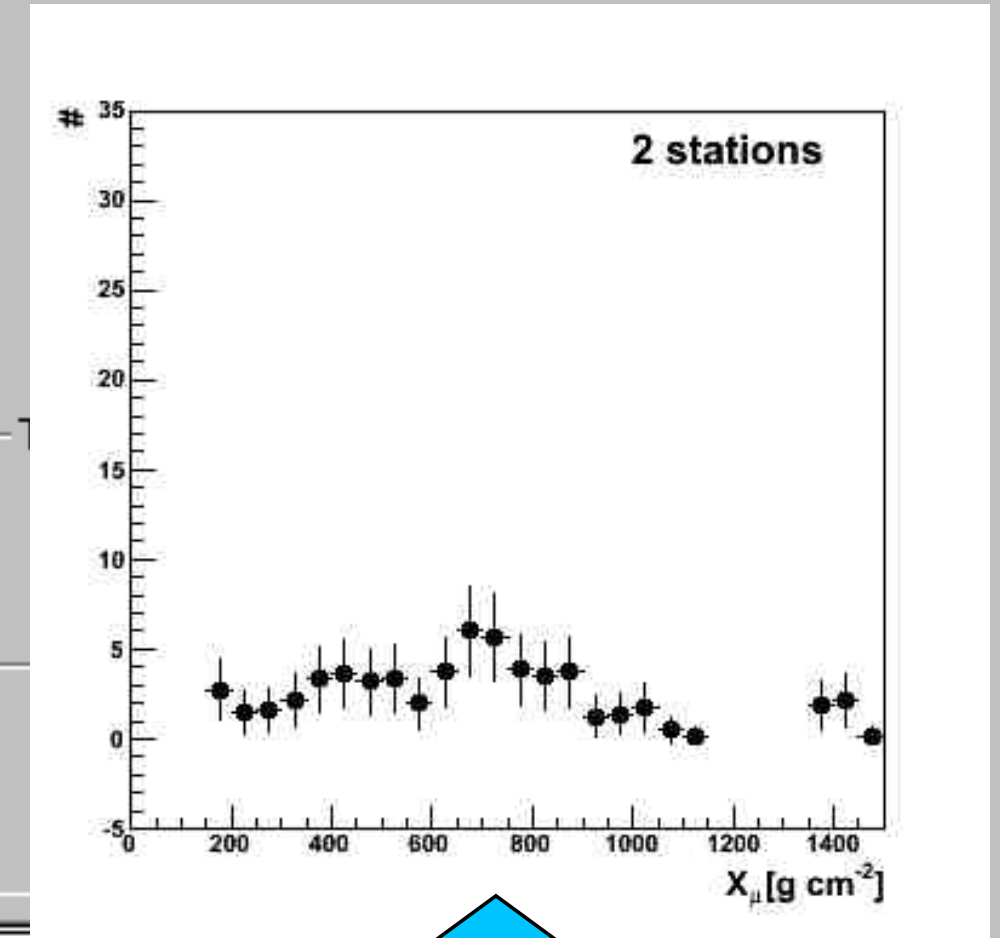


1305 TOT 40.0 VEM
1456 TOT 37.1 VEM
1533 TOT 23.9 VEM
1498 TOT 18.6 VEM
1378 TOT 18.0 VEM
1528 TOT 15.4 VEM
1535 TOT 11.4 VEM
1460 TOT 8.9 VEM
1519 TOT 8.7 VEM
1406 TOT 6.0 VEM
1463 TOT 5.8 VEM
1423 TOT 4.9 VEM

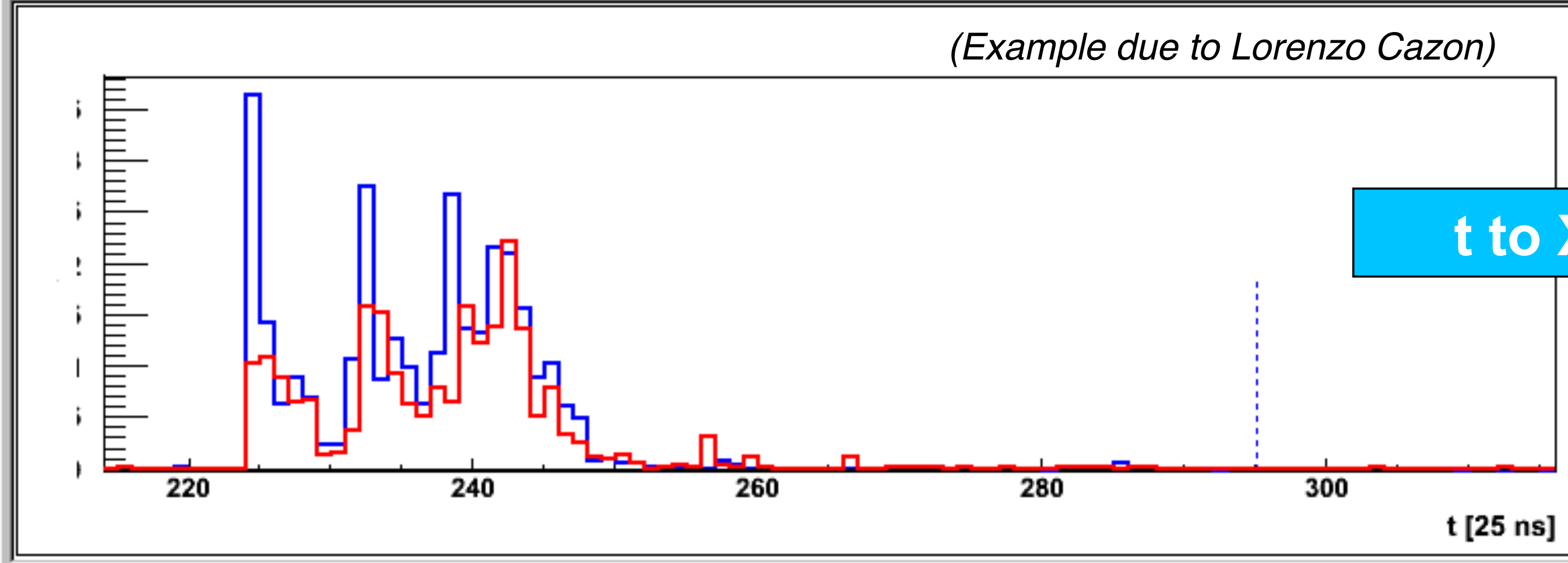


LDF LDF Res

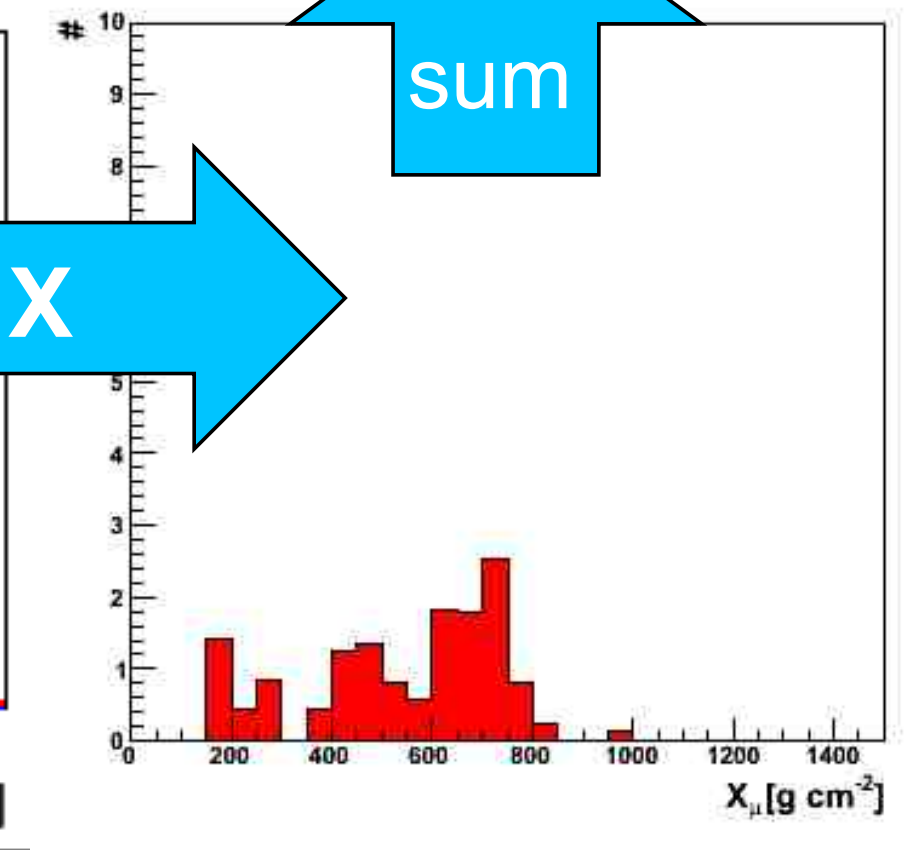
LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)



(Example due to Lorenzo Cazon)

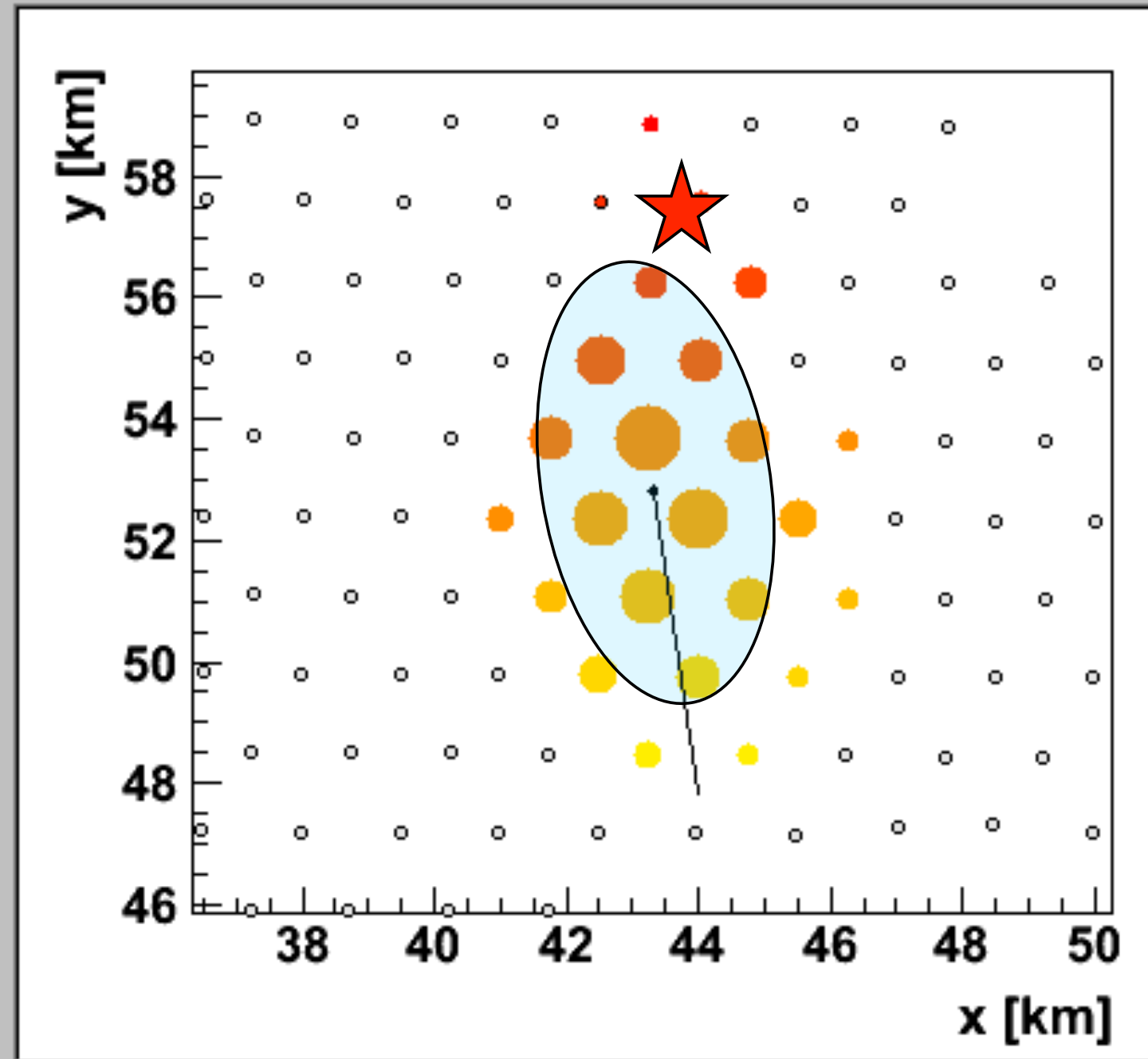


t to X



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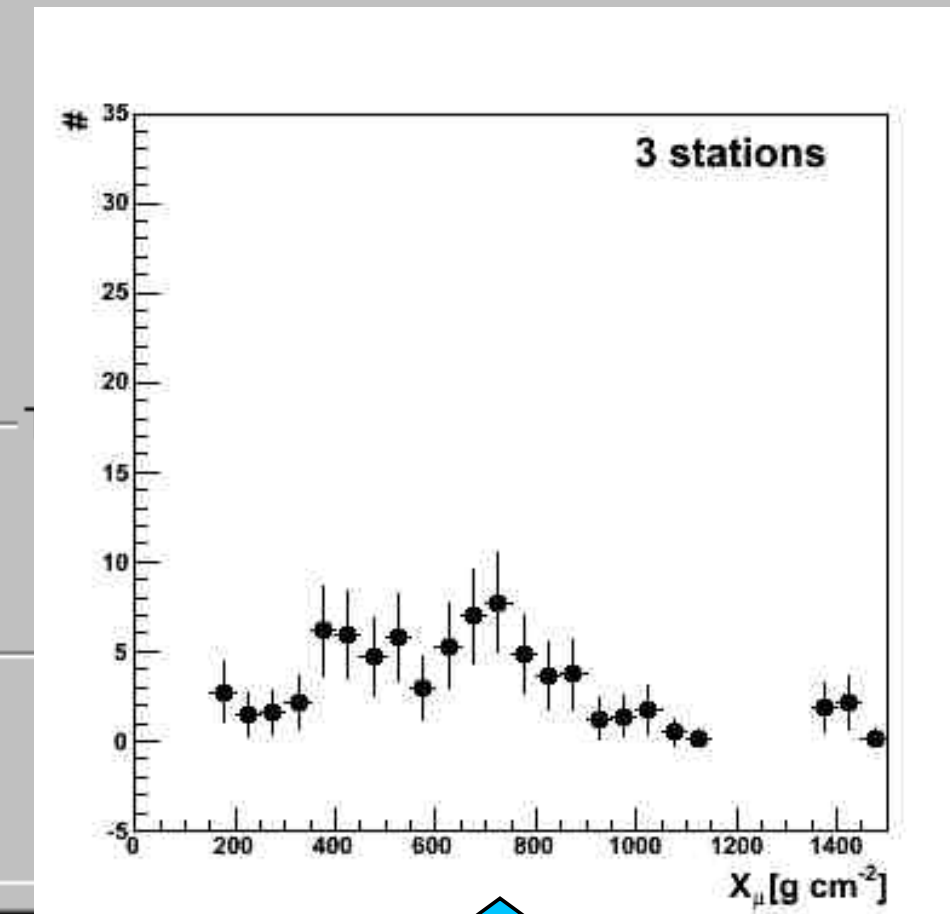


1533 TOT 23.9 VEM
1498 TOT 18.6 VEM
1378 TOT 18.0 VEM
1528 TOT 15.4 VEM
1535 TOT 11.4 VEM
1460 TOT 8.9 VEM
1519 TOT 8.7 VEM
1406 TOT 6.0 VEM
1463 TOT 5.8 VEM
1423 TOT 4.9 VEM
1491 TOT 4.9 VEM
1354 TOT 4.6 VEM

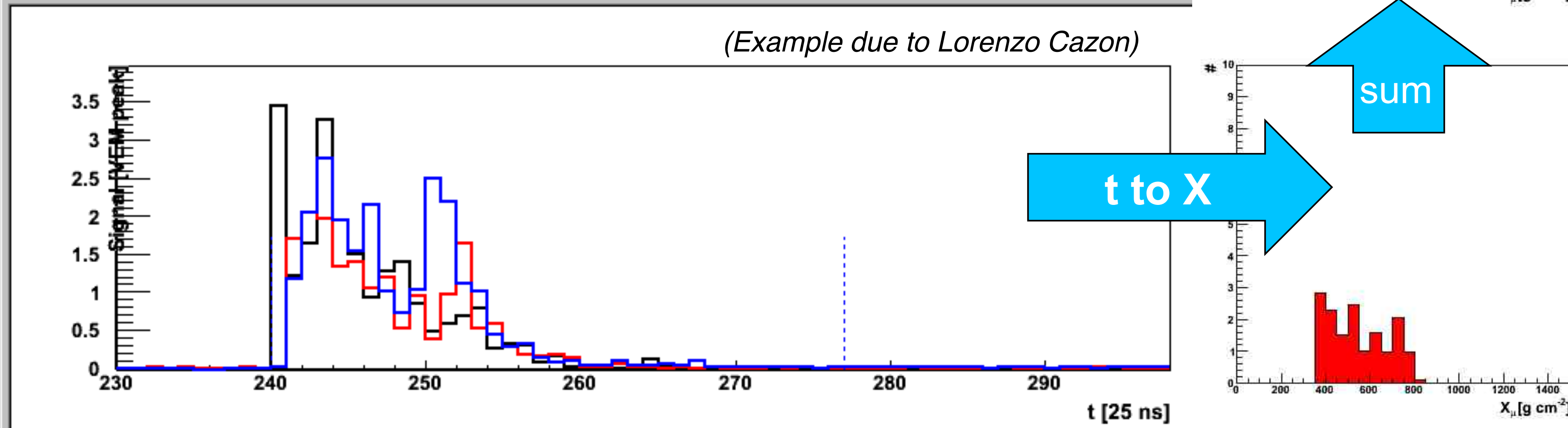


LDF LDF Res

LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)



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Event Info | MC info

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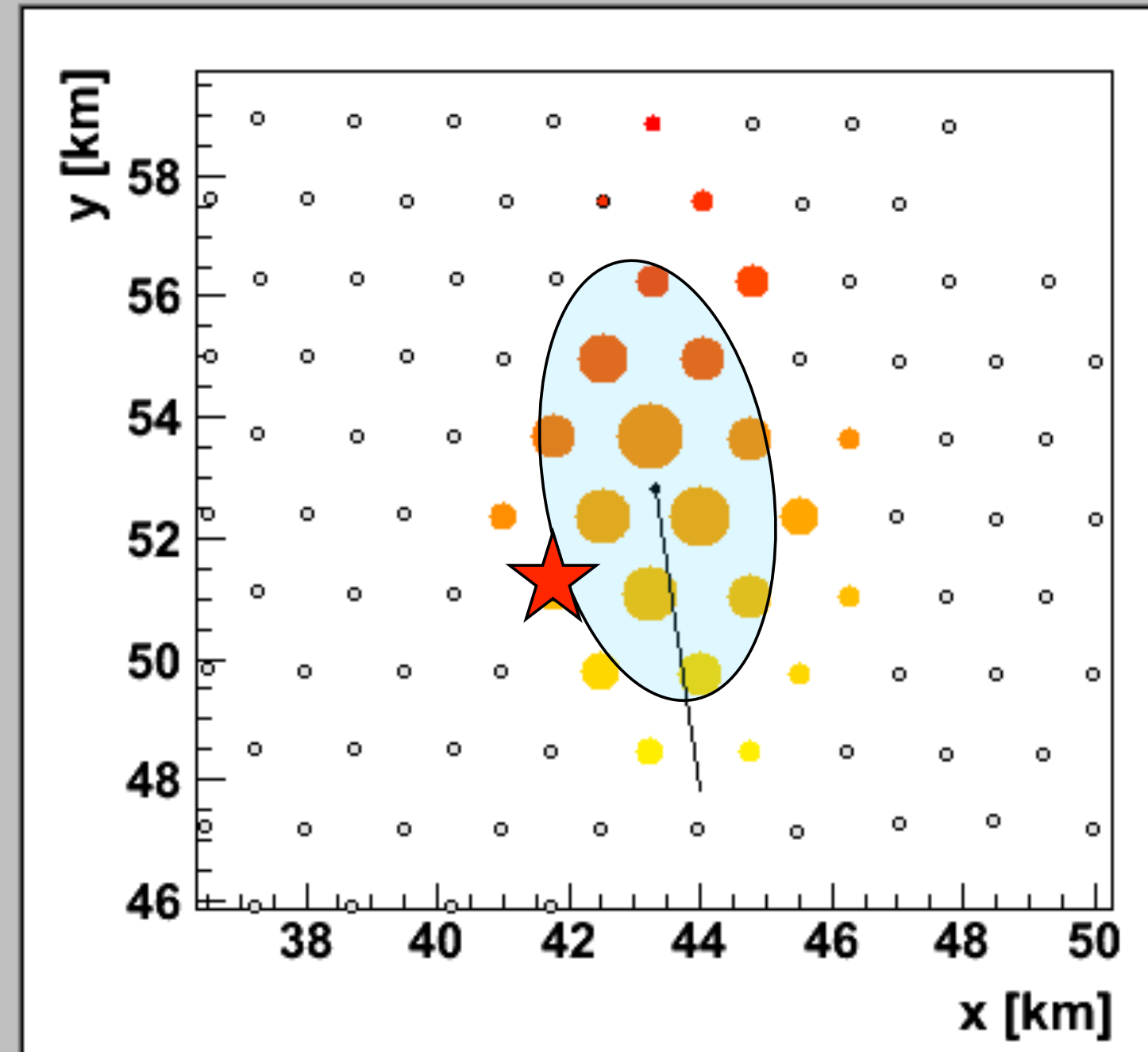
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$R = 20.59 \pm 0.57$ km

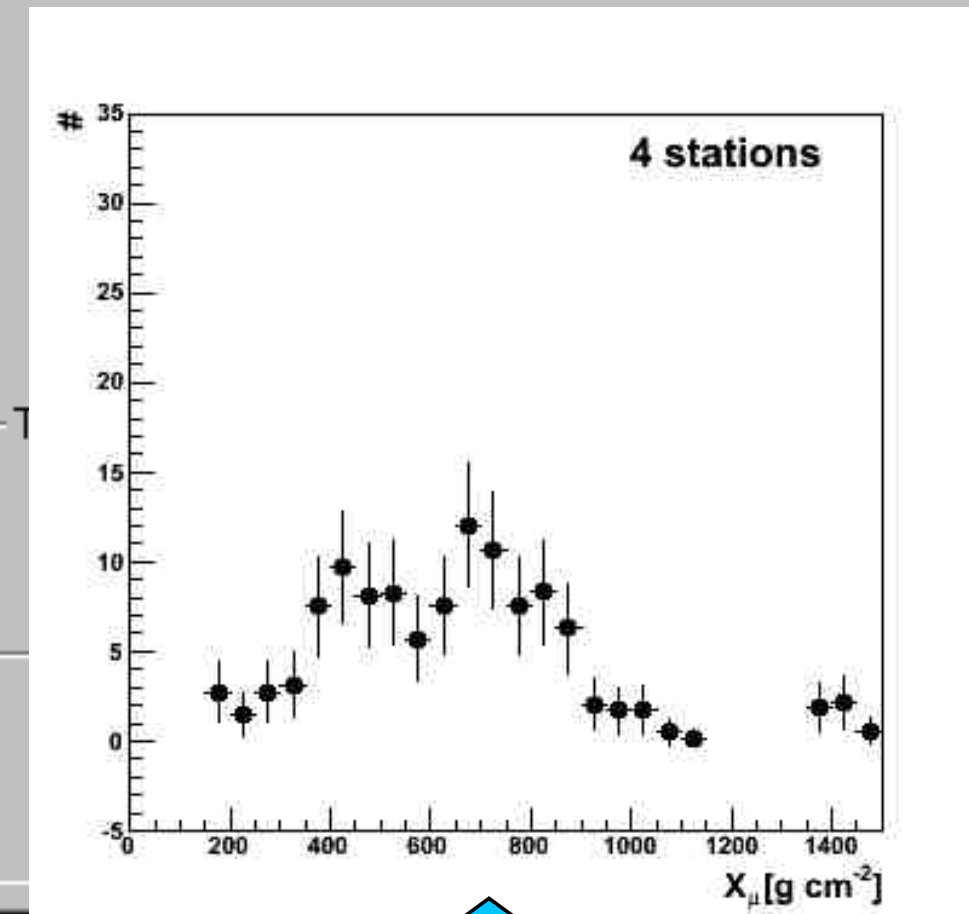
$r_{opt} = 1109.4$ m



LDF LDF Res

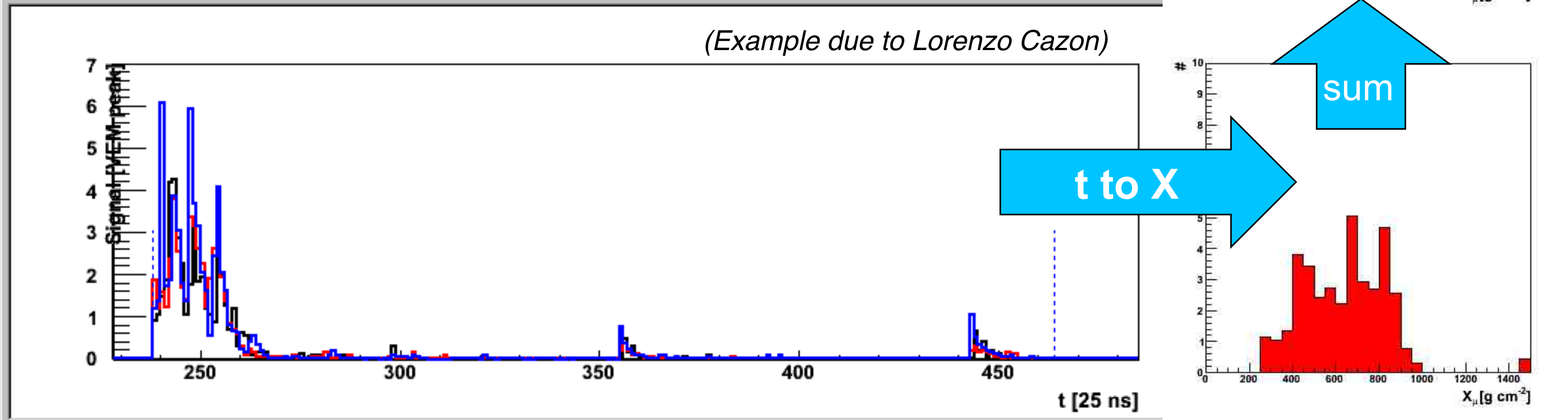


1390	TOT 56.1	VEM
1386	TOT 45.5	VEM
1520	TOT 42.2	VEM
1305	TOT 40.0	VEM
1456	TOT 37.1	VEM
1533	TOT 23.9	VEM
1498	TOT 18.6	VEM
1378	TOT 18.0	VEM
1528	TOT 15.4	VEM
1535	TOT 11.4	VEM
1460	TOT 8.9	VEM
1519	TOT 8.7	VEM



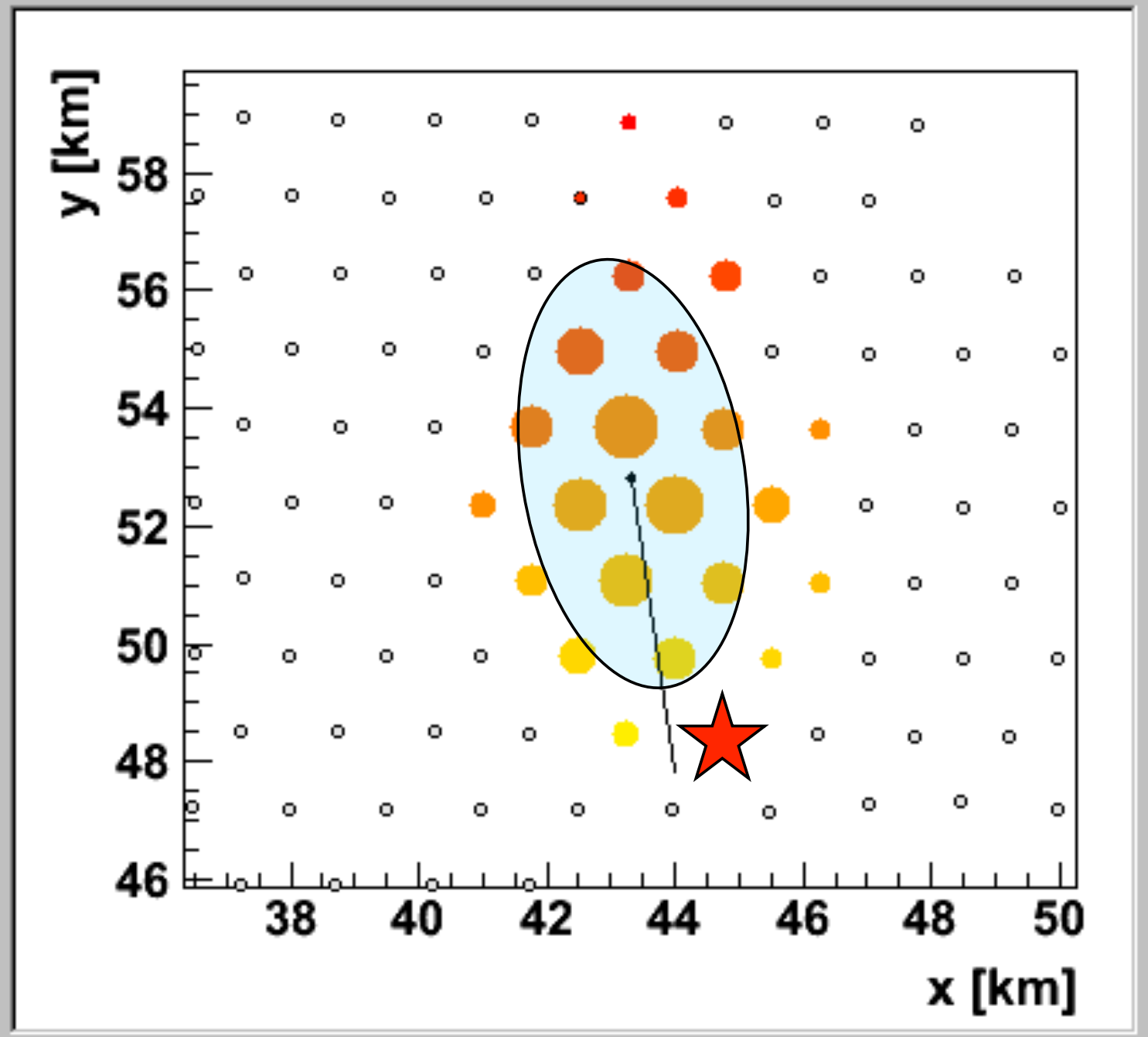
LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)

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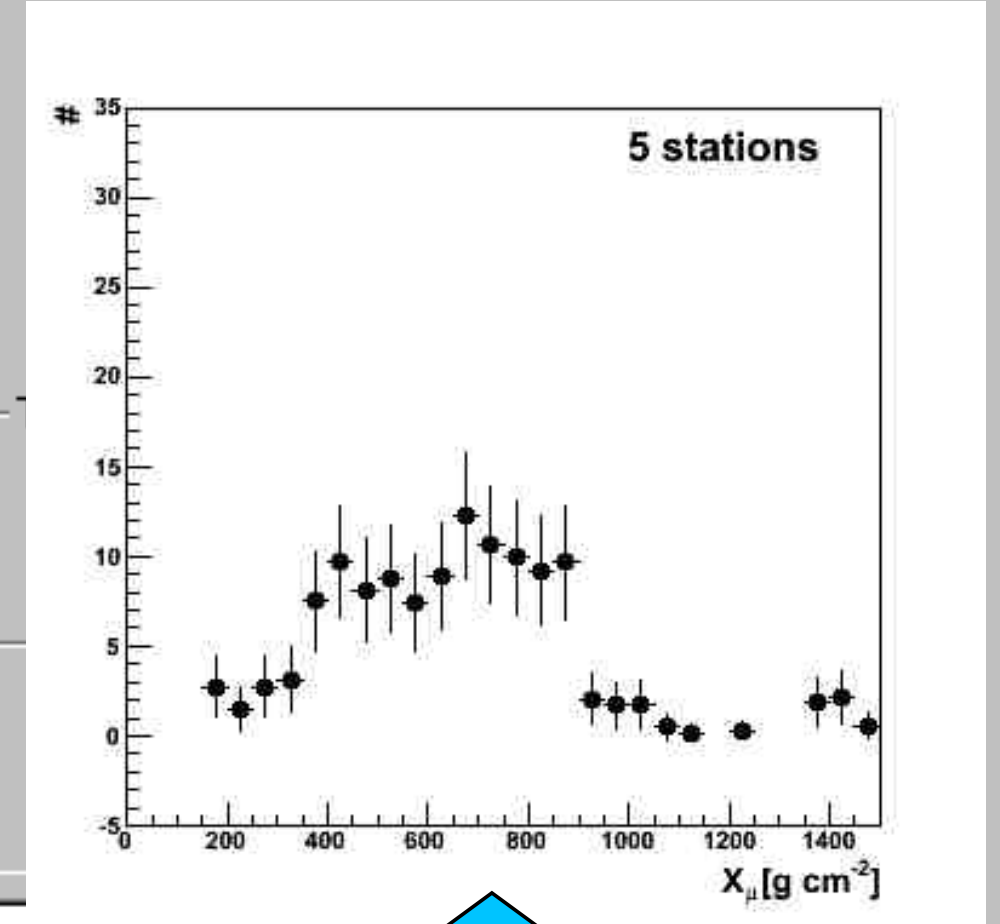


1533 TOT 23.9 VEM
1498 TOT 18.6 VEM
1378 TOT 18.0 VEM
1528 TOT 15.4 VEM
1535 TOT 11.4 VEM
1460 TOT 8.9 VEM
1519 TOT 8.7 VEM
1406 TOT 6.0 VEM
1463 TOT 5.8 VEM
1423 TOT 4.9 VEM
1491 TOT 4.9 VEM
1354 TOT 4.6 VEM

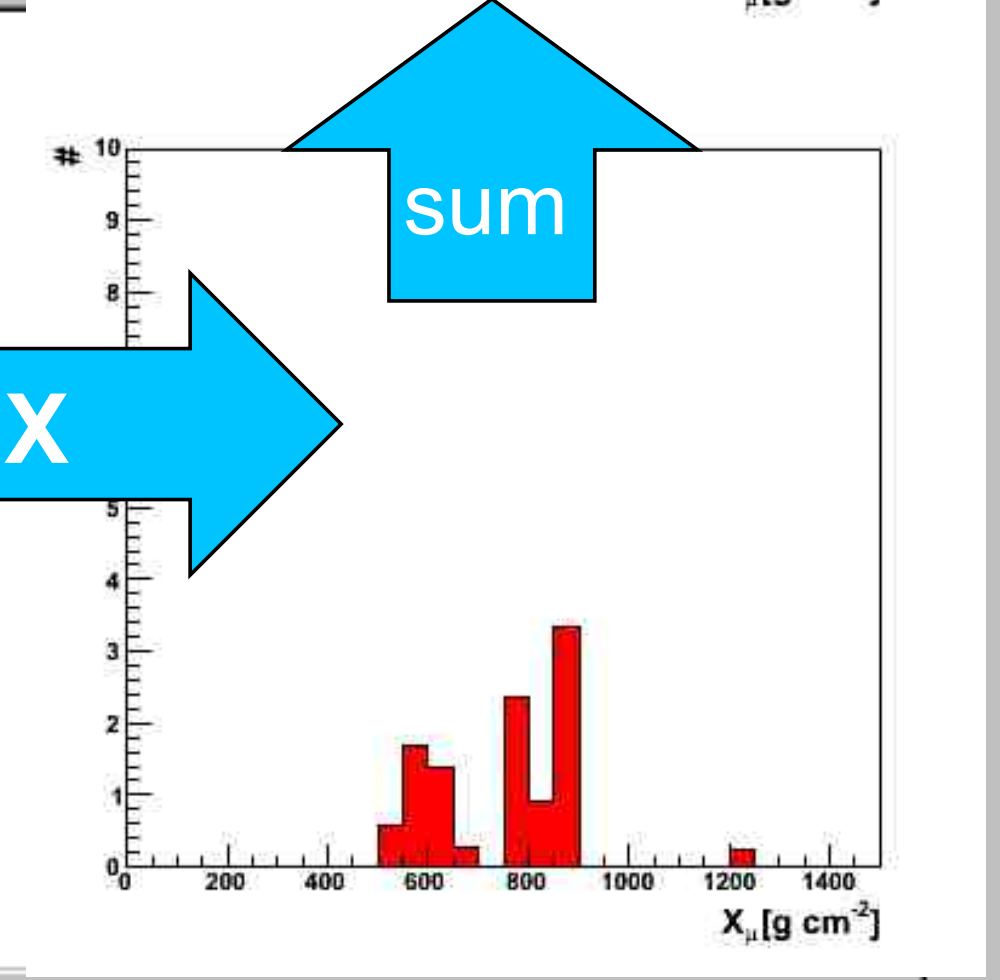
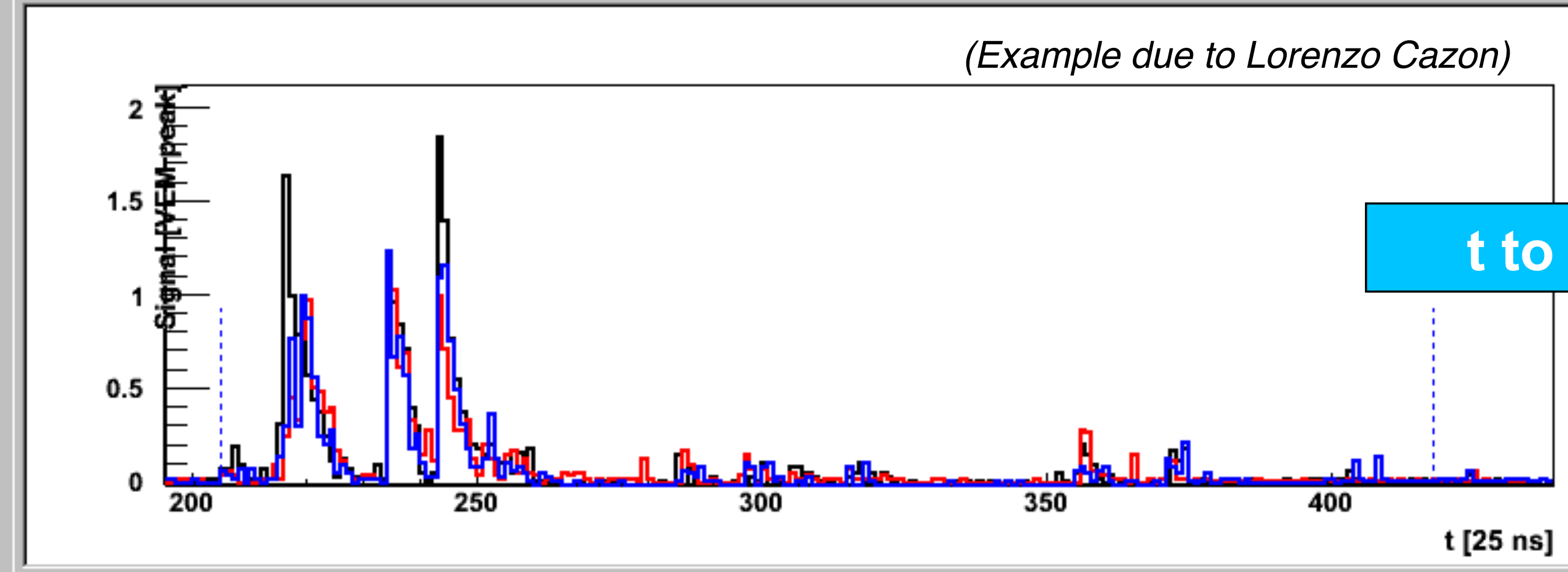


LDF LDF Res

LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)

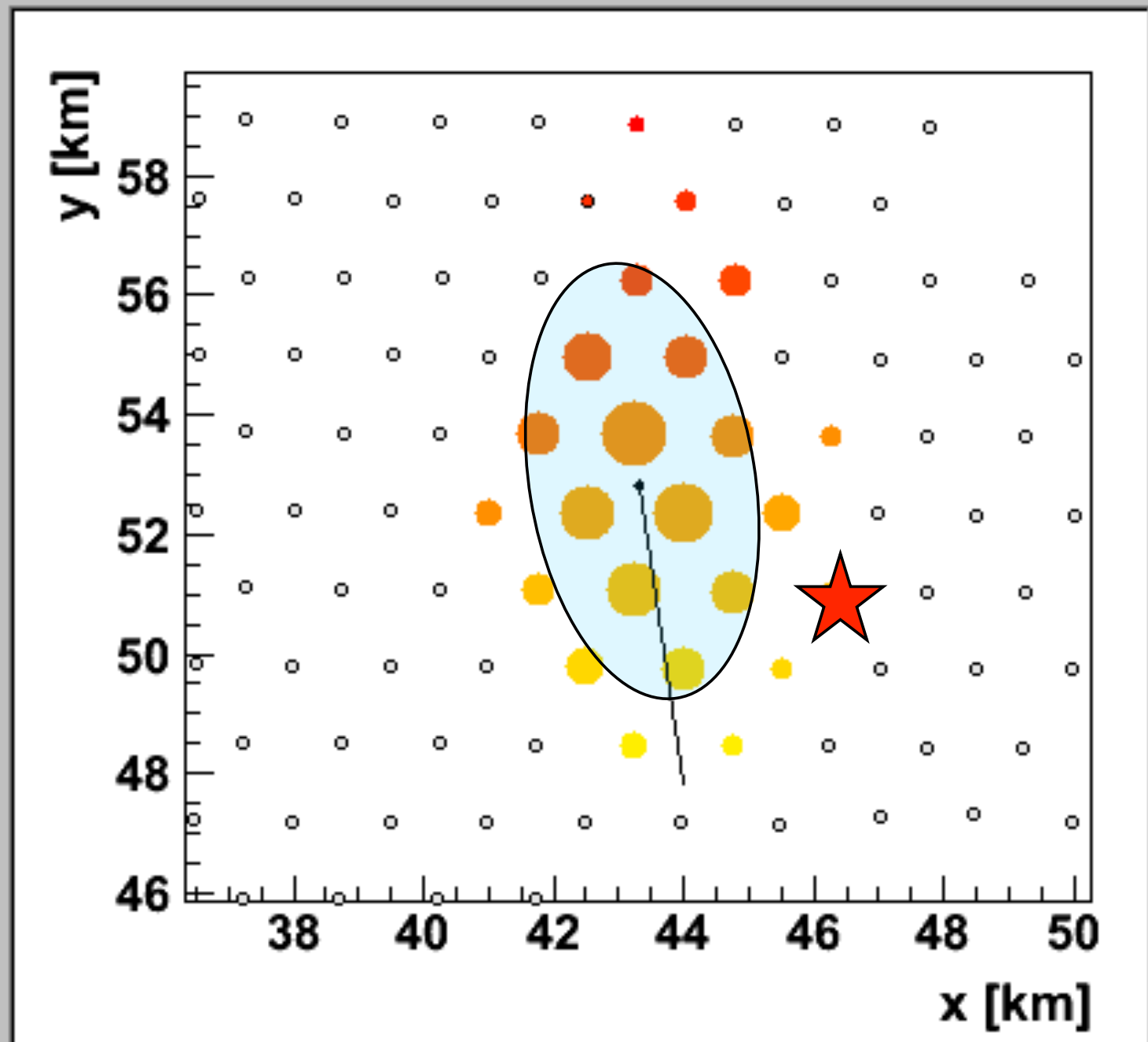


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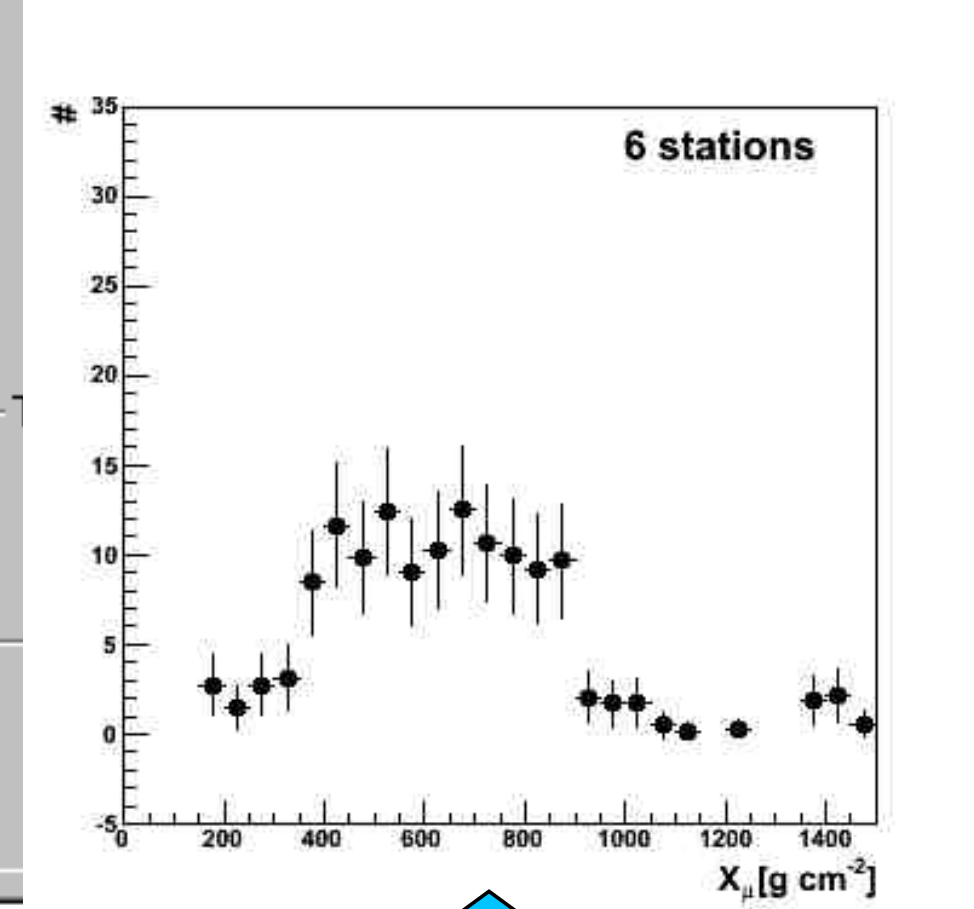


1378 TOT 18.0 VEM
1528 TOT 15.4 VEM
1535 TOT 11.4 VEM
1460 TOT 8.9 VEM
1519 TOT 8.7 VEM
1406 TOT 6.0 VEM
1463 TOT 5.8 VEM
1423 TOT 4.9 VEM
1491 TOT 4.9 VEM
1354 TOT 4.6 VEM
1468 TOT 3.9 VEM
1402 Thr1 2.4 VEM

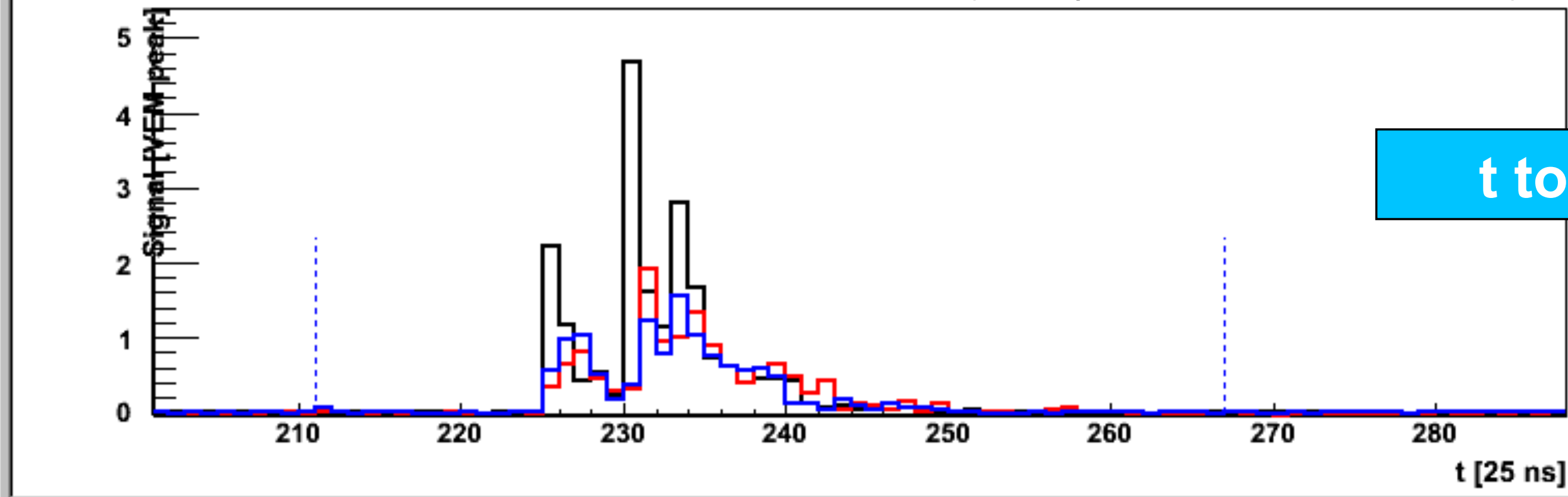


LDF LDF Res

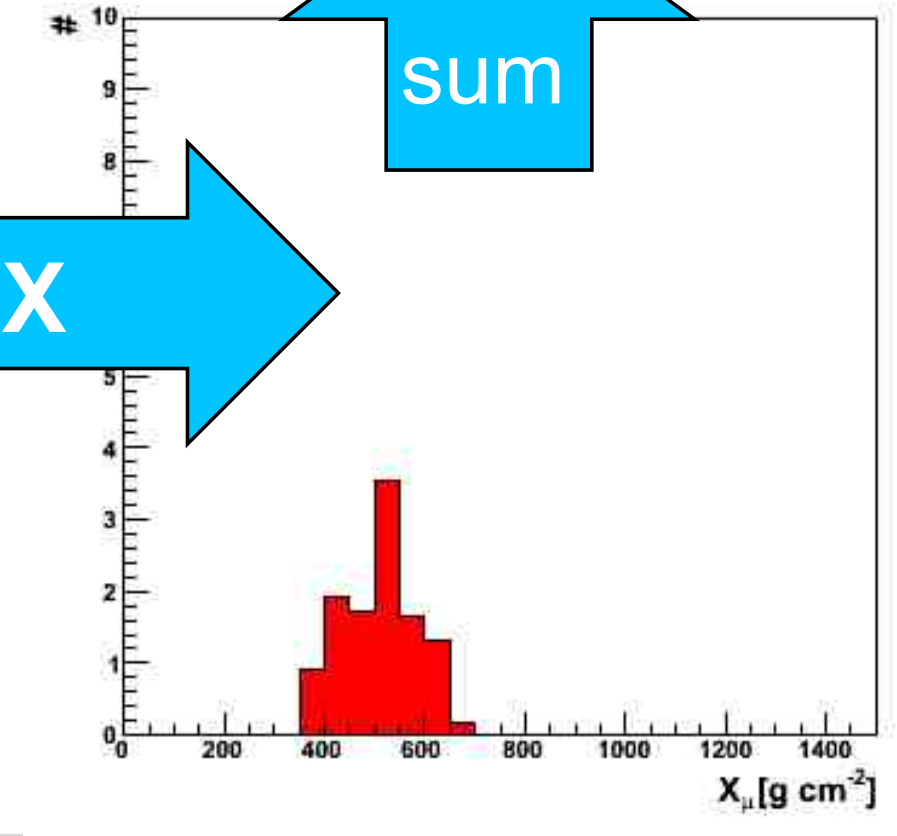
LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)



(Example due to Lorenzo Cazon)

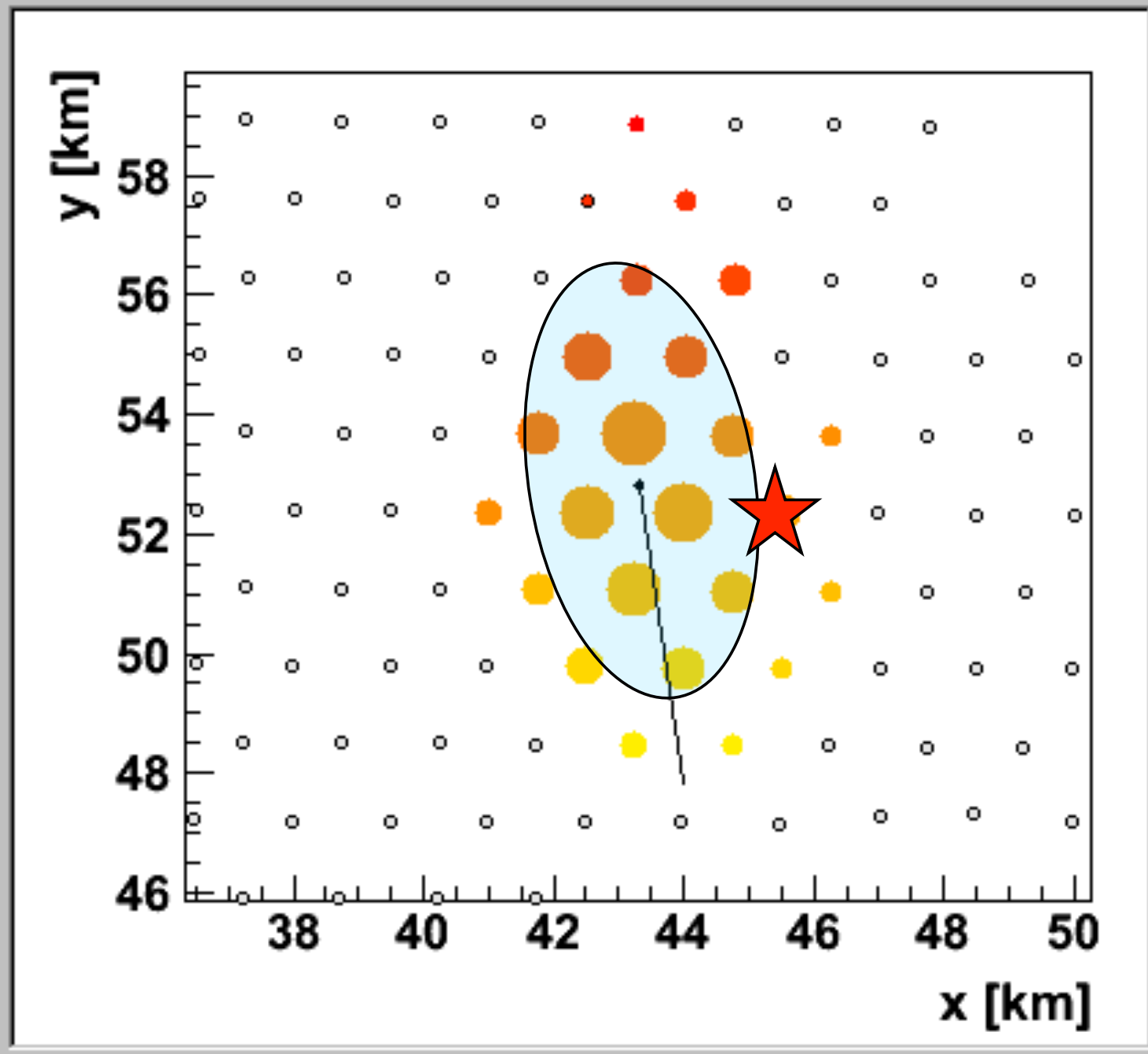


t to X



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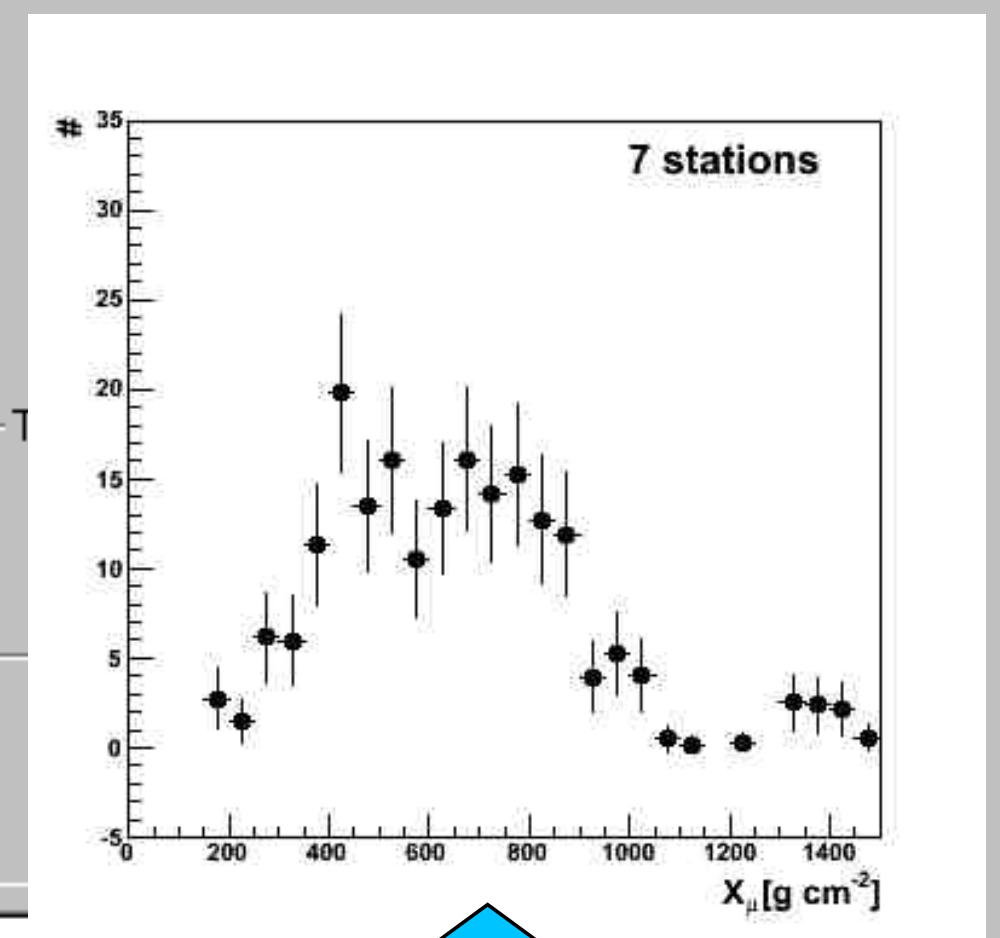


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1522 TOT 365.1 VEM
1396 TOT 207.4 VEM
1523 TOT 179.7 VEM
1391 TOT 81.1 VEM
1390 TOT 56.1 VEM
1386 TOT 45.5 VEM
1520 TOT 42.2 VEM
1305 TOT 40.0 VEM
1456 TOT 37.1 VEM
1533 TOT 23.9 VEM
1498 TOT 18.6 VEM

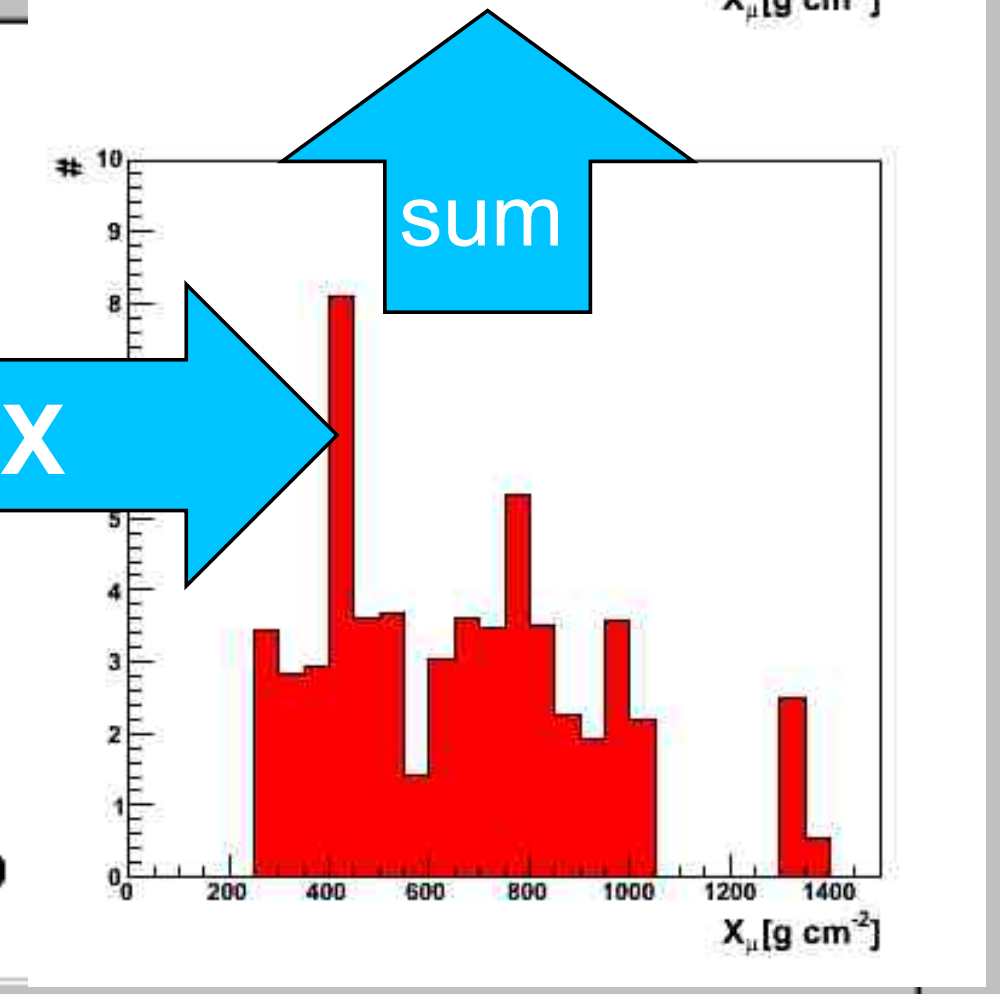
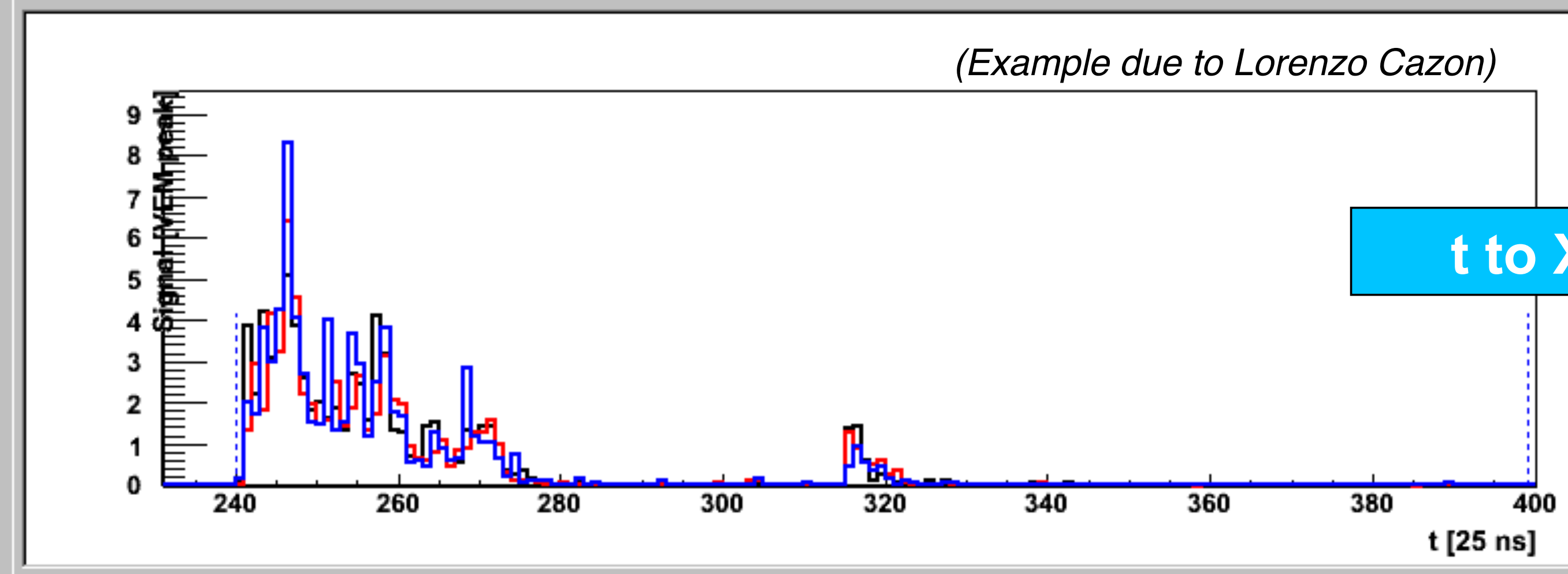


LDF LDF Res

LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)



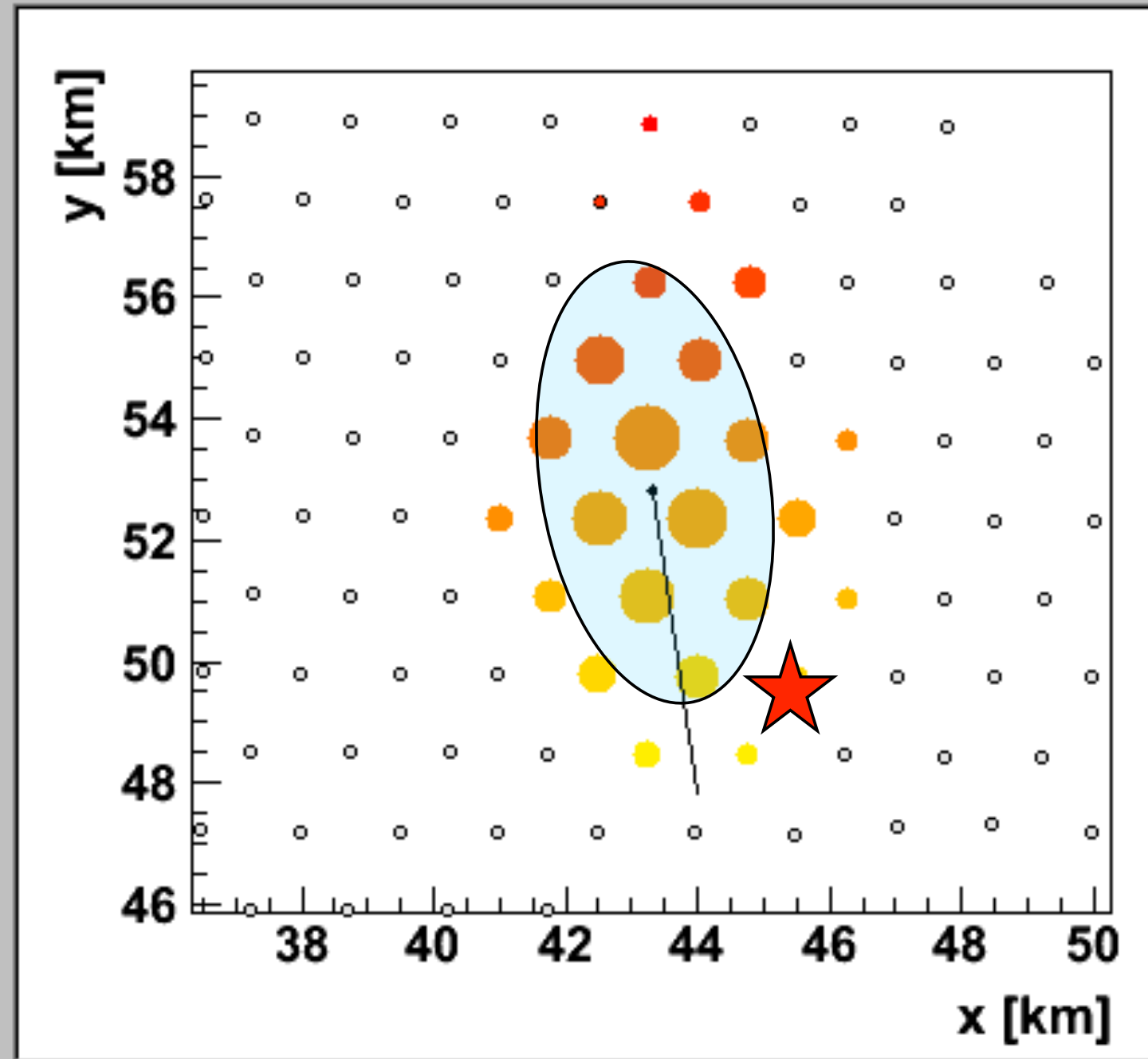
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t to X

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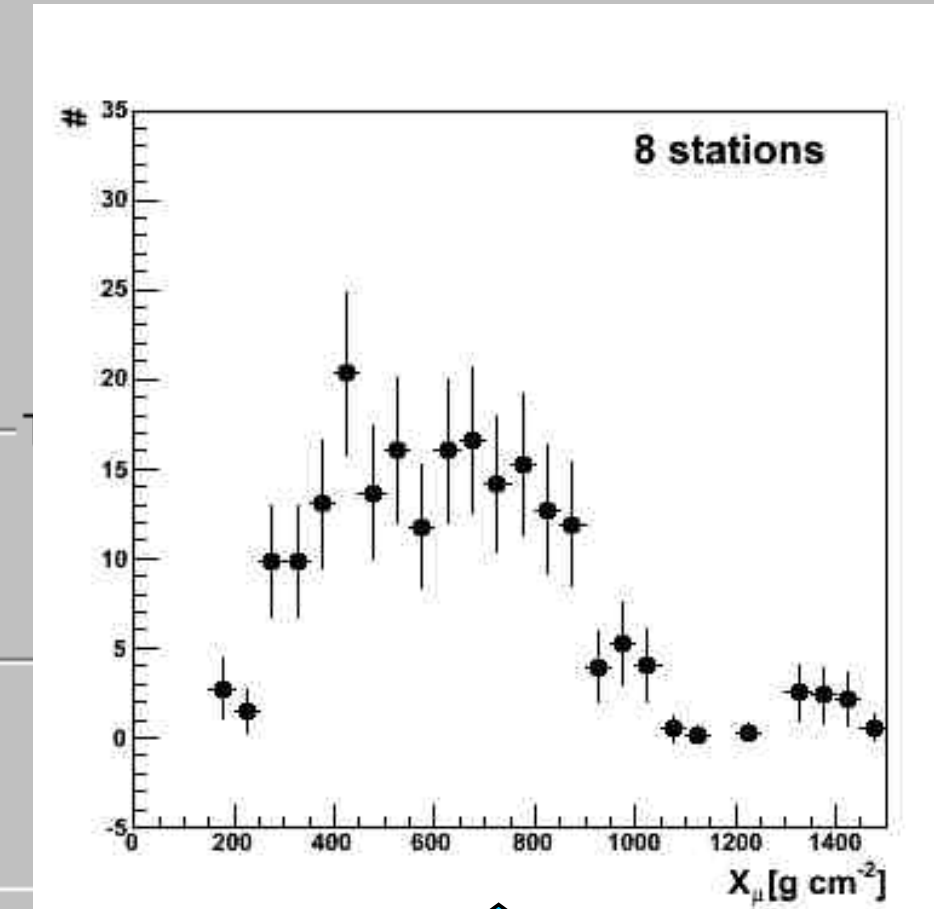


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1463 TOT 5.8 VEM
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1491 TOT 4.9 VEM
1354 TOT 4.6 VEM

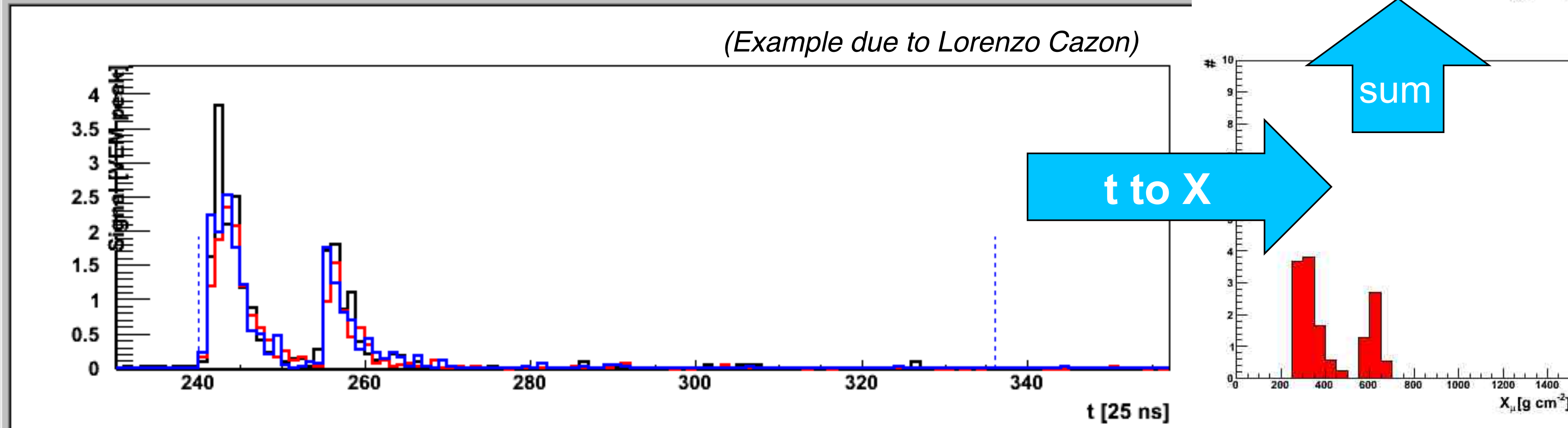


LDF LDF Res

LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)



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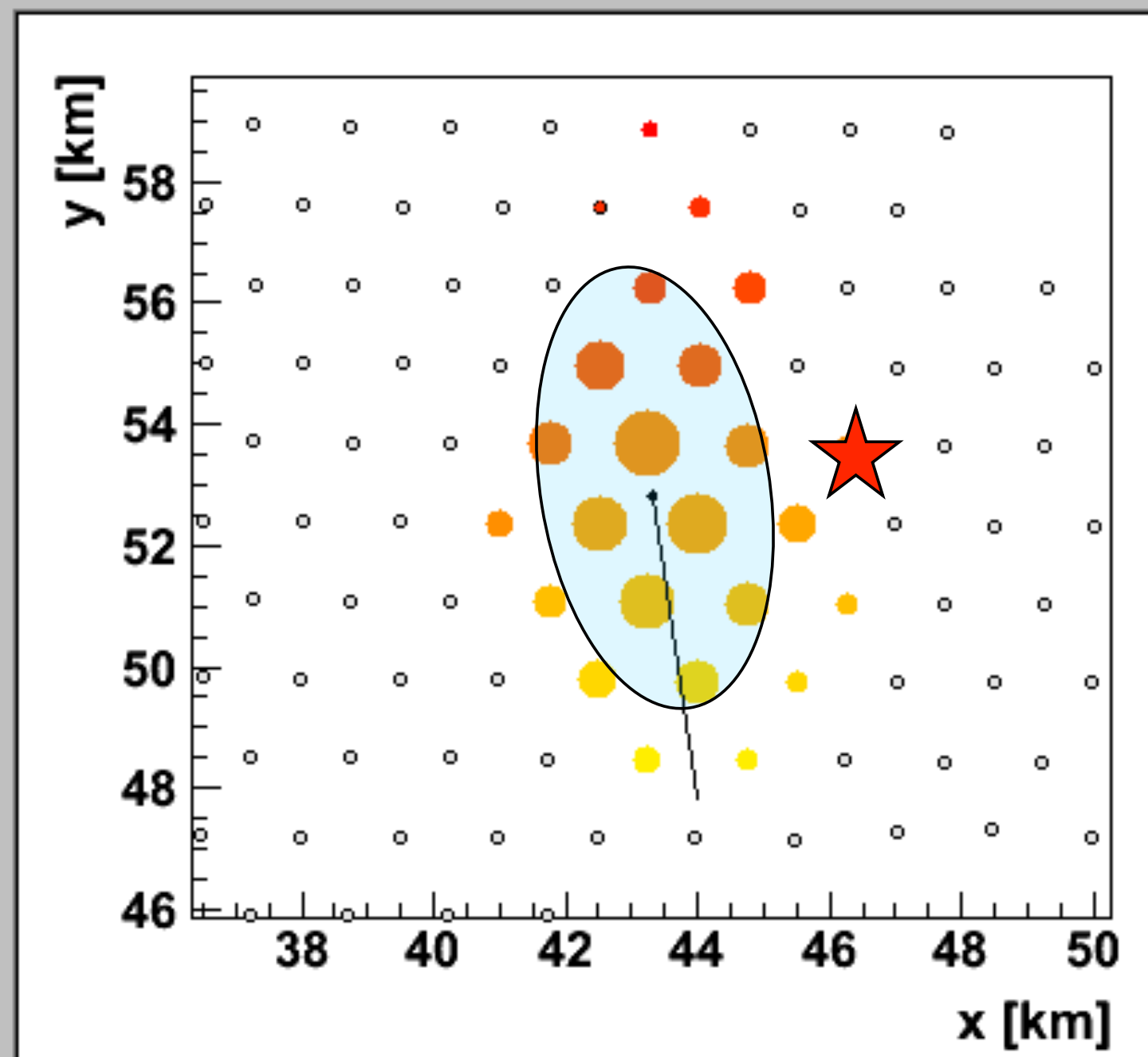
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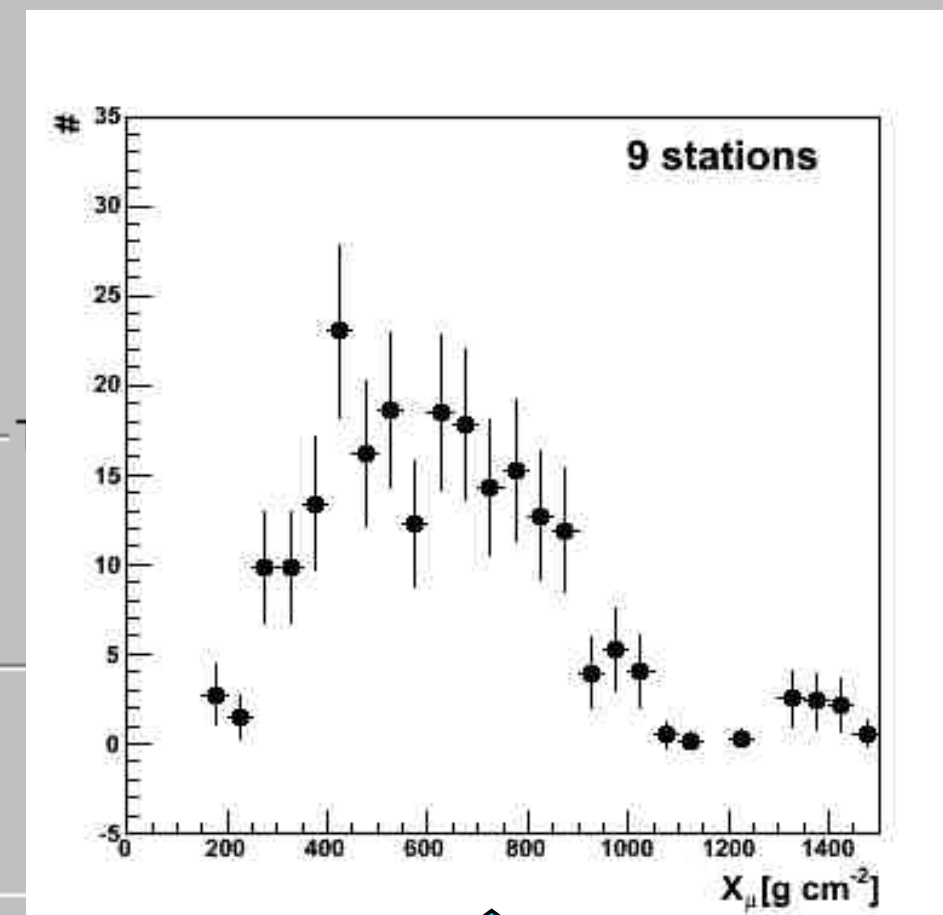
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LDF LDF Res

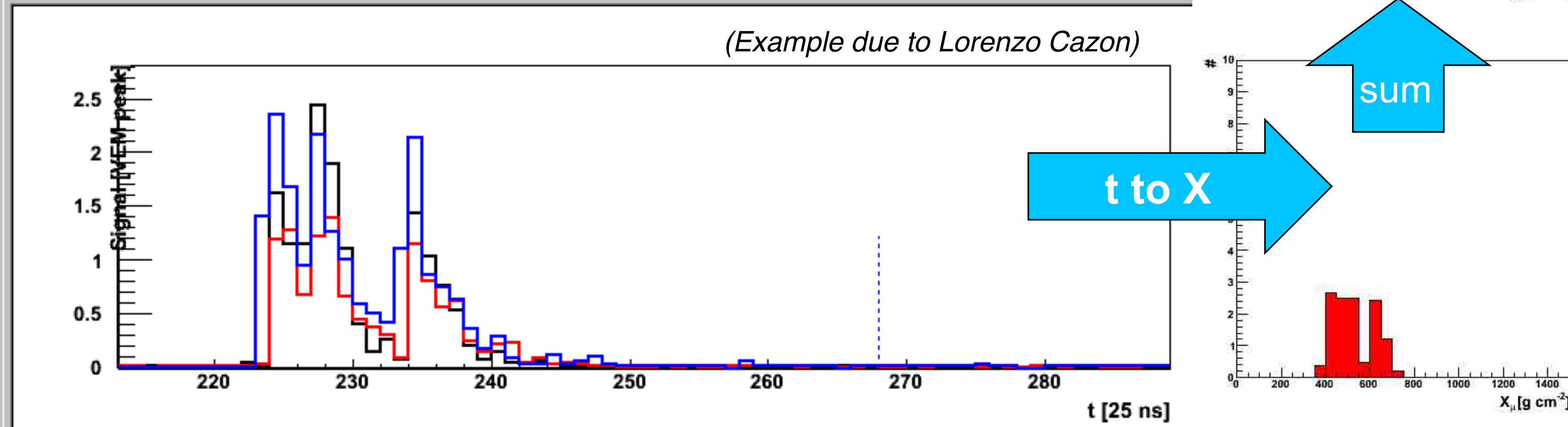


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1491 TOT 4.9 VEM
1354 TOT 4.6 VEM



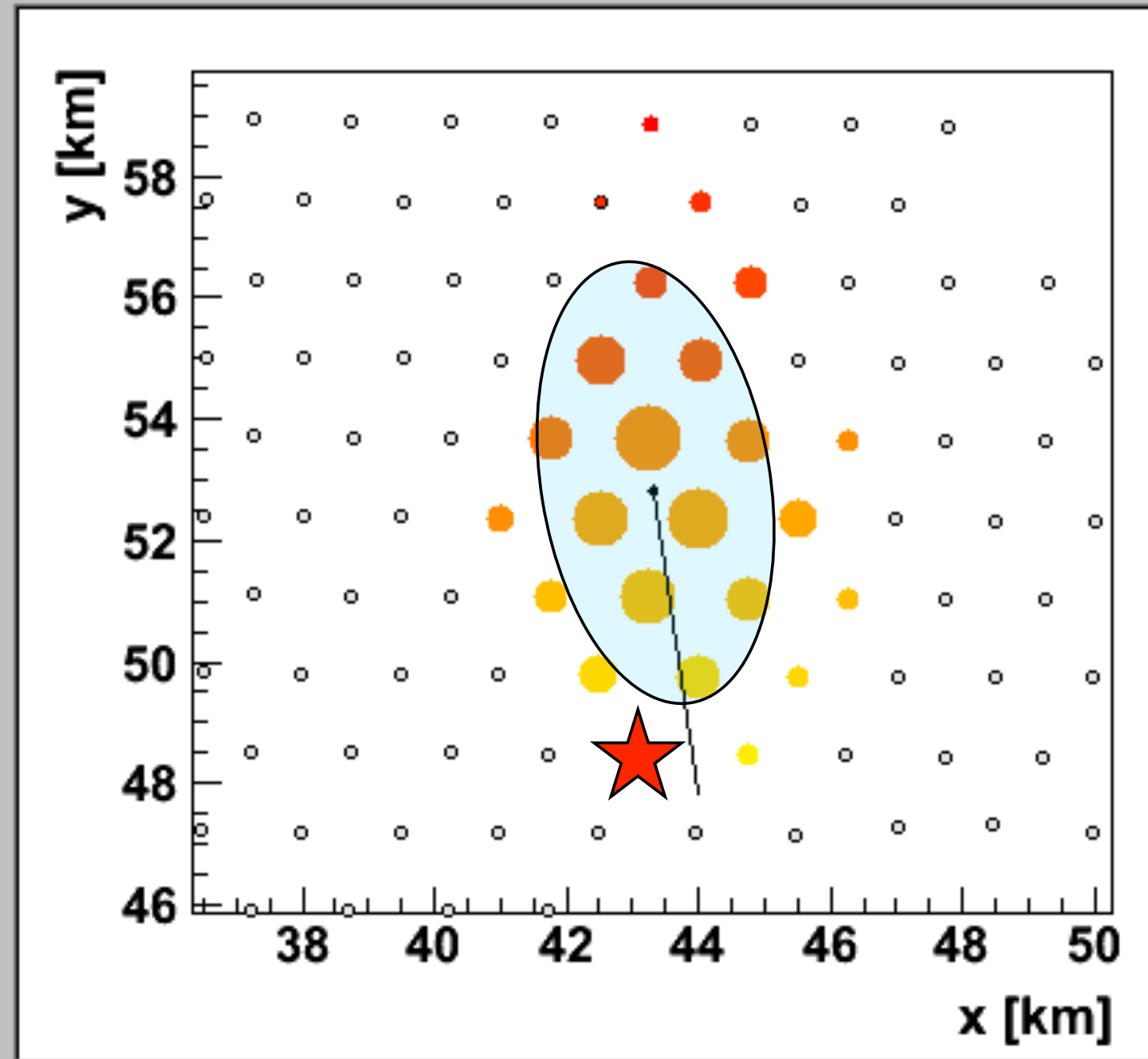
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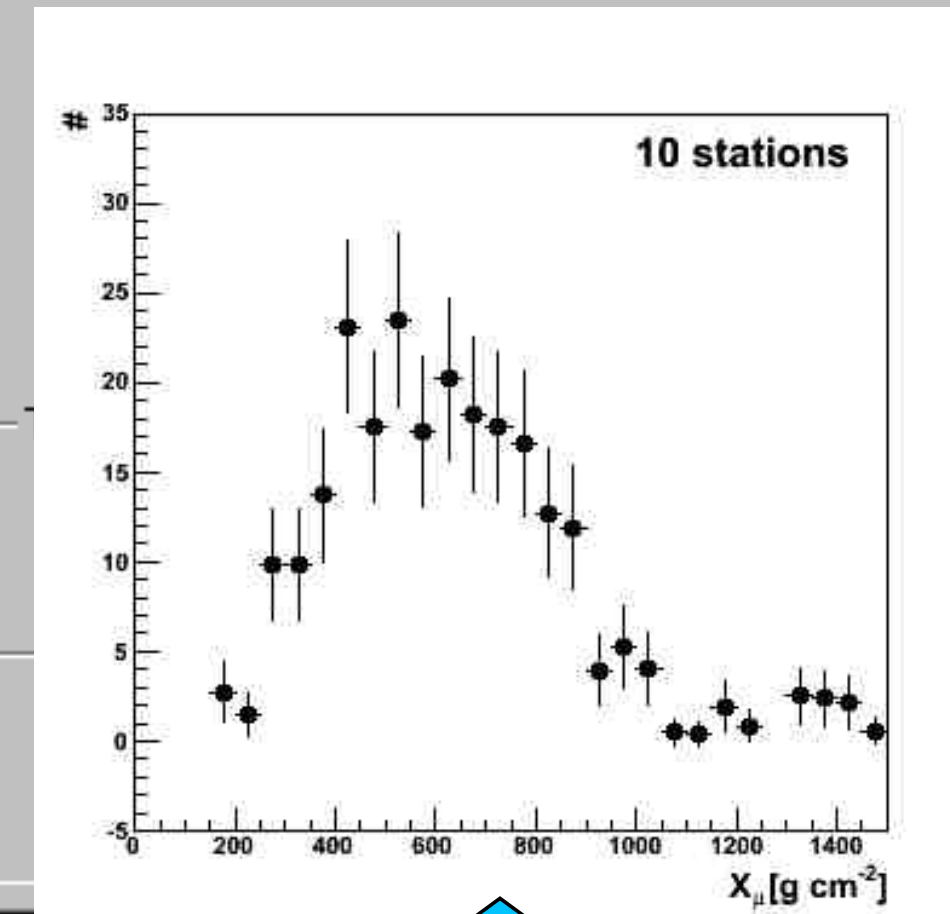


1390 TOT 56.1 VEM
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1520 TOT 42.2 VEM
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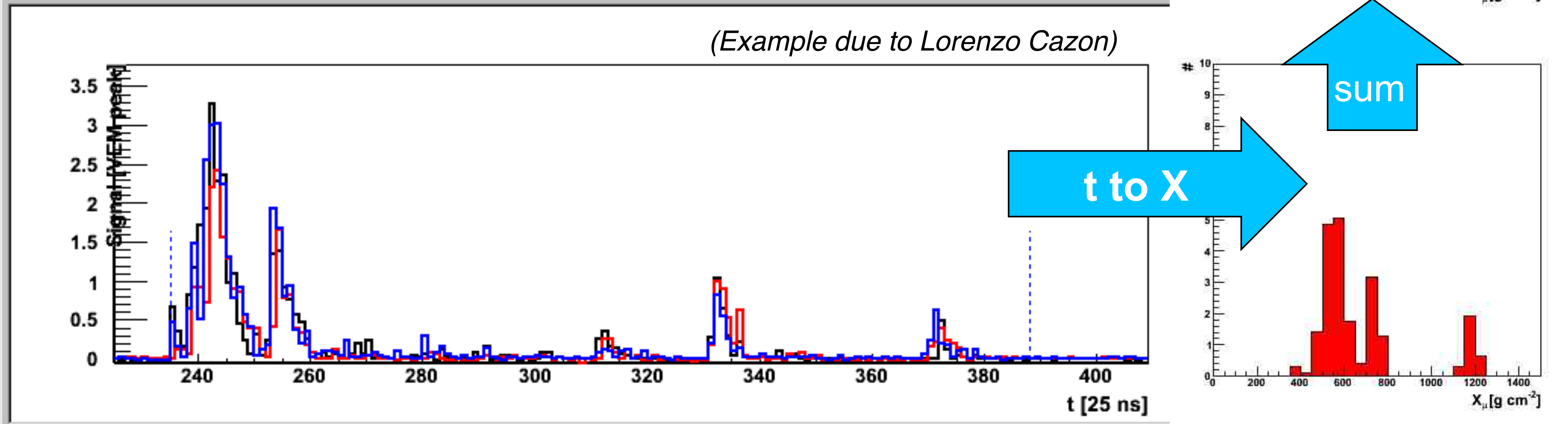


LDF LDF Res

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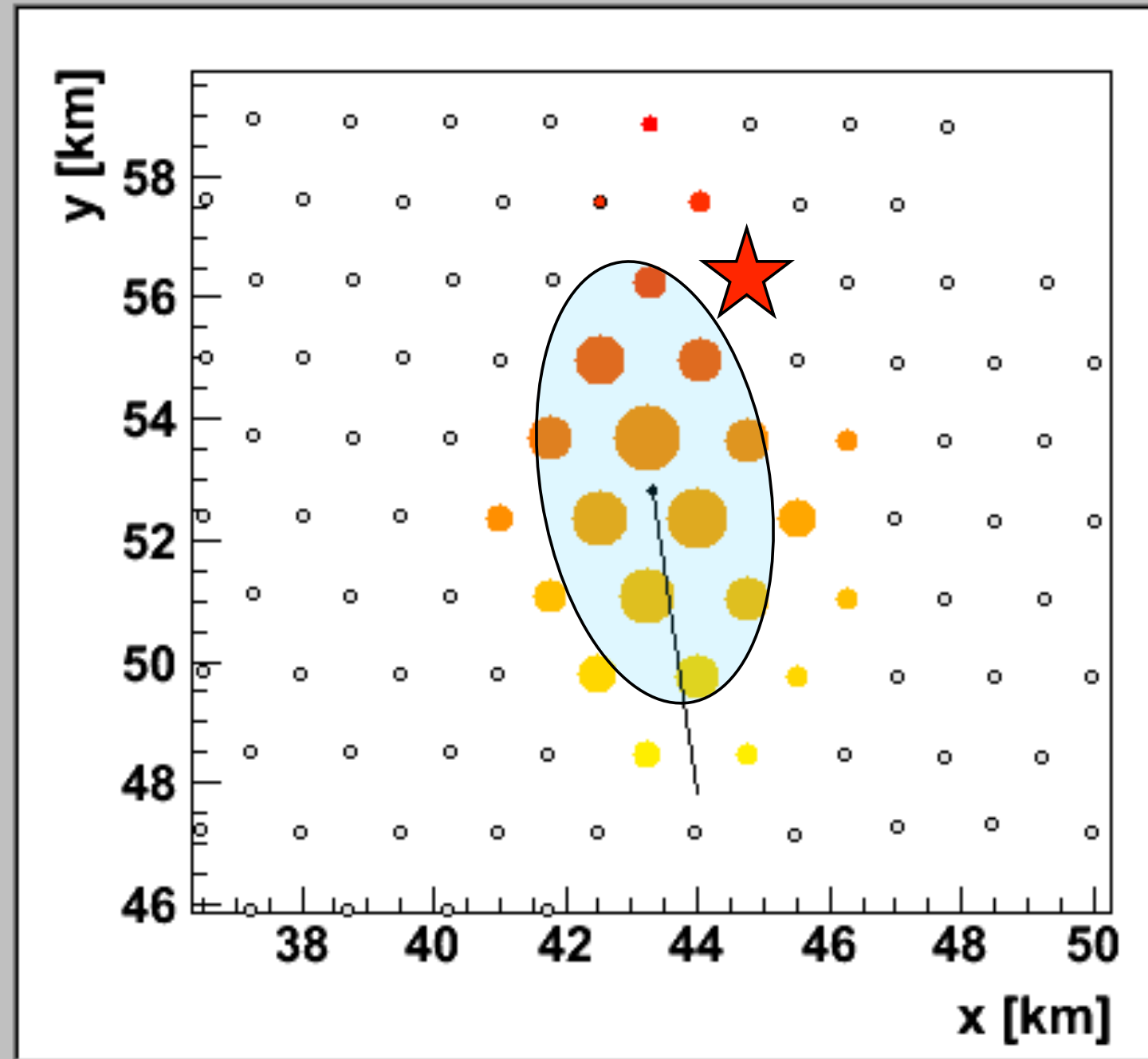


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 $(\theta, \phi) = (59.99 \pm 0.07, 277.85 \pm 0.08)$ deg
 $(x,y) = (43.31 \pm 0.01, 52.80 \pm 0.03)$ km
 β (fixed) = -1.91 (± 0.18)
 $R = 20.59 \pm 0.57$ km
 $r_{opt} = 1109.4$ m

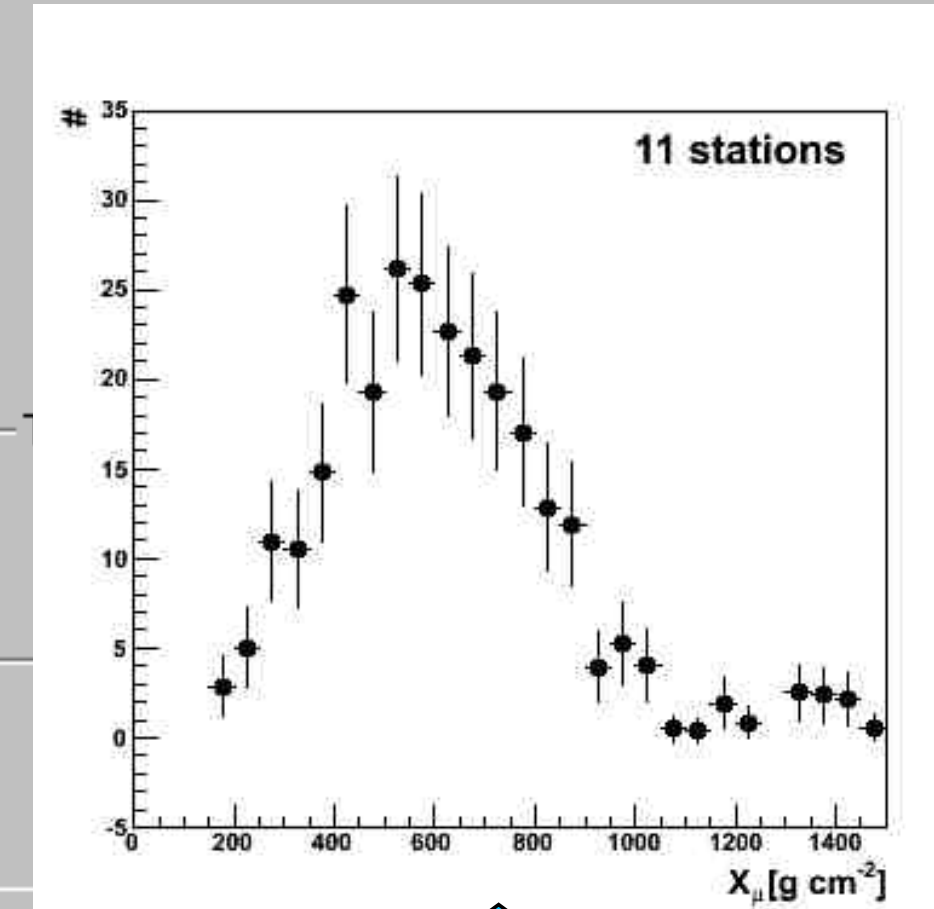


1390 TOT 56.1 VEM
1386 TOT 45.5 VEM
1520 TOT 42.2 VEM
1305 TOT 40.0 VEM
1456 TOT 37.1 VEM
1533 TOT 23.9 VEM
1498 TOT 18.6 VEM
1378 TOT 18.0 VEM
1528 TOT 15.4 VEM
1535 TOT 11.4 VEM
1460 TOT 8.9 VEM
1519 TOT 8.7 VEM

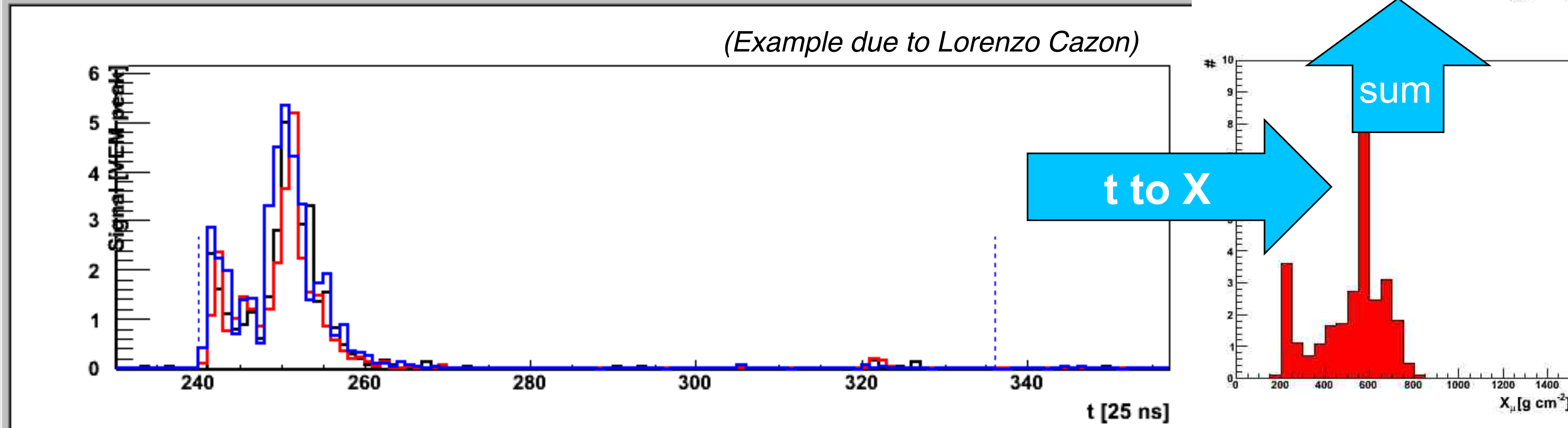


LDF LDF Res

LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)

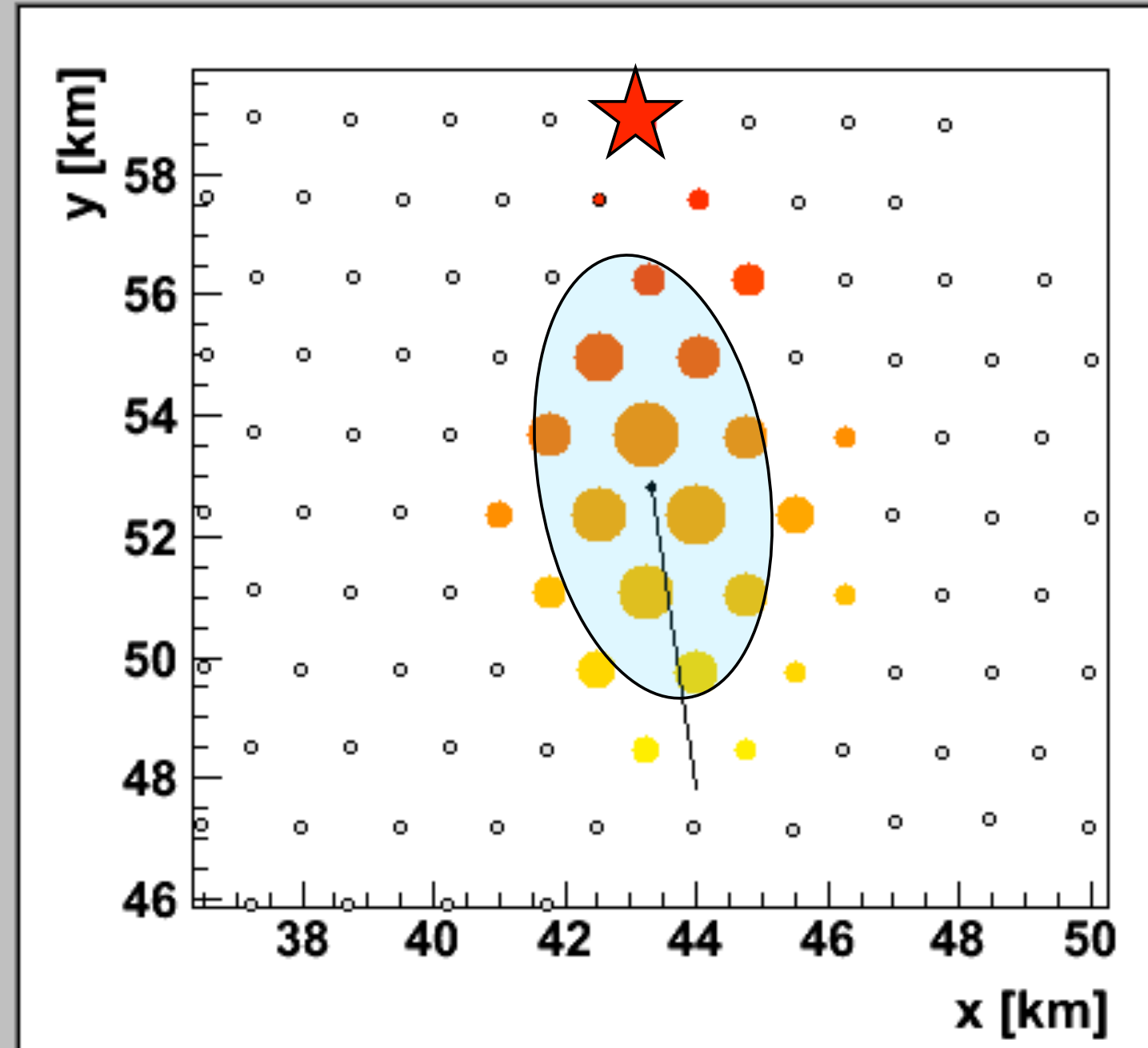


(Example due to Lorenzo Cazon)



Event Info | MC info

Event 8123914 :-)
 Time 933708755 s 768757000 ns
 3TOT & 4C1; T5
 Candidate stations: 24(20 acc)
 $E = (6.08 \pm 0.21) \times 10^{19}$ eV
 $S(1000 \text{ m}) = 131.7 \pm 4.3 (\pm 3.2)$ VEM
 $(\theta, \phi) = (59.99 \pm 0.07, 277.85 \pm 0.08)$ deg
 $(x, y) = (43.31 \pm 0.01, 52.80 \pm 0.03)$ km
 β (fixed) = $-1.91 (\pm 0.18)$
 $R = 20.59 \pm 0.57$ km
 $r_{\text{opt}} = 1109.4$ m

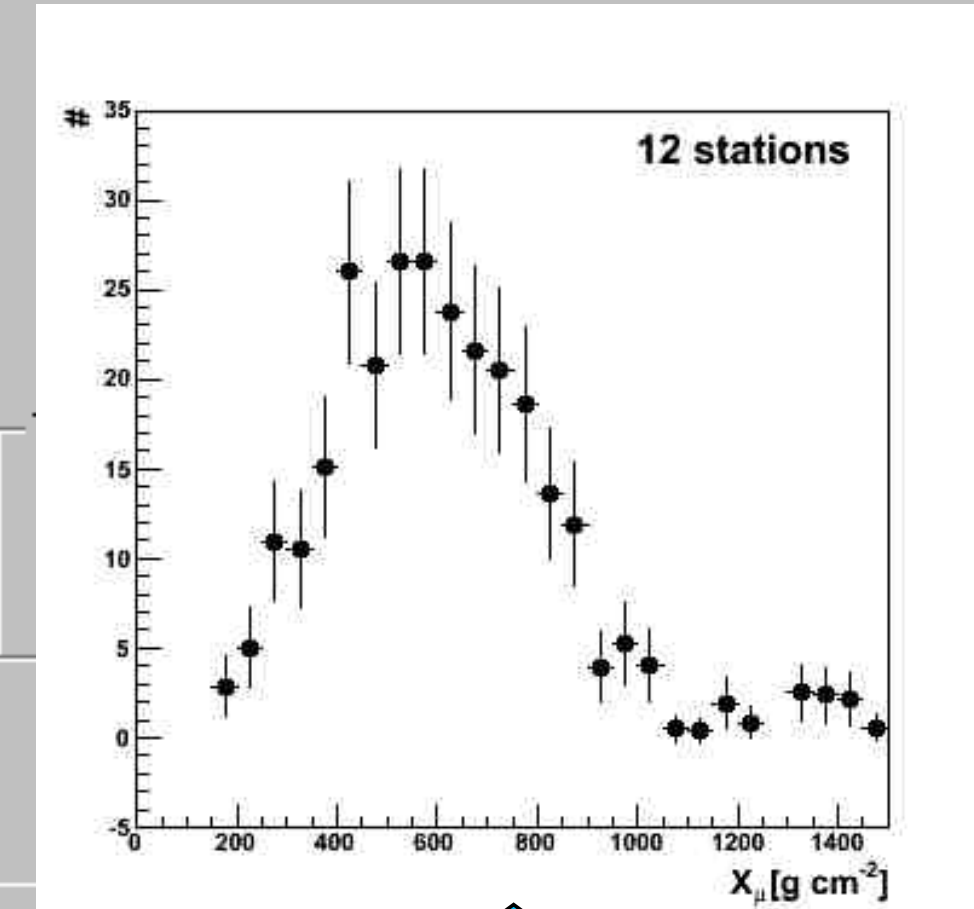


- 1378 TOT 18.0 VEM
- 1528 TOT 15.4 VEM
- 1535 TOT 11.4 VEM
- 1460 TOT 8.9 VEM
- 1519 TOT 8.7 VEM
- 1406 TOT 6.0 VEM
- 1463 TOT 5.8 VEM
- 1423 TOT 4.9 VEM
- 1491 TOT 4.9 VEM
- 1354 TOT 4.6 VEM
- 1468 TOT 3.9 VEM**
- 1402 Thr1 2.4 VEM

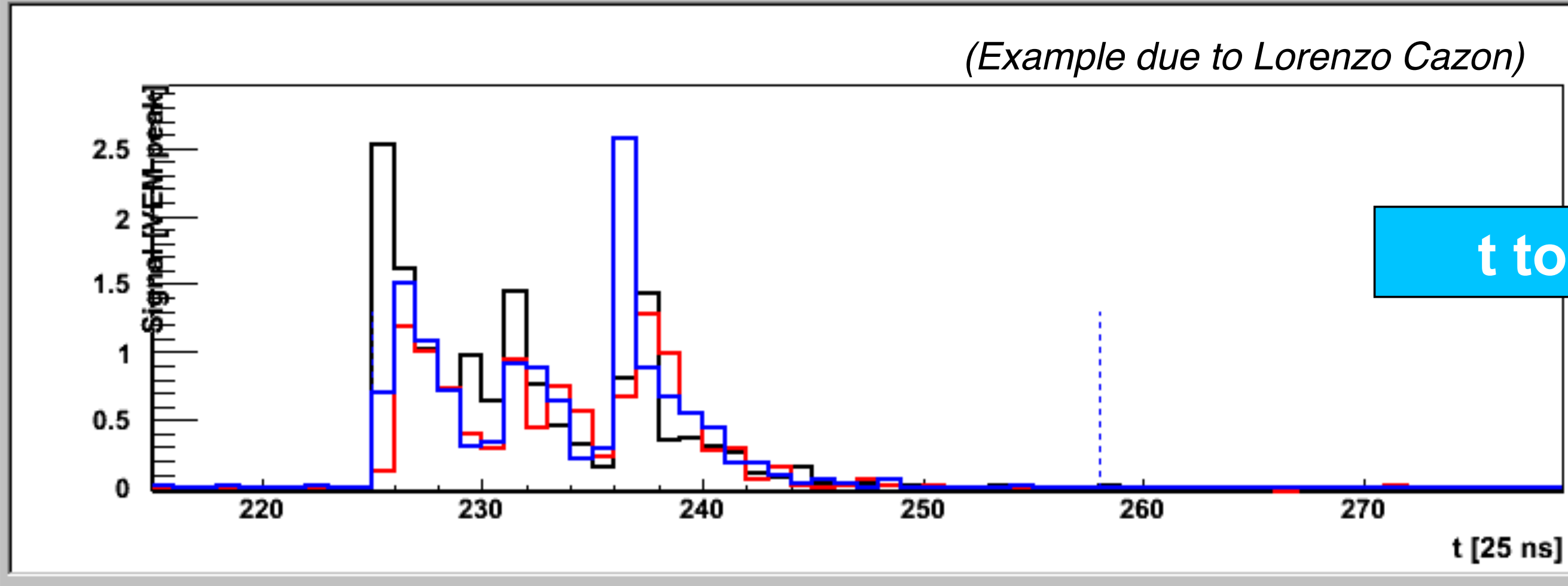


LDF LDF Res

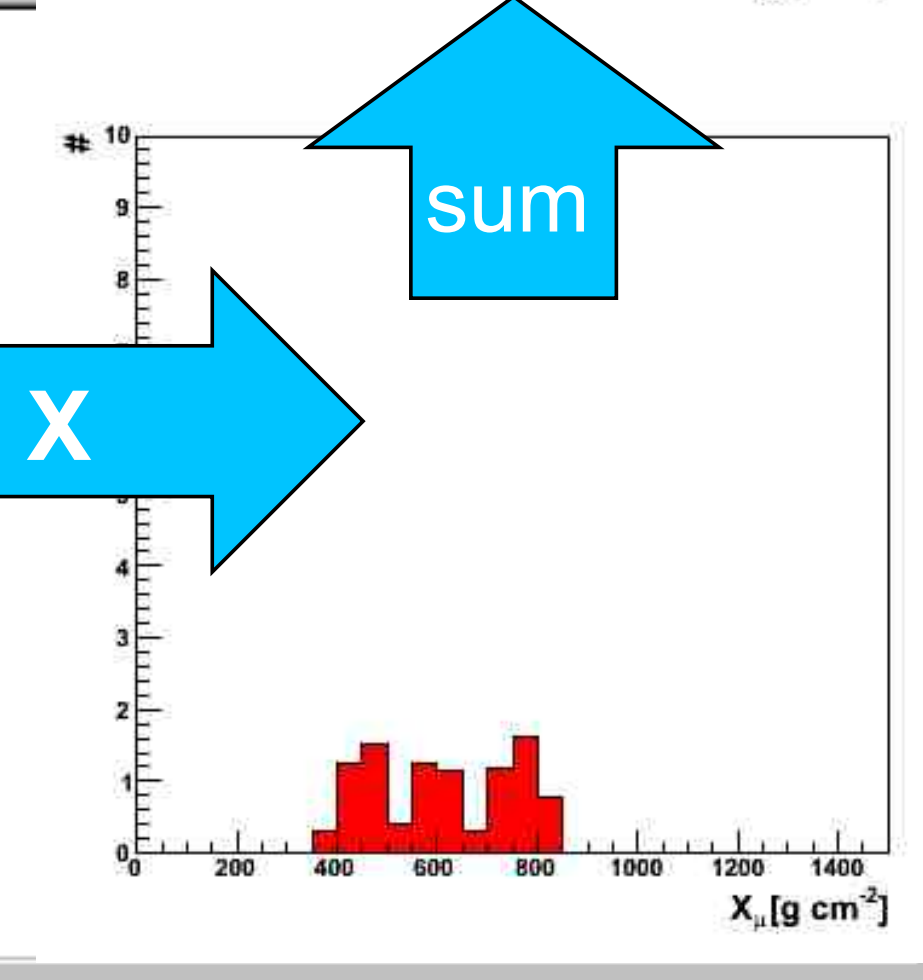
LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)



(Example due to Lorenzo Cazon)

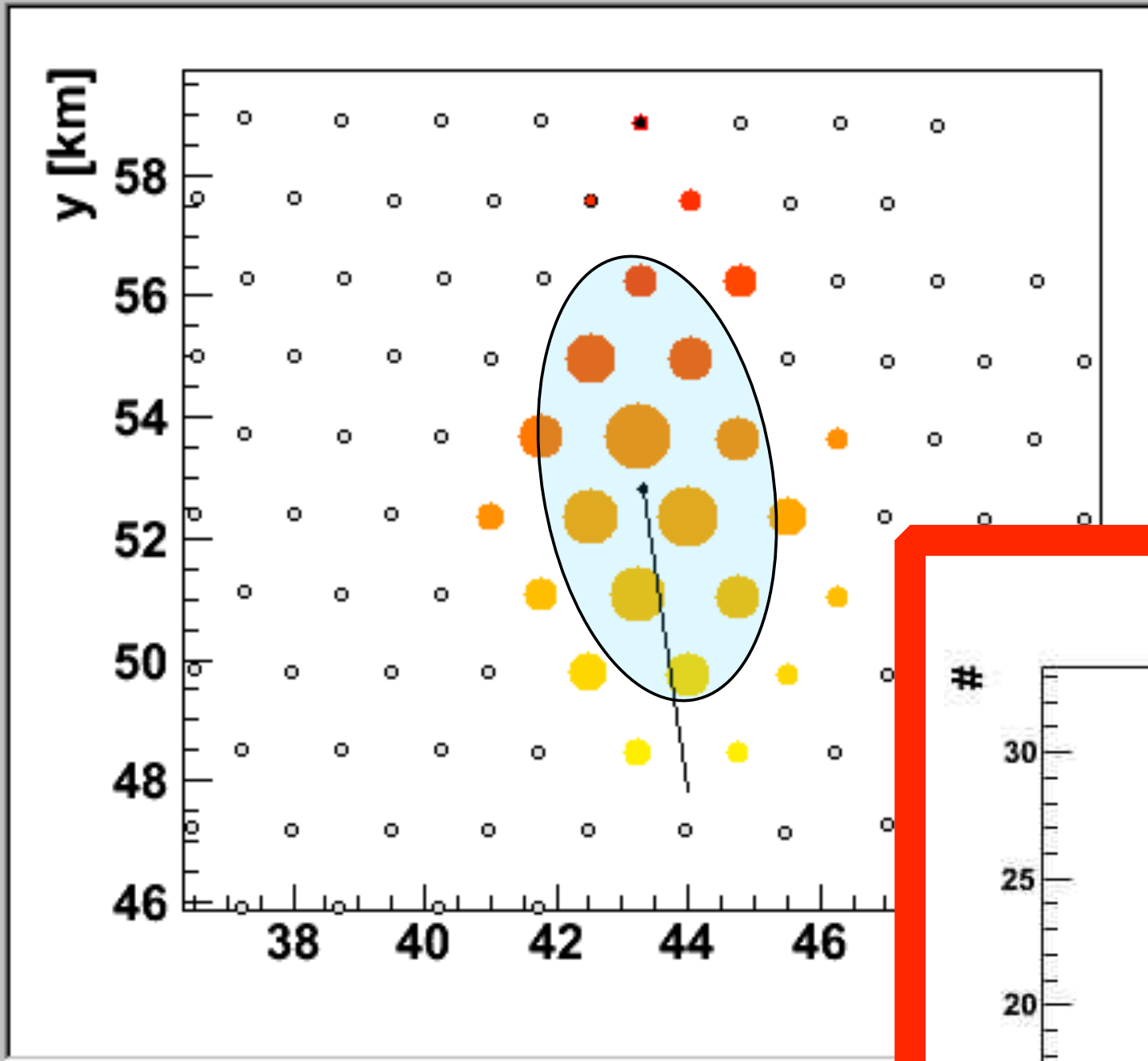


t to X



Event Info | MC info

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3TOT & 4C1; T5
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 β (fixed) = -1.91 (± 0.18)
 $R = 20.59 \pm 0.57$ km
 $r_{\text{opt}} = 1109.4$ m



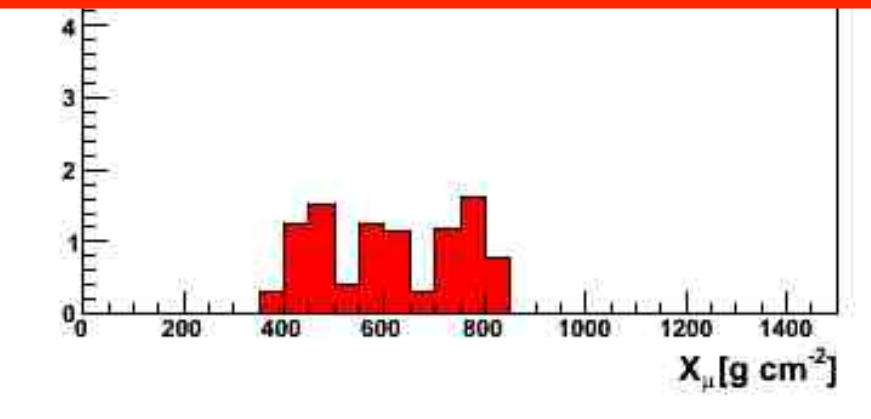
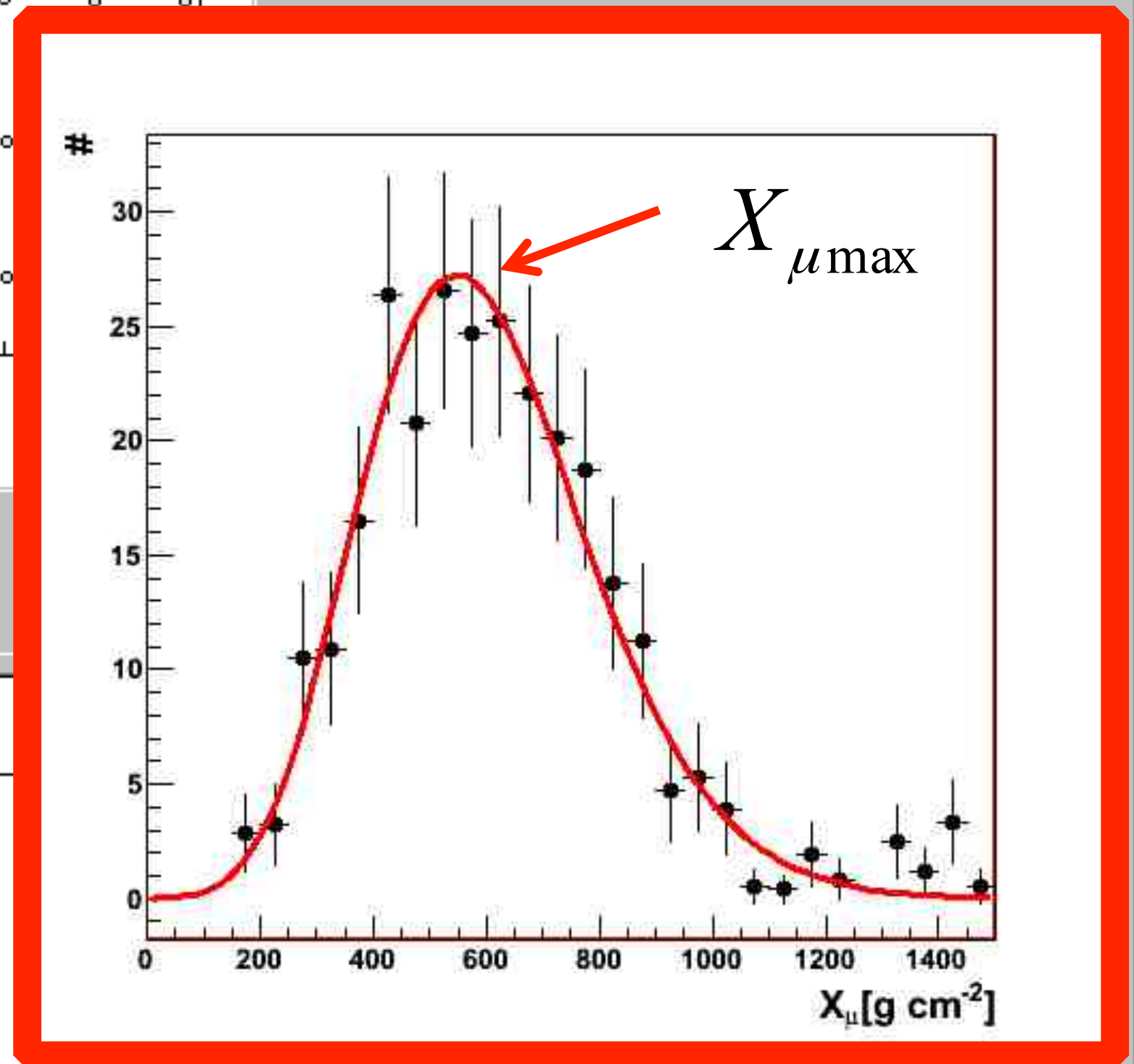
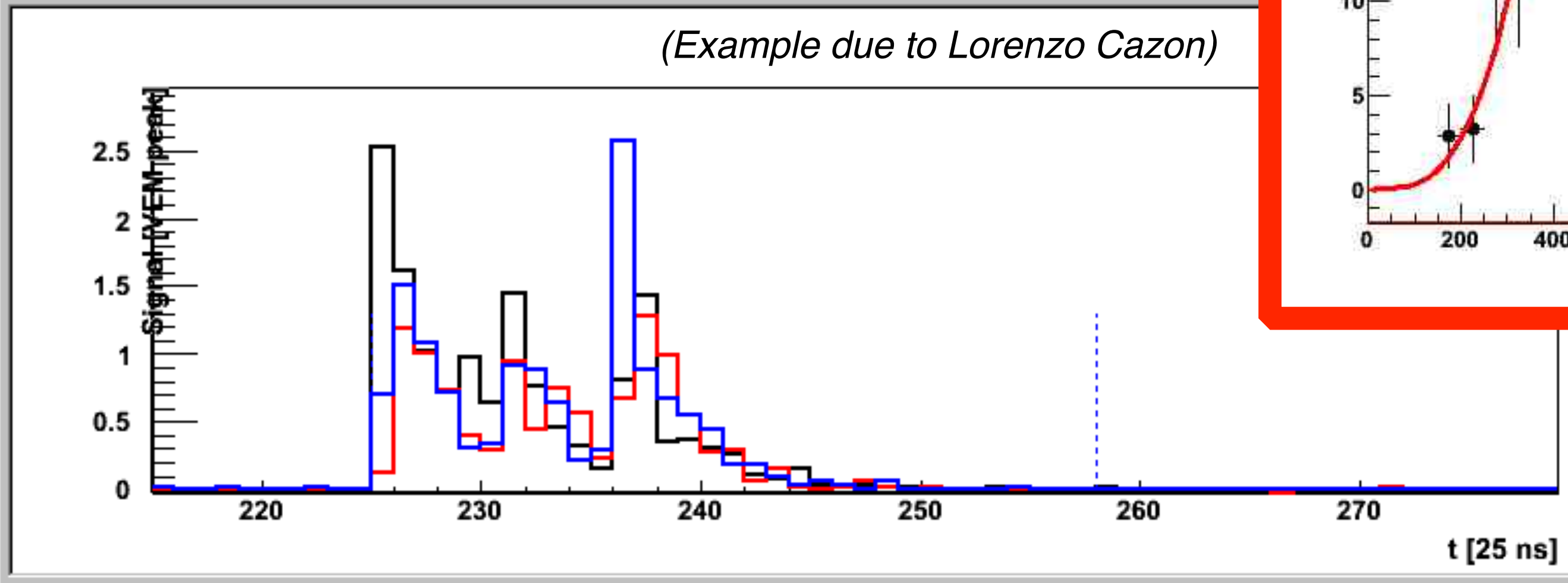
1378 TOT 18.0 VEM
1528 TOT 15.4 VEM
1535 TOT 11.4 VEM
1460 TOT 8.9 VEM
1519 TOT 8.7 VEM
1406 TOT 6.0 VEM
1463 TOT 5.8 VEM
1423 TOT 4.9 VEM
1491 TOT 4.9 VEM
1354 TOT 4.6 VEM
1468 TOT 3.9 VEM
1402 Thr1 2.4 VEM



LDF LDF Res

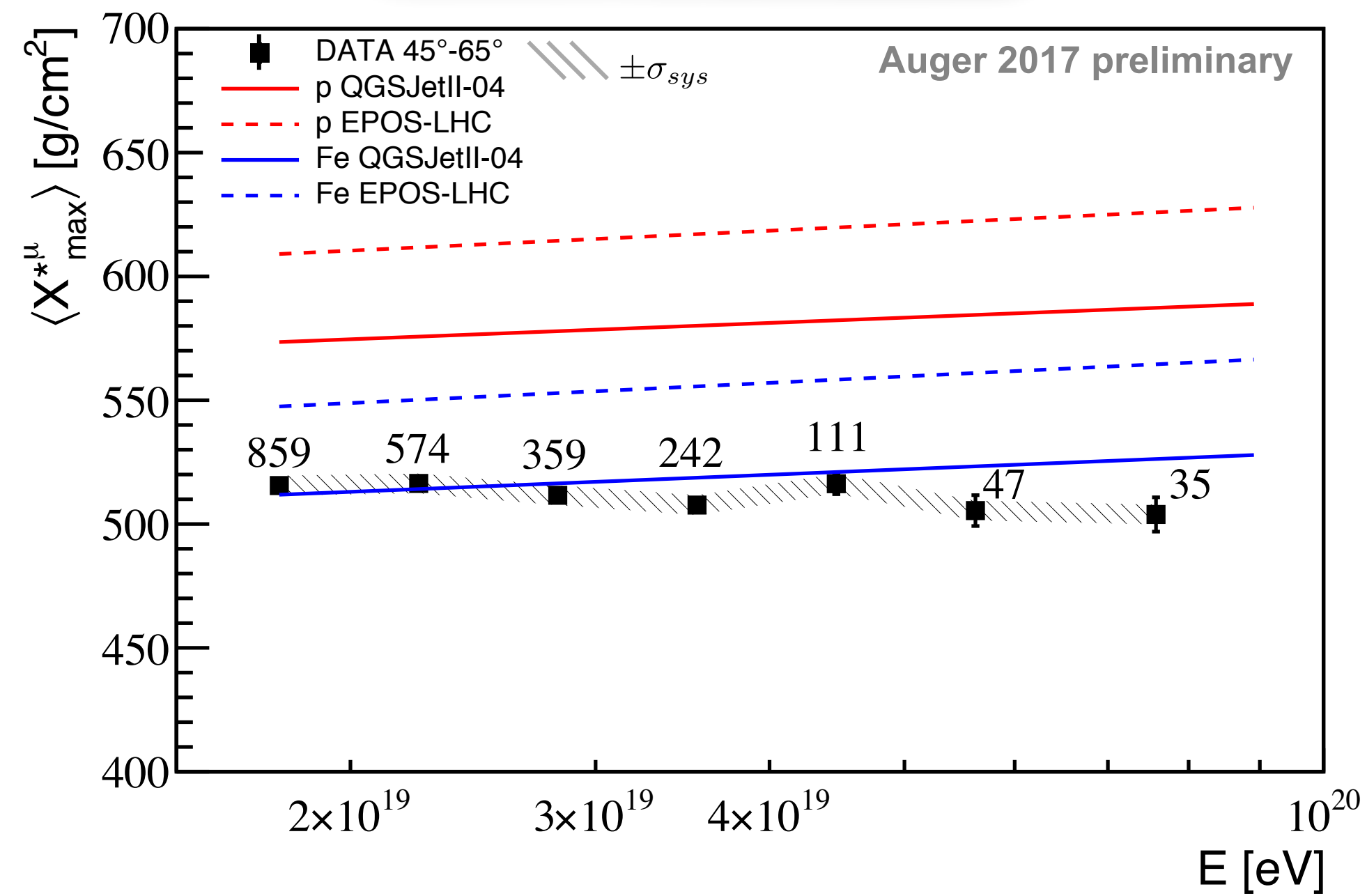
LDF and Time Residuals | VEM Traces | Dynode (HG) | Anode (LG)

(Example due to Lorenzo Cazon)

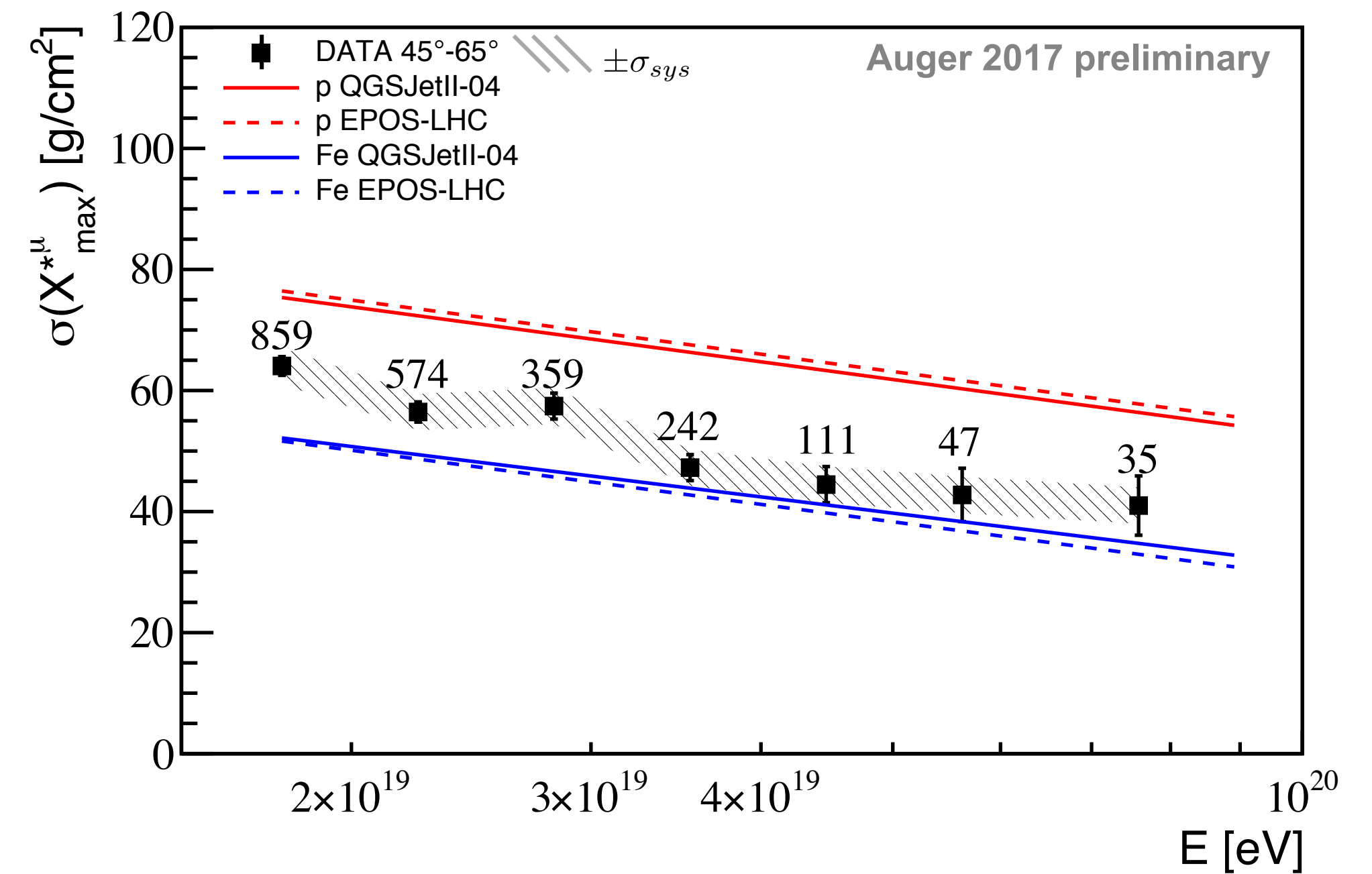


Depth of maximum for muon production

Mean values



Shower-by-shower fluctuations

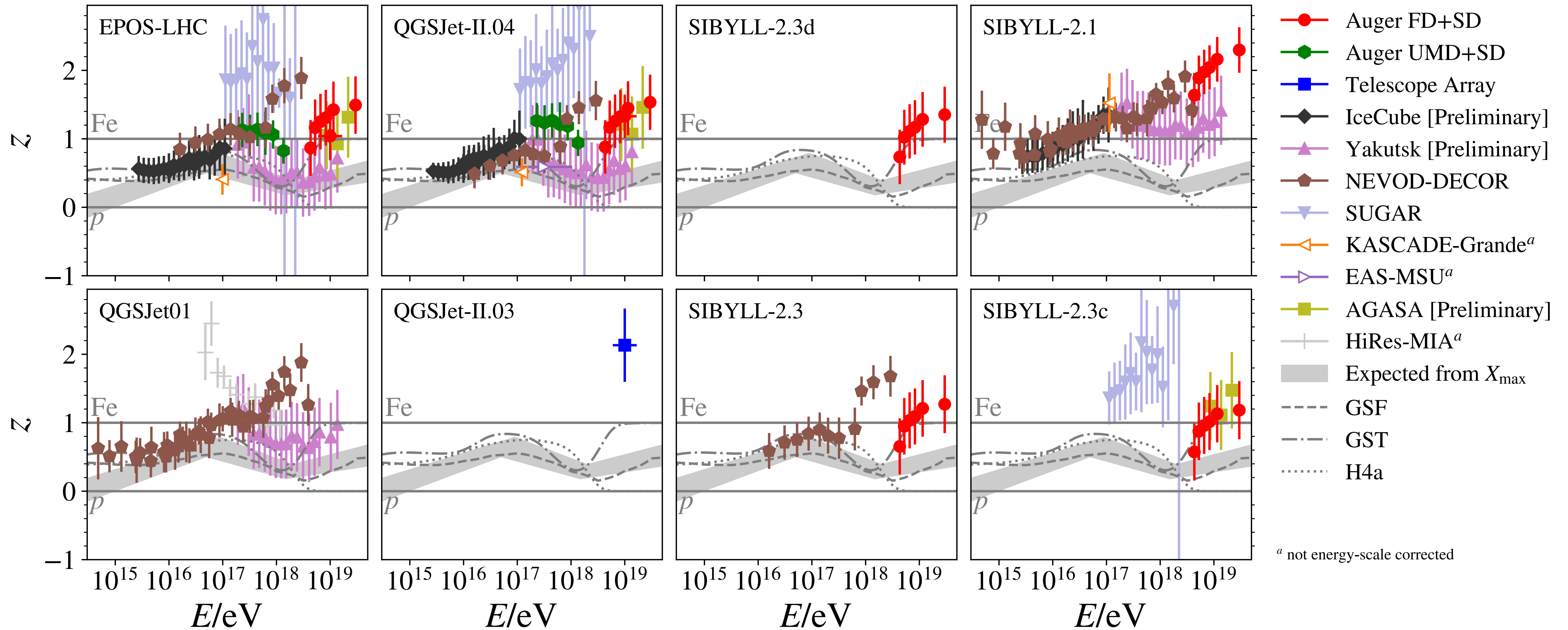


Similar situation for muon production depth

$E > 15 \text{ EeV}$
 $\theta = 45^\circ - 65^\circ$
 $r > 1200 \text{ m}$

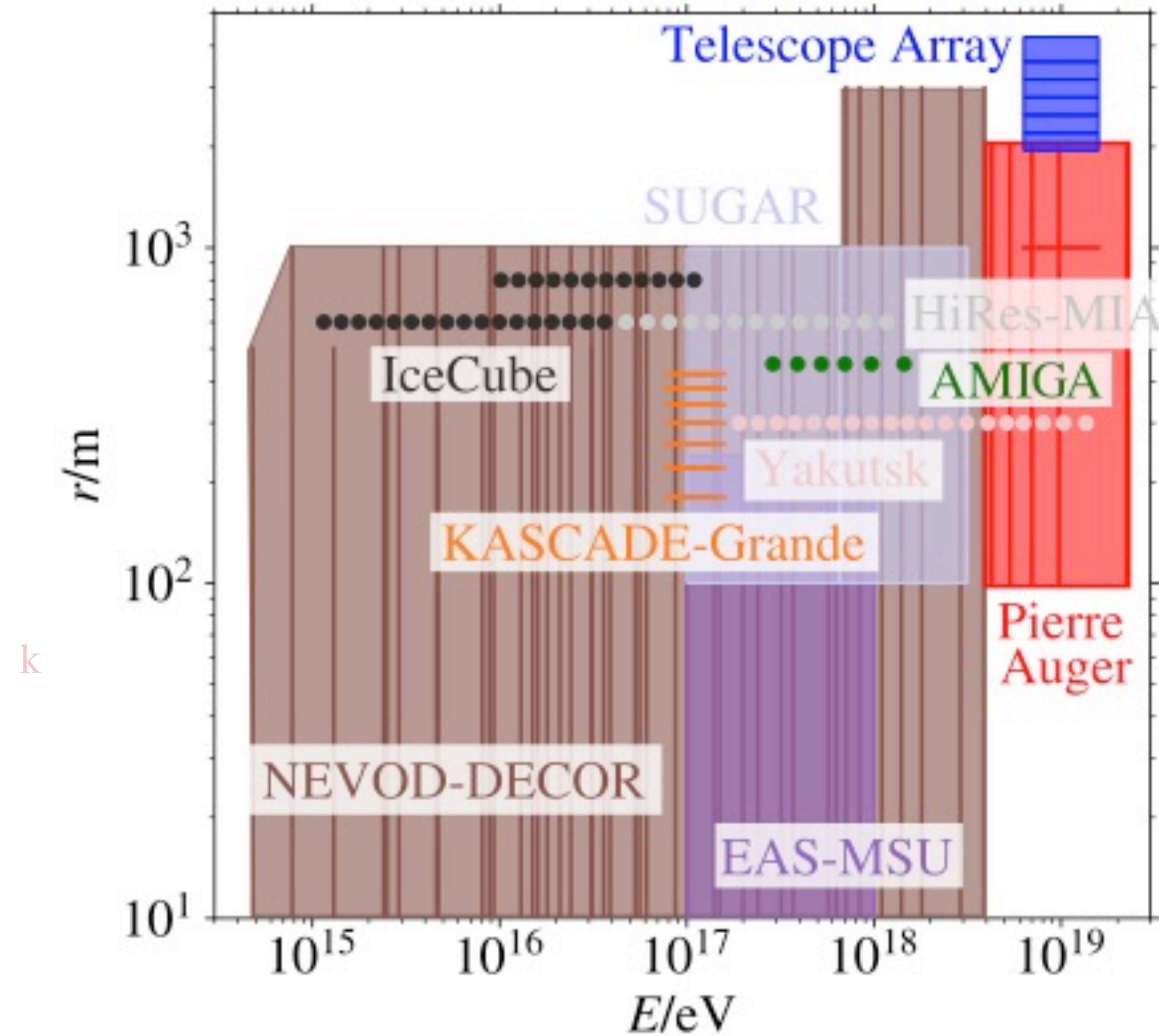
WHISP: Compilation of muon-sensitive measurements

Scaling variable z : relative number of muons with proton predictions as reference

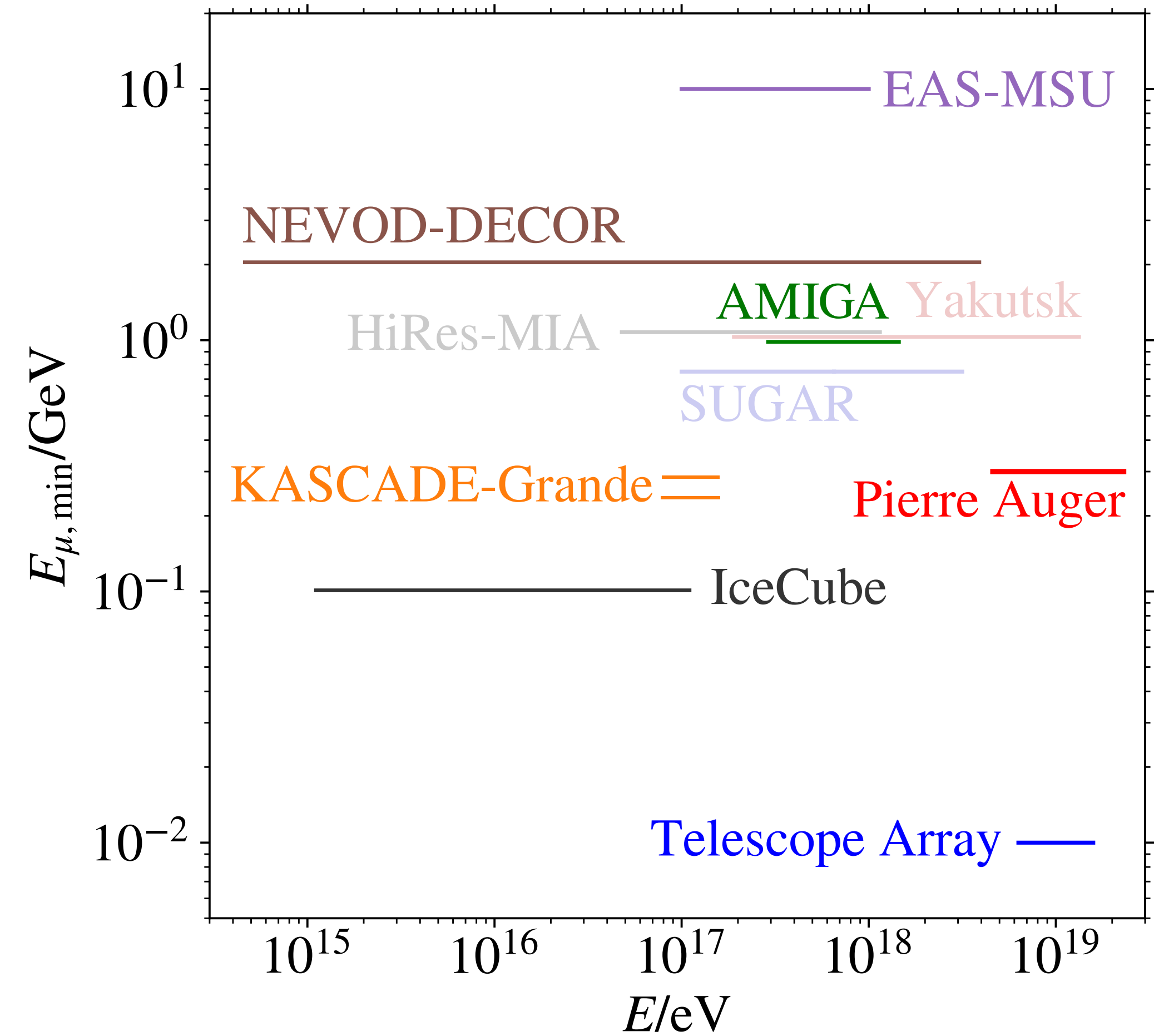


Analysis of world data set on muons (i)

Muon lateral distance

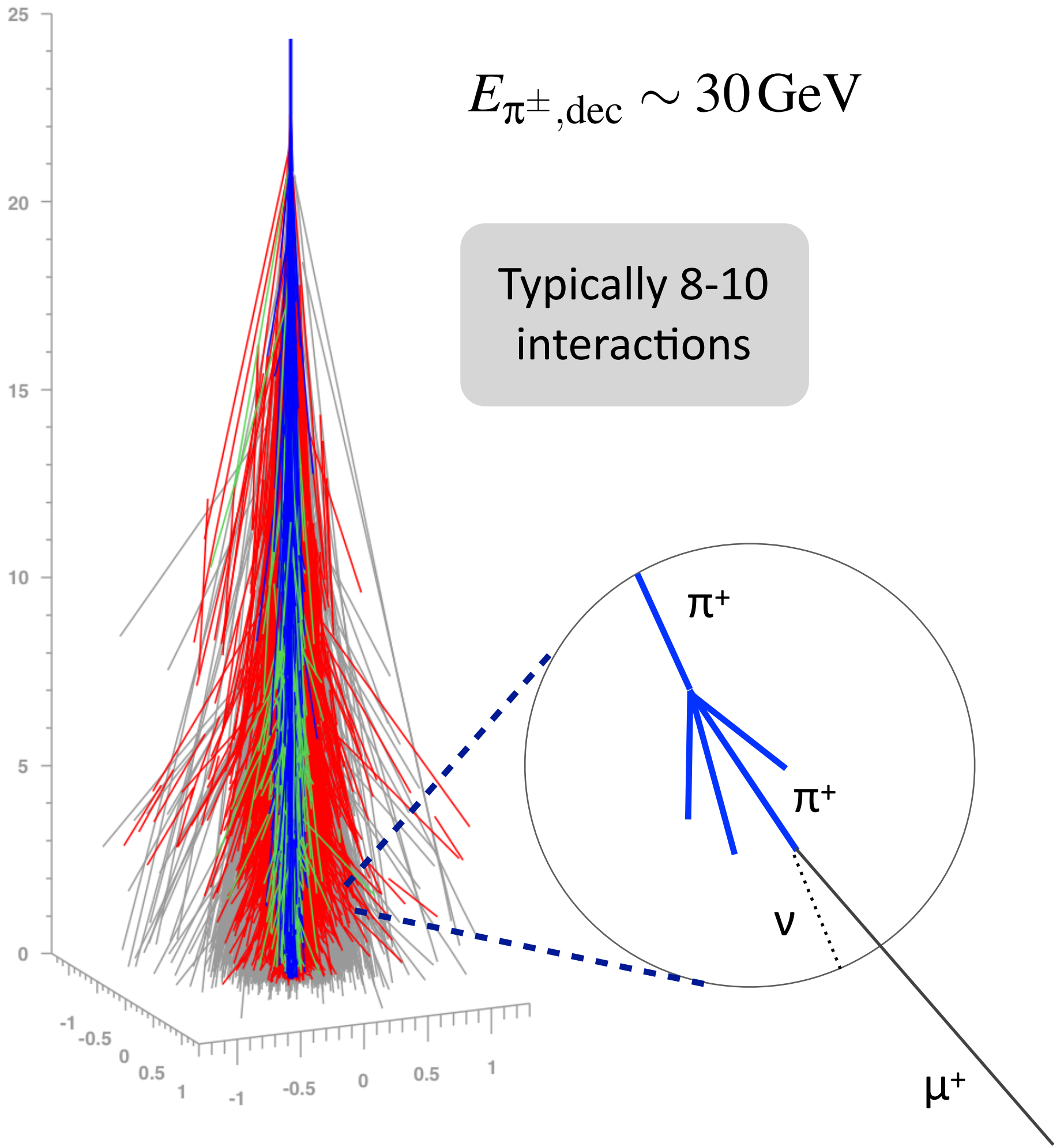


Muon energy thresholds



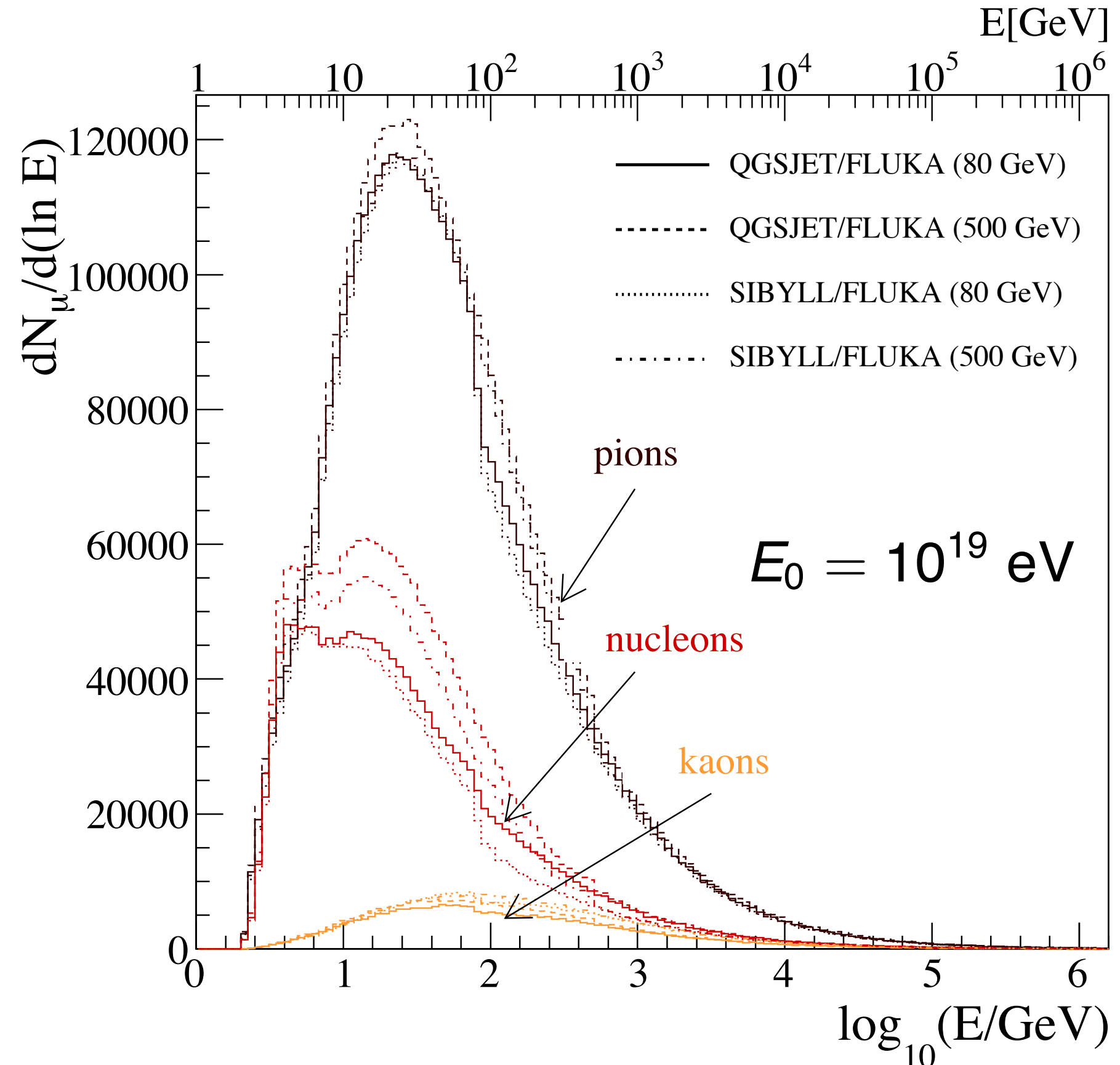
4. Closer look at muon production in showers

Muon production at large lateral distance



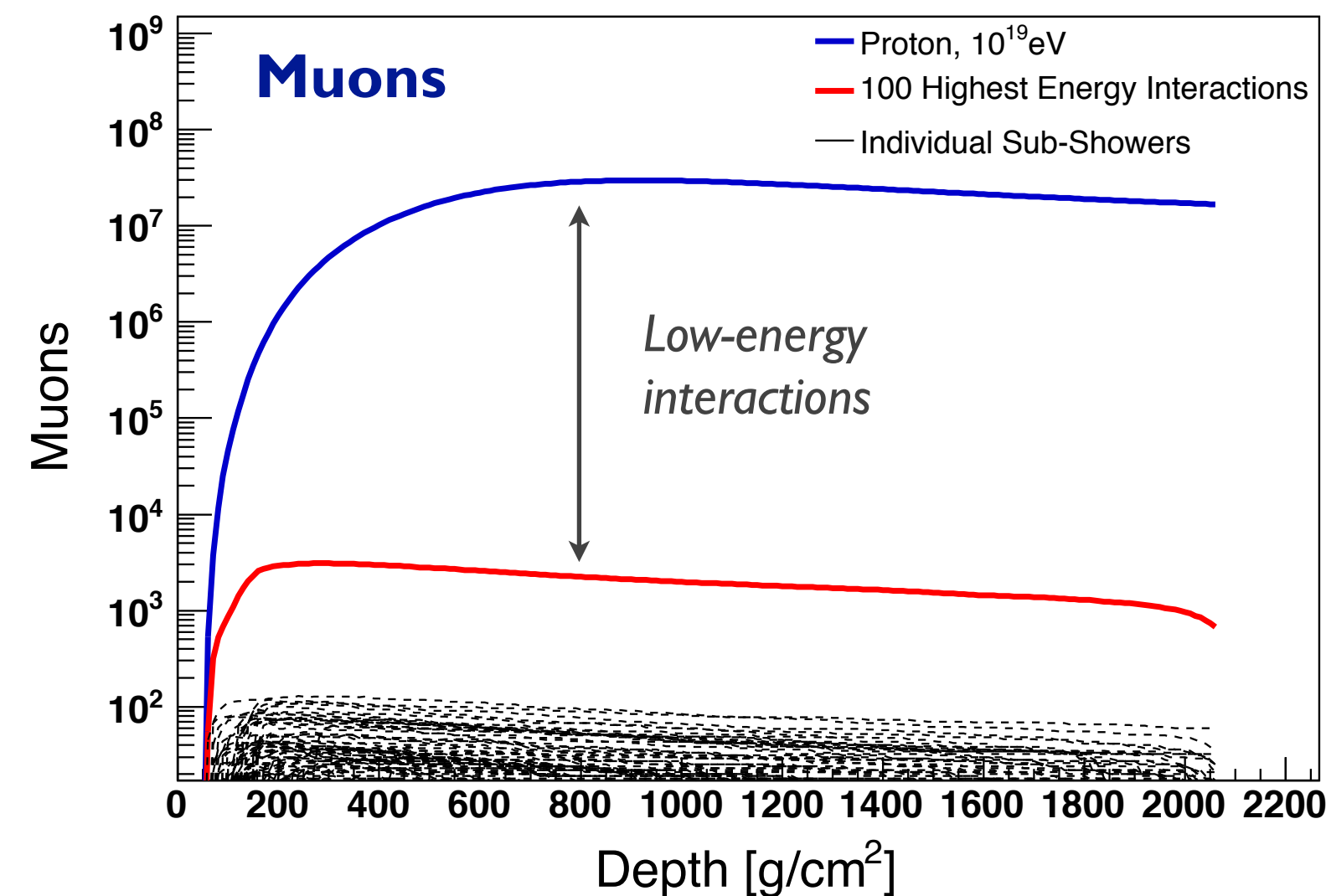
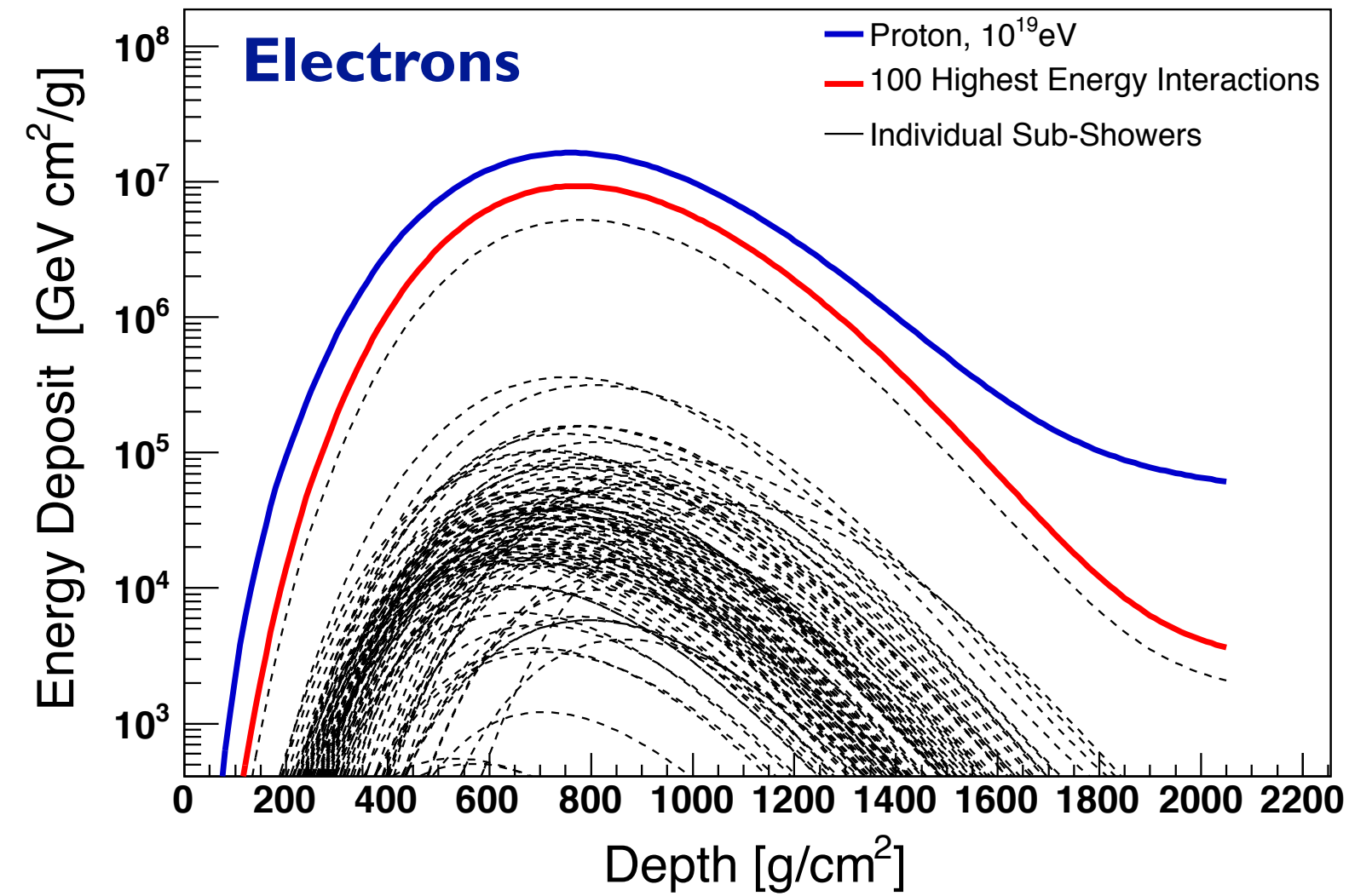
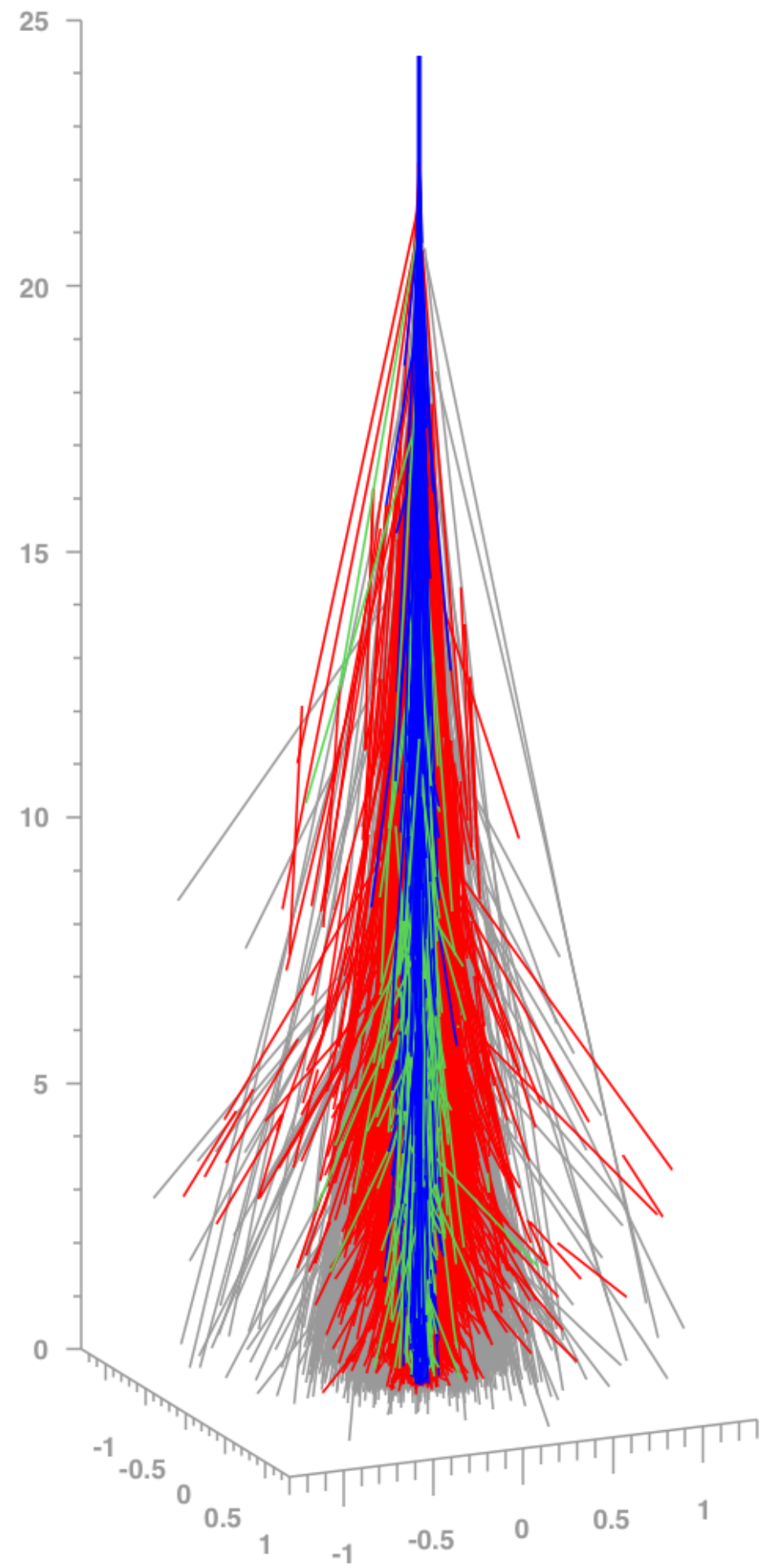
Muon observed at 1000 m from core

Energy distribution of last interaction that produced a detected muon



(Maris et al. ICRC 2009)

Importance of hadronic interactions at different energies



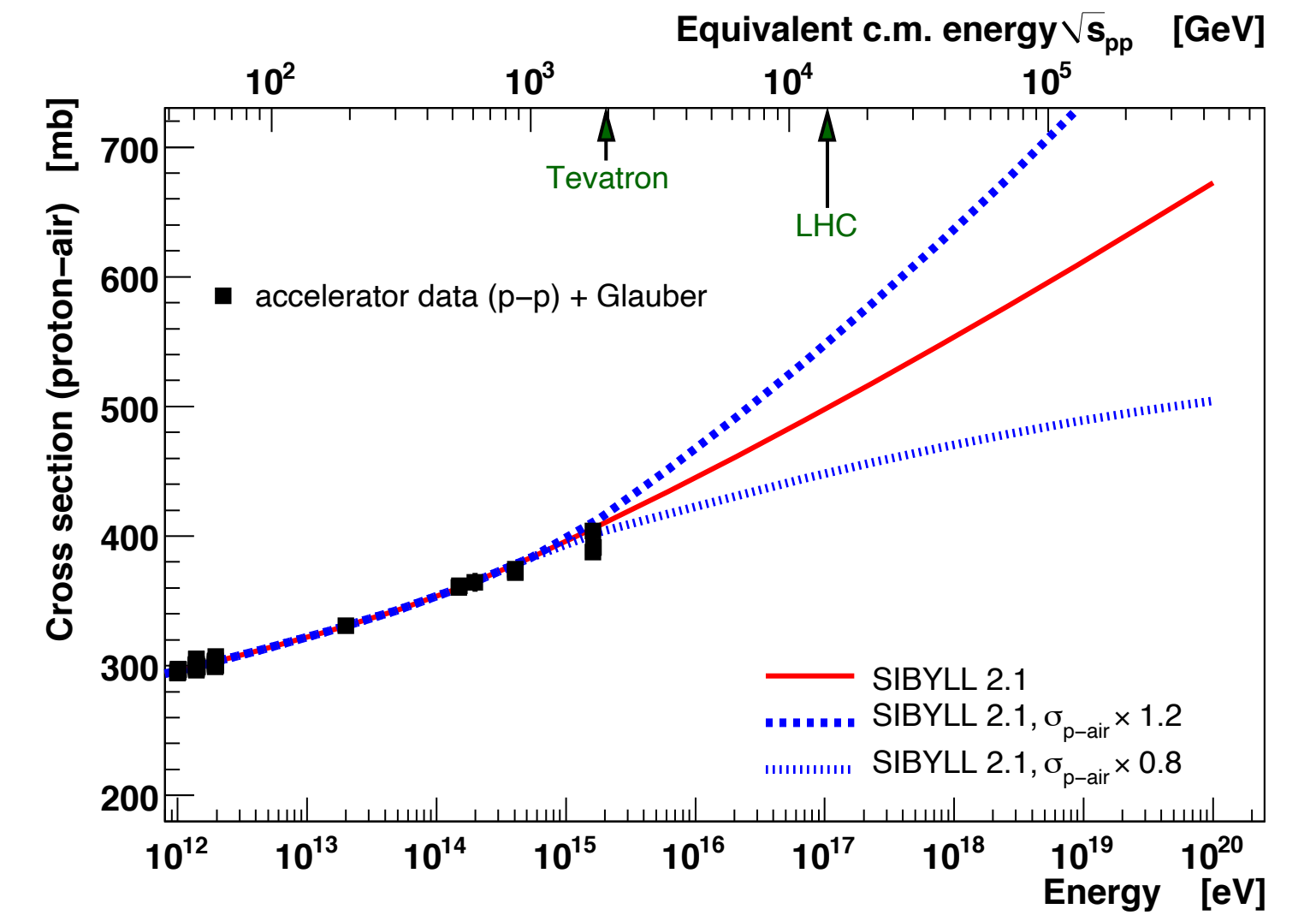
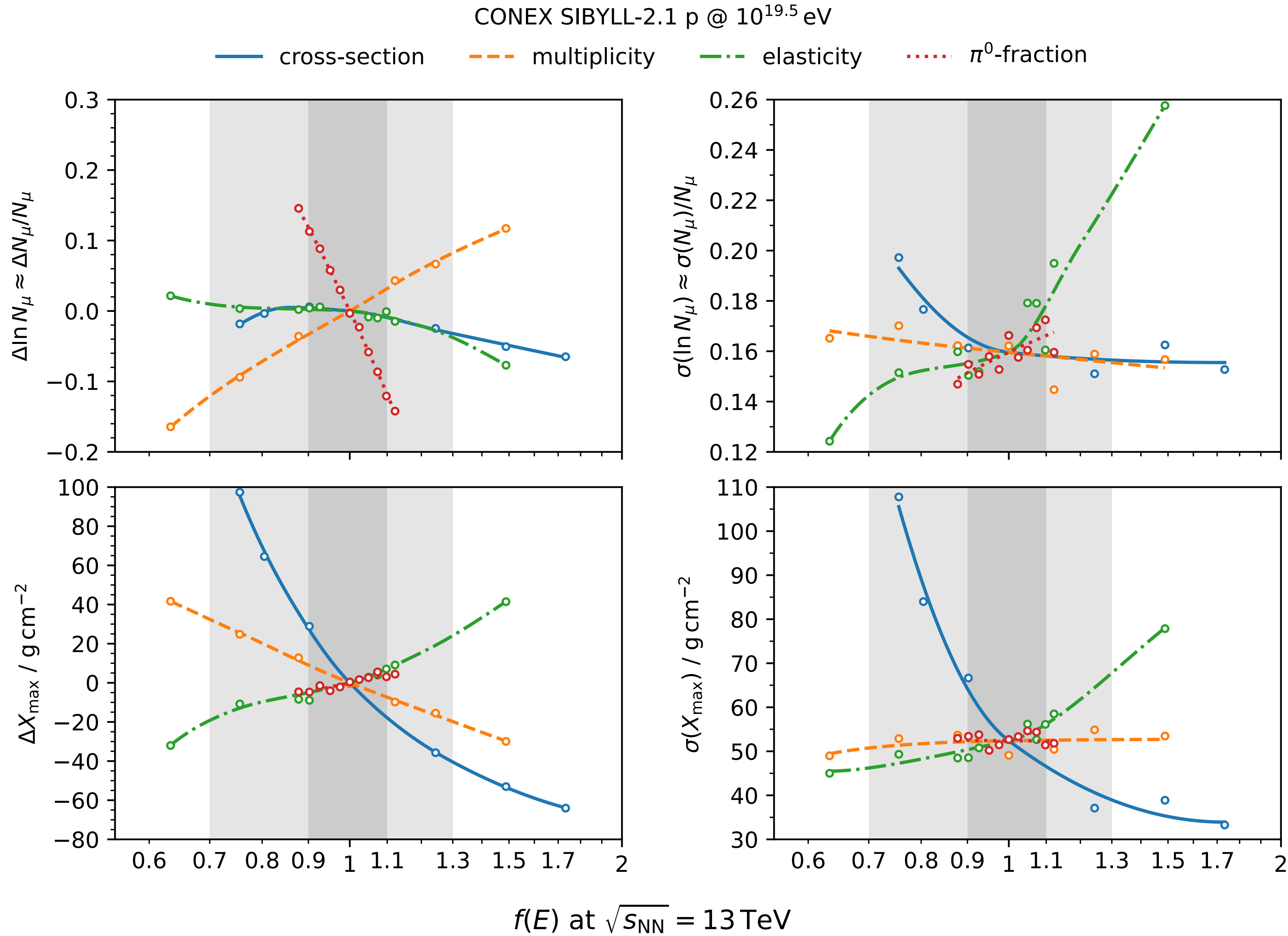
Shower particles produced in 100 interactions of highest energy

Electrons/photons:
high-energy interactions

Muons/hadrons:
low-energy interactions

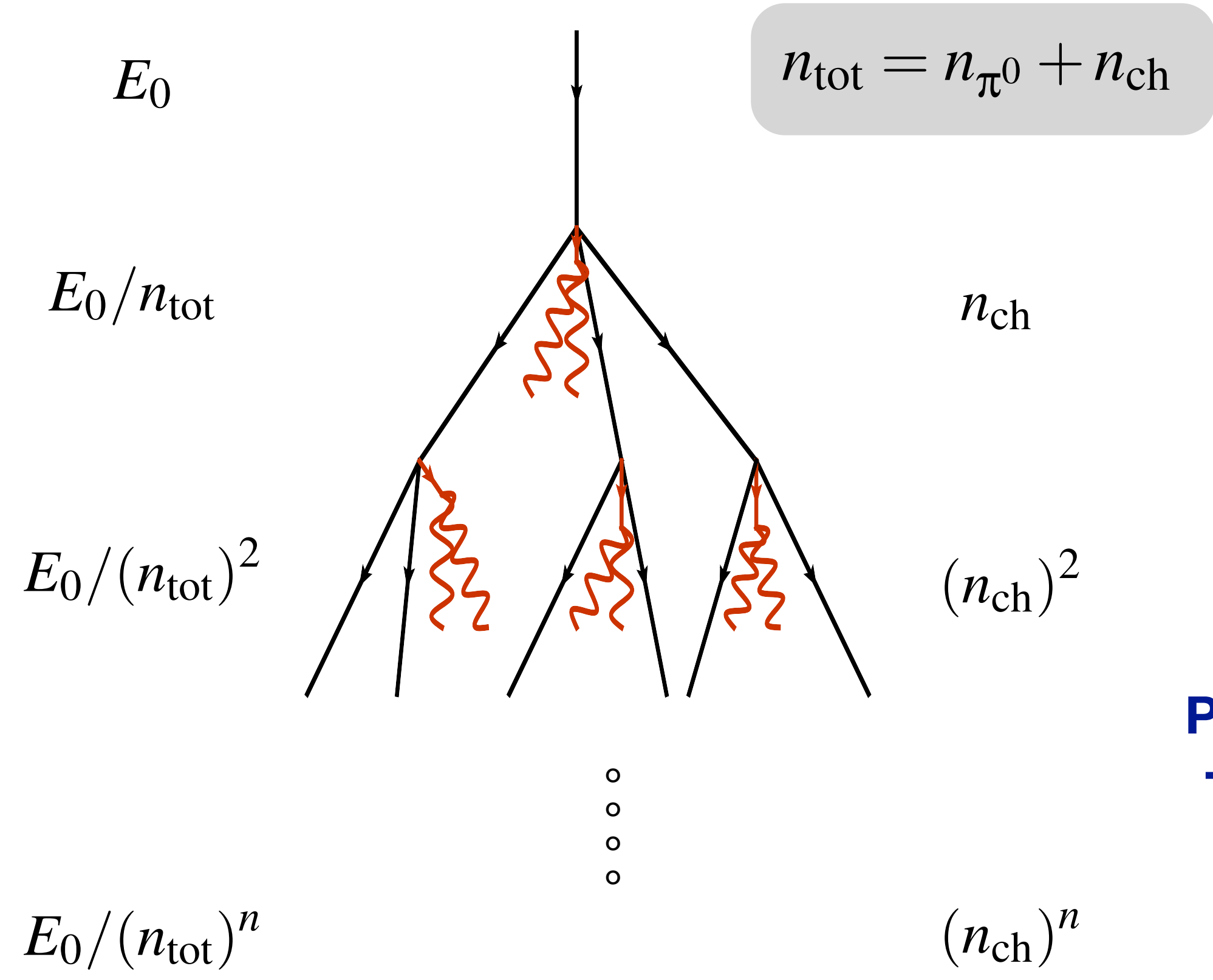
Muons: 8 – 12 generations,
majority of muons produced
in ~30 GeV interactions

Systematic study of relation to interaction properties



(Ulrich et al. Phys. Rev. D 83 (2011) 054026)

Muon production in hadronic showers



**Pion decay energy ~30 GeV,
Typically 8-12 generations**

Primary particle proton

π^0 decay immediately

π^\pm initiate new cascades

$$N_\mu = \left(\frac{E_0}{E_{\text{dec}}} \right)^\alpha$$

$$\alpha = \frac{\ln n_{\text{ch}}}{\ln n_{\text{tot}}} \approx 0.82 \dots 0.95$$

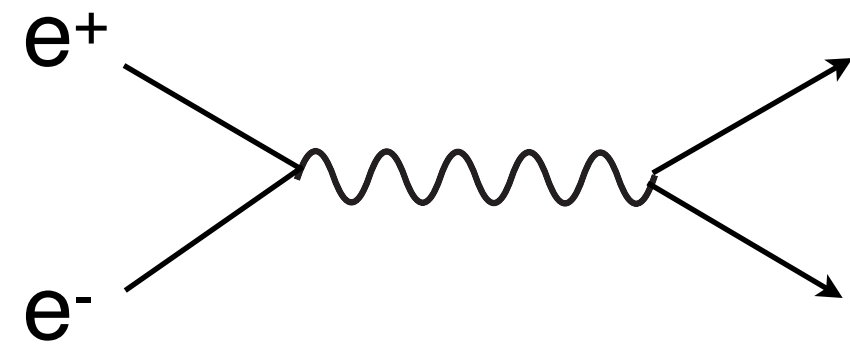
Assumptions:

- cascade stops at $E_{\text{part}} = E_{\text{dec}}$
- each hadron produces one muon

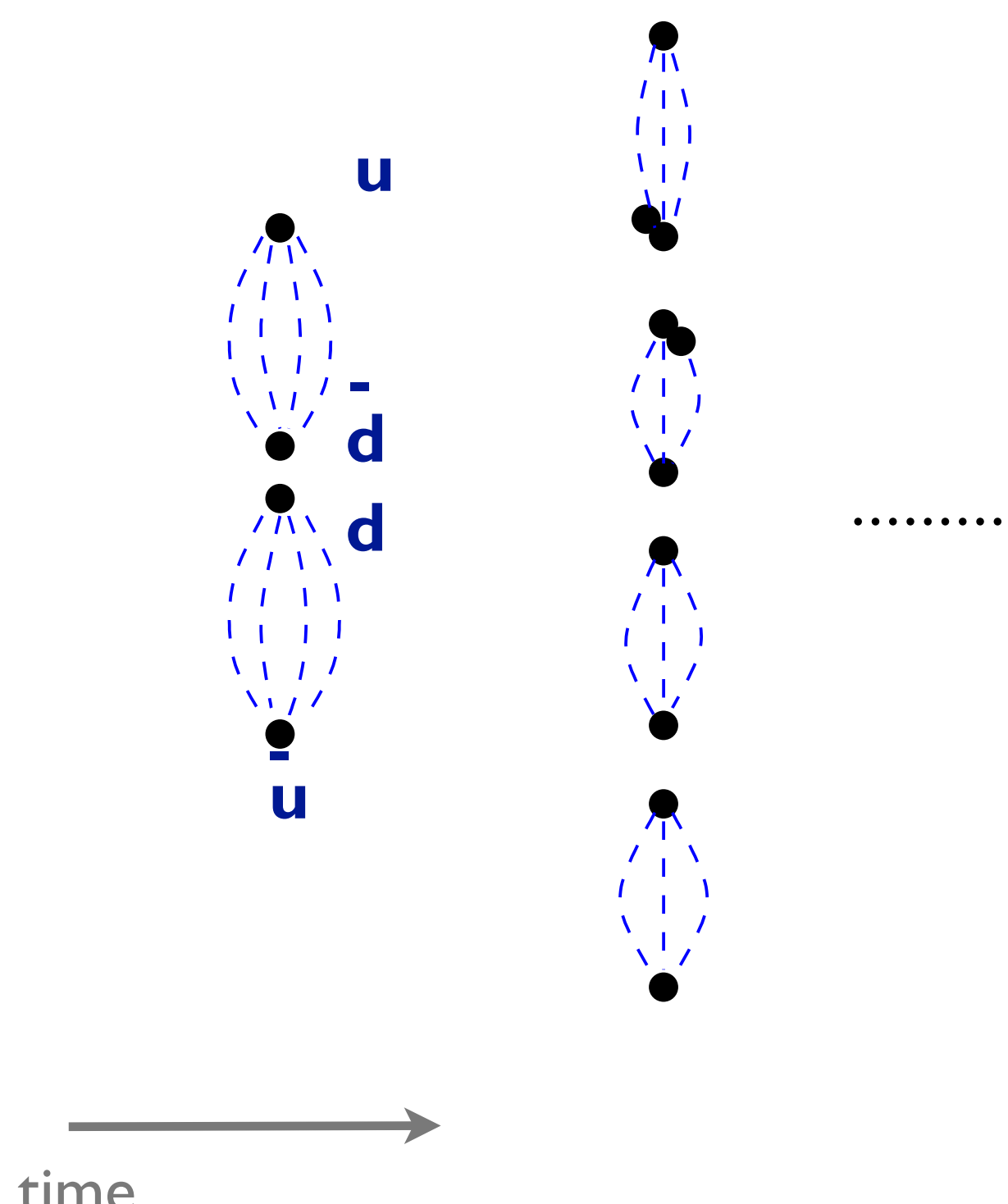
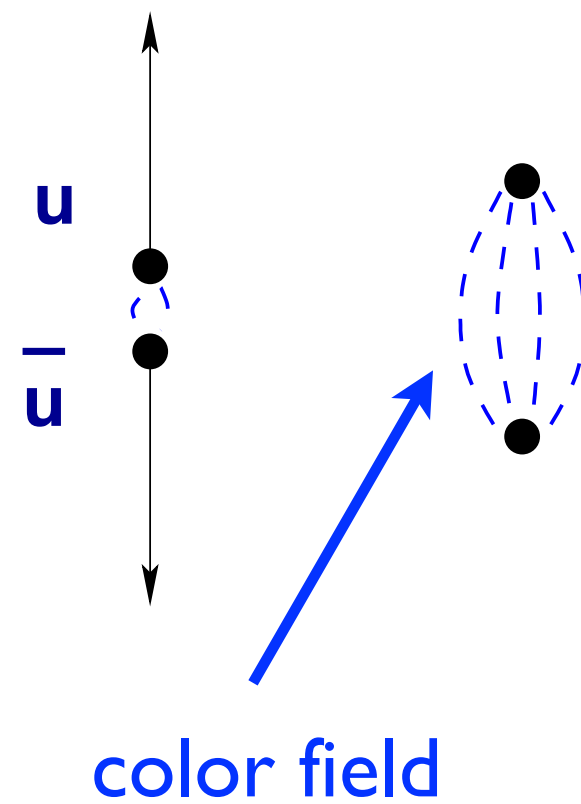
(Matthews, *Astropart.Phys.* 22, 2005)

Comparison to e^+e^- annihilation into quarks

e^+e^- annihilation at high energy



Quarks together are color-neutral system



- | | | |
|-----|-------------------|-----------|
| •• | $u\bar{d}$ | π^+ |
| •• | $d\bar{u}$ | π^- |
| ••• | $\bar{u}u\bar{d}$ | \bar{p} |
| ••• | udd | n |
| •• | $u\bar{s}$ | K^+ |
| •• | $s\bar{d}$ | K^0 |
| •• | $u\bar{d}$ | π^+ |
| •• | $q\bar{q}$ | |
| •• | $q\bar{q}$ | |
| •• | $q\bar{q}$ | |

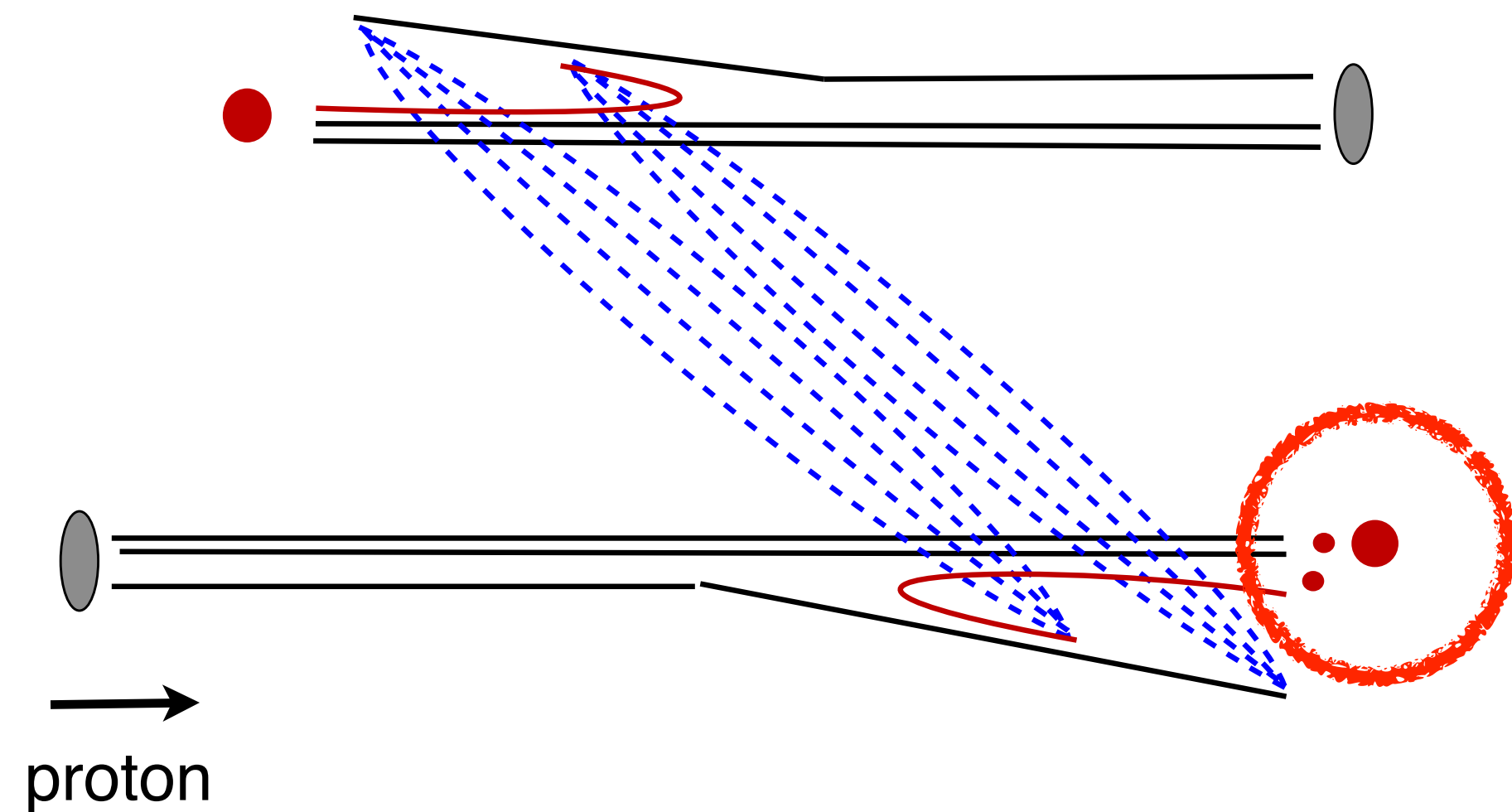
String fragmentation

Composition
u:d:s ~ 1:1:0.3

Confinement in QCD

$$V(r) = -\frac{4}{3} \frac{\alpha_s}{r} + \lambda r$$

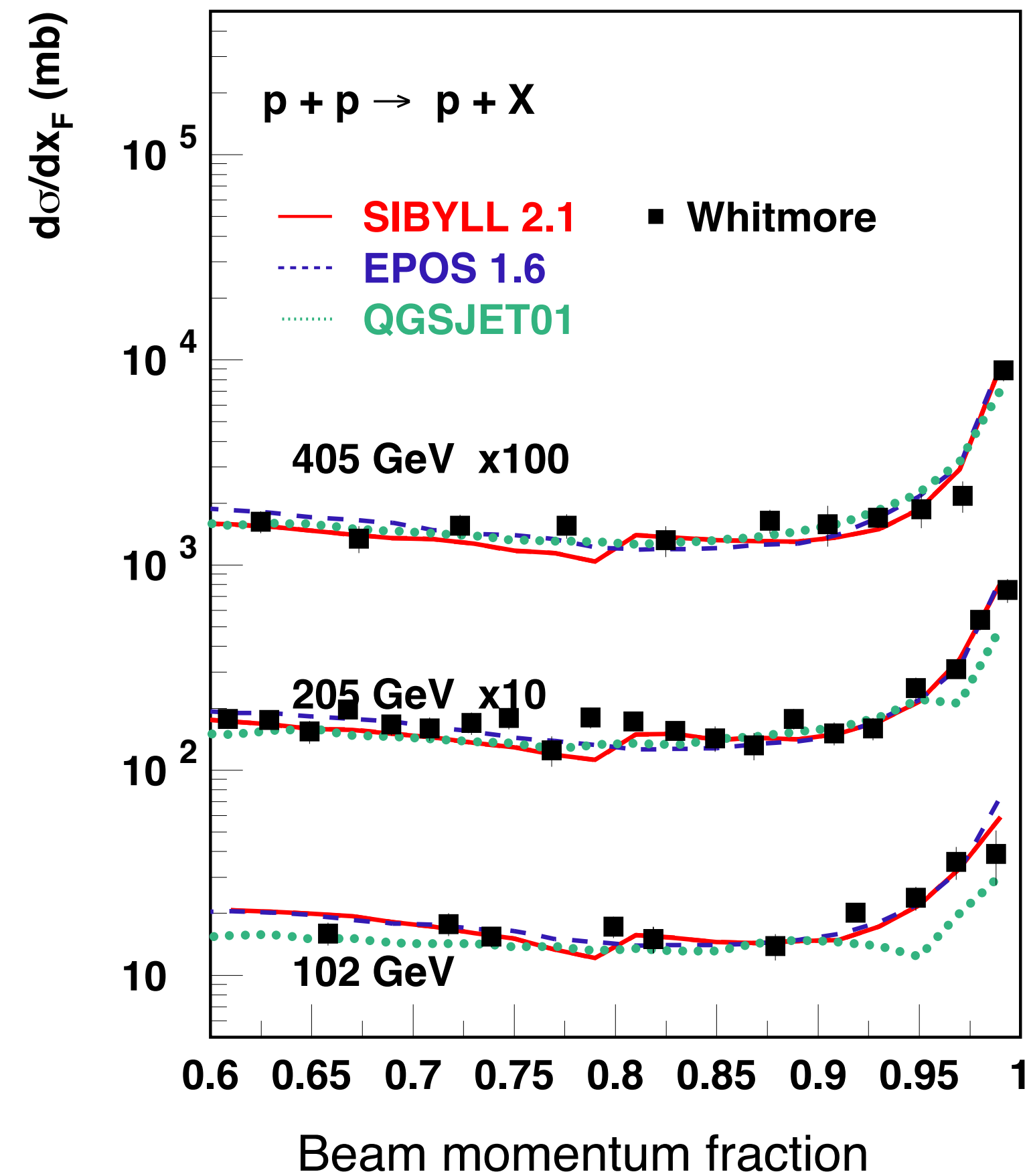
Particle production in hadronic interactions (i)



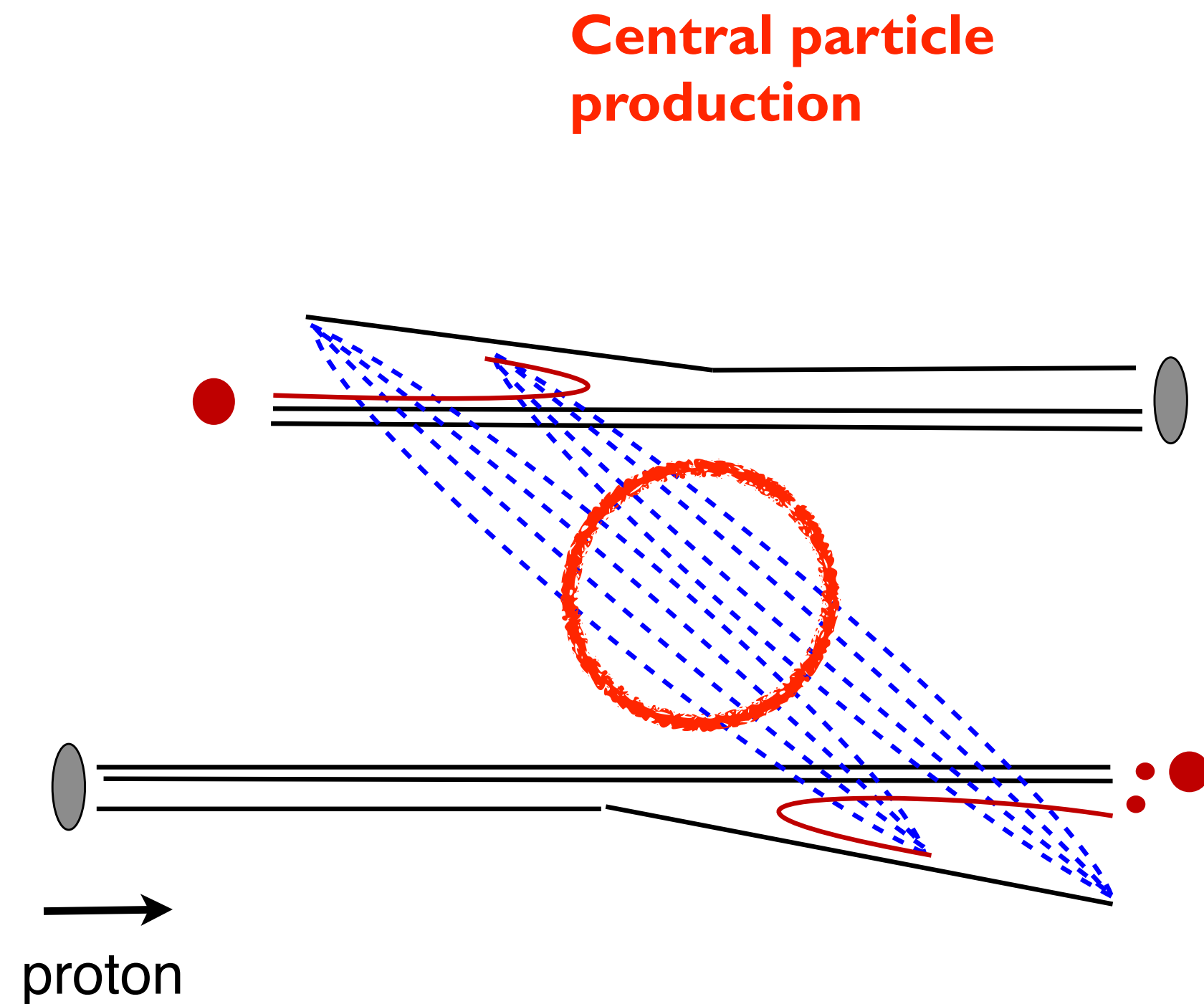
Fluctuations: generation of sea quark anti-quark pair and leading/excited hadron

Leading particle effect:

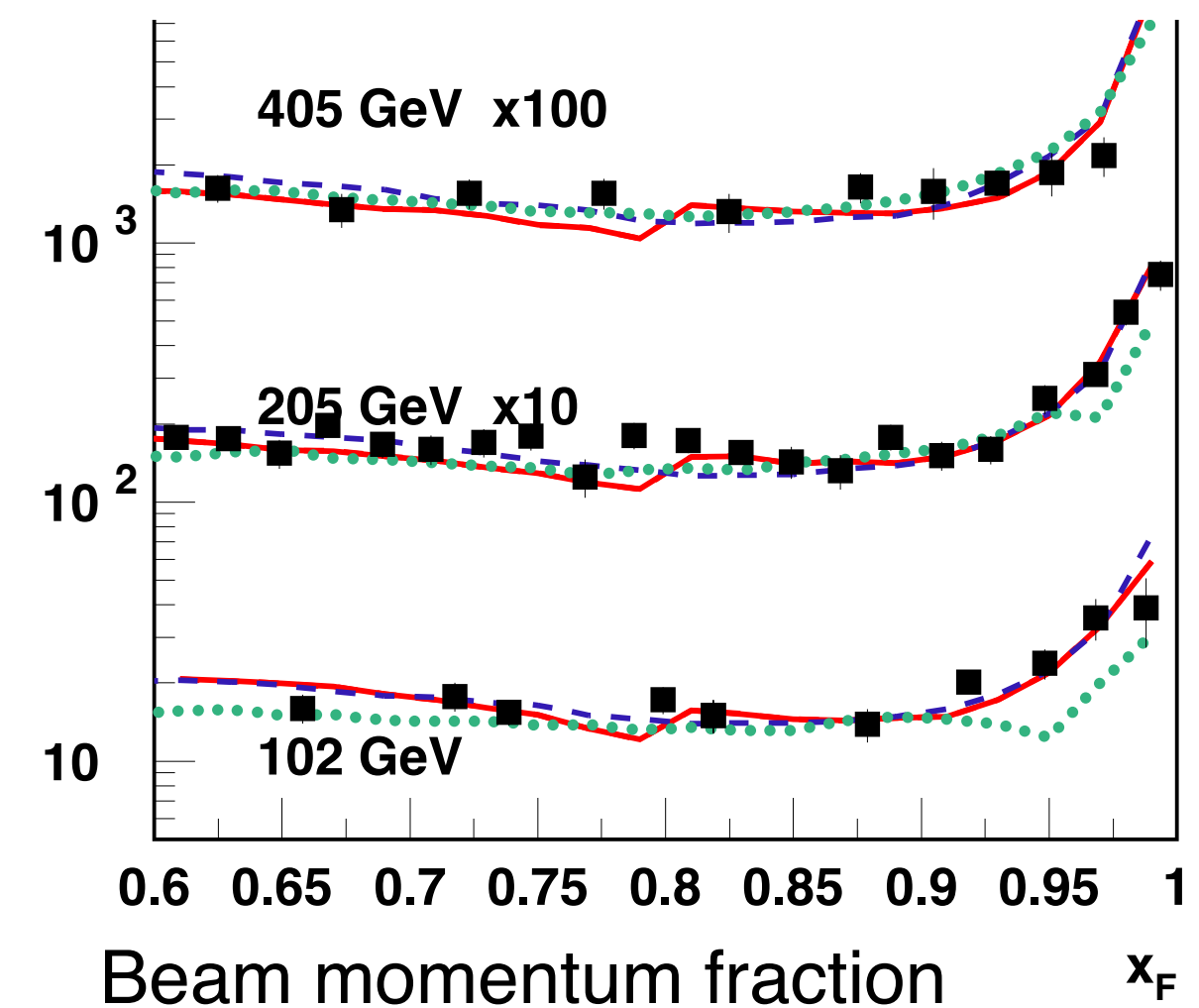
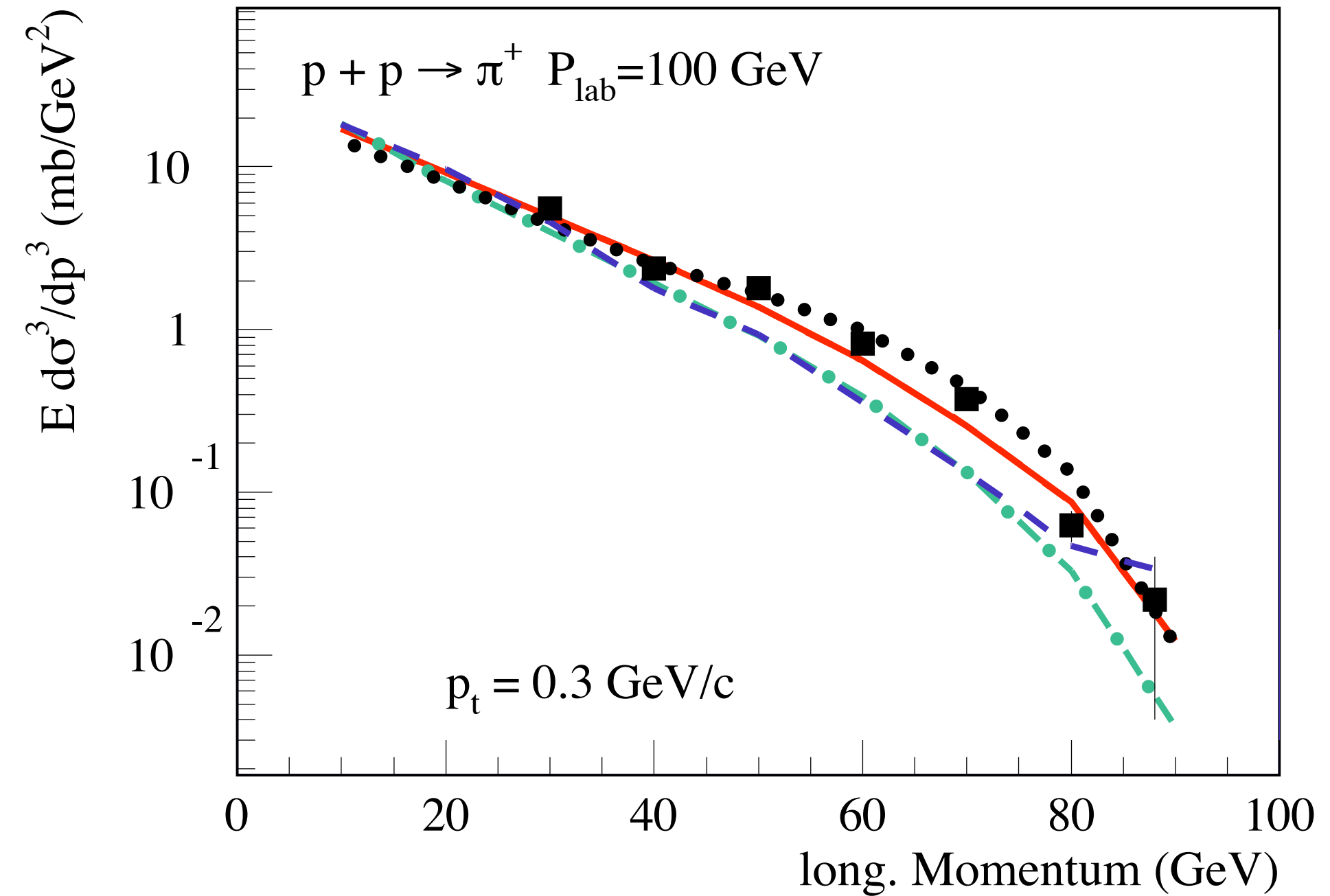
approx. 40–50% of energy of primary particle given to leading particle



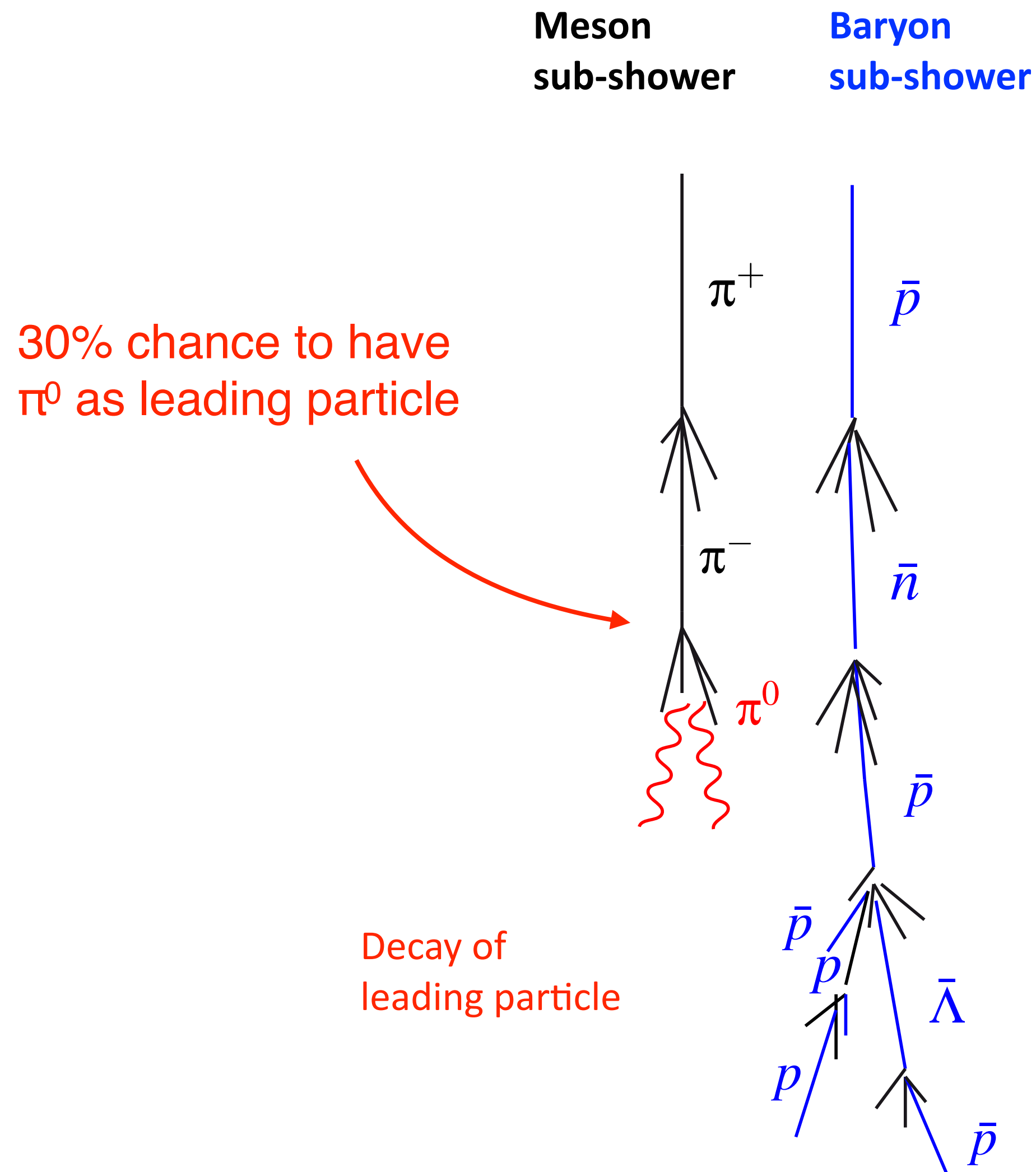
Particle production in hadronic interactions (ii)



Fluctuations: generation of sea quark anti-quark pair and leading/excited hadron



Muon production depends on hadronic energy fraction



1 Baryon-Antibaryon pair production *(Pierog, Werner 2008)*

- Baryon number conservation
- Low-energy particles: large angle to shower axis
- Transverse momentum of baryons higher
- Enhancement of mainly **low-energy** muons

(Grieder ICRC 1973; Pierog, Werner PRL 101, 2008)

2 Leading particle effect for pions *(Drescher 2007, Ostapchenko 2016)*

- Leading particle for a π could be ρ^0 and not π^0
- Decay of ρ^0 to 100% into two charged pions

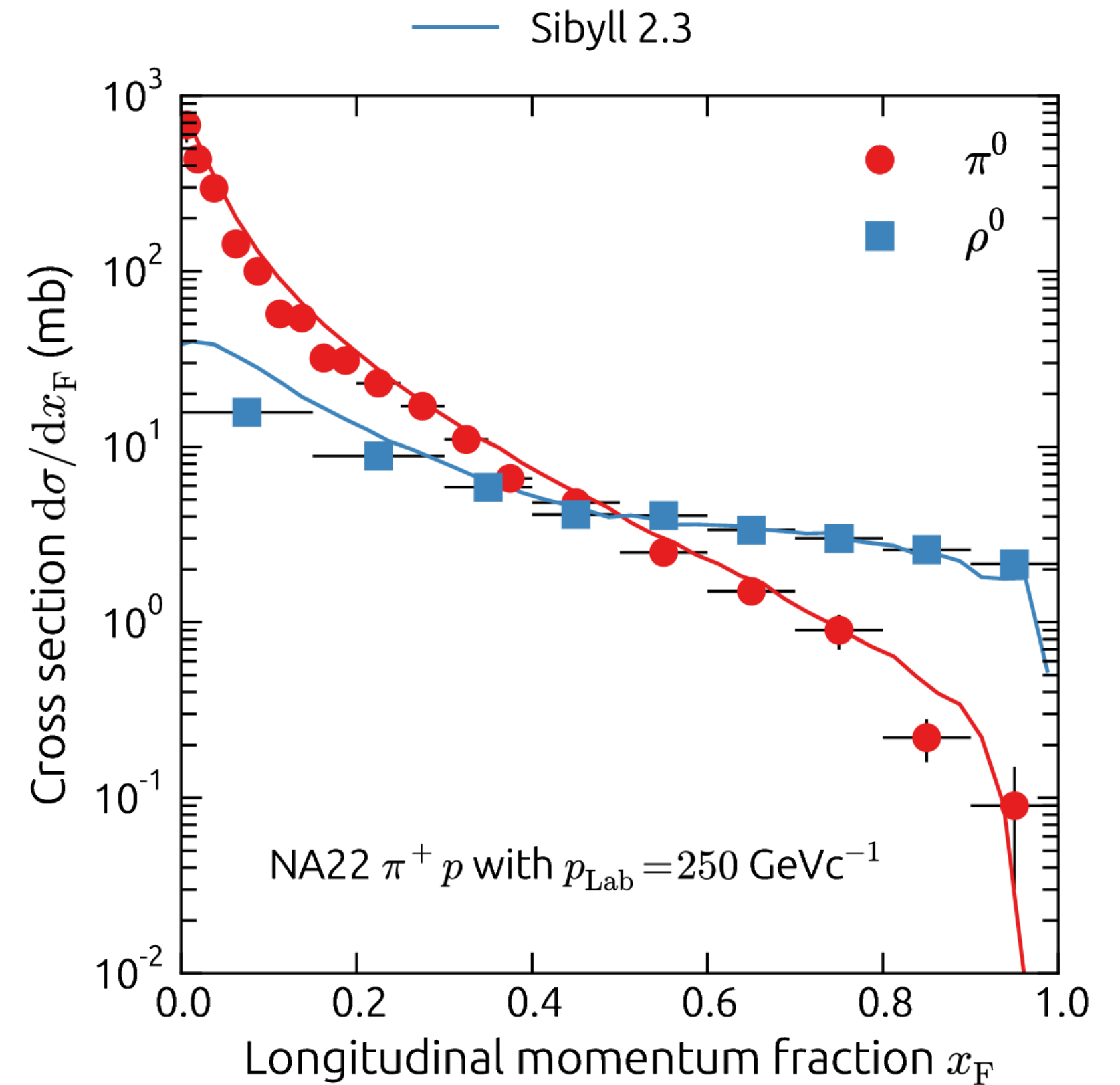
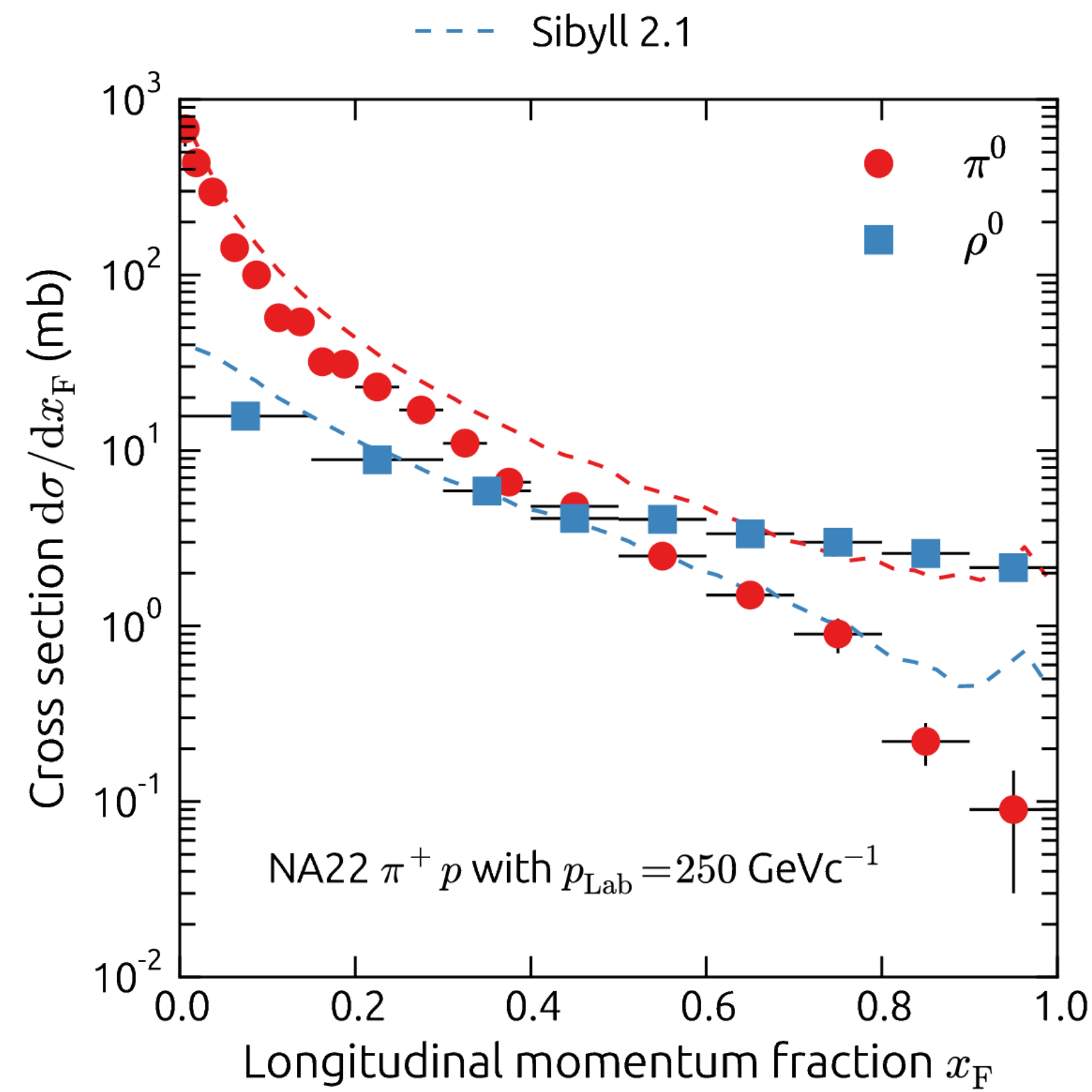
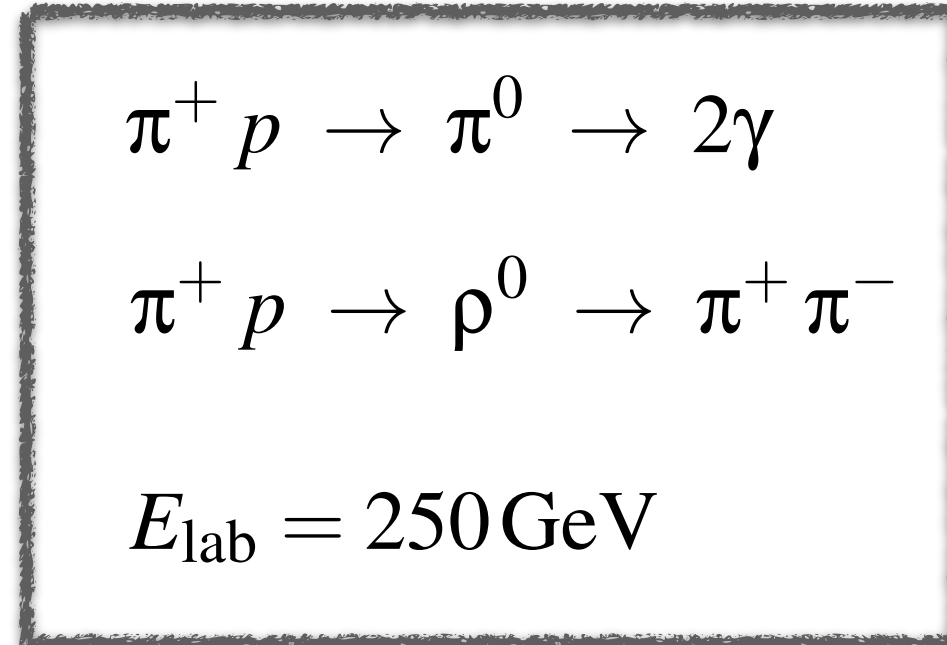
Core-Corona model (Pierog et al.)

3 New hadronic physics at high energy *(Farrar, Allen 2012)*

- Inhibition of π^0 decay (Lorentz invariance violation etc.)
- Chiral symmetry restoration

Rho production in π -p interactions (Sibyll 2.1 \rightarrow Sibyll 2.3)

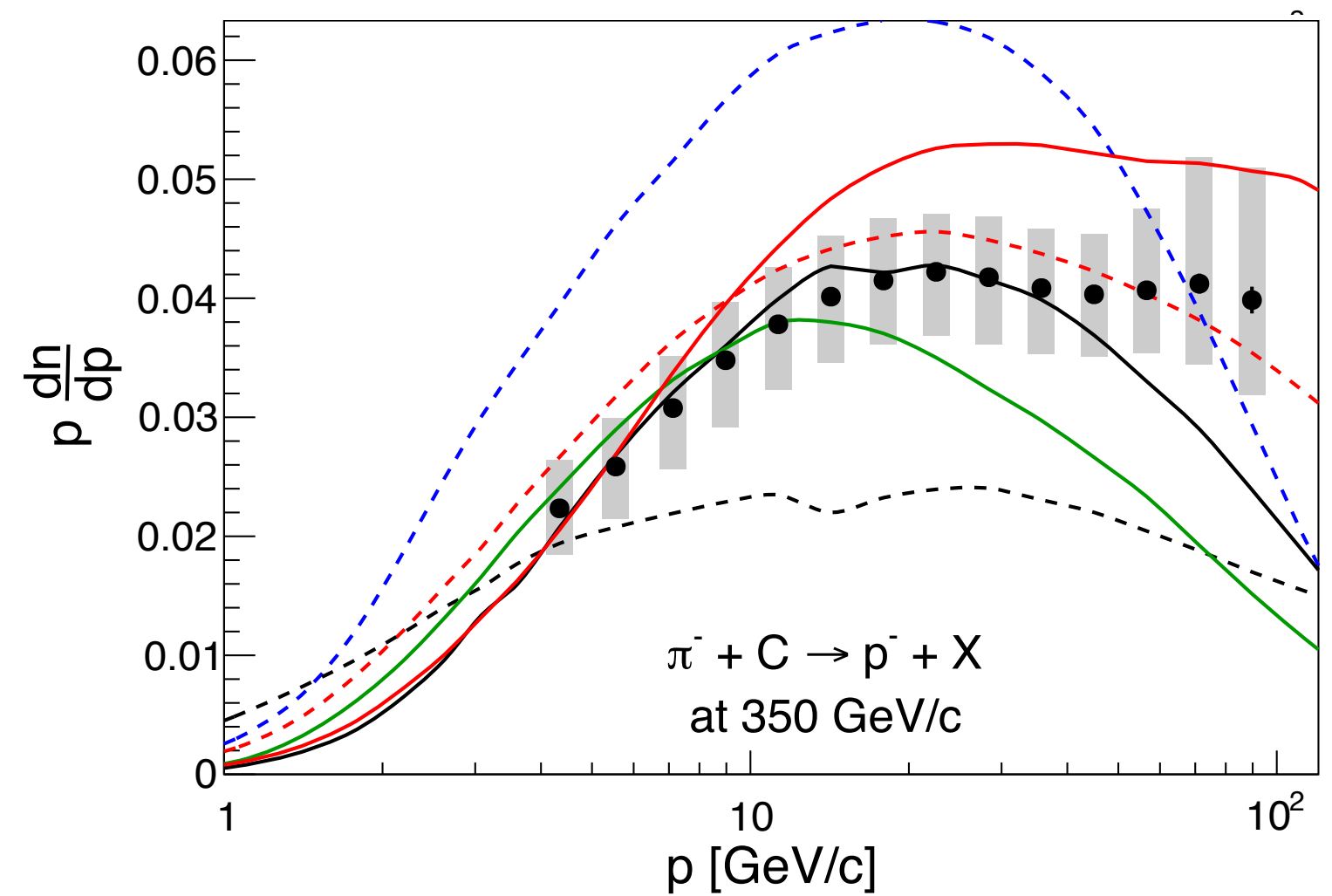
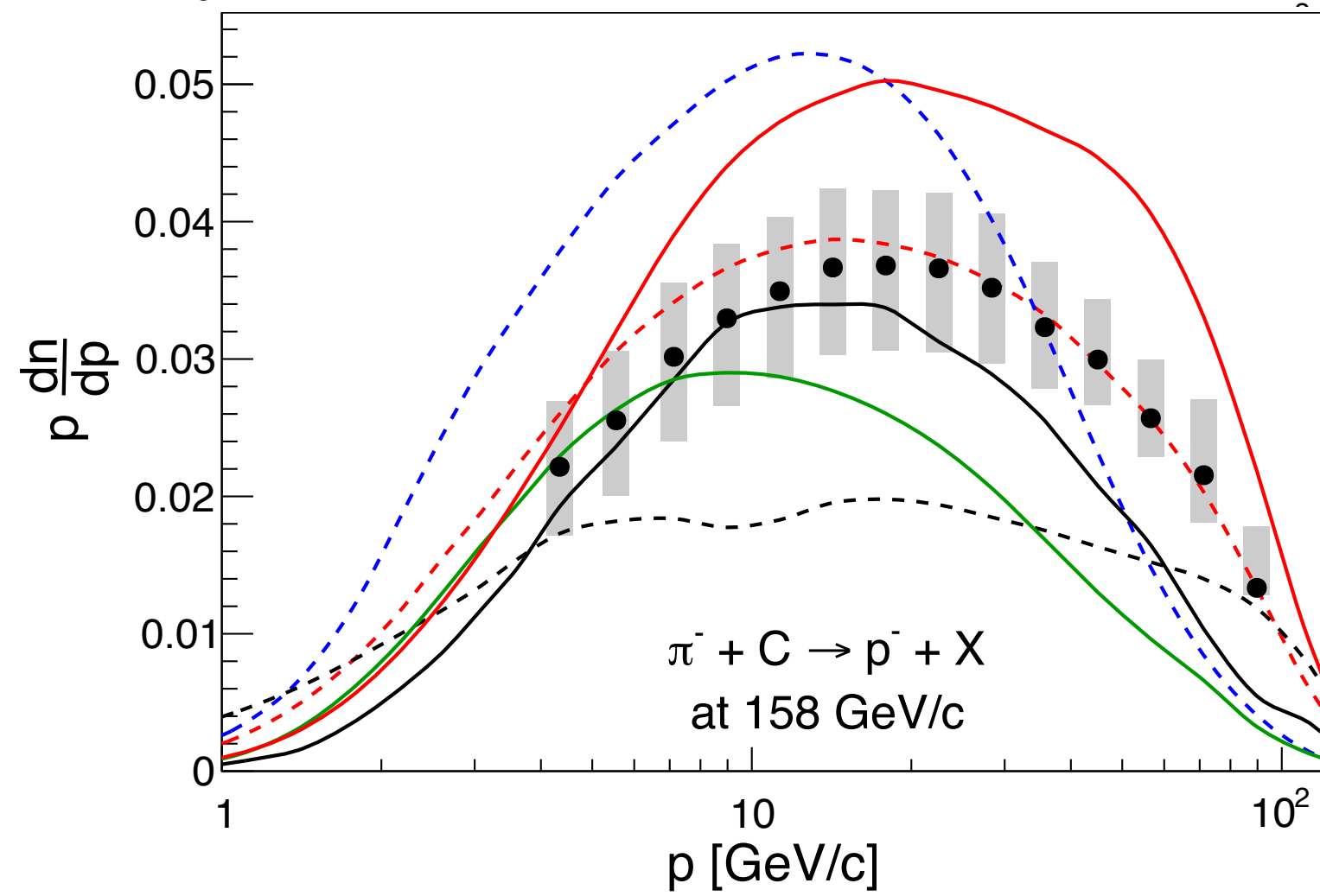
Leading particle production



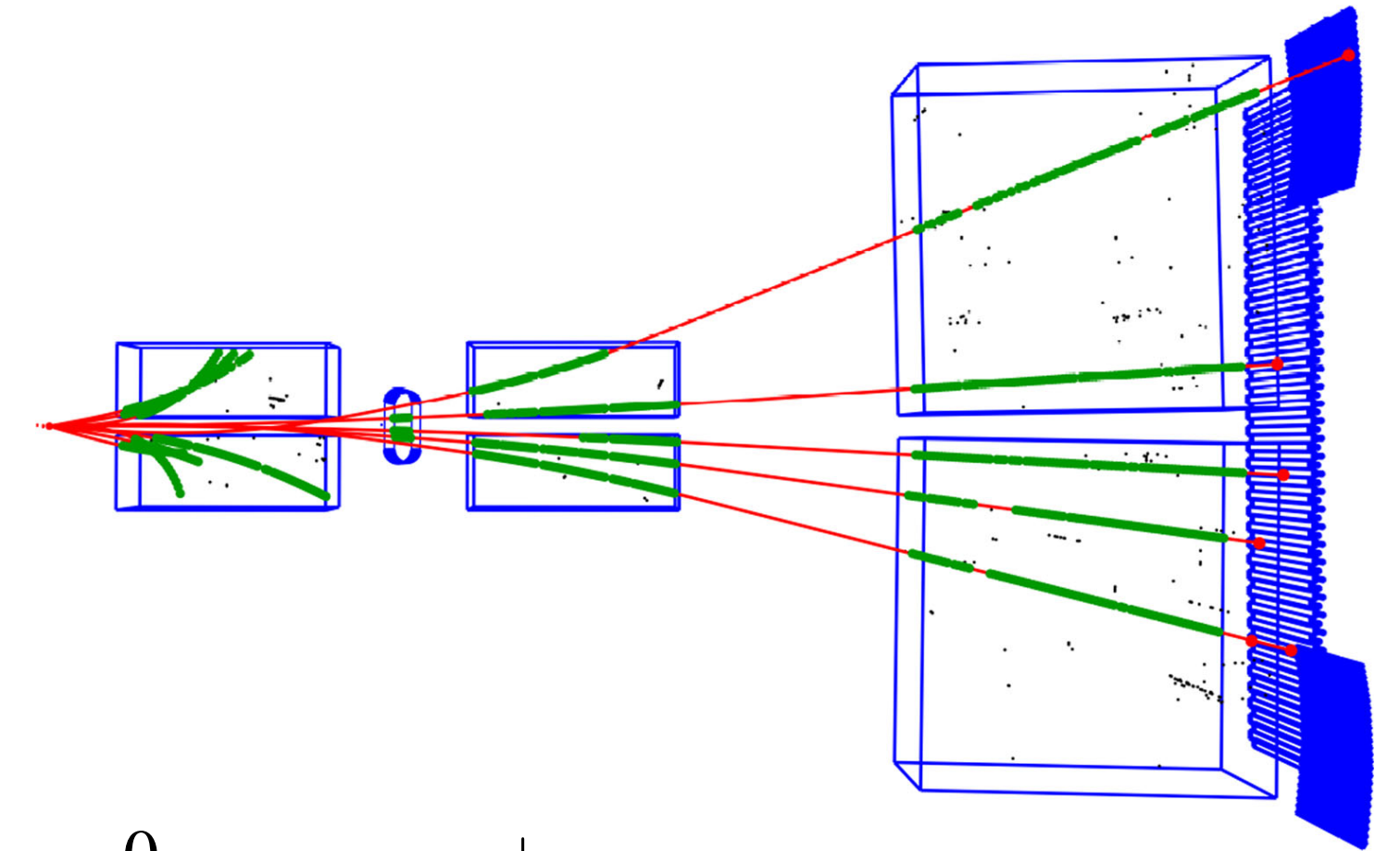
$$x_F = p_{\parallel} / p_{\text{max}}$$

NA61 experiment at CERN SPS

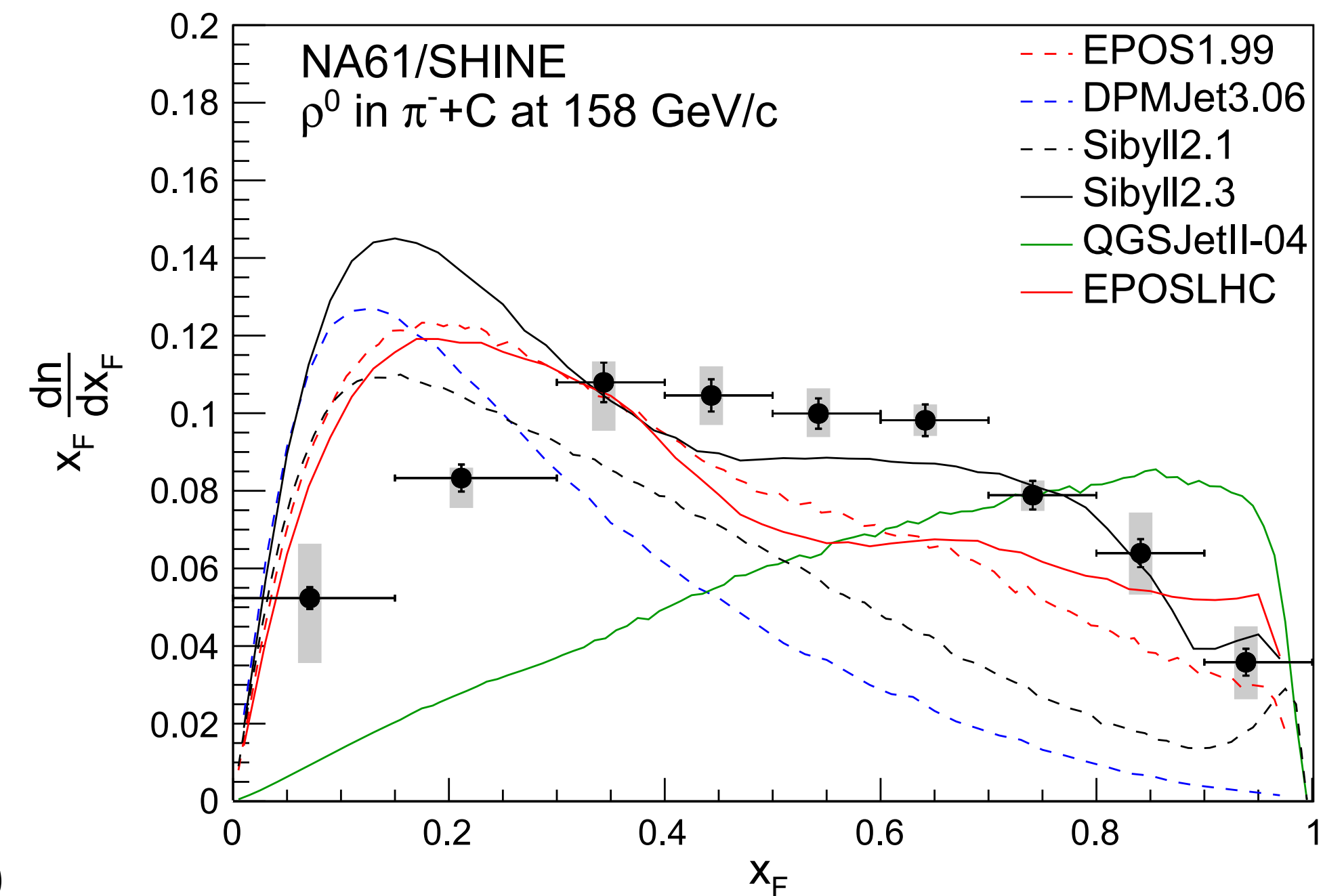
$$\pi^- C \rightarrow \bar{p} X$$



Dedicated cosmic ray runs
(π -C at 158 and 350 GeV)

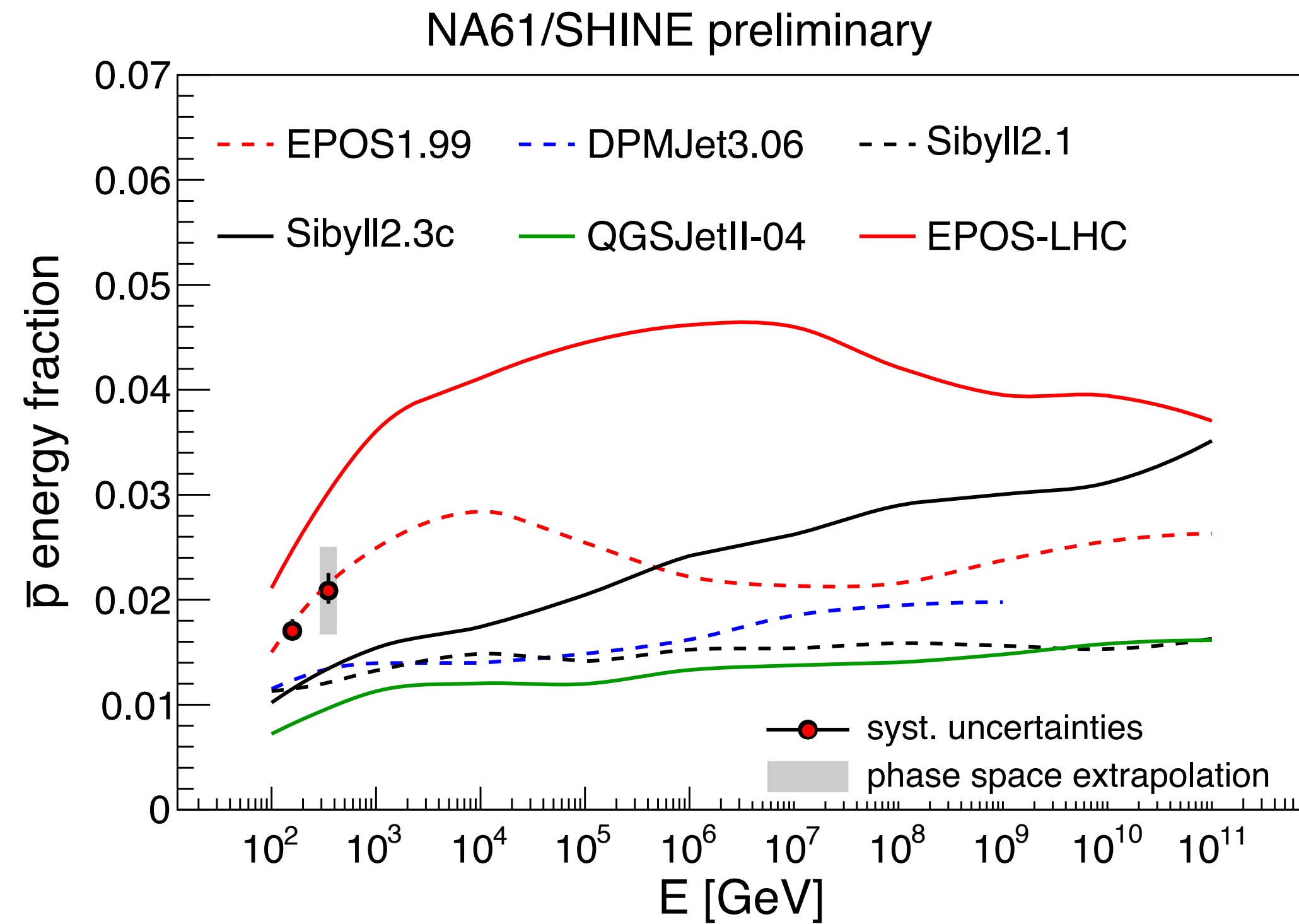


$$\pi^- C \rightarrow \rho^0 X \rightarrow \pi^+ \pi^- X$$

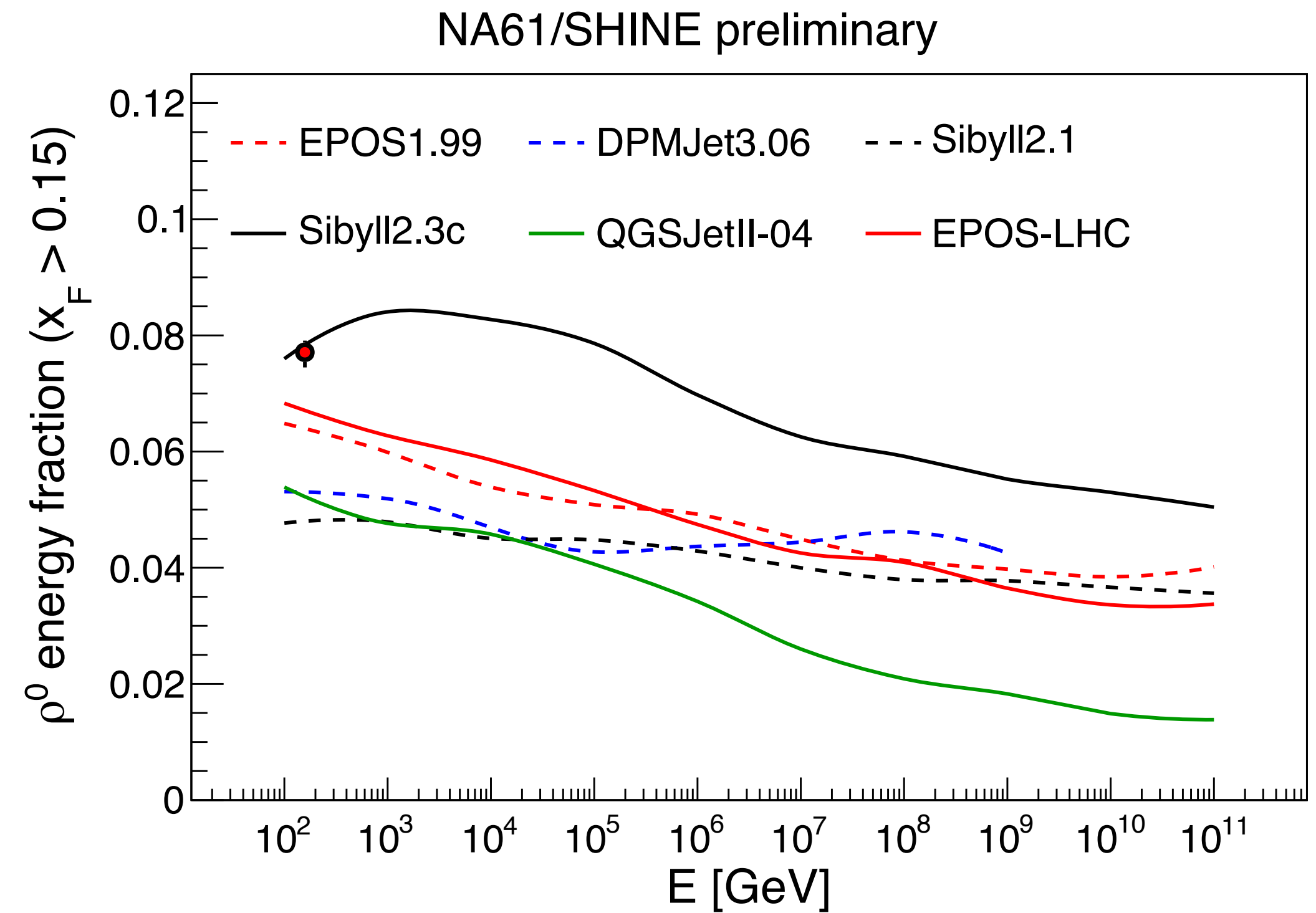


(NA61, EPJ 77, 2017)

NA61 results and extrapolation to high energy

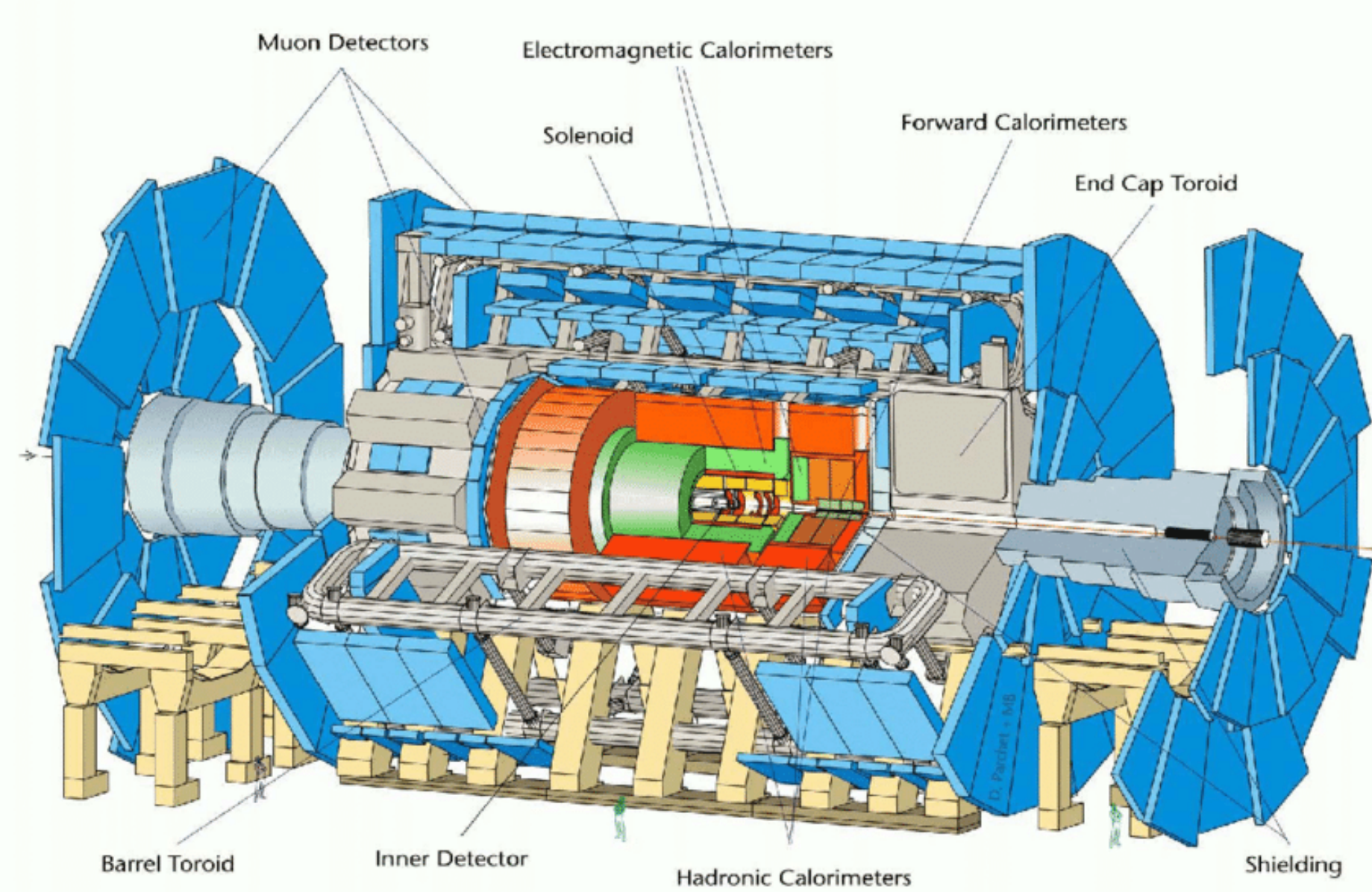


\bar{p} energy fraction in $\pi^- + C$

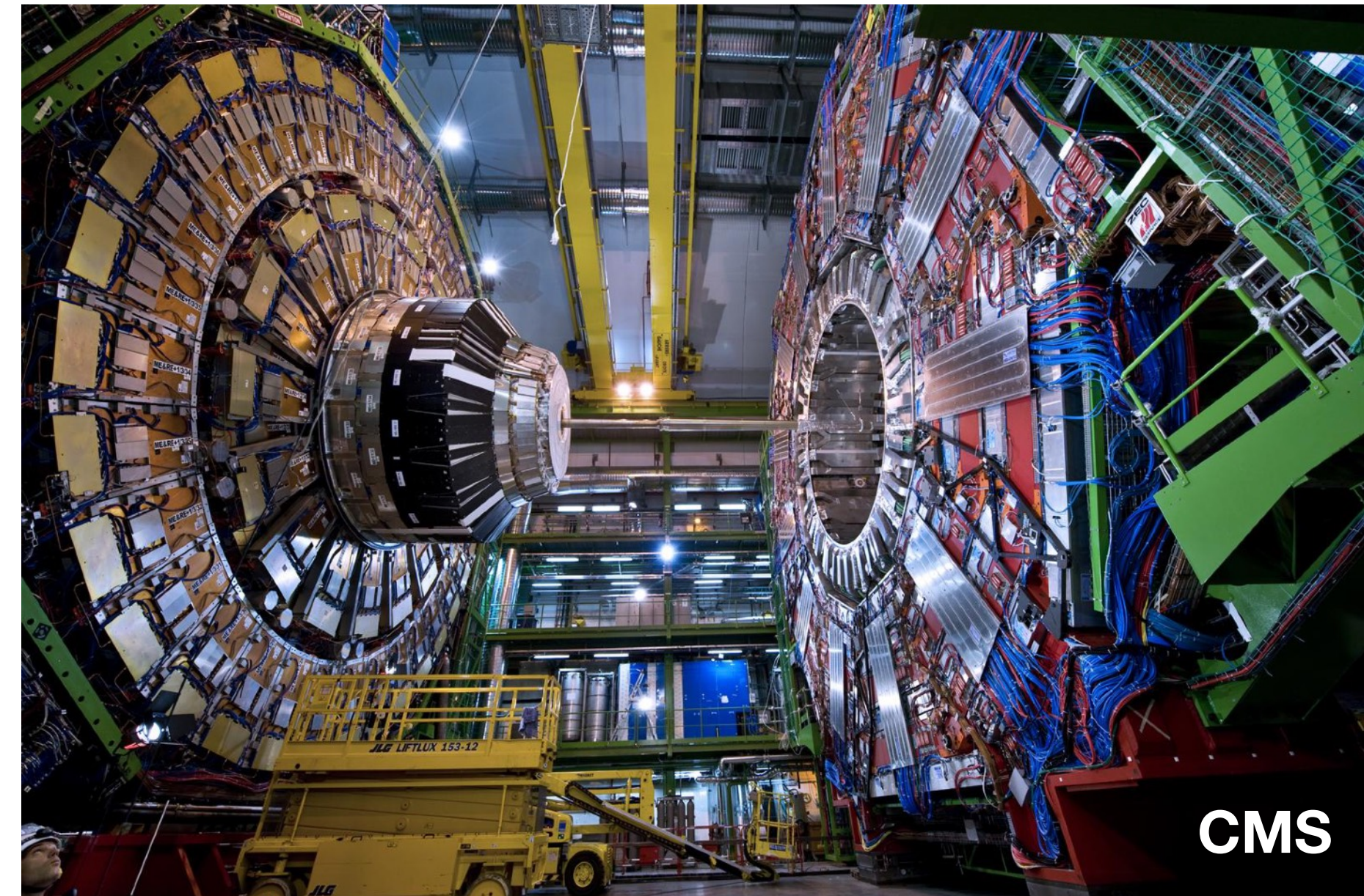


ρ^0 energy fraction in $\pi^- + C$

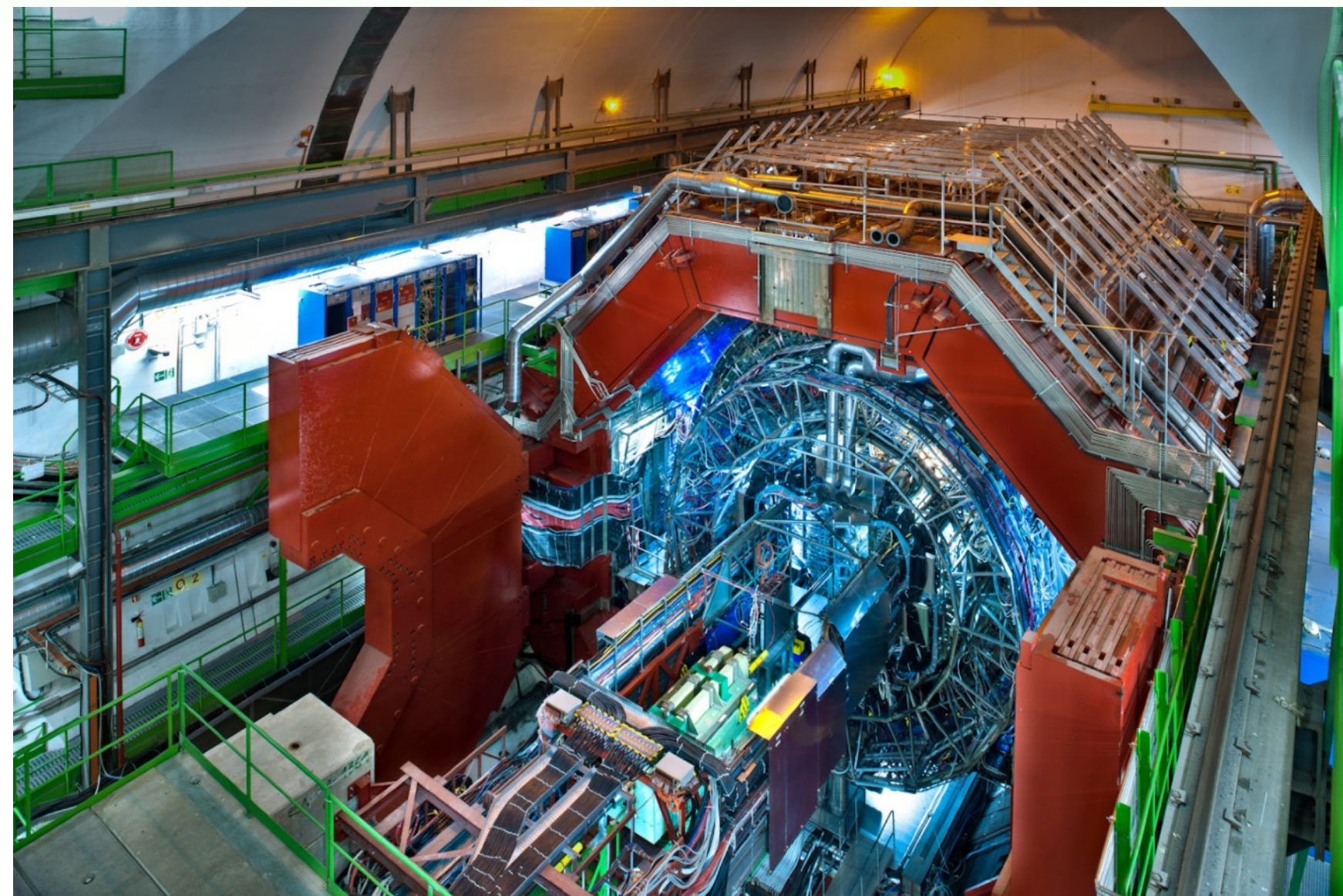
LHC and its experiments ($E_{\text{equiv}} \sim 10^{17}$ eV)



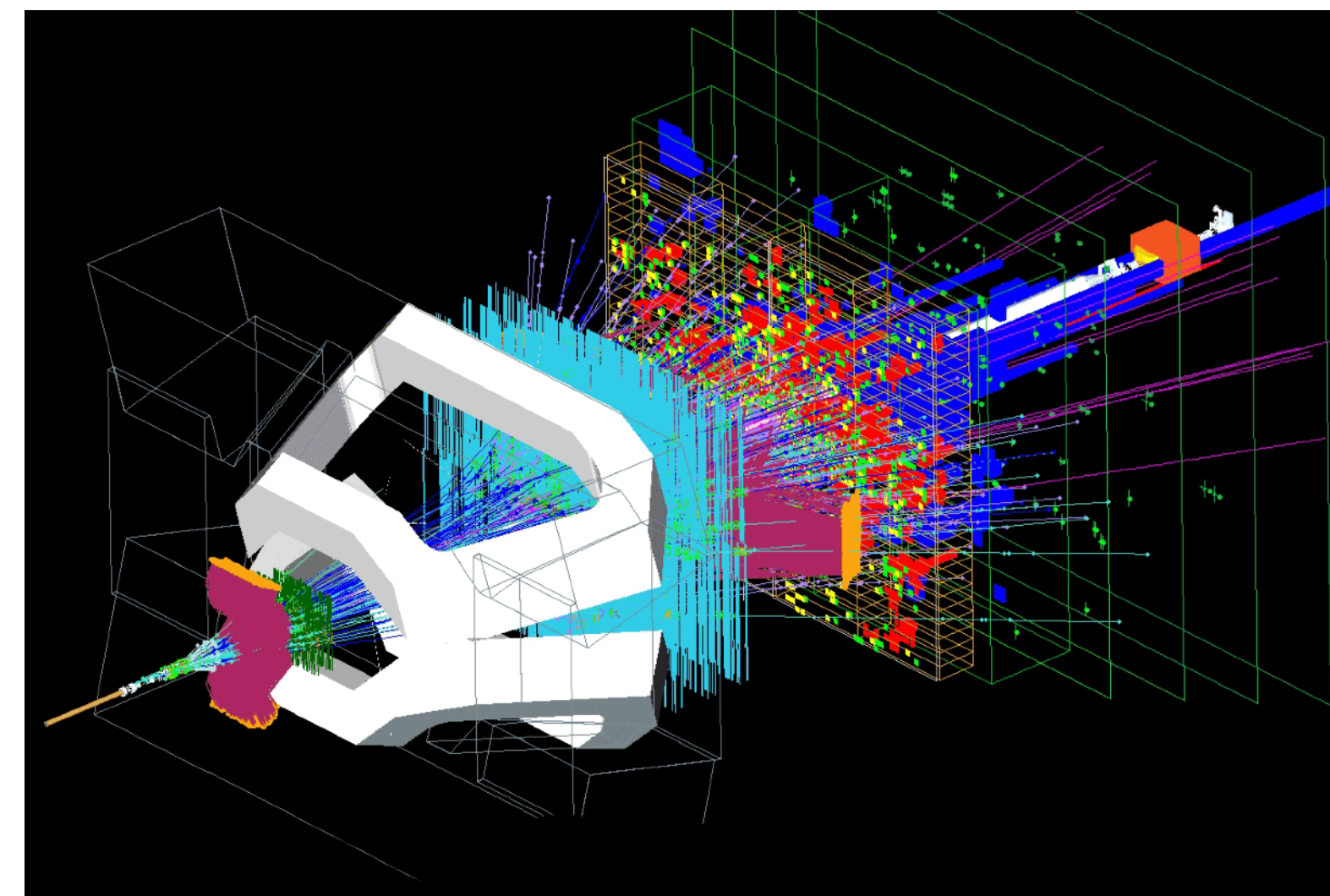
ATLAS



CMS

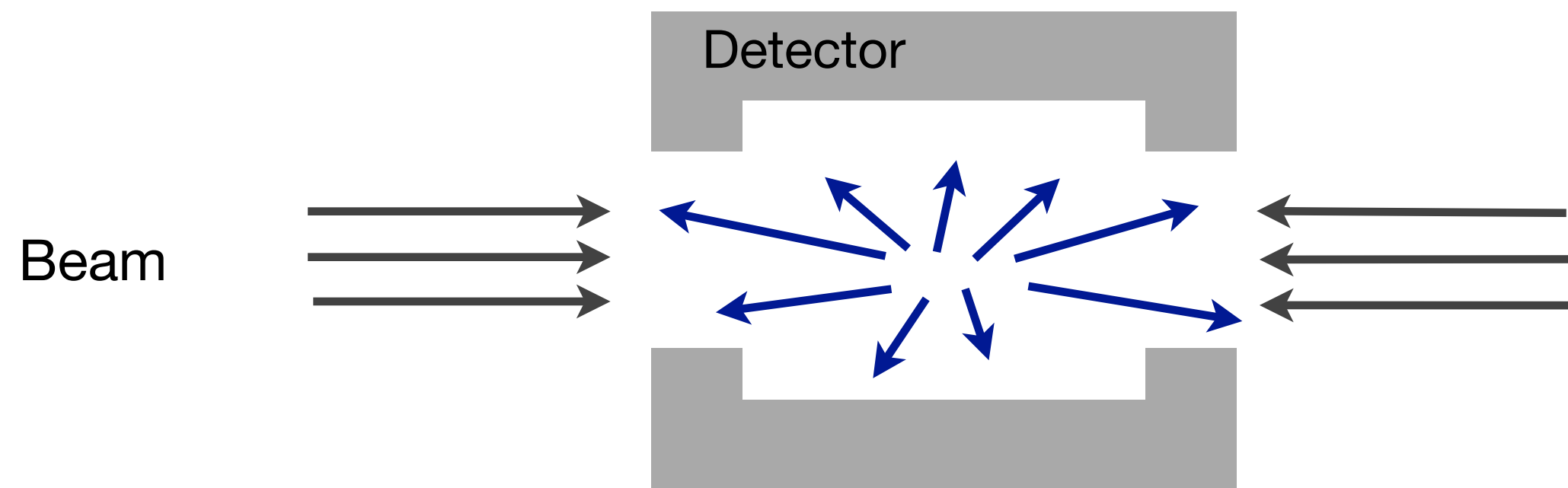


ALICE



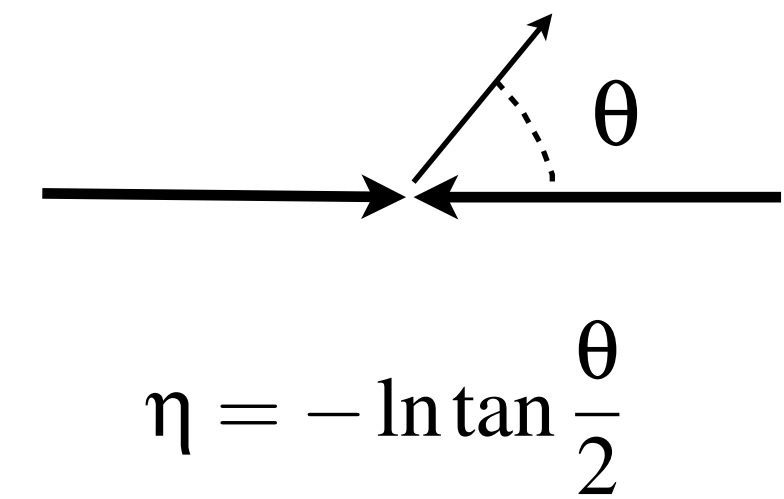
LHCb

Problem of limited phase space coverage

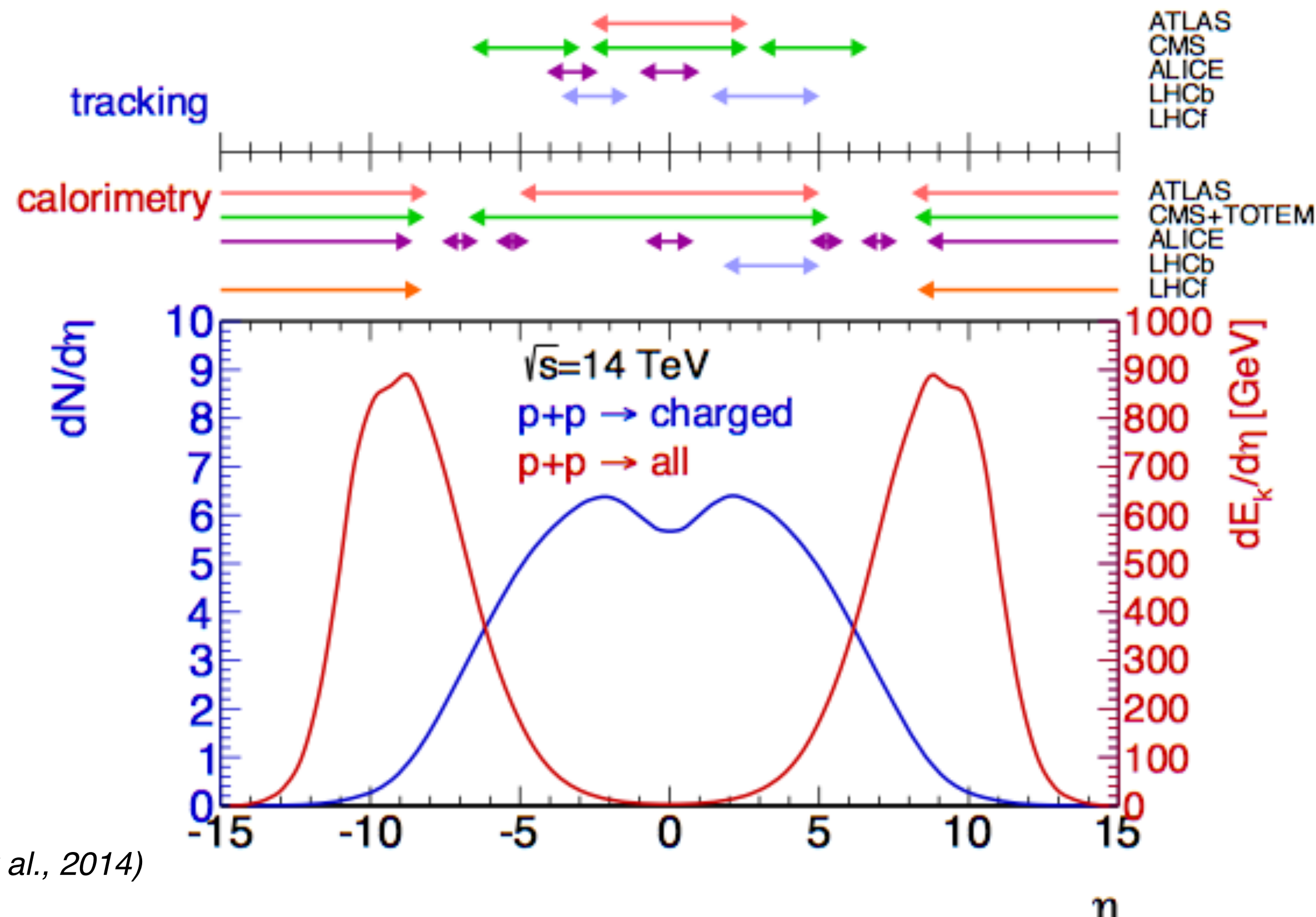


Collider setup

Beam



Pseudorapidity

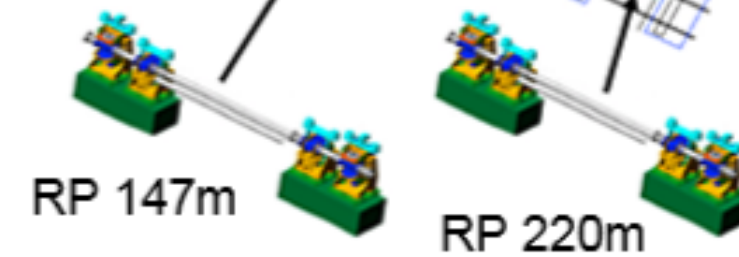
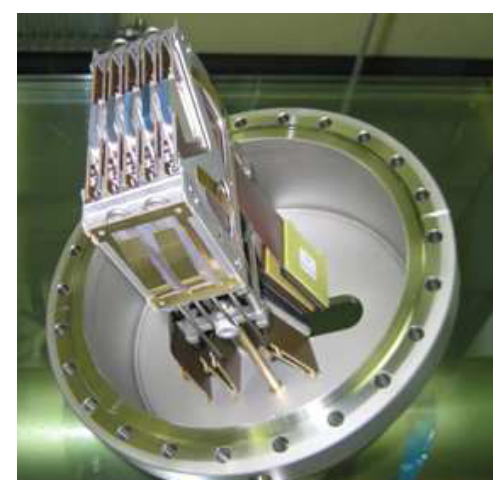
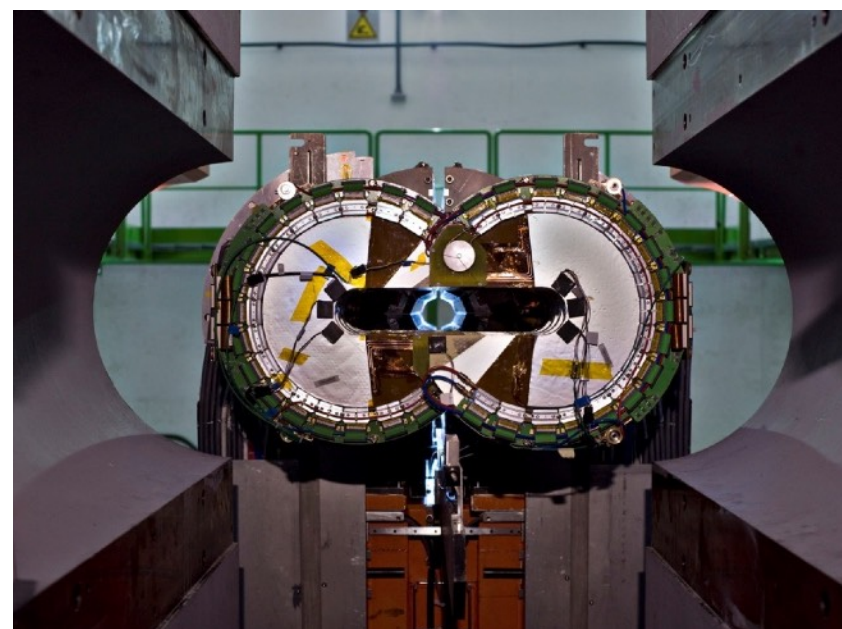
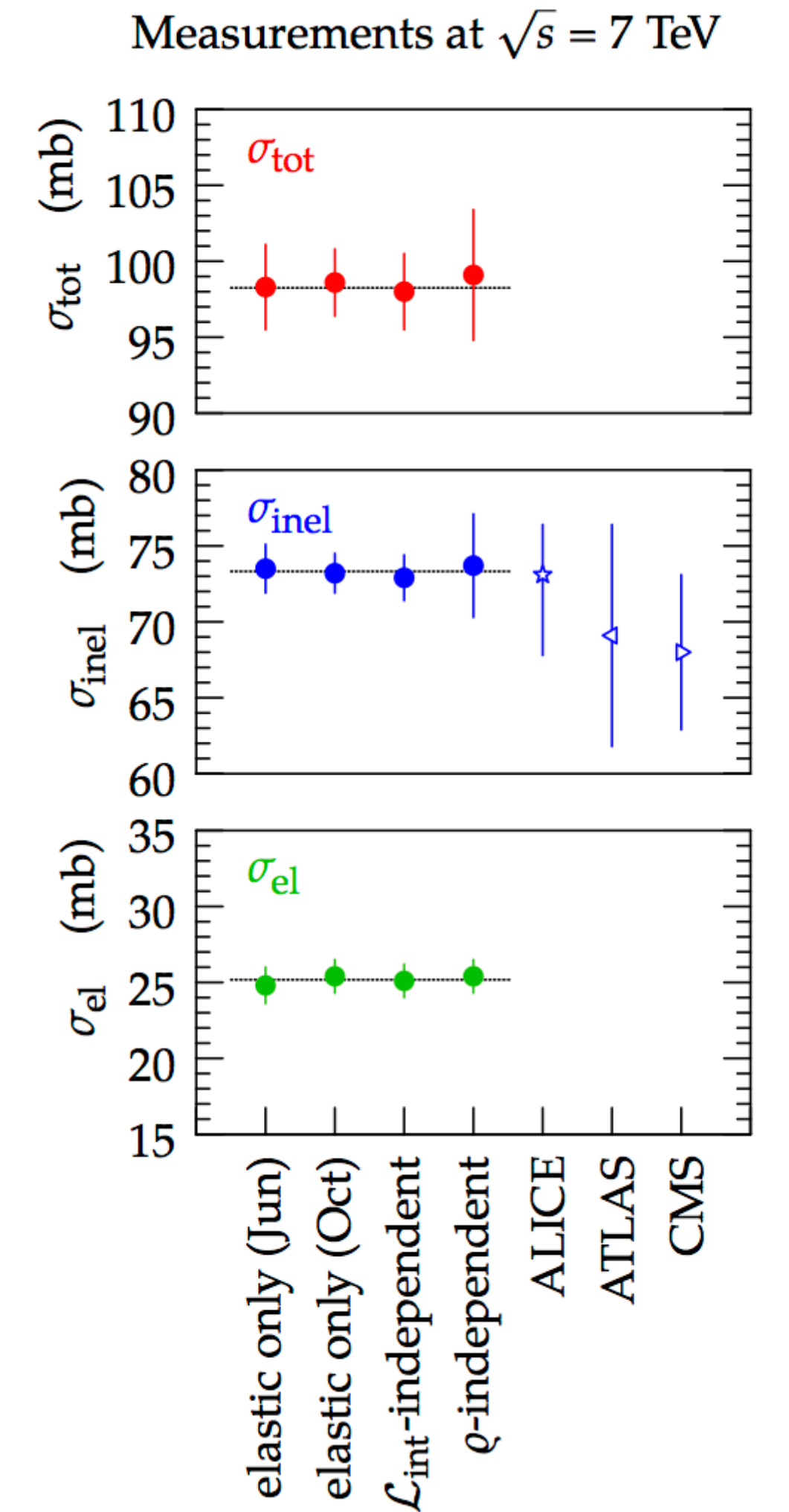
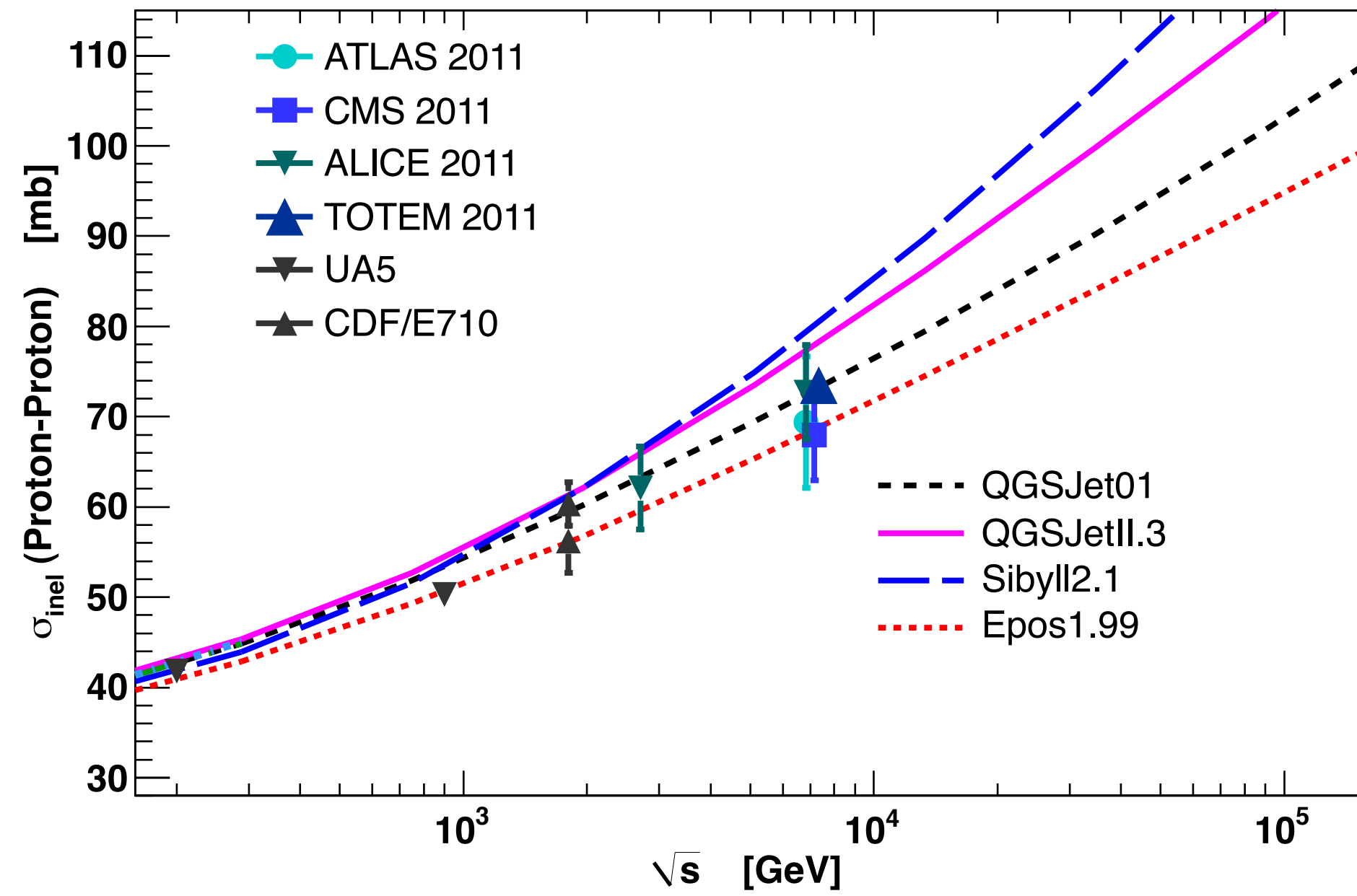
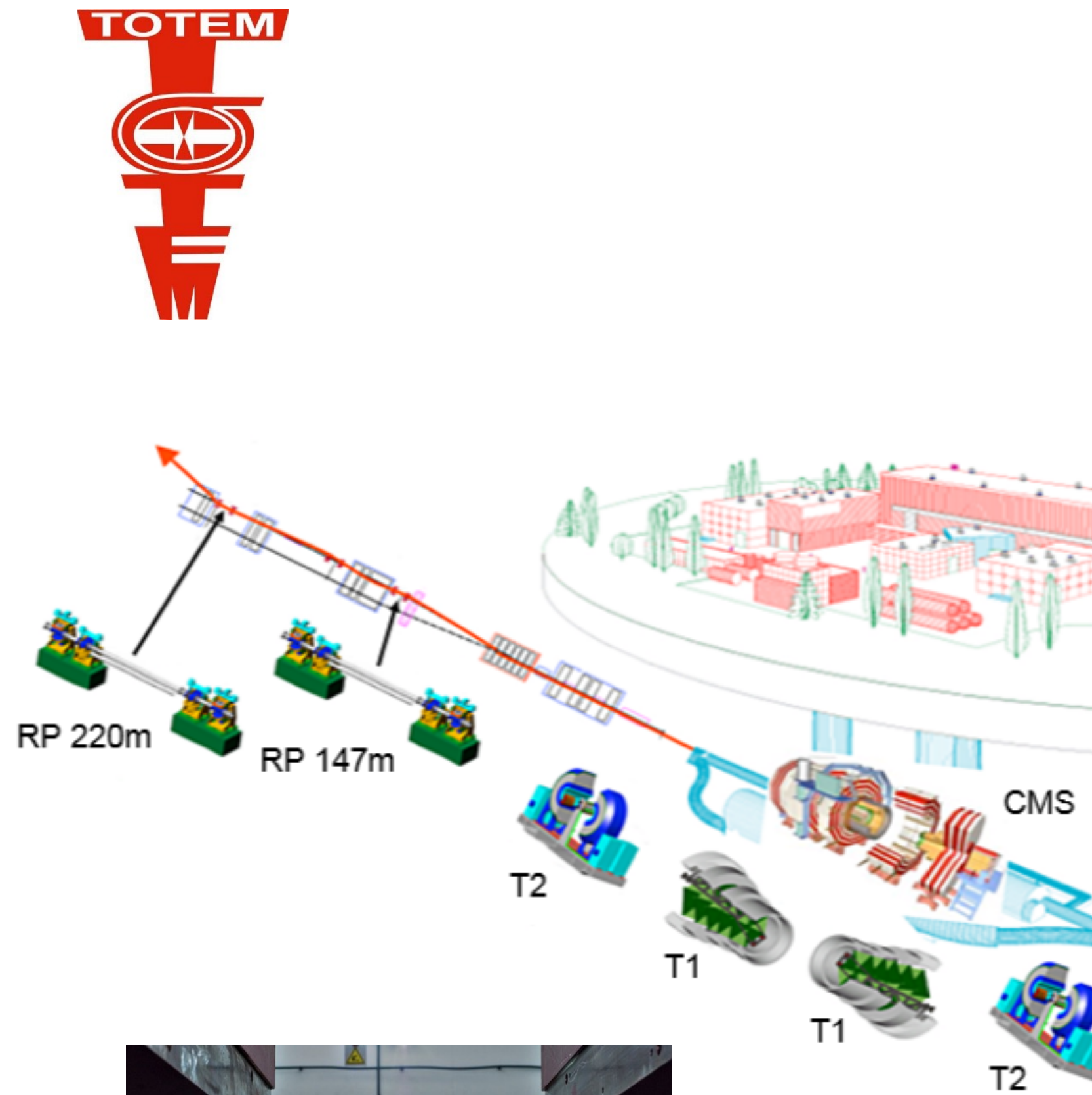


Air showers: Particles of highest energy most important

η	deg.	mrاد.
3	5.7	97
5	0.77	10
8	0.04	0.7
10	0,005	0,009

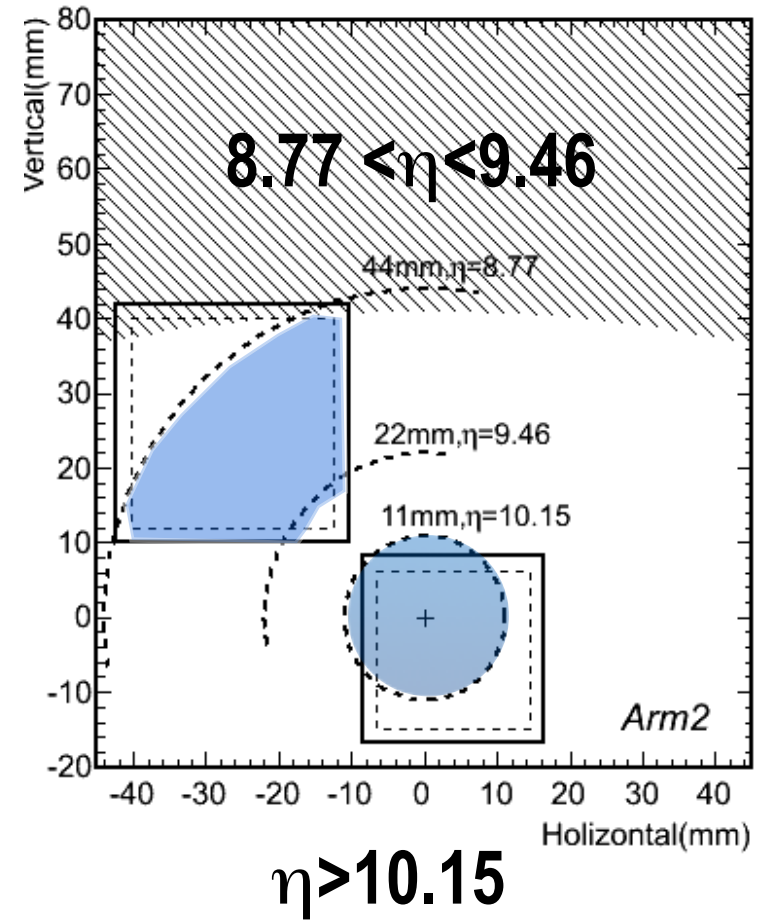
No particle identification in forward direction

Cross section measurements at LHC

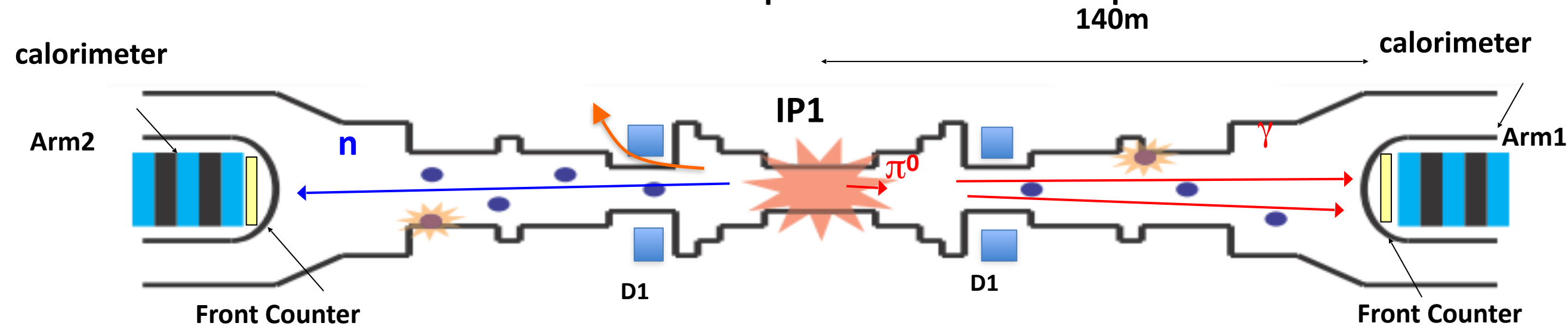


LHCf: very forward photon production at 7 TeV

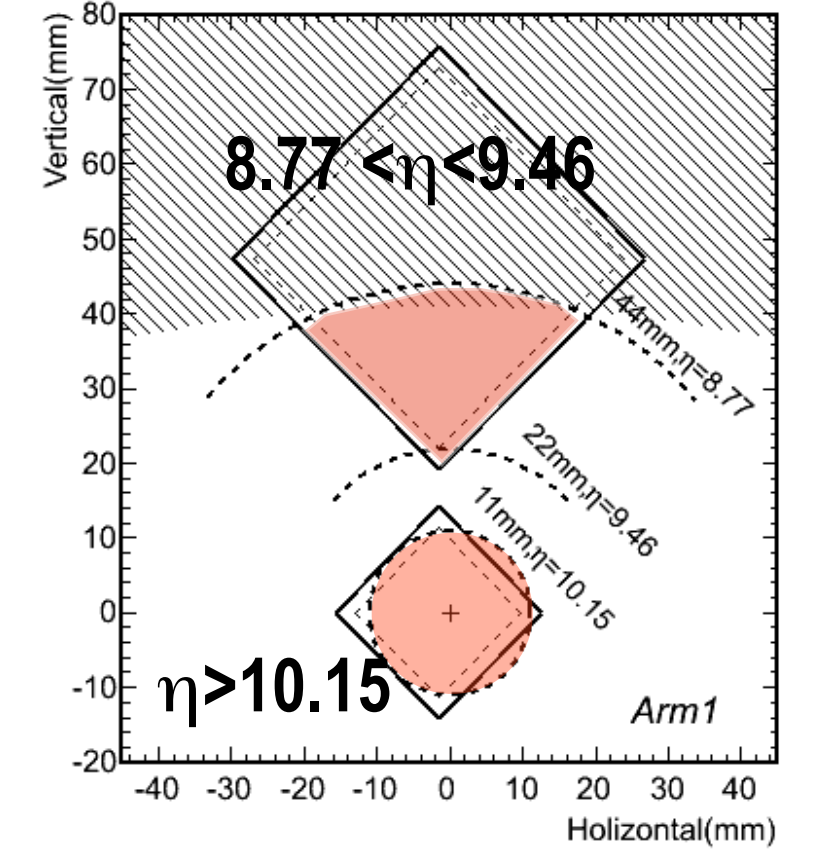
Arm 2



The LHCf experimental setup

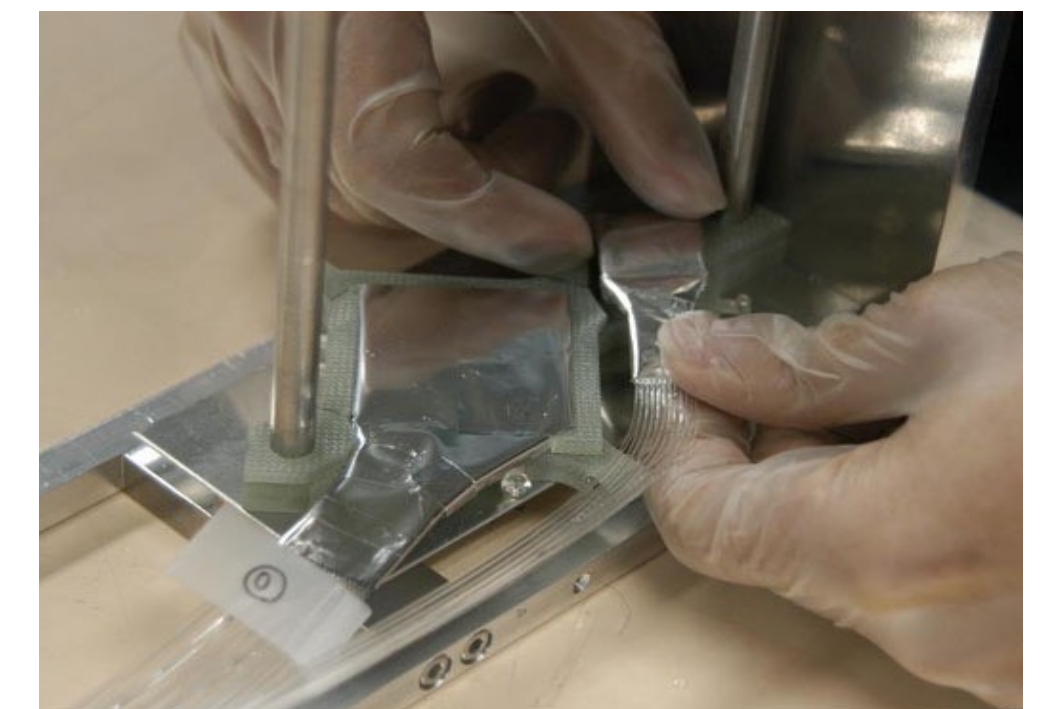
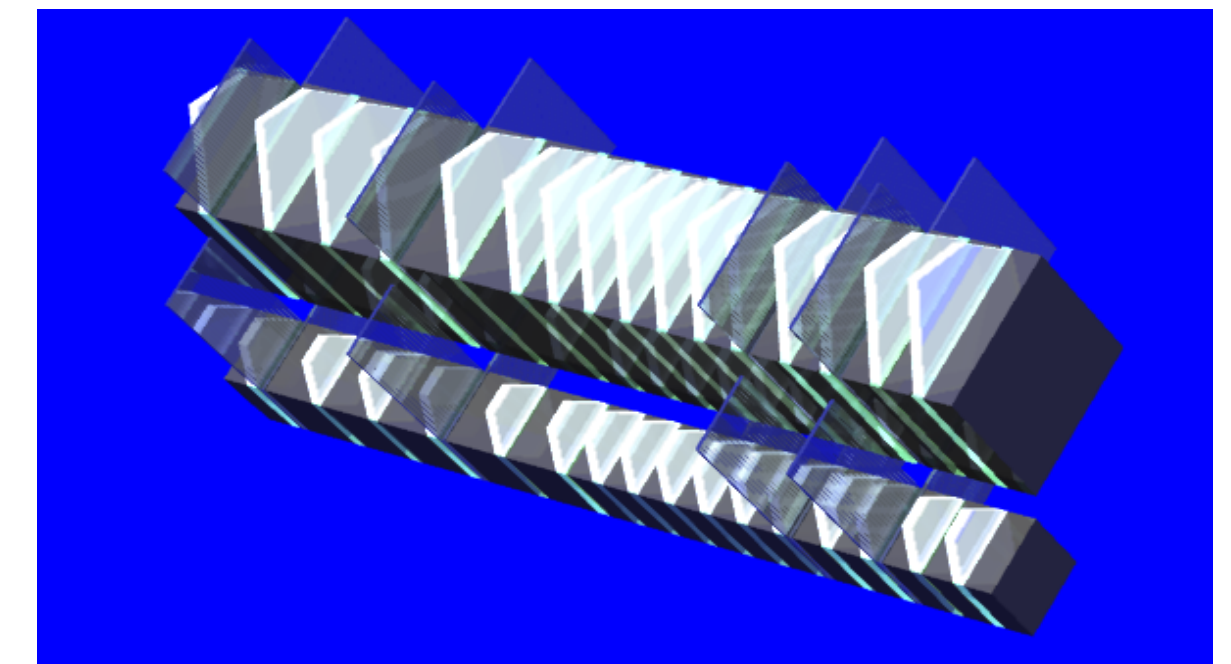
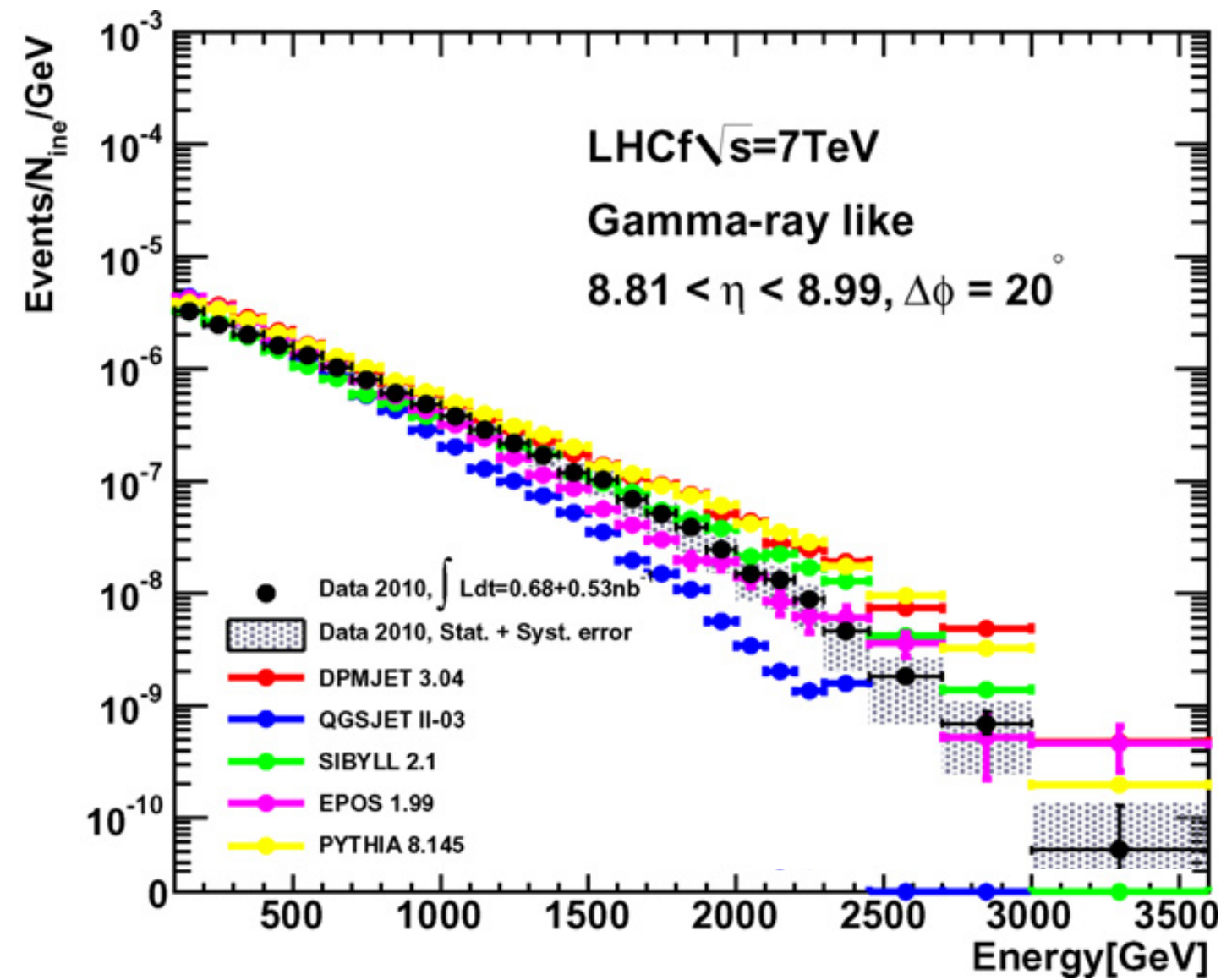
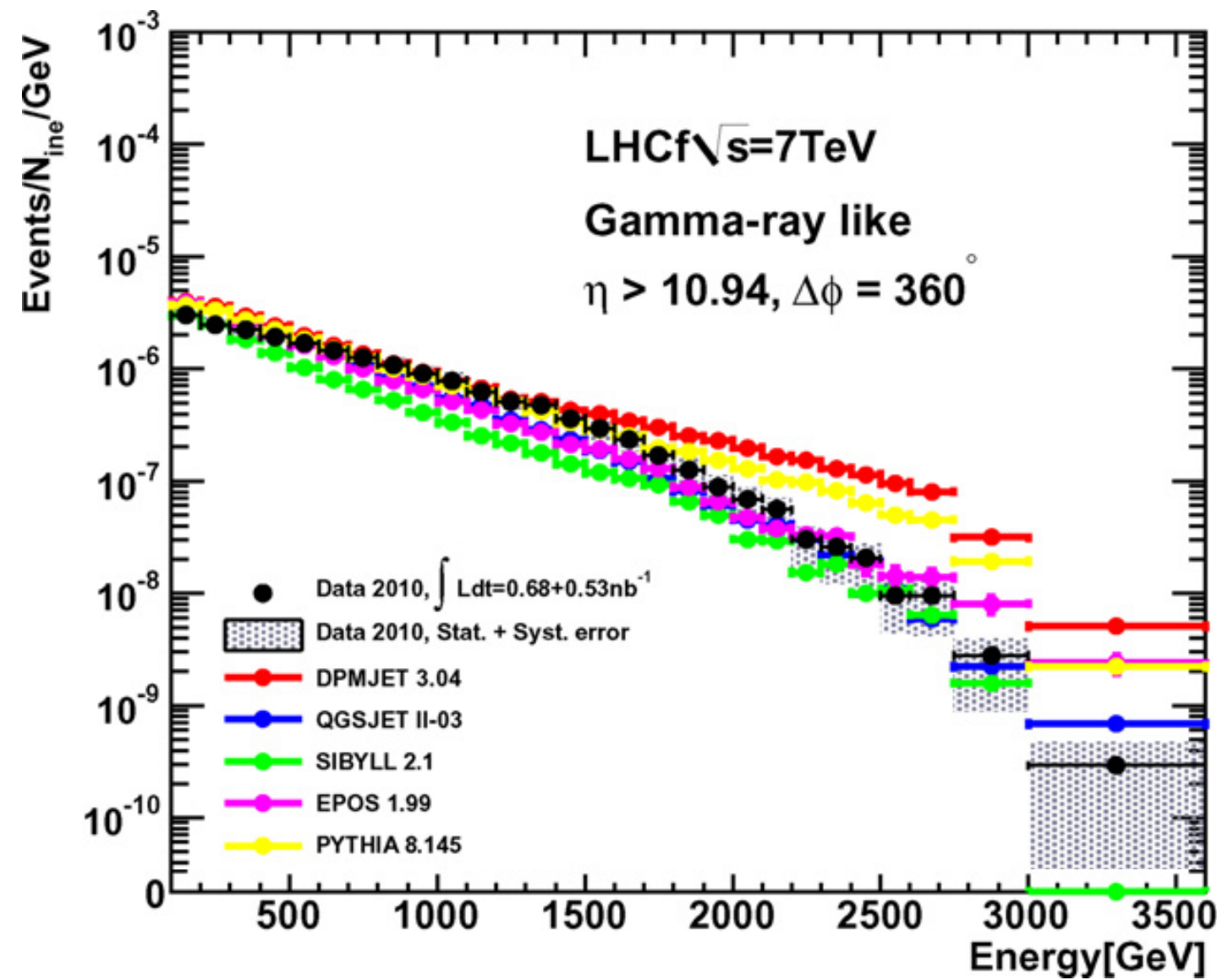


Arm 1

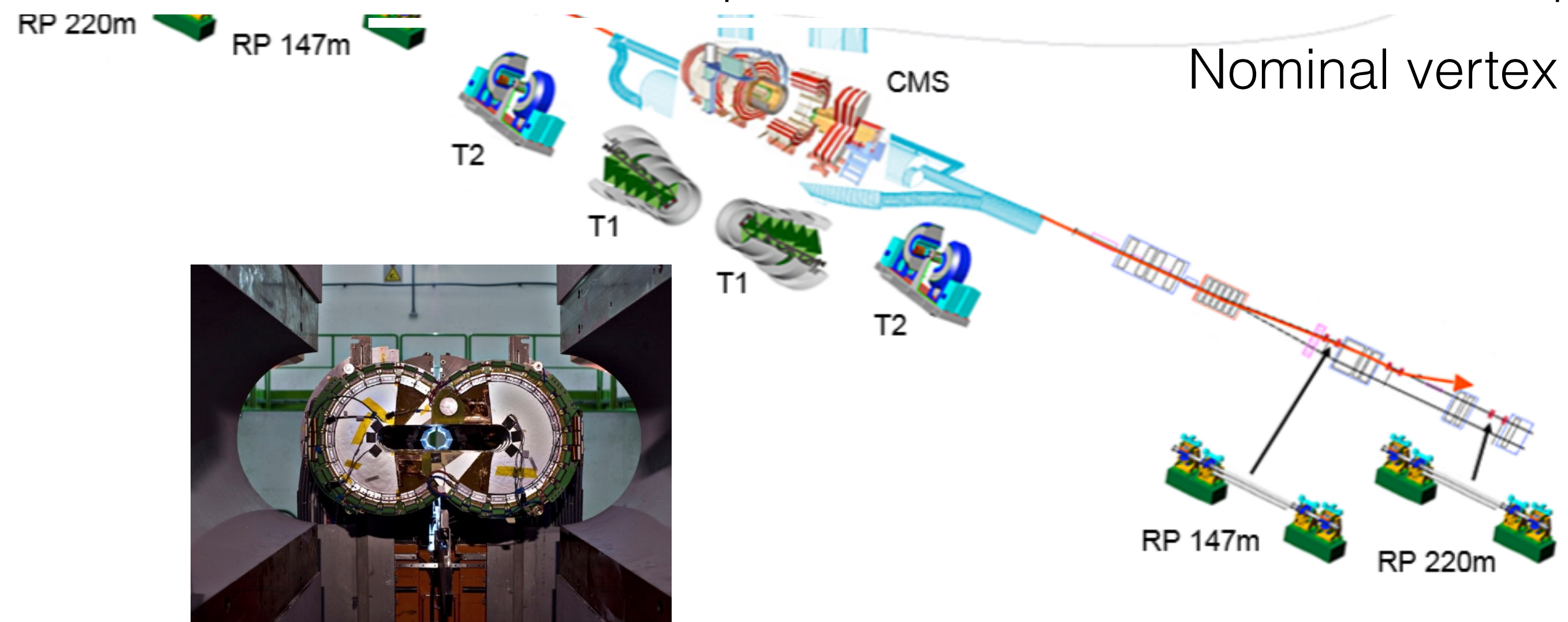
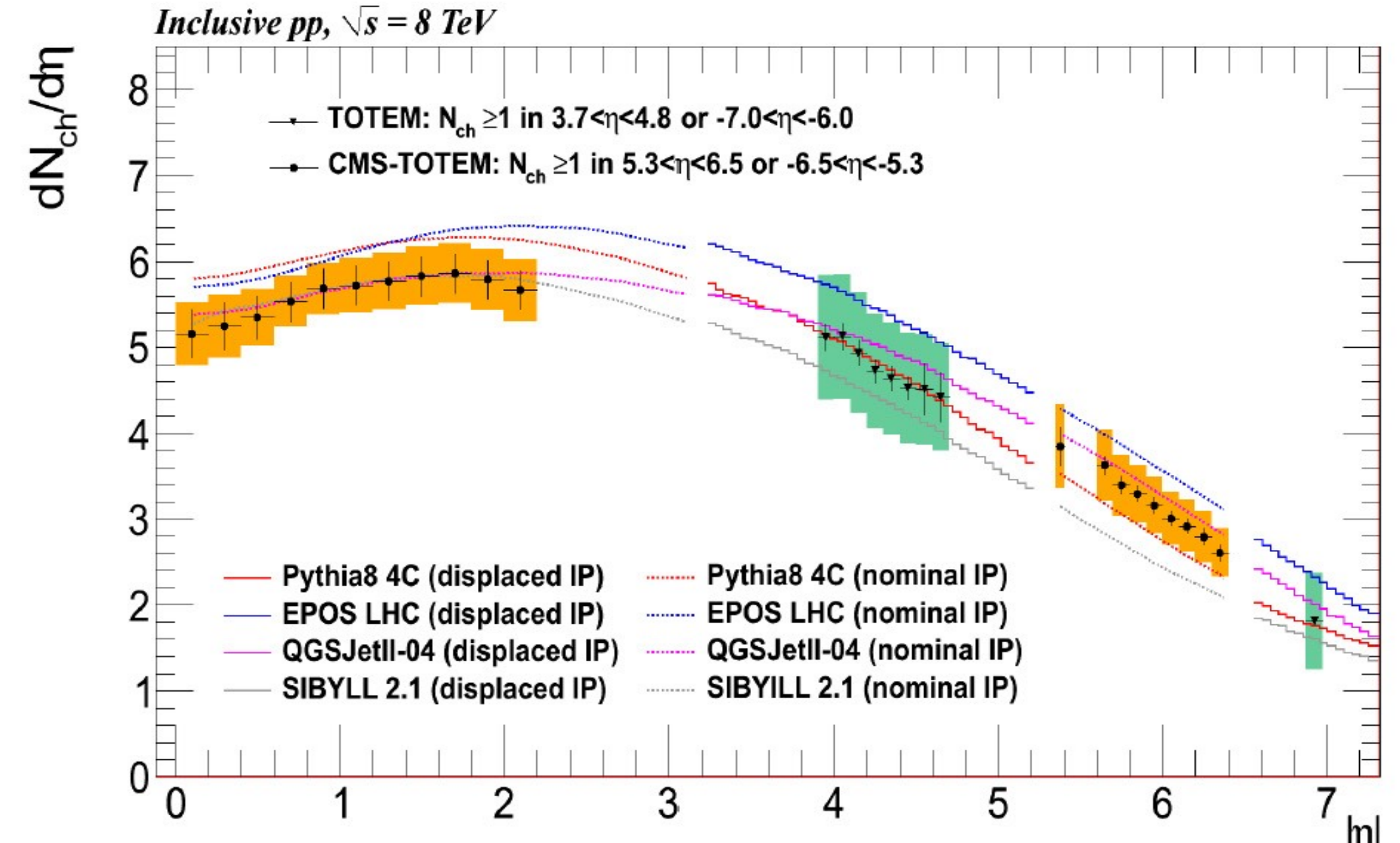
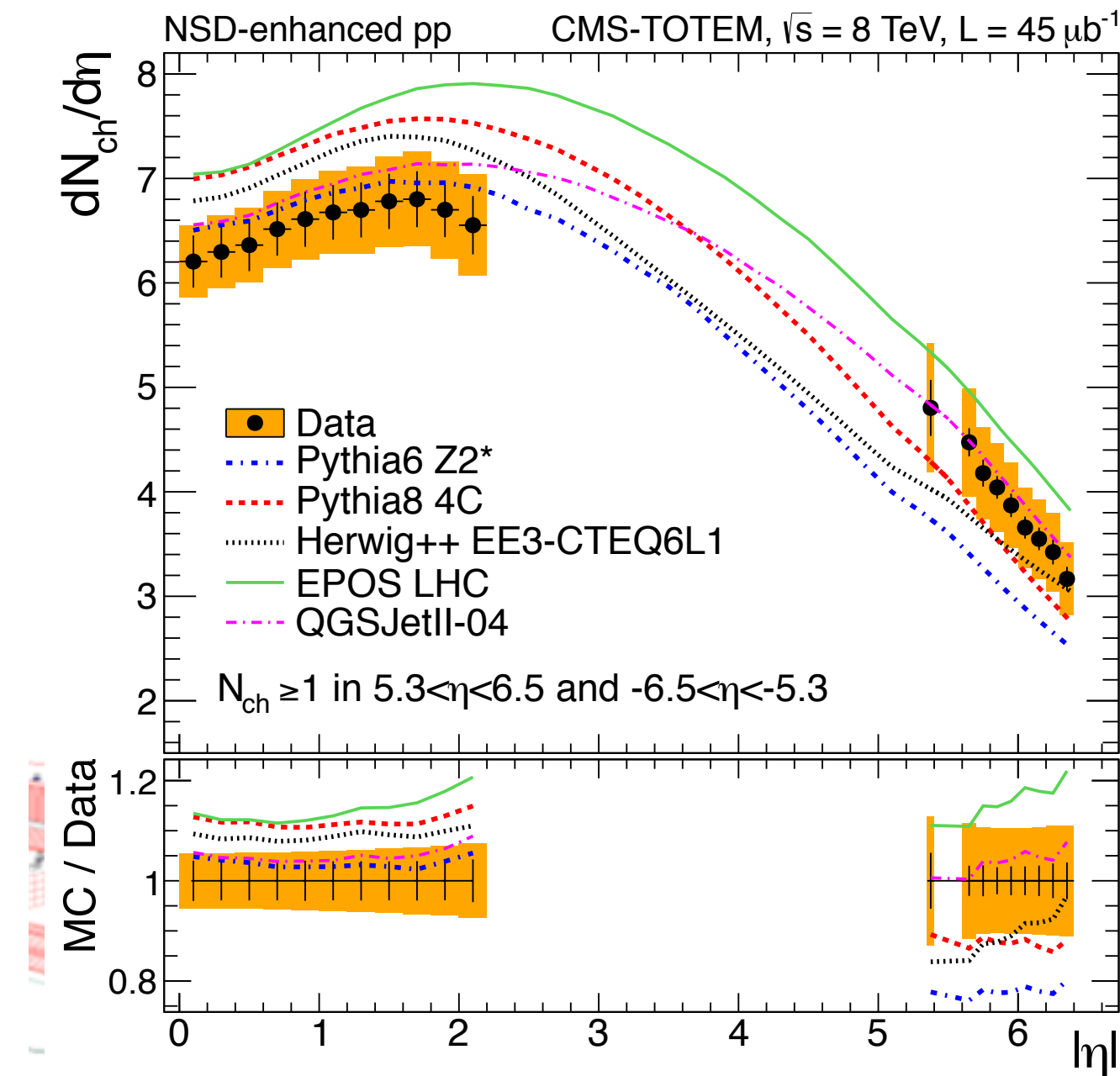
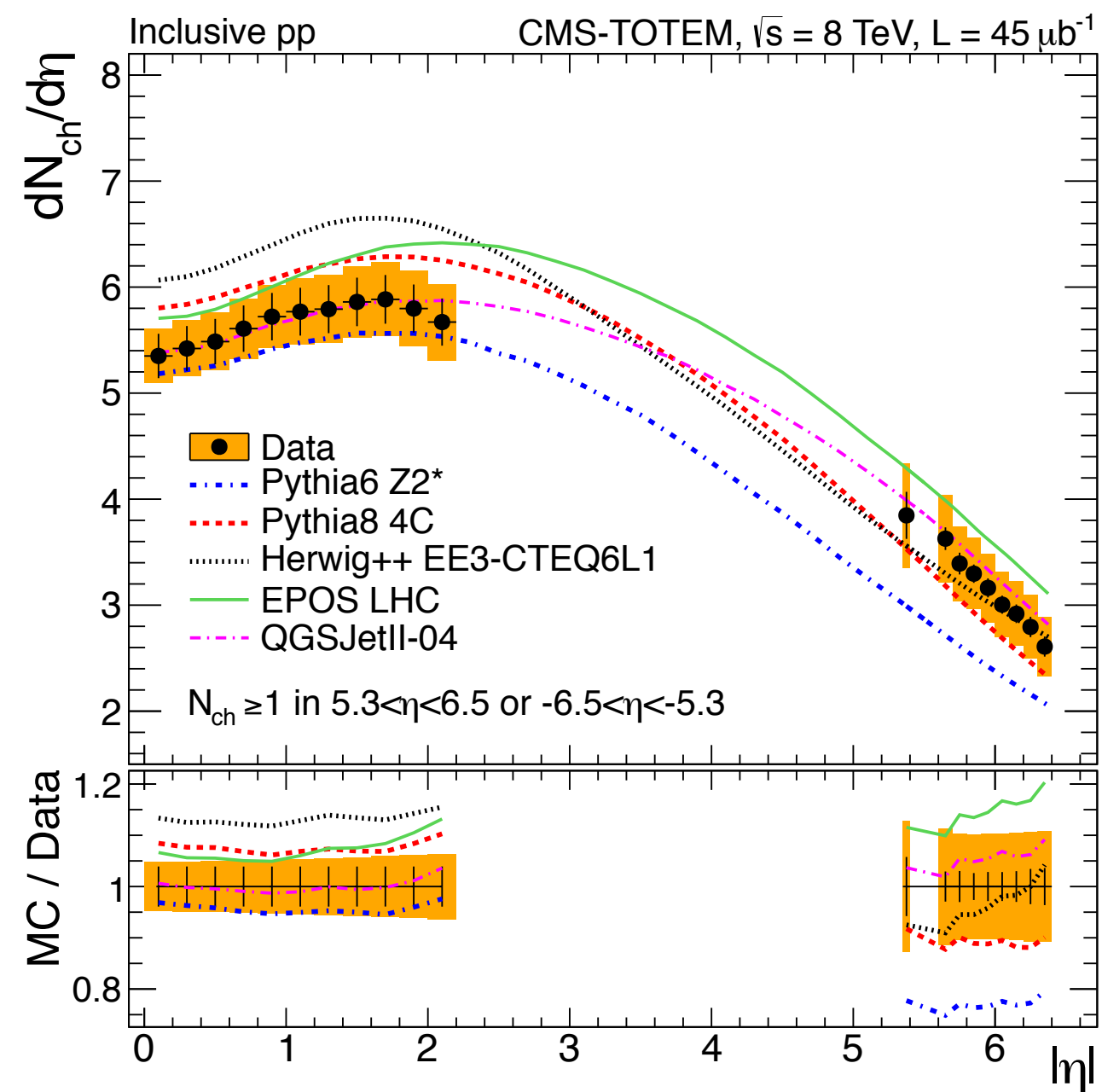


$$pp \rightarrow \gamma X$$

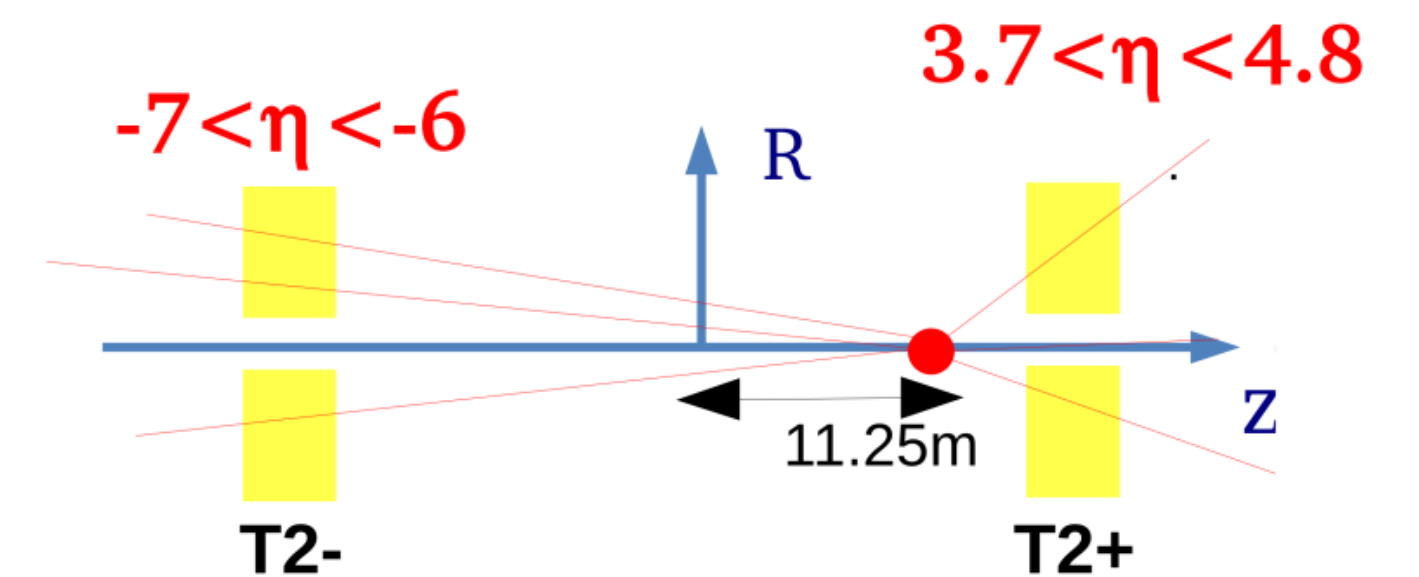
(LHCf Collab., Phys. Lett. B 703, 2011)



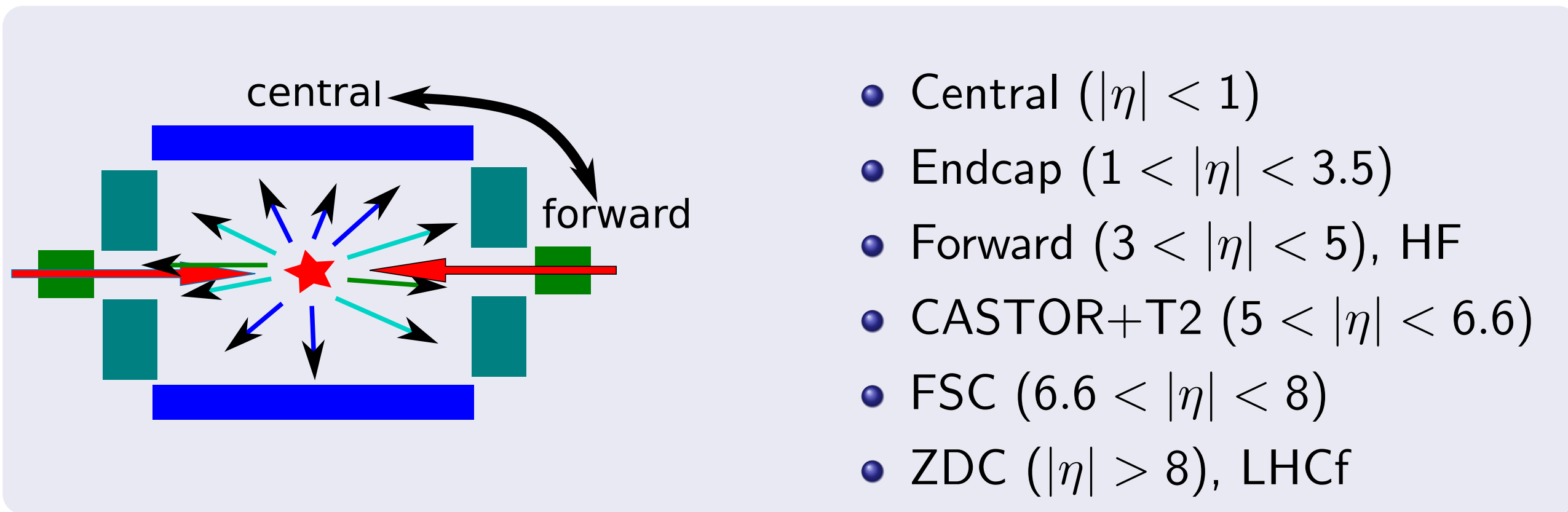
Combined CMS and TOTEM measurements



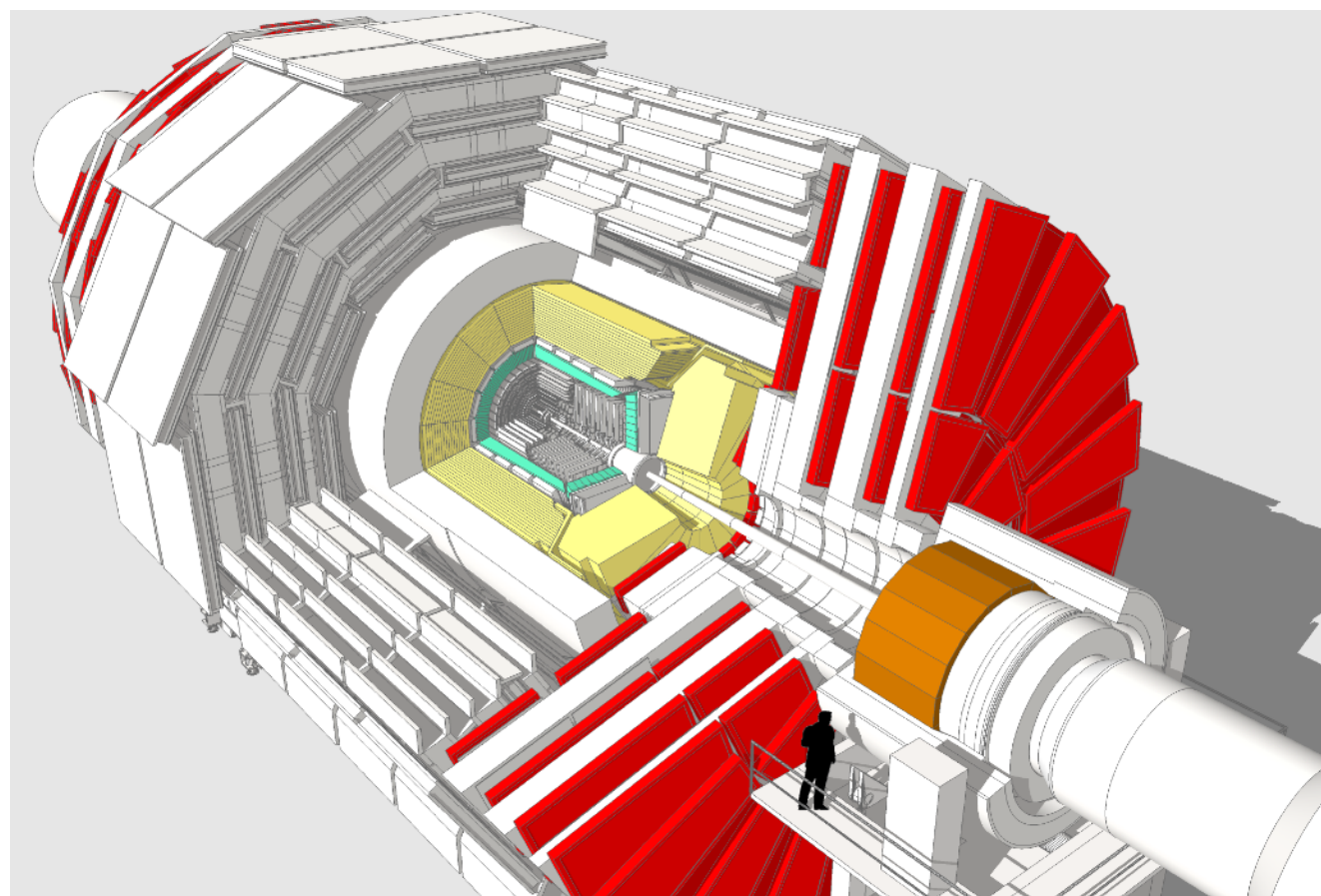
Shifted vertex



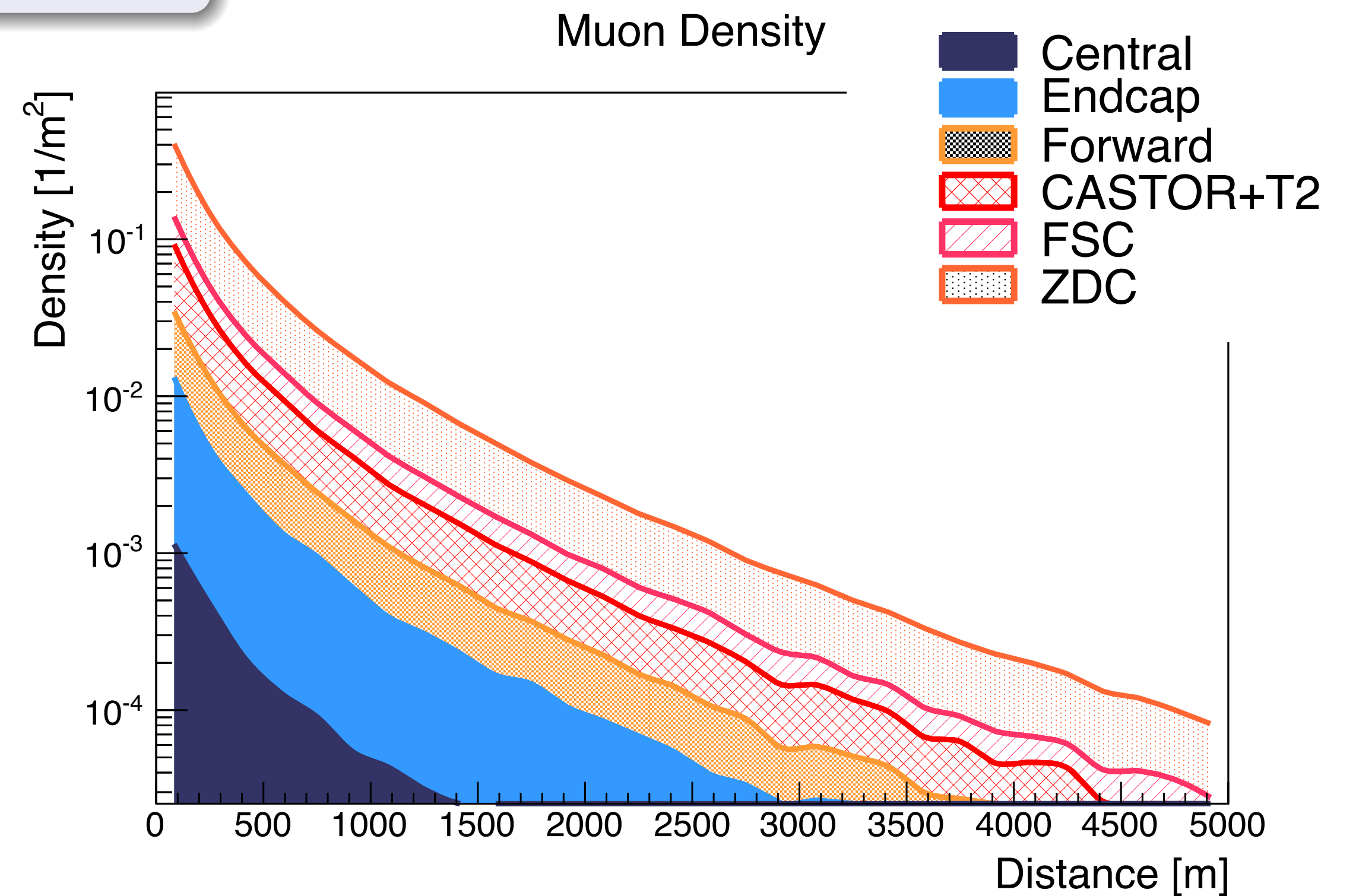
Challenge of limited phase space coverage



(Ulrich, DPG 2014)



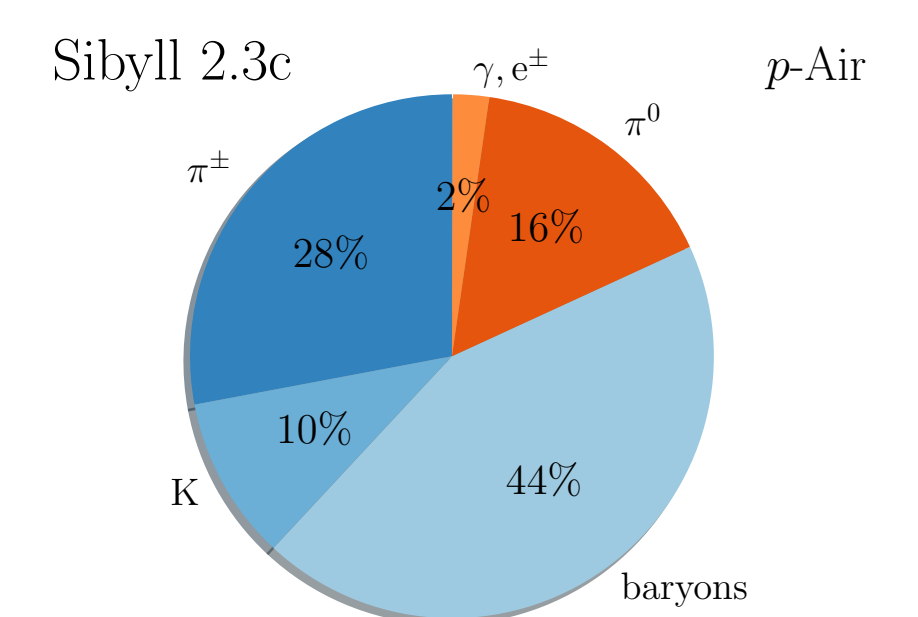
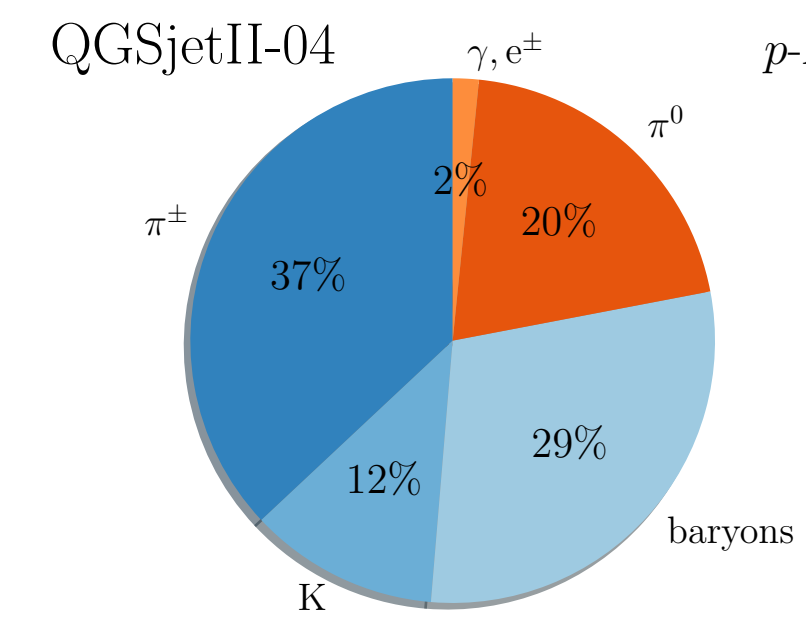
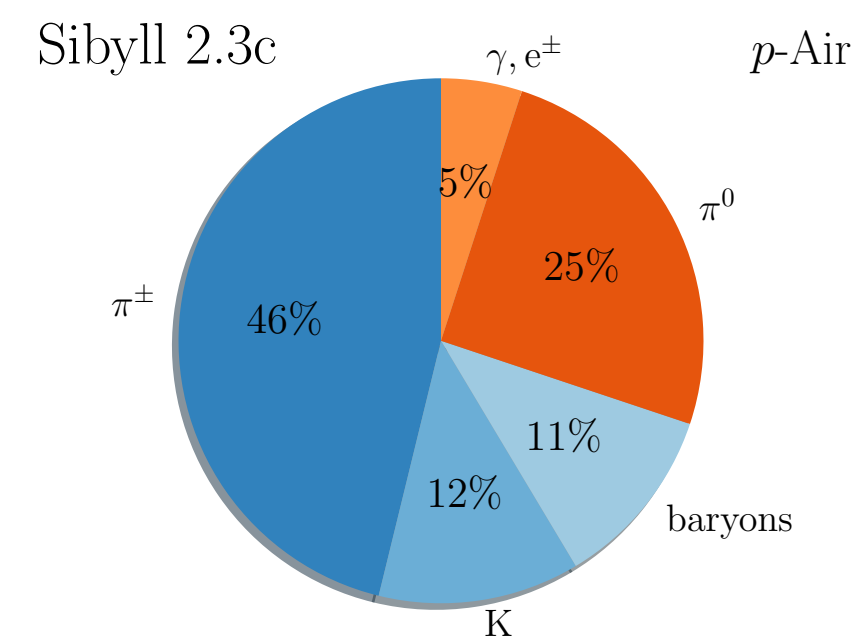
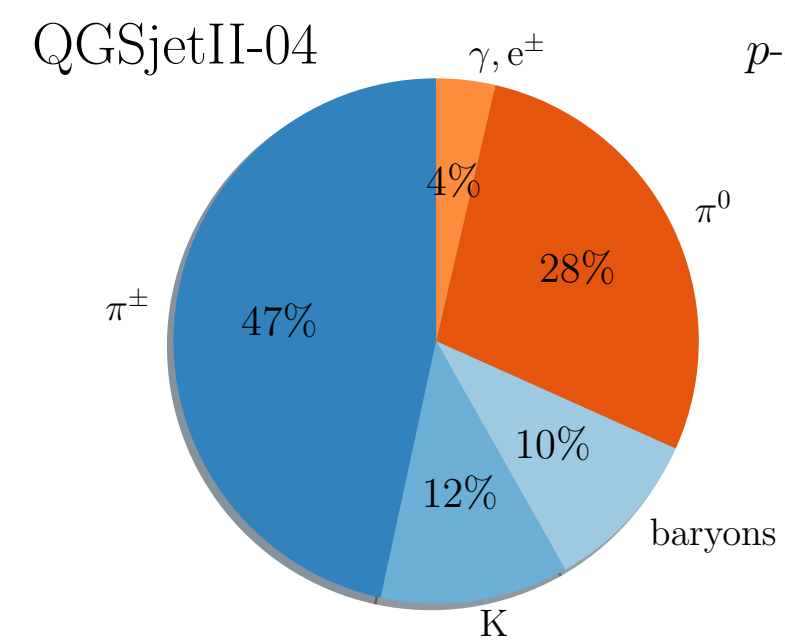
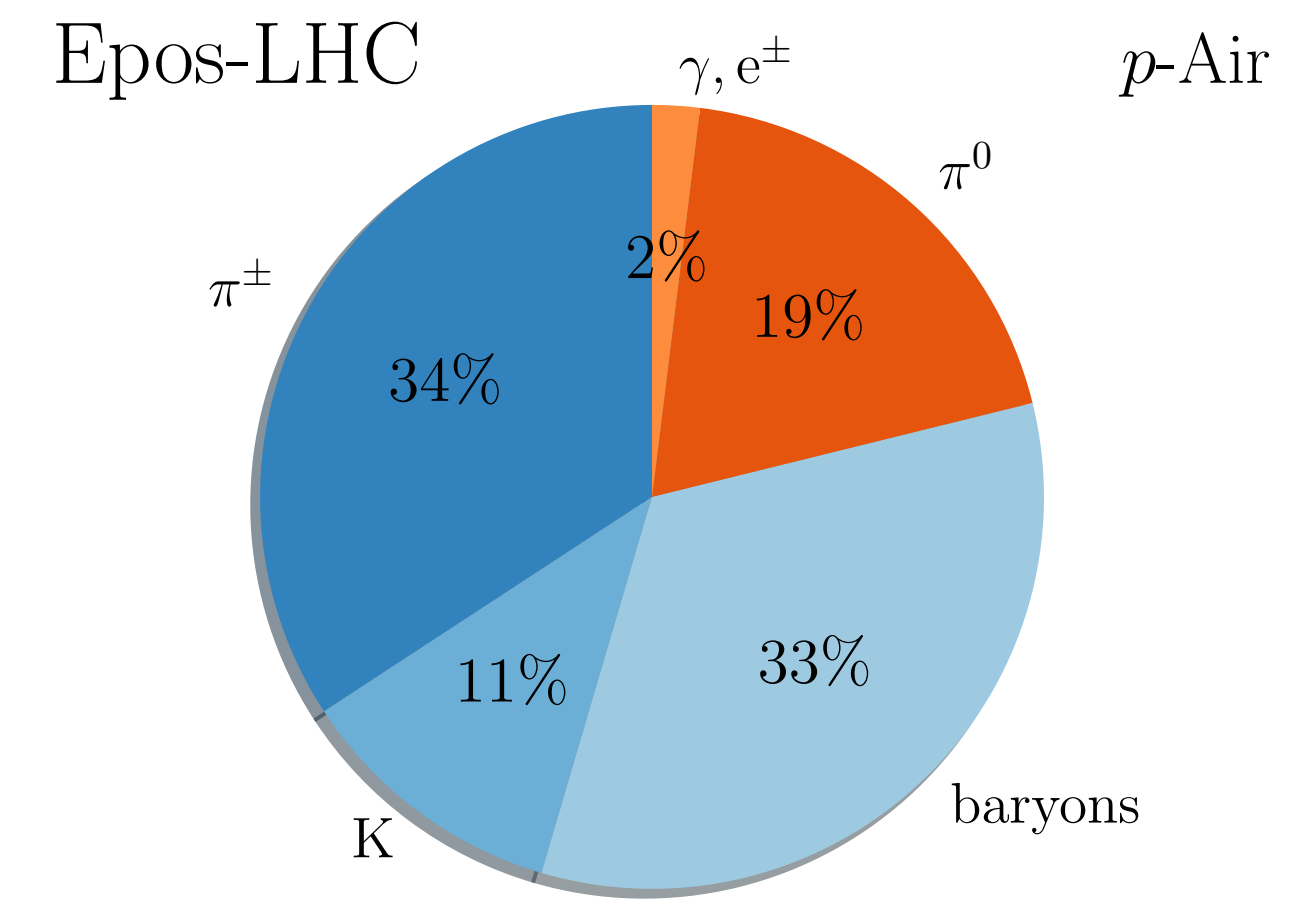
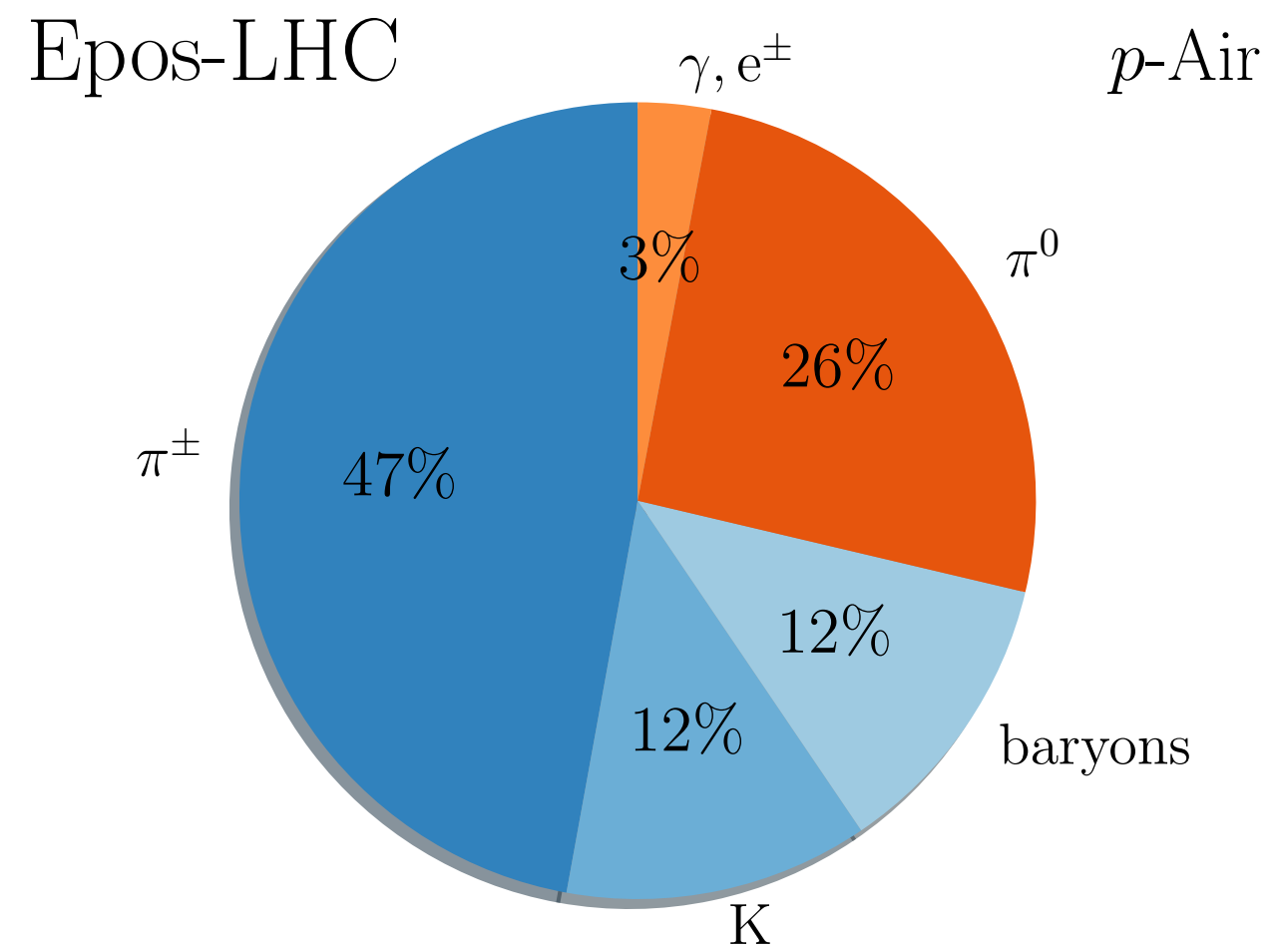
(data from all LHC experiments, CMS shown as example)



Model predictions for secondary particles: p-air

Particle multiplicity (10^{19} eV)

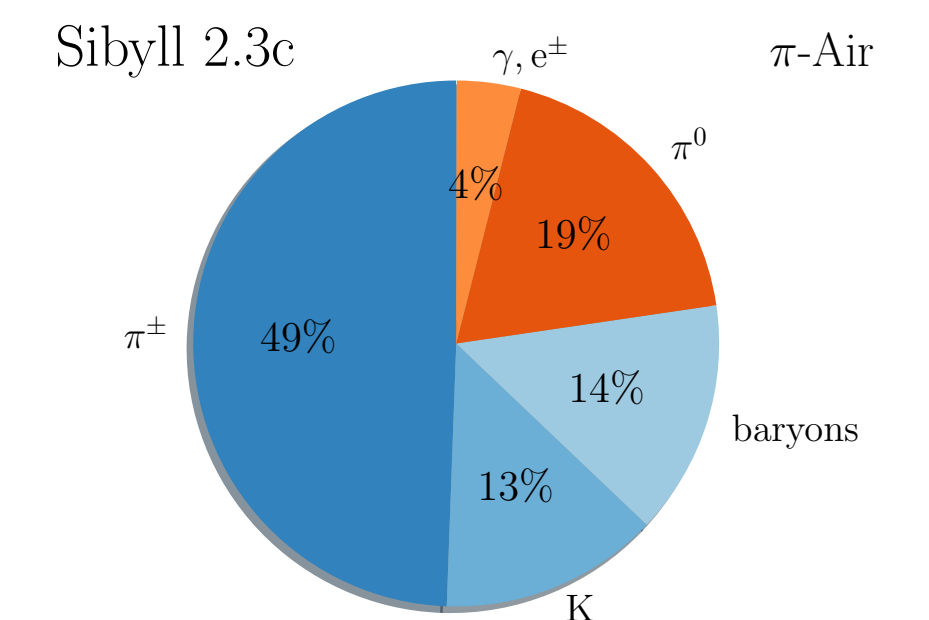
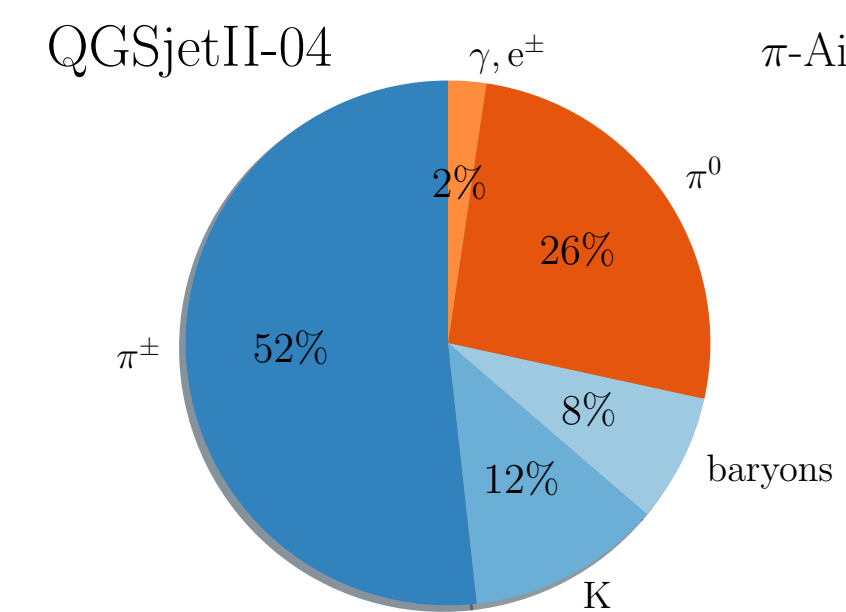
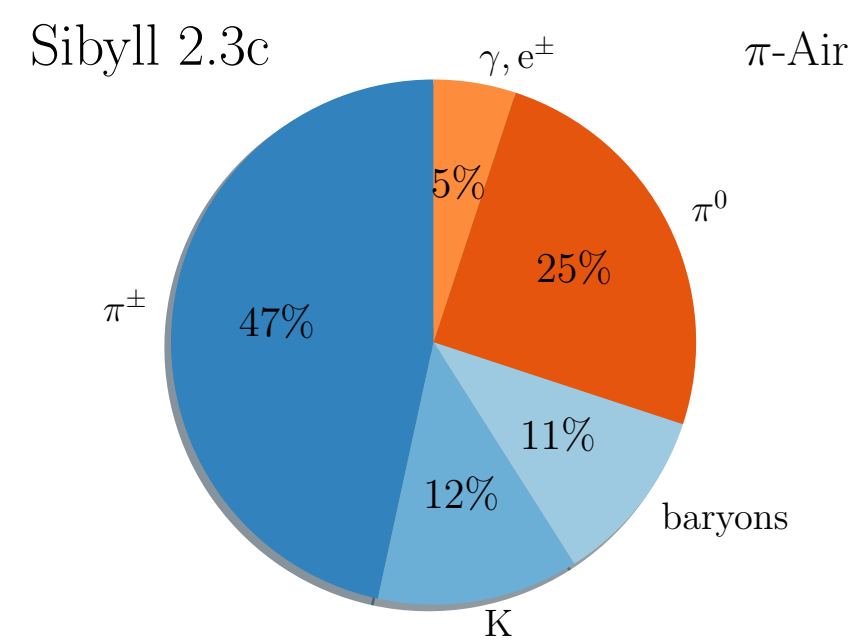
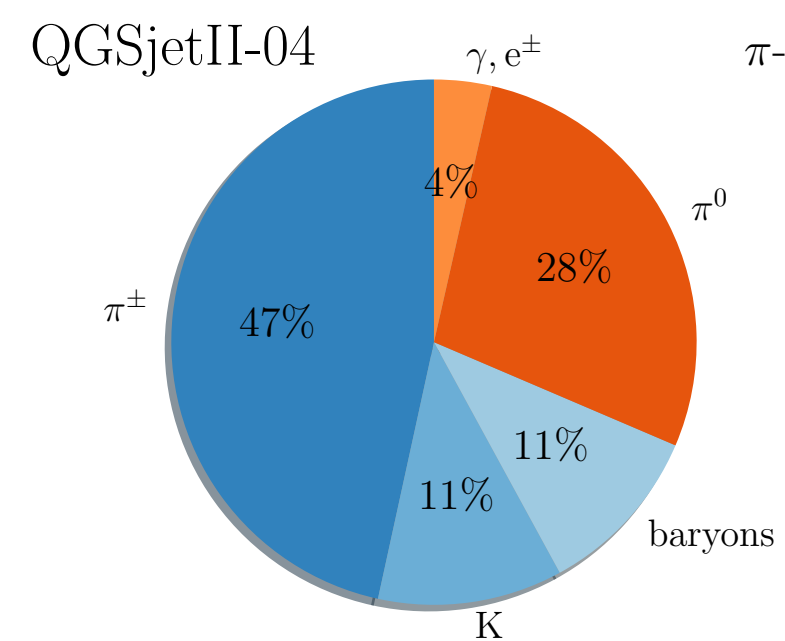
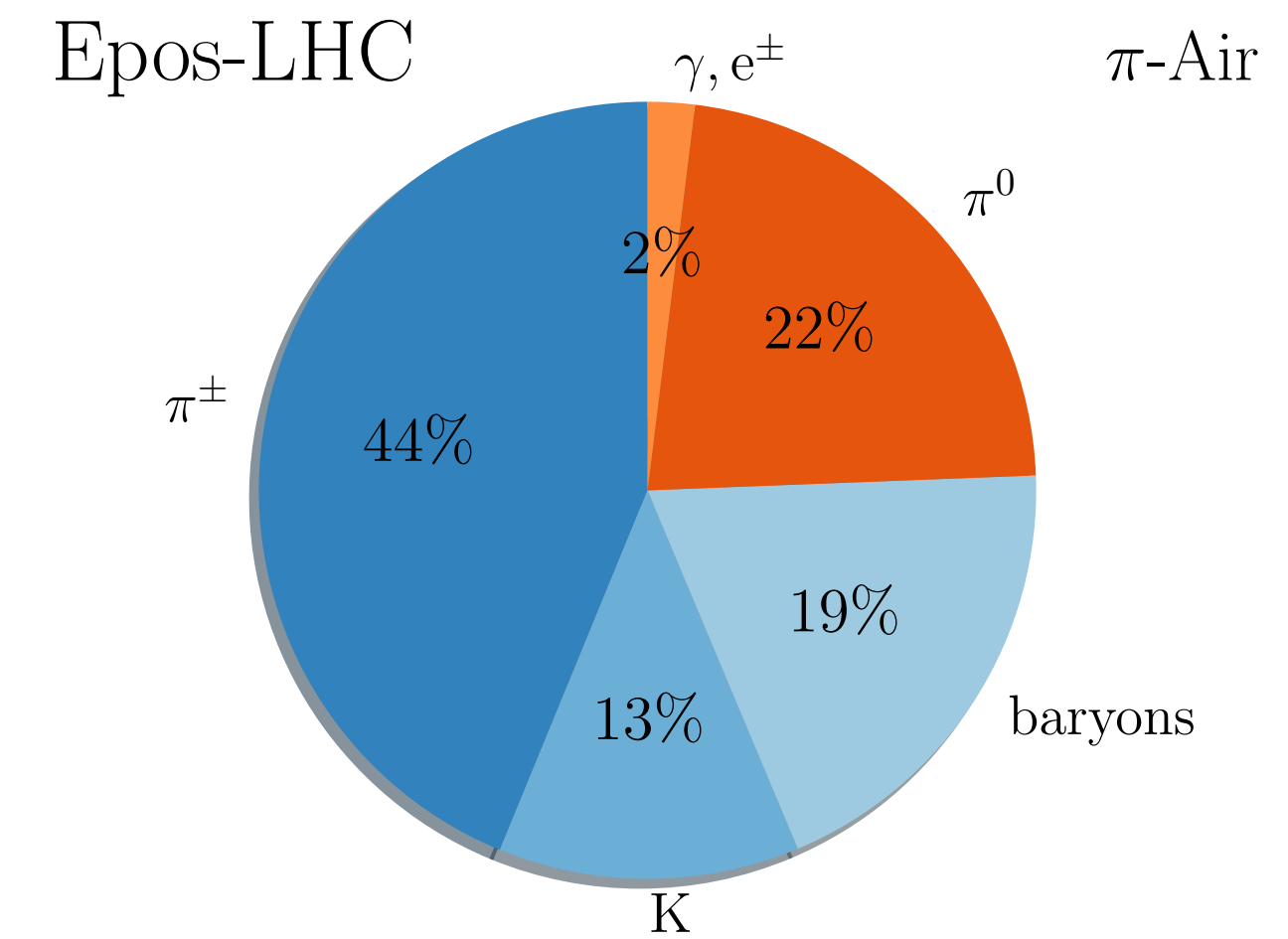
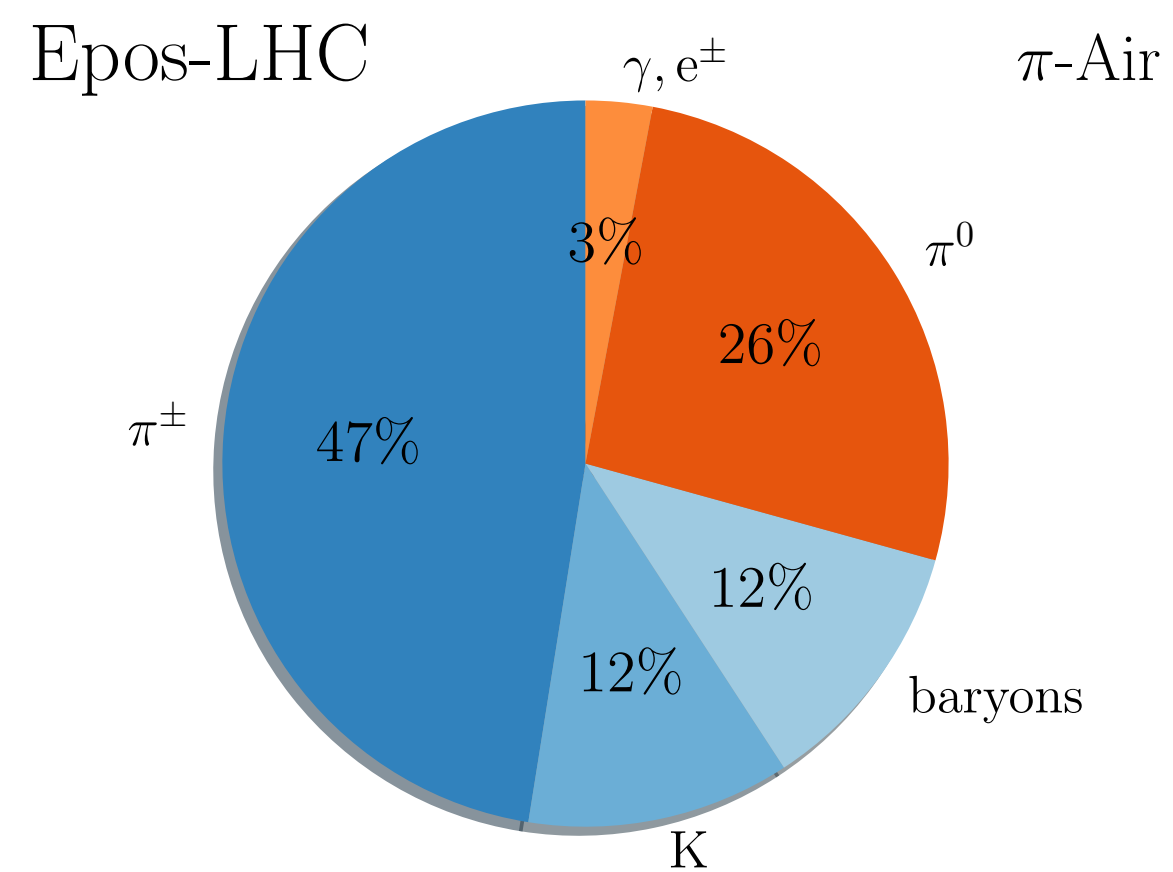
Particle energy fraction (10^{19} eV)



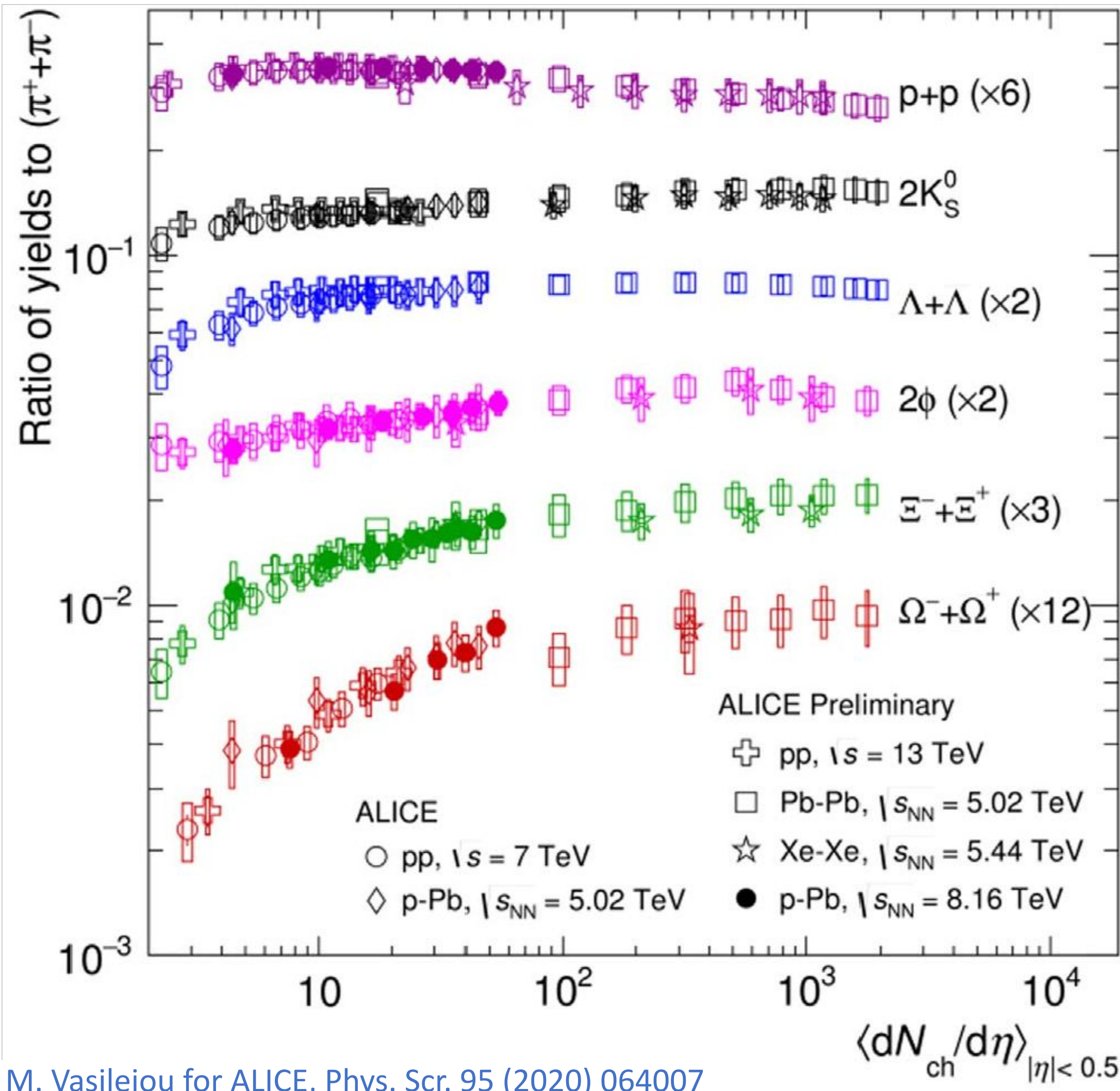
Model predictions for secondary particles: π -air

Particle multiplicity (10^{19} eV)

Particle energy fraction (10^{19} eV)

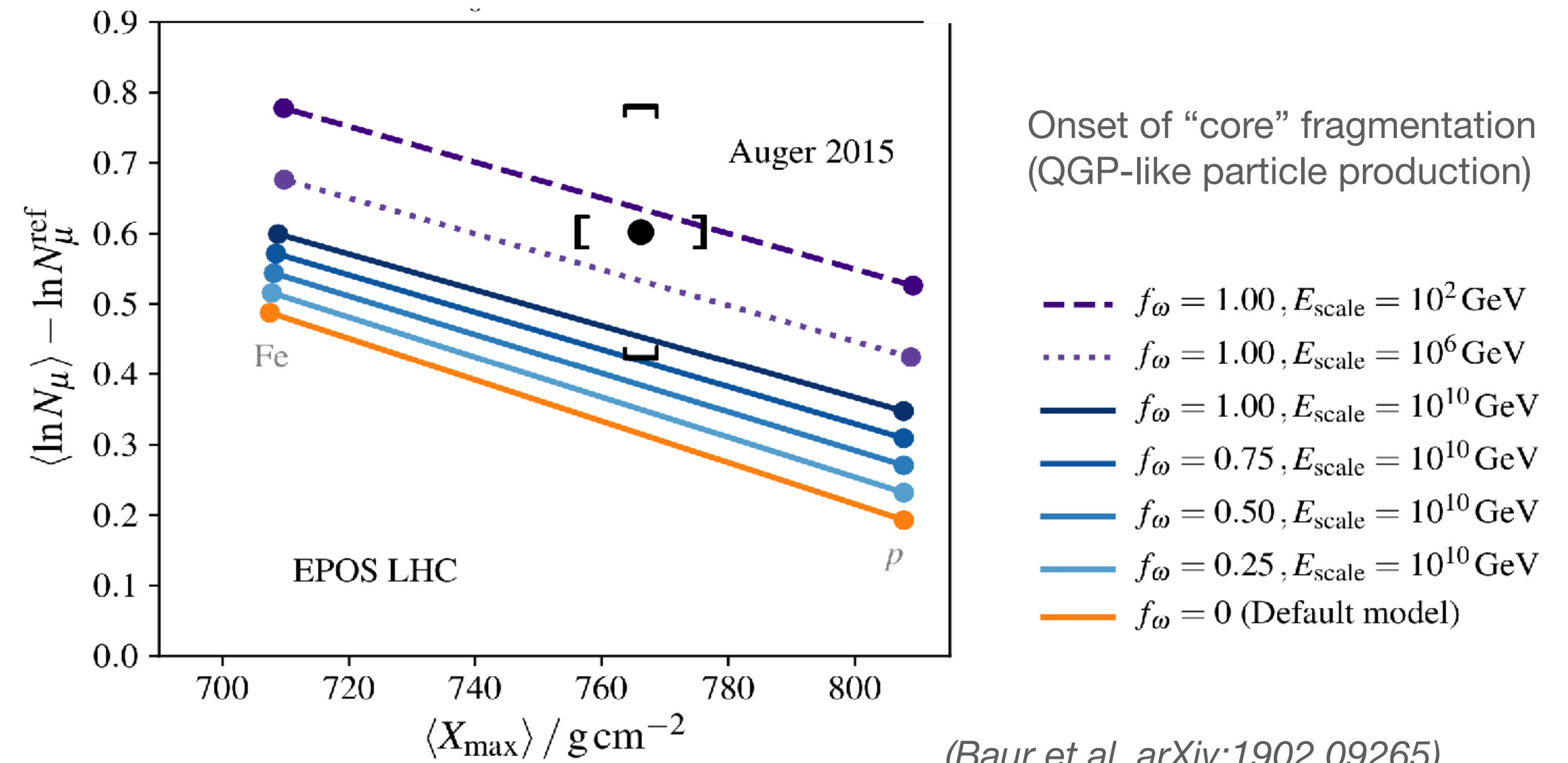


Universal particle scaling and core-corona model in EPOS

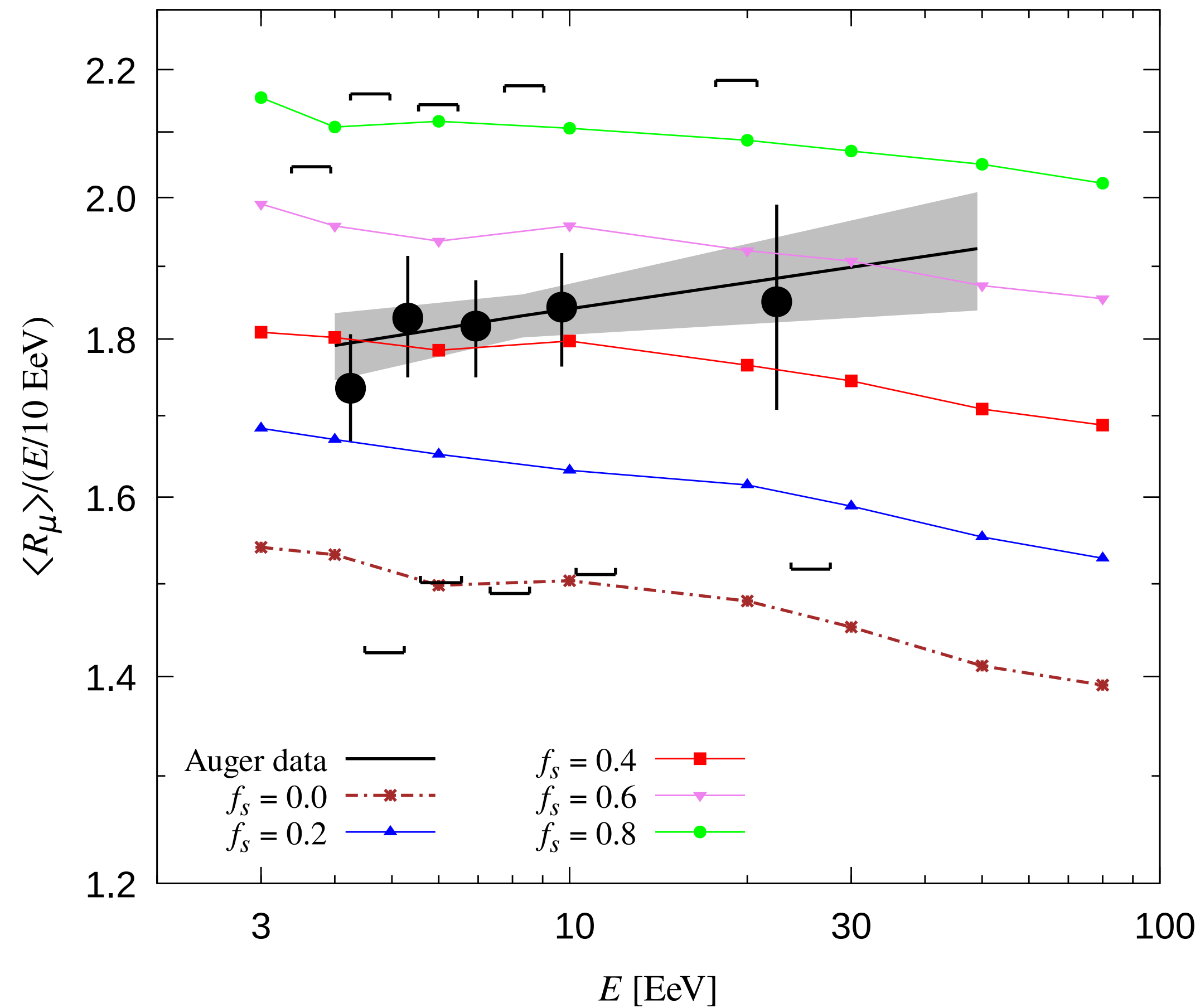


ALICE: observation of **universal scaling of enhancement of heavy particles** with particle multiplicity or density (*Nature Phys.* 13 (217) 535)

Does the same/similar scaling apply also in forward direction?



Phenomenological kaon enhancement model



Probability f_s to change particles

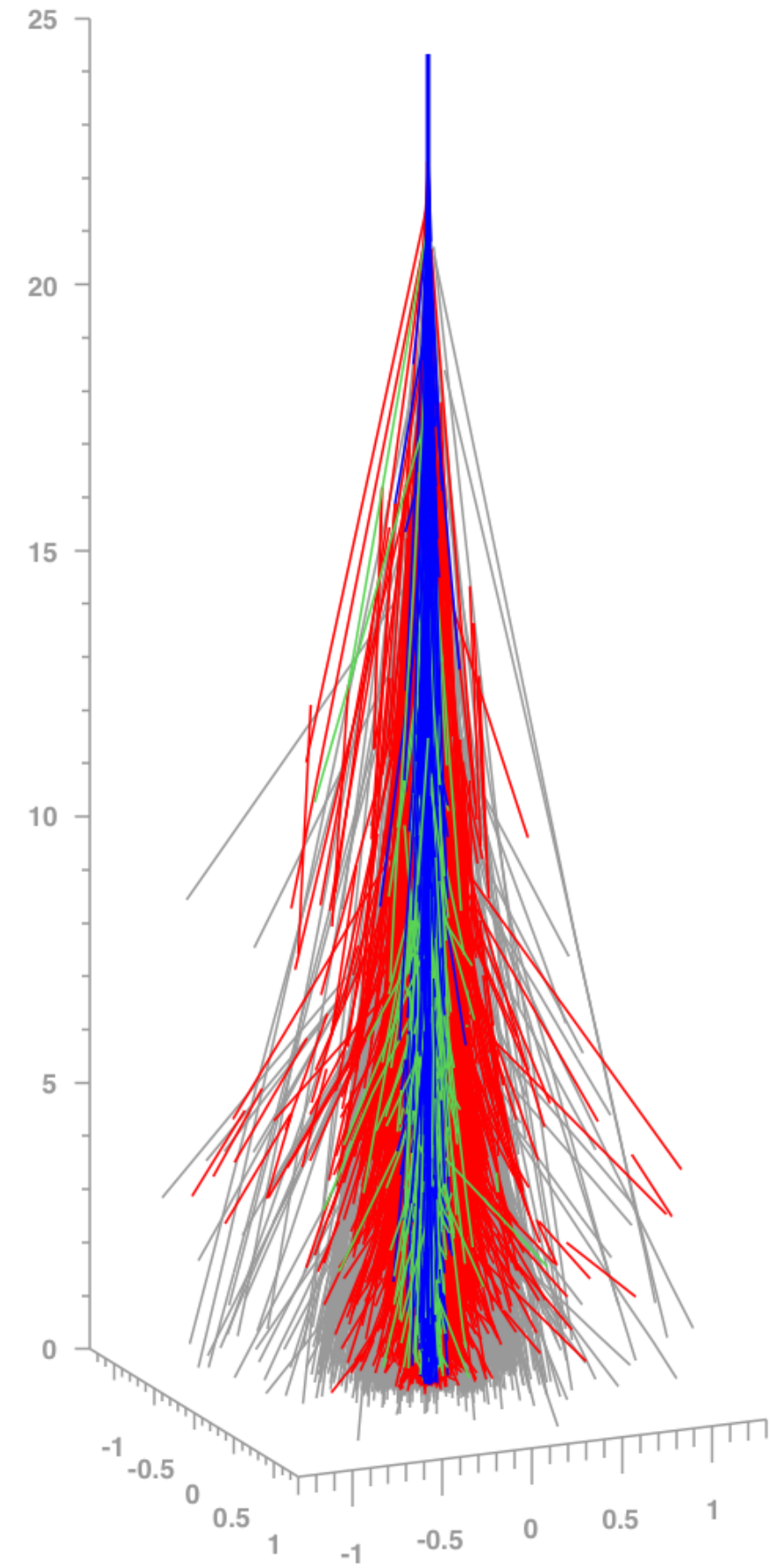
$$\pi^0 \longrightarrow K_S^0 / K_L^0$$

$$\pi^\pm \longrightarrow K^\pm$$

TABLE II: Global counters for the refined model with $f_s = 0.7$, in the case of 10^{19} eV proton showers inclined 67° .

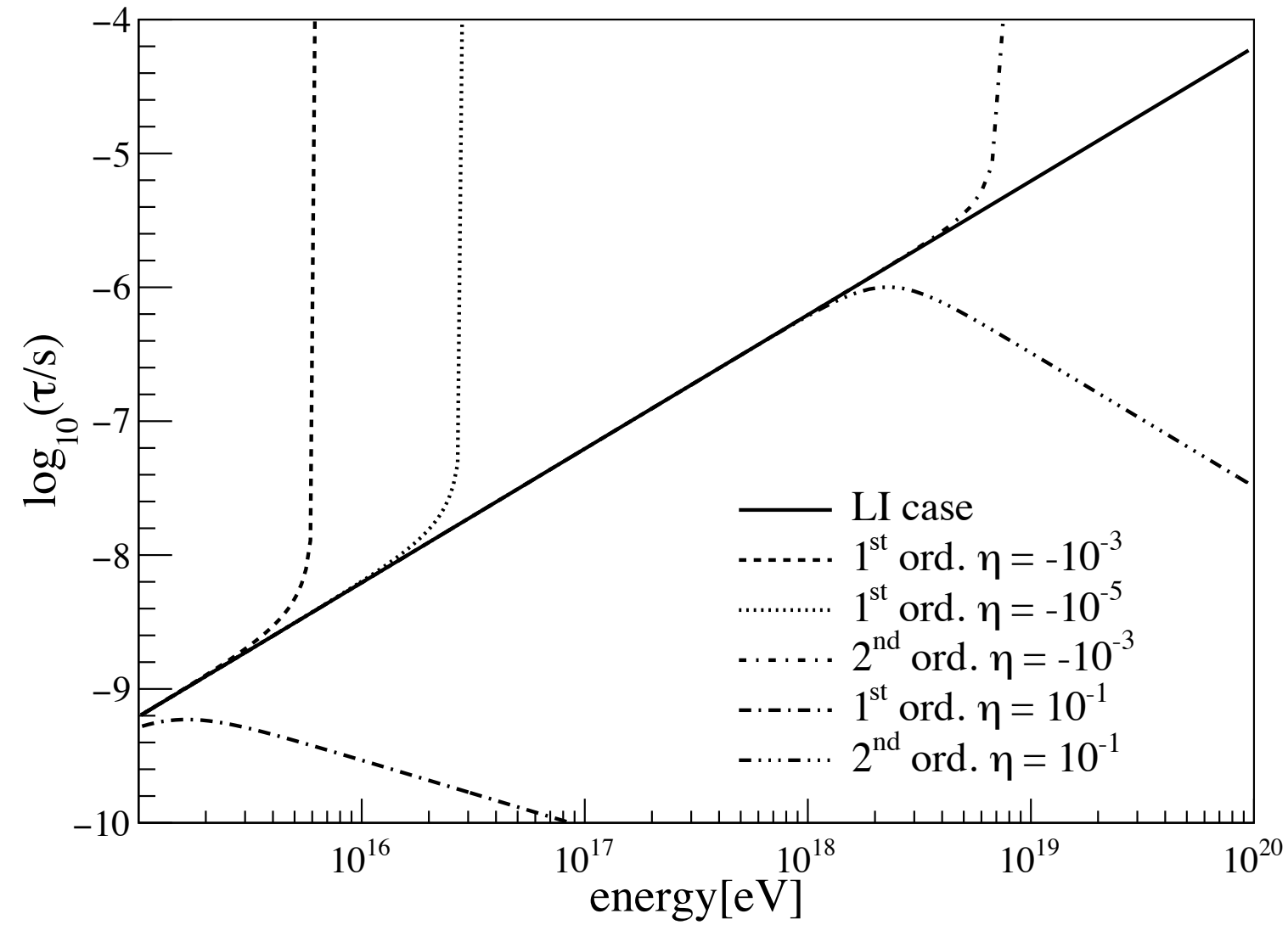
Total hadronic collisions per shower	264,600	100.00 %
Collisions with $E_{\text{proj}} < E_{\text{pmin}}$	262,070	99.04 %
Collisions with $E_{\text{proj}} > E_{\text{pmin}}$	2,530	0.96 %
Total number of secs. produced	6,806,244	100.00 %
Secs. from colls. with $E_{\text{proj}} < E_{\text{pmin}}$	6,544,194	96.15 %
Secs. from colls. with $E_{\text{proj}} > E_{\text{pmin}}$	262,050	3.85 %
Total number of pions scanned	134,060	1.97 %
Pions considered for swapping:		
Central ($ \eta_{\text{CM}} < 4$)	99,790	1.47 %
Peripheral ($ \eta_{\text{CM}} > 4$)	34,270	0.50 %
Total (central + peripheral)	134,060	1.97 %
Pions actually swapped	23,988	0.35 %

Lorentz invariance violation (LIV) and muon production



(Auger, ICRC 2021)

Lorentz-dilated lifetime of neutral pions

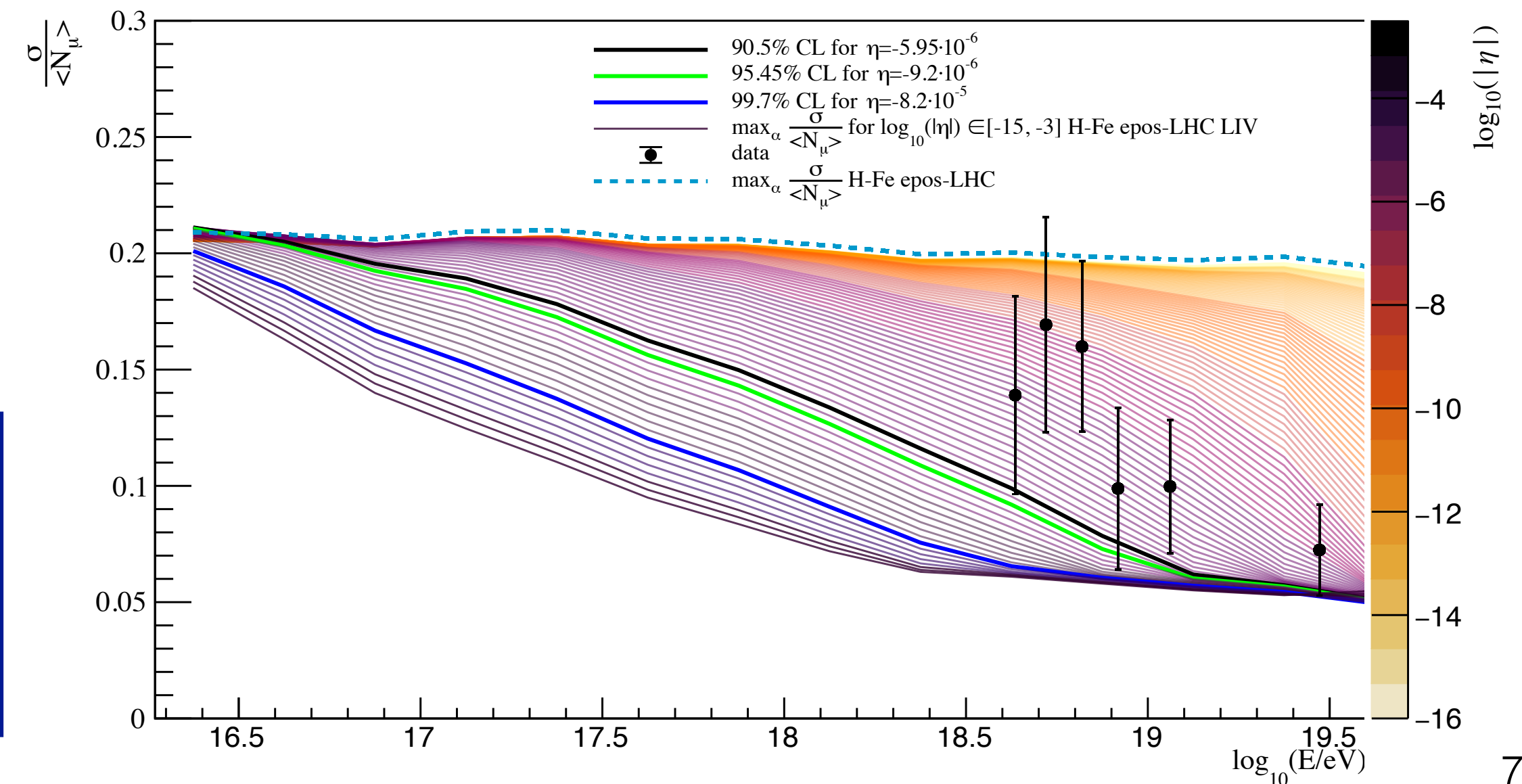


Comparison of model simulations with data on muon number fluctuations
 Muon enhancement, limits on LIV

$$E^2 - p^2 = m^2 + \eta^{(n)} \frac{p^{n+2}}{M_{\text{Pl}}^n}$$

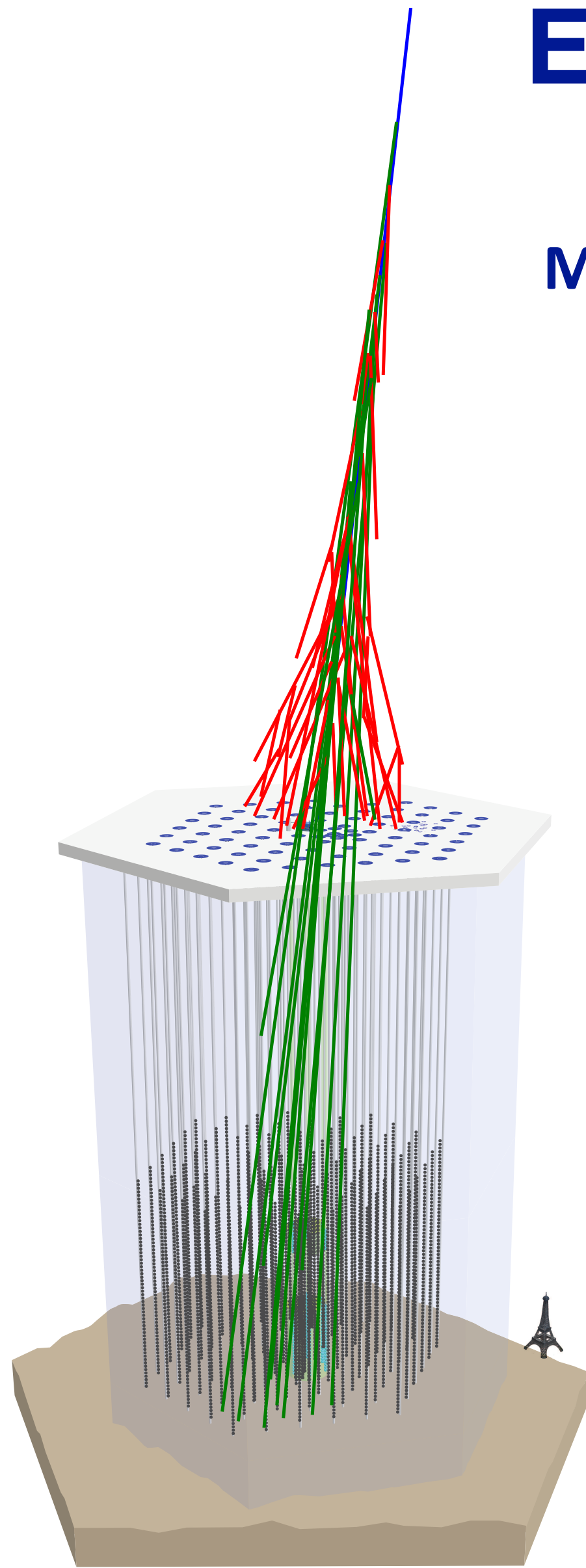
$$\gamma_{\text{LIV}} = E / m_{\text{LIV}}$$

$$m_{\text{LIV}}^2 = m^2 + \eta^{(n)} \frac{p^{n+2}}{M_{\text{Pl}}^n}$$



Energy spectrum of muons in air showers

Muon energy spectrum in EAS relative to that of Sibyll 2.1

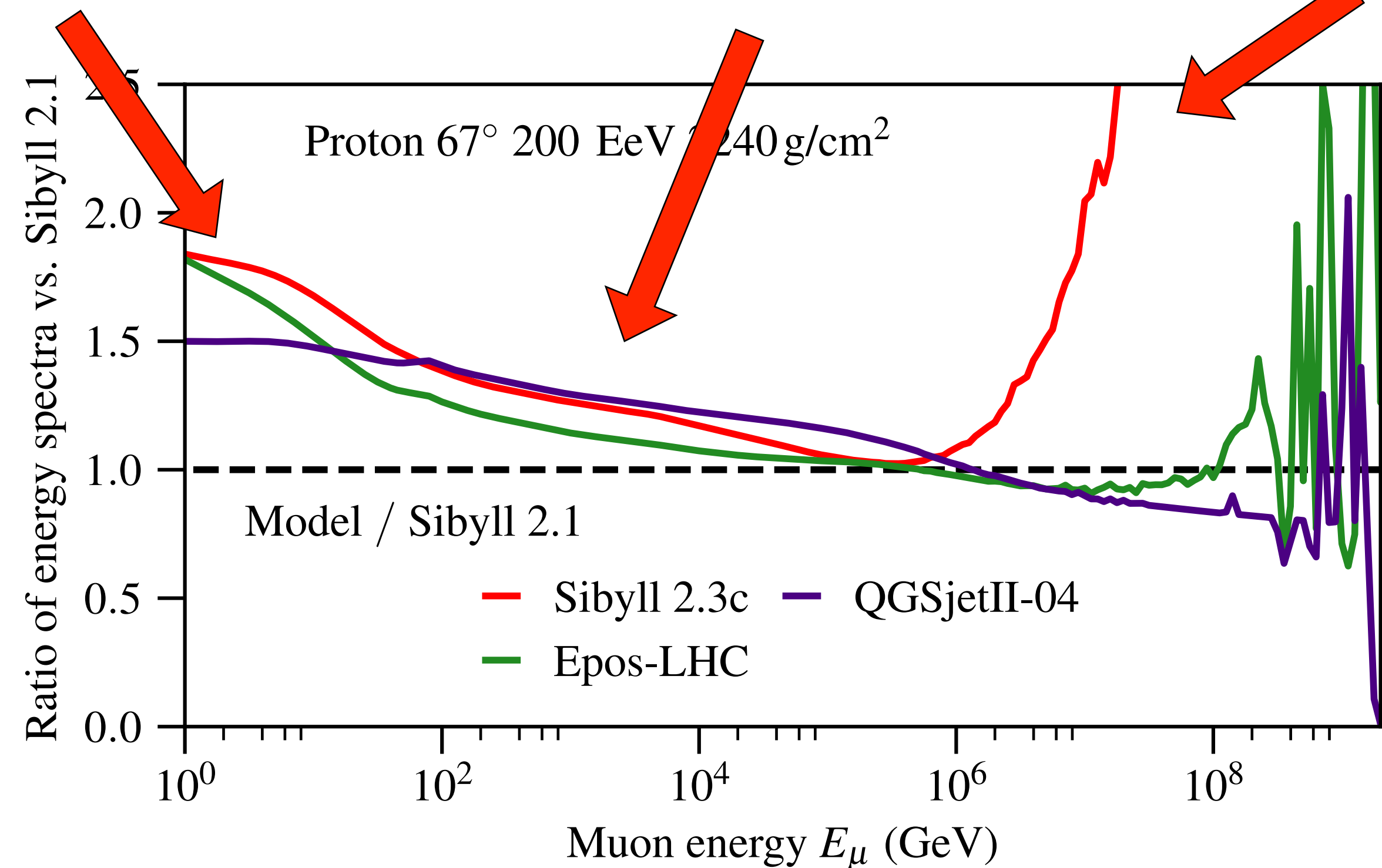


Correlation of low energy muons (surface $\sim 1\text{ GeV}$) and in-ice ($\sim 500\text{ GeV}$) muon bundles

Low-energy enhancement due to baryon pair production

Rho-0 production

Charm particles (only Sibyll 2.3, and Sibyll 2.3c)



Discrimination by IceCube possible (surface array and in-ice muon data)

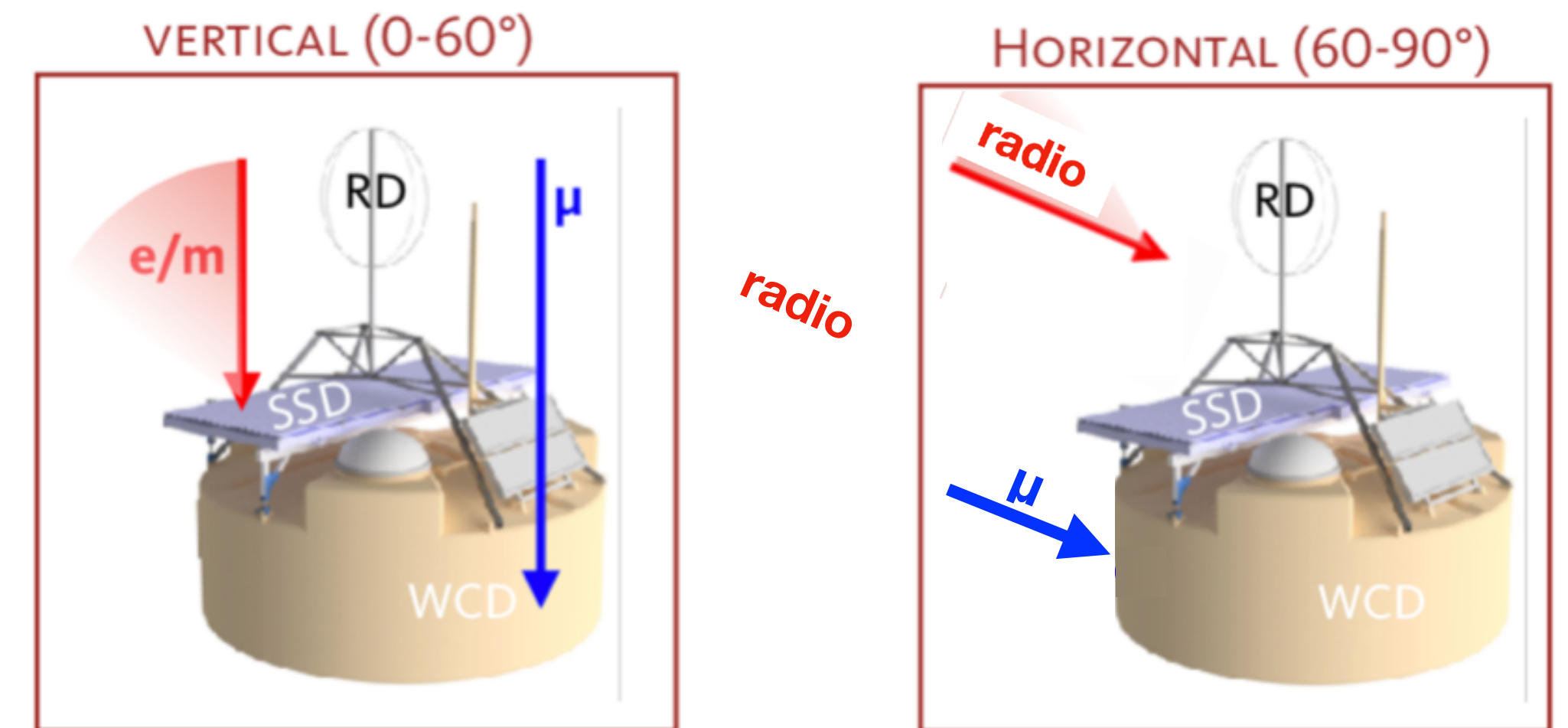
Backup slides

Upgrade of the Observatory – AugerPrime

Physics motivation

- Composition measurement up to 10^{20} eV
- Composition selected anisotropy
- Particle physics with air showers
- Much better understanding of **new and old** data

Composition sensitivity with 100% duty cycle

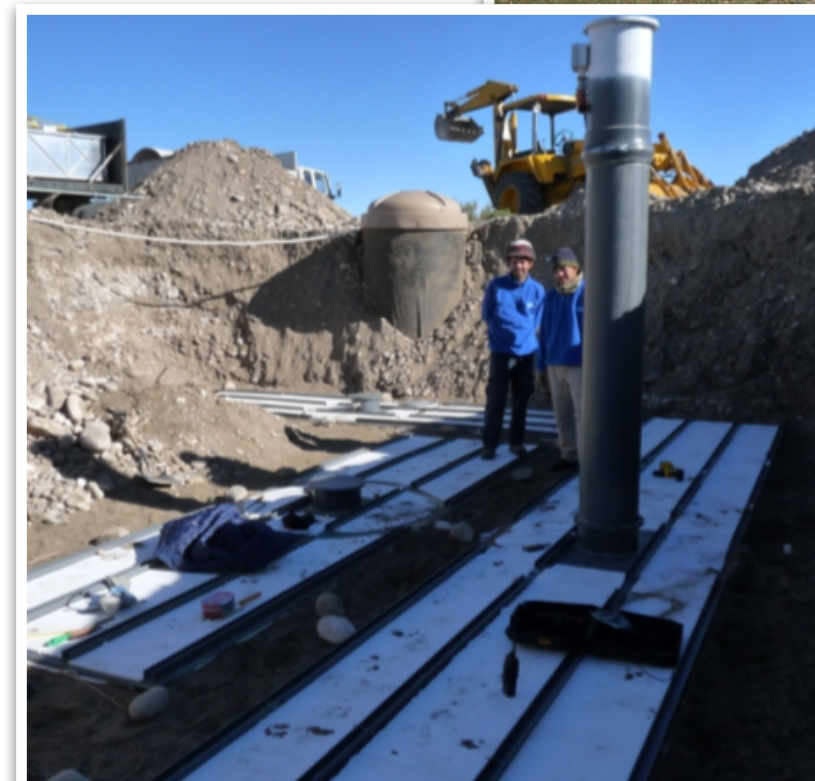
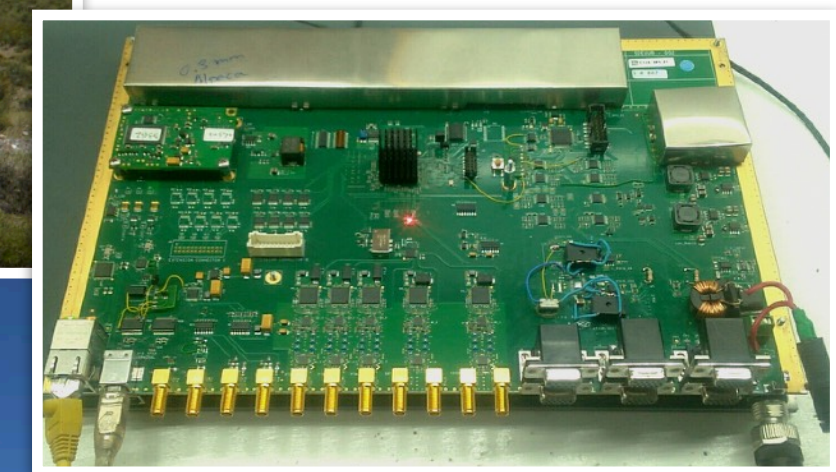


Components of AugerPrime

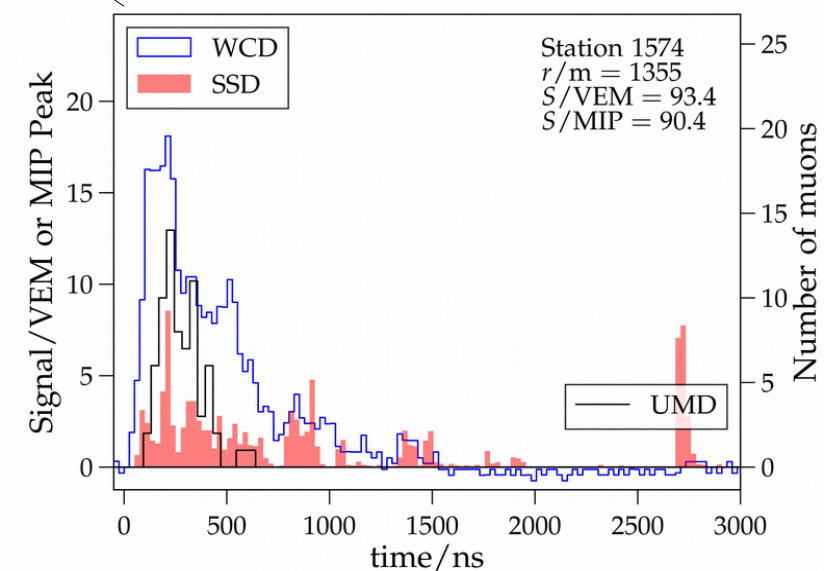
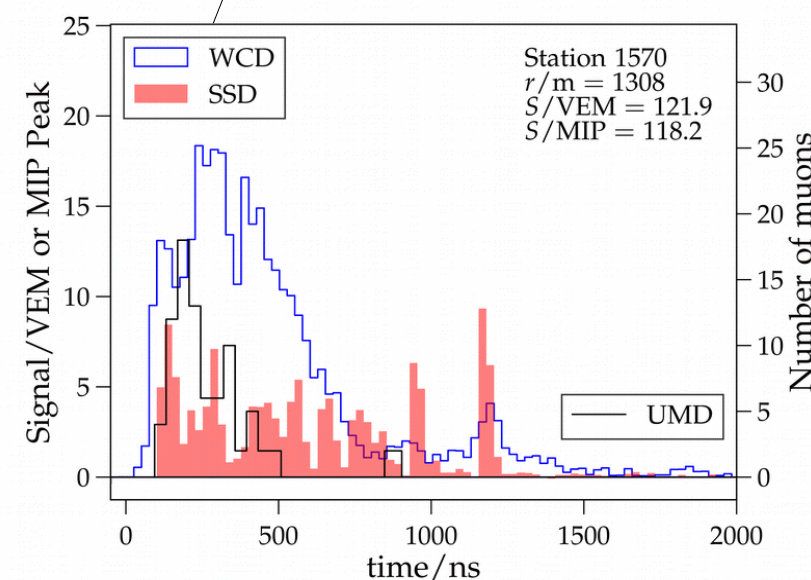
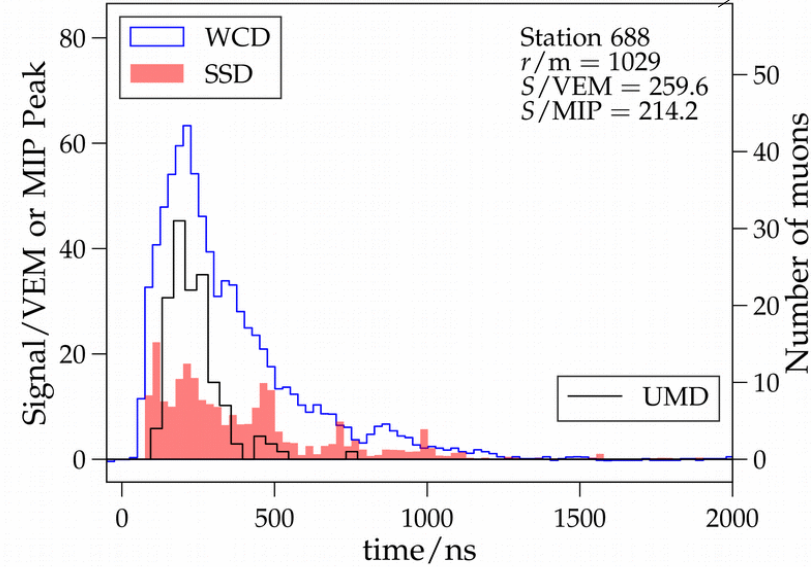
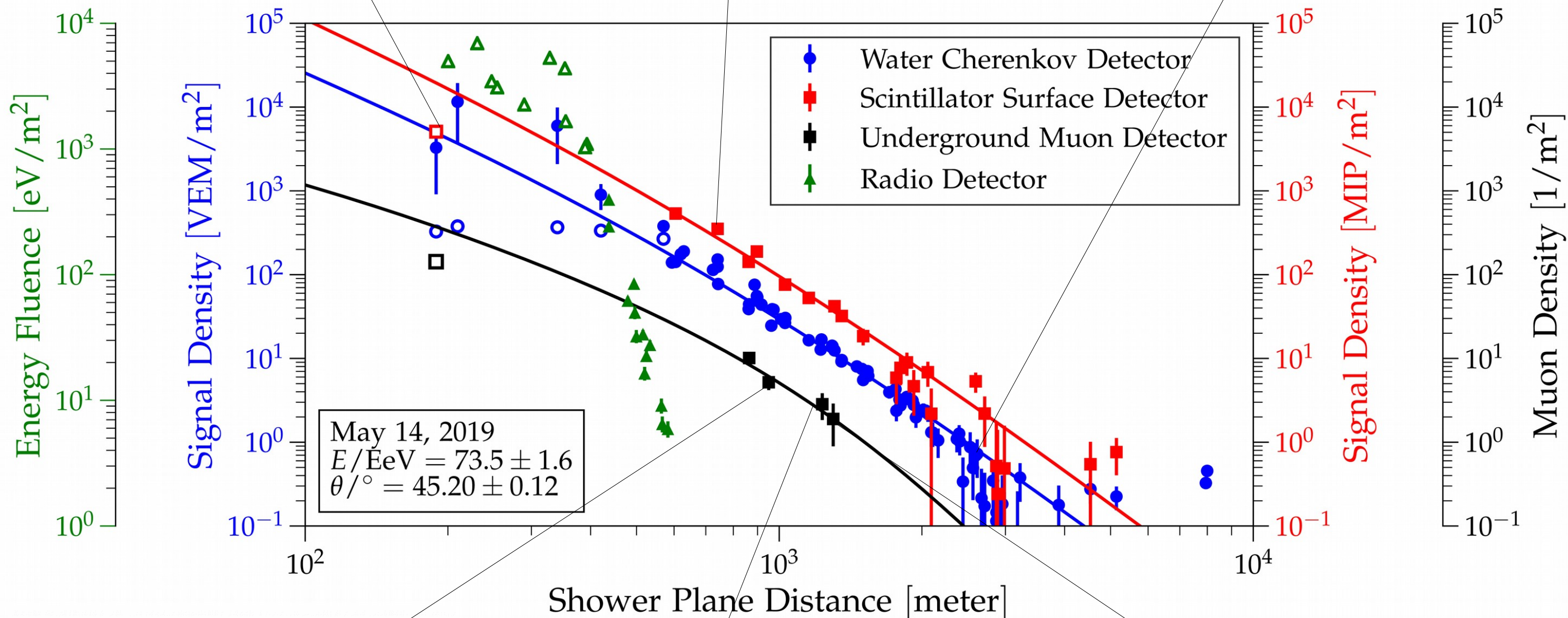
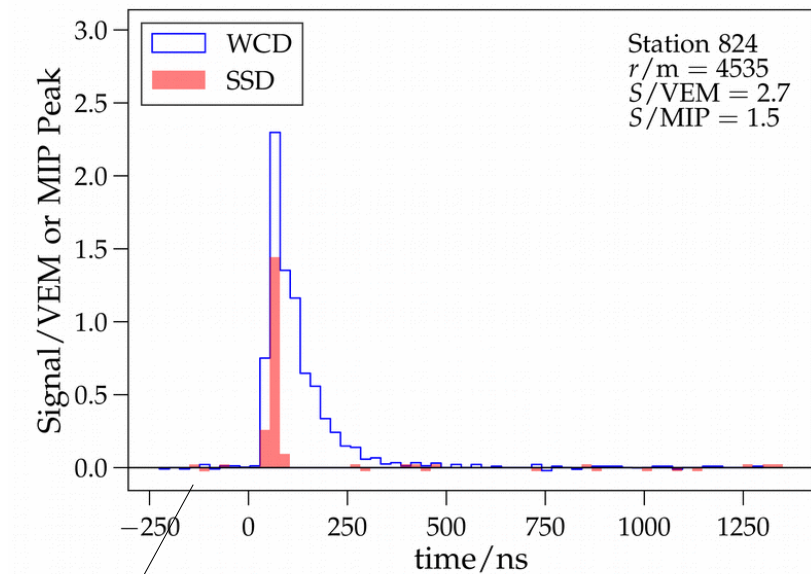
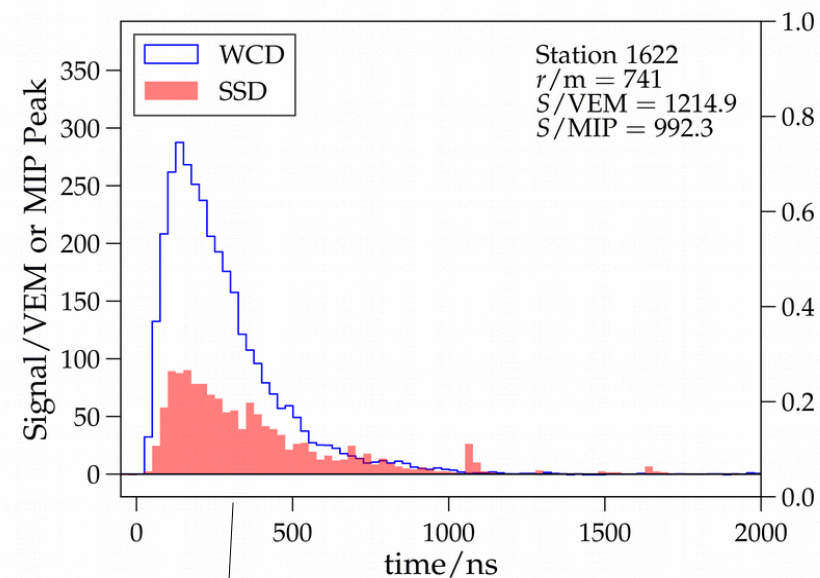
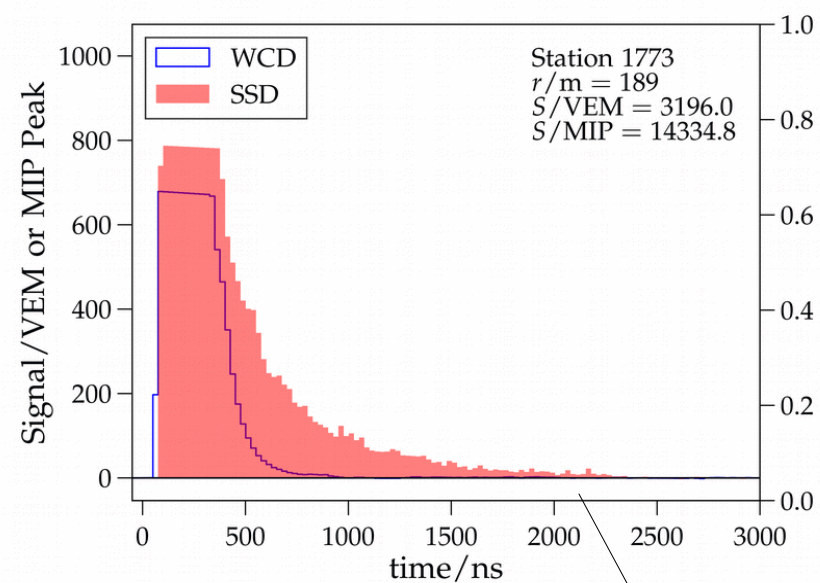
- 3.8 m² scintillator panels (SSD)
- New electronics (40 MHz -> 120 MHz)
- Small PMT (dynamic range WCD)
- Radio antennas for inclined showers
- Underground muon counters (750 m array, 433 m array)
- Enhanced duty cycle of fluorescence tel.



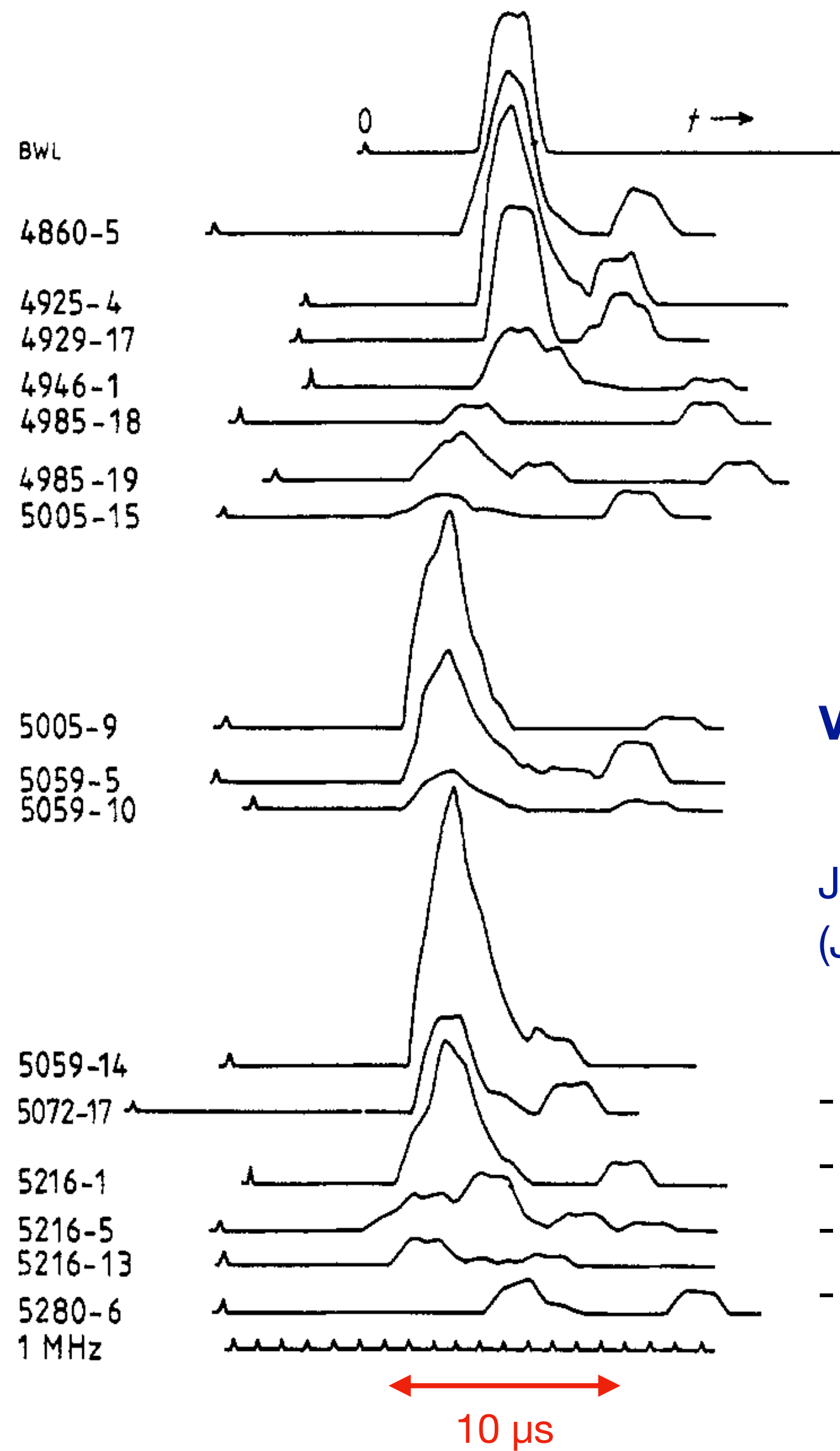
(AugerPrime design report 1604.03637)



AugerPrime: New quality of data – multi-hybrid measurements



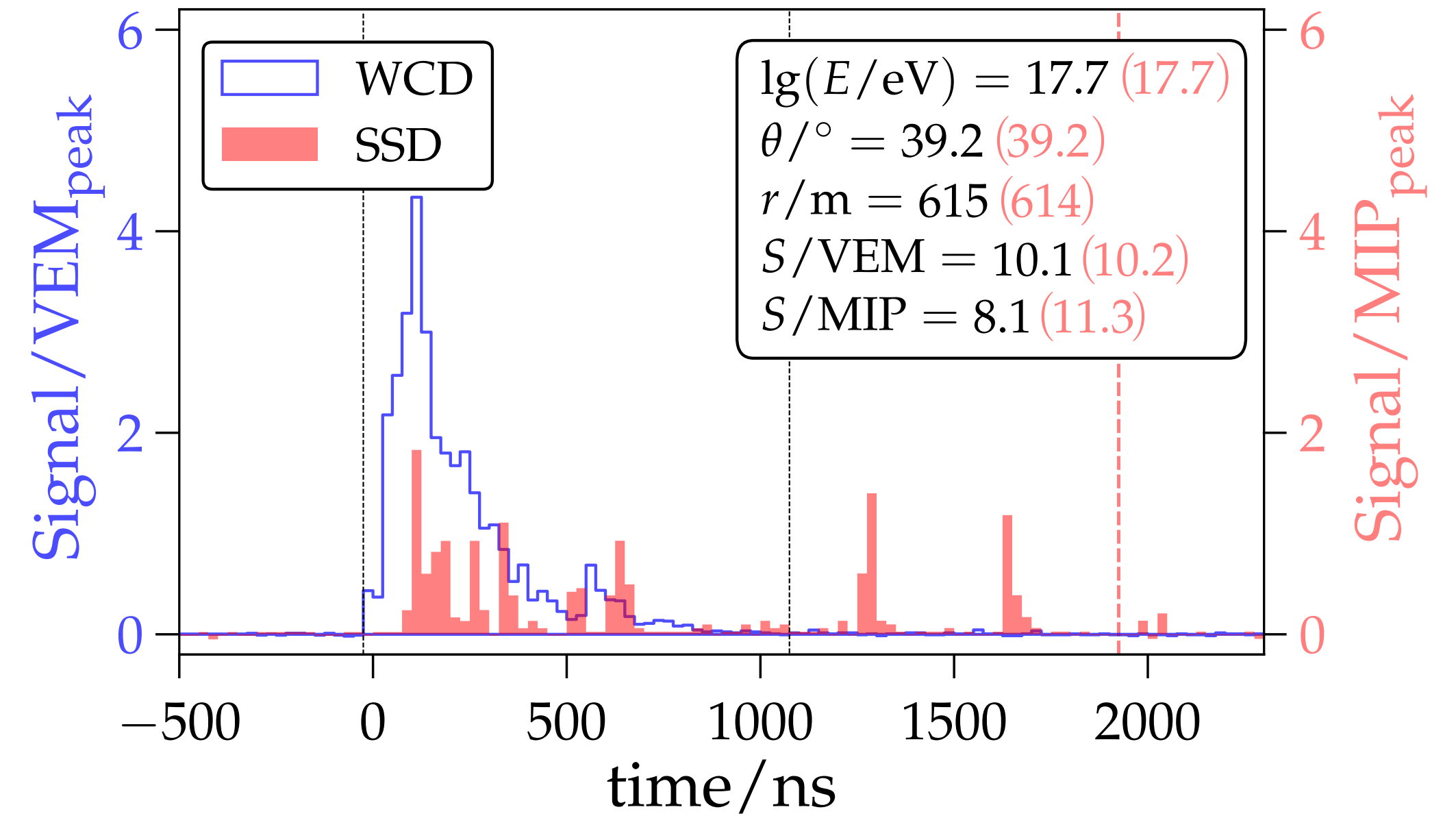
Sub-luminal neutrons in air showers



Vulcano Ranch (1962-63)

J. Linsley
(J. Phys. G: Nucl. Phys. 10 (1984) L191)

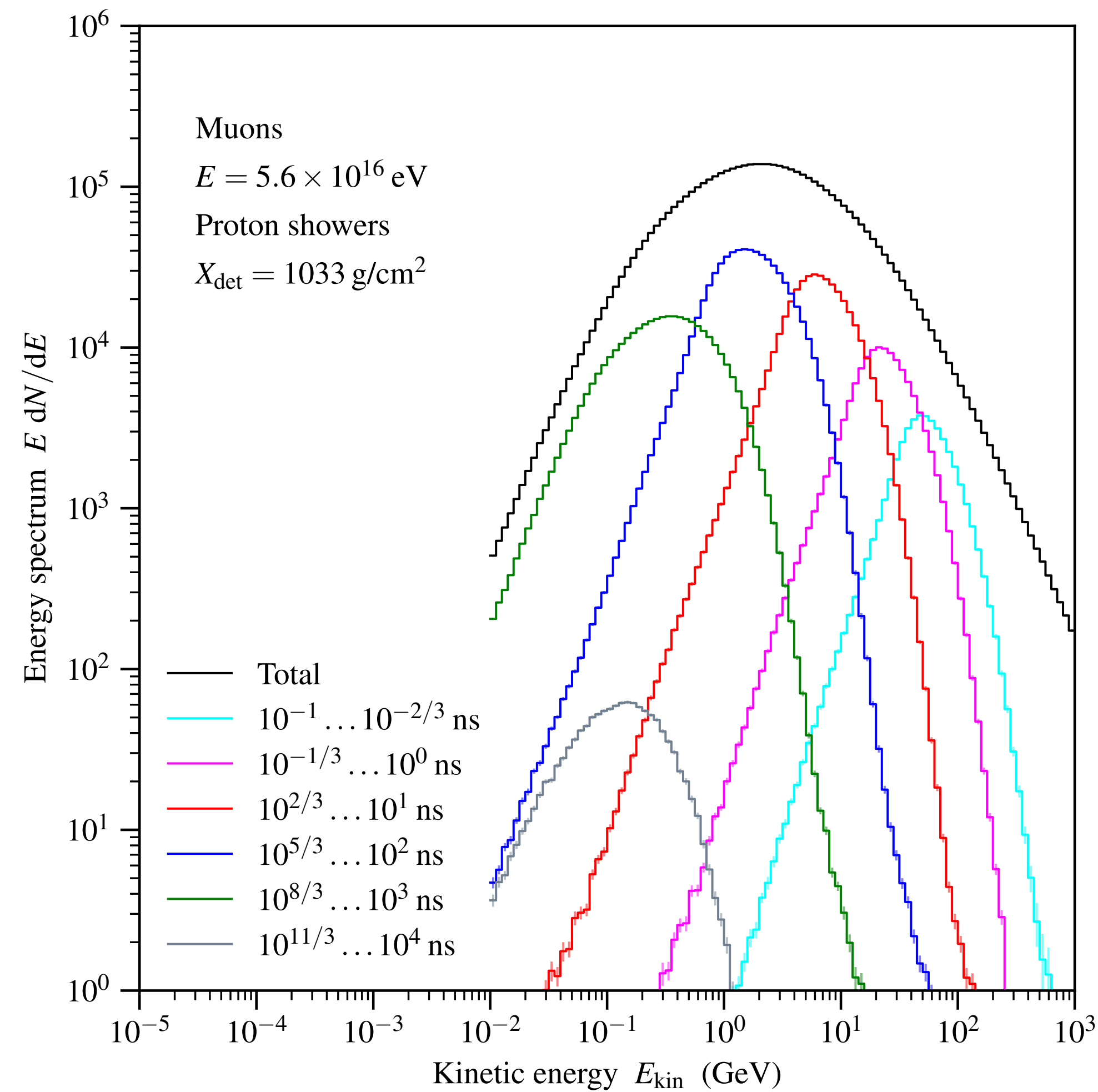
- Sub-luminal pulses with a delay of at least $3\mu\text{s}$
- Sometimes several pulses observed
- Typically 1 km from core, high-energy showers
- Greisen: **neutrons** as sub-luminal particles



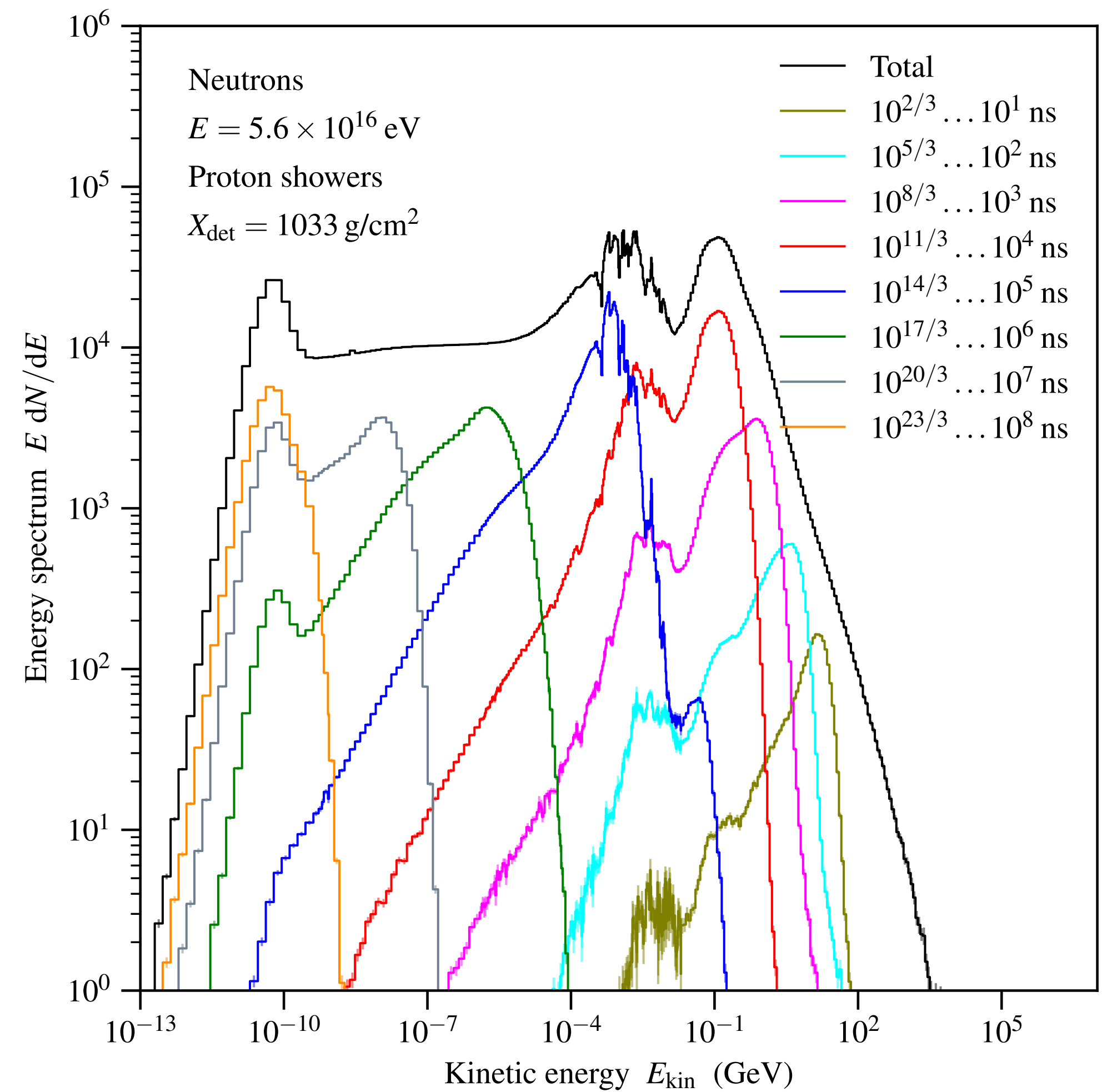
AugerPrime (2020-21)

- D. Schmidt, Pierre Auger Collaboration
(this conference)
- Late signals seen in scintillators (SSD)
 - Late pulses have no coincident signal in water-Cherenkov detectors (WCD)
 - Similar height distribution of late pulses?

Air shower results: time delay distribution

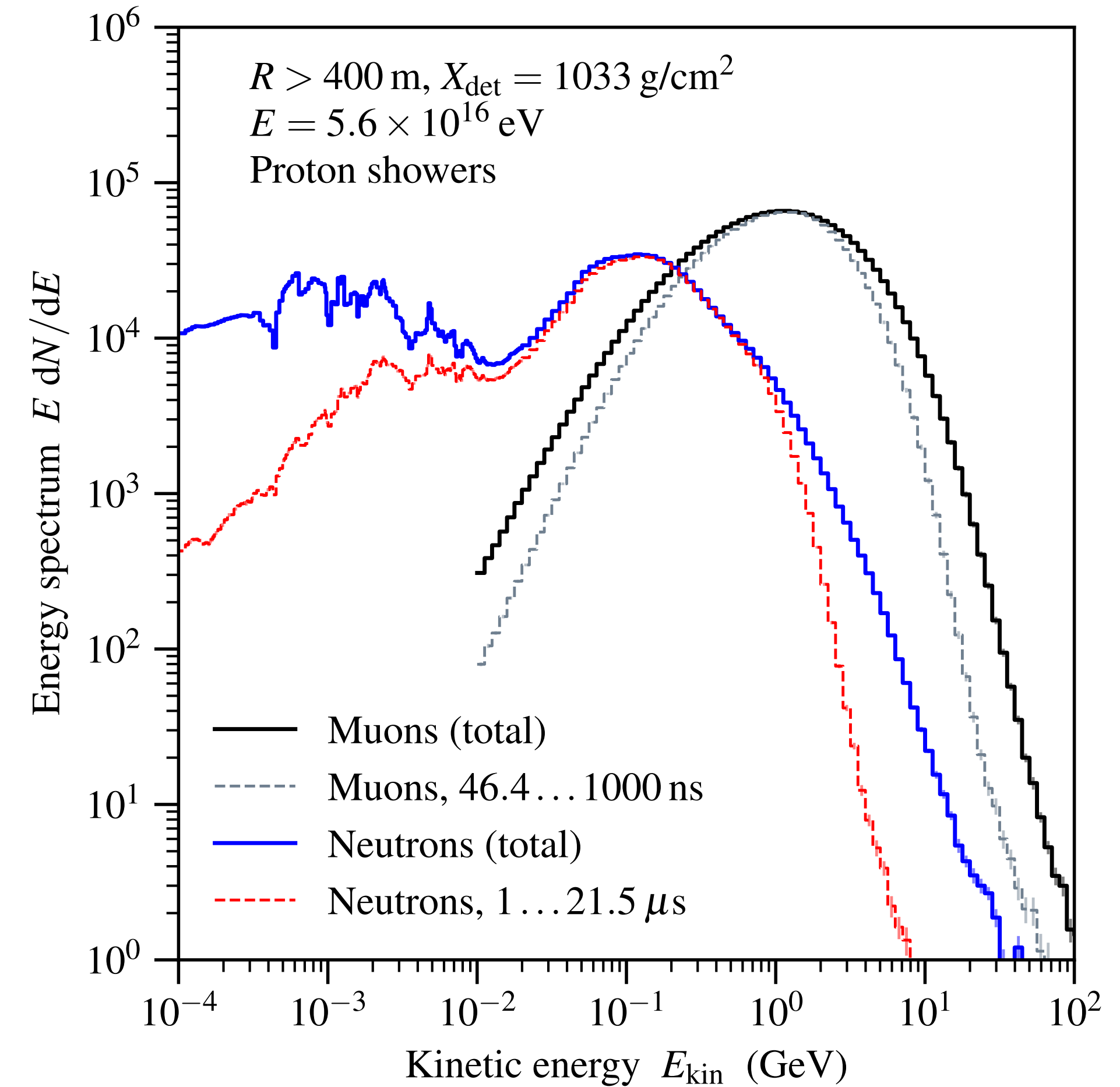
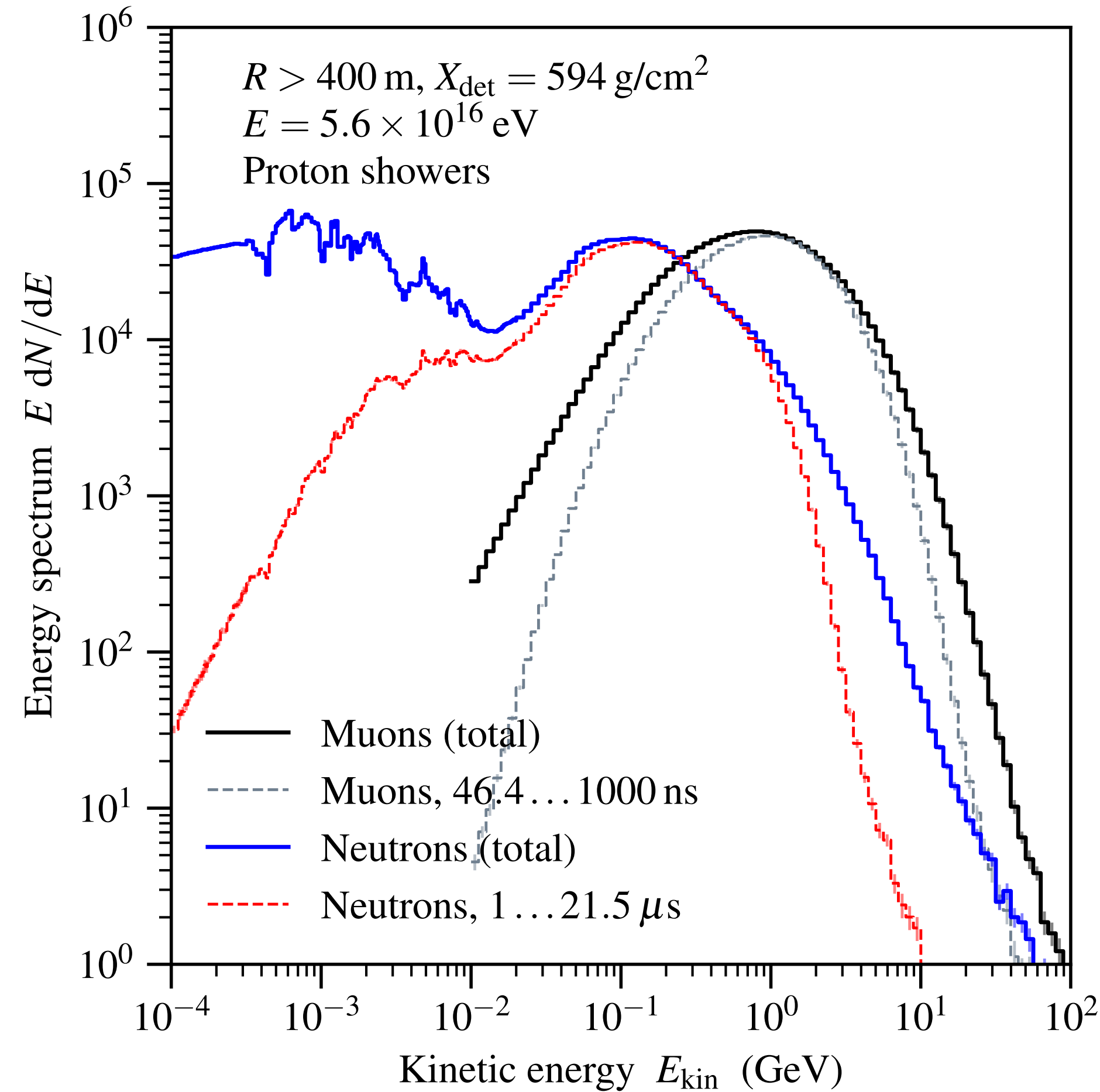


Muons: time delay of bulk of particles: 1 - 500 ns



Neutrons: time delay of high-energy particles: 1 - 20 μ s,
 slow (thermal) neutrons up to 100 ms

Air shower results: muons vs. neutrons at large distance



Close to shower maximum: neutrons as abundant as muons

Past shower maximum: neutrons much less abundant than muons

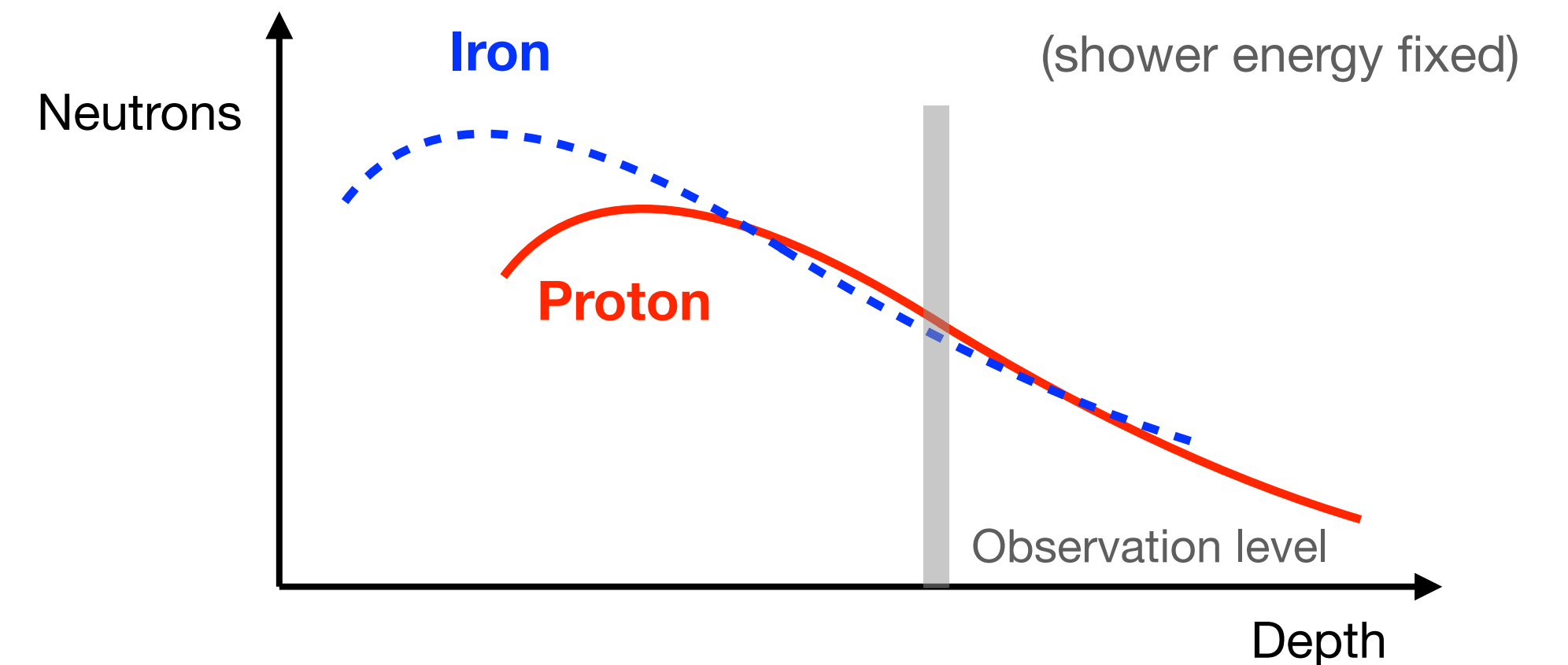
Do we learn anything from sub-luminal neutrons?

Neutrons

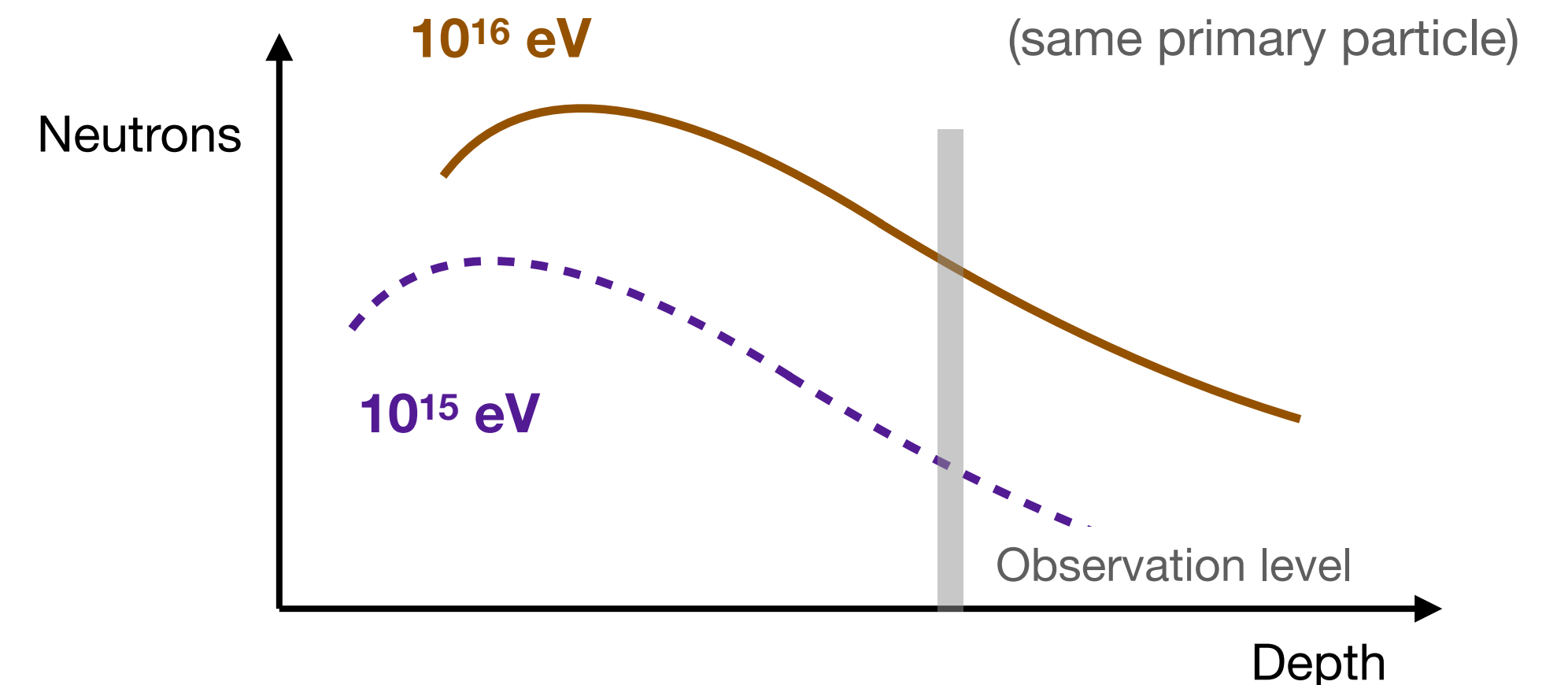
- Interesting sub-luminal particles
- Feature-rich and very wide energy spectrum
- Notoriously difficult to detect
- Very difficult to simulate accurately (environment)
- Expected to produce late pulses in scintillators

Scaling observations

- Energy scaling of production similar to muons
- Primary dependence of production like muons
- Attenuation (neutron removal) length 80 ... 200 g/cm²
- Very wide lateral distribution, wider than muons
- Typical delay in arrival time ~ 1 ... 20 μs ($E_{\text{kin}} > 20$ MeV)
- Thermal neutrons up to ~ 100 ms



Reduced composition sensitivity?



Scaling faster than $\sim E^{0.9}$